COMP90038
Assignment Project Exam Help
Algorit
https://eduassistpro.github.io/

Lecture 17:
Add WeChat edu\_assist\_pro
(with thanks to Harald Sønde hael Kirley)

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## Recap

- We talked about using some memory space (in the form of extra tables, arrays, etc.) to speed up our computation.

  \* Memory is cheap, time's not.

  \* Memory is cheap, time's not.

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 Sorting by counting Add WeChat edu\_assist\_pro

Horspool's Algorithm

# Sorting by counting

- Lets go through this example carefully:
  - The keys are: [1 2 3 4 5]
  - The data is: [5 5 1 5 A s signment 5 Project Exam Help

• Lets count the appearan https://eduassistpro.github.io/

Key 1 5

Occurrences WeChat edu\_assist\_pro

Lets add up the occurrences

Occurrences			
Cumulation			

# Sorting by counting

• Lets sort the d	ata	:				Κe	∋y					1		2		3		4		5
						Cι	ımı	ılati	on			4		5		8		10		20
			A	ssi	gni	nR	eq	Pr	oje	ect	Ex	car	n F	<del>le</del> l	p					19
															_			9		
					htt	os	://€	edu	ıas	ssis	stp	ro.	git	hu	b.i	0/				18
					Ad	d	<b>W</b>	eC	hat	e	du_	_a	ssi	st_	pr	7				
Index	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
Unsorted	5	5	1	5	4	1	2	3	5	5	1	5	5	3	5	1	3	5	4	5
Sorted								3		4									5	5

## Horspool's algorithm

- Lets go through this example carefully:
  - The pattern is TAACG (A=1, T=2, G=3, C=4 → P[.] = [2 1 1 4 3], m =5)
     The string is GACCGCGFGAGATAACGTCA
- This algorithm creates https://eduassistpro.github.io/

function FINDSHIFTS( $P[A], m$ )		А	Т	G	C
function FINDSHIFTS( $P[A]dO$ )WeChat eq for $i \leftarrow 0$ to alphasize $-1$ do	du_assist_p	) <b>ro</b> 5	5	5	5
A	j=0	5	4	5	5
<b>for</b> $j \leftarrow 0$ to $m-2$ <b>do</b>	j=1	3	4	5	5
$Shift[P[j]] \leftarrow m - (j + 1)$	j=2	2	4	5	5
$Simil[ry]] \leftarrow m - (j+1)$	j=3	2	4	5	1

## Horspool's algorithm

We append a sentinel at the end of the data to guarantee completion

• The string is now GACCGCGTGAGATAACGTCATAACG Assignment Project Exam Help

				-0												_									
	0	1	2											13	14	15	16	17	18	19	20	21	22	23	24
STRING	G	Α	С	h <sup>.</sup>	ttp	S:	//e	dι	ıas	ssi	stı	orc	).C	ıit∤	<u>լ</u>	þ.¢	O/S	Т	С	Α	Т	Α	Α	С	G
T[.]	3	1	4	4	3	l	_	2	. 3						1	4	3	2	4	1	2	1	1	4	3
FAILED (C!=A)	Т	Α	Α	A	de	7	Ve	$\mathbf{C}$	ha	t e	dι	ı a	as:	sis	t	or	0								
IS 'CG' SOMEWHERE ELSE?	Т	Α	Α	С	G	Ι΄ ΄																			
(NO, SHIFT BY G)																									
FAILED (A!=G, SHIFT BY A)						Т	Α	Α	C	G															
FAILED (A!=G, SHIFT BY A)								Т	Α	Α	С	G													
FAILED (A!=G, SHIFT BY A)										Т	Α	Α	С	G											
FAILED (C!=G, SHIFT BY C)												Т	Α	Α	C	G									
FOUND AT 16													Т	Α	Α	С	G								

## Horspool's algorithm

• For this algorithm, at the end of **while True do** iteration, [i k] are:

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k
2
0
0
0
0

# Hashing

- Hashing is a standard way of implementing the abstract data type
   "dictionary", a collection of <attribute name, value> pairs. For example an
   student record: Assignment Project Exam Help
  - Attributes: Student ID, N major, etc...

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- Implemented well, it makes data retriat edu\_assist \_pro
- A key identifies each record. It can be anything: integers, alphabetical characters, even strings
  - It should map efficiently to a positive integer.
  - The set *K* of keys need not be bounded.

# Hashing

- We will store our records in a **hash table** of size m.
  - m should be large enough to allow efficient operation, without taking up excessive memoryAssignment Project Exam Help
- https://eduassistpro.github.io/
   The idea is **to have a f**e **key** k, and determines an index in the hash talddTWeChtht edu assisttiono.
  - A record with key k should be stored in location h(k).
- The **hash address** is the value of h(k).
  - Two different keys could have the same hash address (a collision).

# Hashing

Data of Few example application are: arbitrary Text length • The MD5 algorithm used for data

Assignment Project Exam Help integrity verification. https://eduassistpro.github.io/ Α • The blockchain structure de McChat edu assist pro function crypto currencies Fixed length E83H6F20

mathematical

Hash (digest)

### The Hash Table

 We can think of the hash table as an abstract data structure supporting operations:

• Find Assignment Project Exam Help

Insert

Lookup (search and inserhttps://eduassistpro.github.io/

Initialize

Delete Add WeChat edu\_assist\_pro

Rehash

- The challenges in implementing a table are:
  - Design a robust hash function
  - Handling of same addresses (collisions) for different key values

## The Hash Function

- The hash function:
  - Must be easy (cheap) to compute.
     Ideally distribute keys evenly across the hash table.

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Examples:

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• If the keys are integers, we could define  $h(n) = n \mod m$ . If m=23:

n	19	392	179	359	262	321	97	468
h(n)	19	1	18	14	9	22	5	8

If the keys are strings, we could define a more complex function.

# Hashing of strings

#### • Assume:

- this table of 26 characters.
- a hash table of sizesignment Project Exam Help J
- the hash function:

char a

char a

char a

W

18

19

20

21

22

23

24

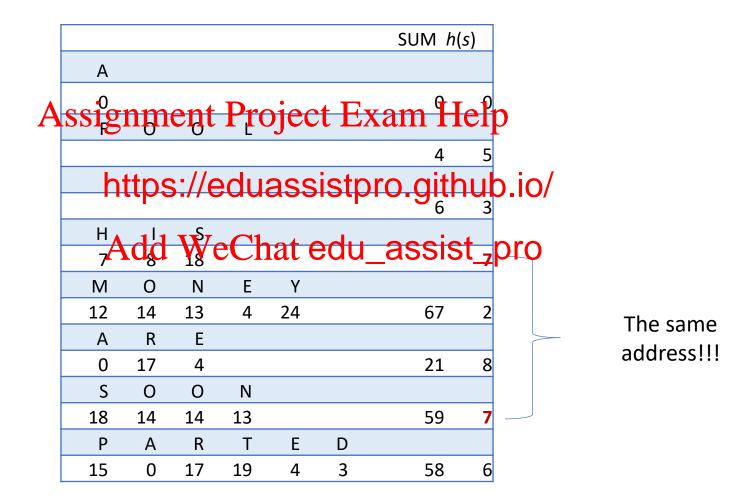
25

$$h(s) = \left(\sum_{i=0}^{|s|-1} a_i\right) \quad \mathbf{m}$$

A 11337 (C1 /)			M	12
$\operatorname{Add}_{\operatorname{mod}} \operatorname{WeChat} \operatorname{edu}$	ı_as	SIST_	_pr <sub>Q</sub>	13
	F	5	O	14

 and the following list of keys:
 [A, FOOL, AND, HIS, MONEY, ARE, SOON, PARTED]

## Calculating the addresses



## A more complex hash function

- Assume a binary representation of the 26 characters
  - We need **5 bits** per character (0 Assignmenta Project Example p bin(a) to 31) 01001
- https://eduassistpro.gith@b.io/1010 Instead of adding, we concatenate the binary strin

Add

•	Our hash table is of size 101 (m
	is prime)

Our key will be 'MYKEY'

We	Ch	iat edu	ass	<b>St</b> 12	<b>pro</b> 01100
Ε	4			13	01101
F	5	00101	0	14	01110
G	6	00110	Р	15	01111
Н	7	00111	Q	16	10000
l	8	01000	R	17	10001

char	a	bin(a)
S	18	10010
Т	19	10011
U	20	10100
V	21	10101
W	22	10110
Χ	23	10111
Υ	24	11000
Z	25	11001

01011

## A more complex hash function

			STRING				KEY mod
	M	Υ	K	E	Υ	KEY	101
int	12	Assignm	ient Proje	ect Exam	Help 24		
bin(int)	01100	1.44	// 1		11,000		
Index	4	http	s://eduas	sistpro.g	ithub.io/ <sub>0</sub>		
		A dd	LW <sub>0</sub> Chat		ciet pro		
32^(index)	1048576	32768	1024	cuu_asa	sist_pro <sub>1</sub>		
a*(32^index)	12582912	786432	10240	128	24	13379736	64

- By concatenating the strings, we are basically multiplying by 32
- Note that the hash function is a polynomial:

$$h(s) = a_{|s|-1} 32^{|s|-1} + a_{|s|-2} 32^{|s|-2} + \dots + a_1 32 + a_0$$

## Handling Long Strings as Keys

What would happen if our key is the longer string 'VERYLONGKEY'

$$h(VERYLONGKEY) = (21 \times 32 \text{Project}_3 \text{Exam}_4 \text{Help}_{32+24}) \mod 101$$

- The stuff between par quickly
   https://eduassistpro.github.io/mes a very large number
   Add WeChat edu\_assist\_pro
  - DEC: 23804165628760600

Calculating this polynomial by brute force is very expensive

## Horner's rule

 Fortunately there is a trick, Horner's rule, that simplifies polynomial calculation.

Assignment<sub>3</sub> Project<sub>2</sub> Exam Help  
$$p(x) = a_3 \times x^3 + a_2 \times x^2 + a_1 \times x + a_0$$

• By factorizing x we have <a href="https://eduassistpro.github.io/">https://eduassistpro.github.io/</a>

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• If we apply the modulus we have:

$$p(x) = ((((a_3 \times x) + a_2) \times x + a_1) \times x + a_0) \mod m$$

## Horner's rule

• We then can use the following properties of modular arithmetic:

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• Given that modulus distributes acro edu\_assist\_pro, then we have:

$$p(x) = (((((a_3 \boxtimes x) \boxplus a_2) \boxtimes x) \boxplus a_1) \boxtimes x) \boxplus a_0$$

• The results of each operation will not exceed m.

## Handling collisions

• The hash function should be as random as possible.

• However, in some cases different keys will be mapped to the same hash table address. For exam <a href="https://eduassistpro.github.io/">https://eduassistpro.github.io/</a>

KEY	19	392	479	<b>3</b> 58	166	edu	200	321	y 97	468	814
ADDRESS	19	1	18	14	1	caa_	Lago	22	5	8	9

- When this happens we have a collision.
- Different hashing methods resolve collisions differently.

## Separate Chaining

 Each element k of the hash table is a linked list, which makes collision handling very easy

Assignment Project Exam neip																					
ADDRESS	0 1	2	3	4	5								14	15	16	17	18	19	20	21	22
LIST	392				97	httr	0./	lad	110	cic	tor		359		i/		179	19			
						TILL	JS./	<del>C</del> u	ua	2012	thi	O.C	ונוו	JU.	10/		639	663			

Aggignment Project Even Heln

- Exercise: add to this table [83 WeChat edu\_assist\_pro
- The **load factor**  $\alpha = n/m$ , where n is the number of items stored.
  - Number of probes in **successful** search  $\sim$  (1 +  $\alpha$ )/2.
  - Number of probes in **unsuccessful** search  $\sim \alpha$ .

# Separate chaining: advantages and disadvantages

• Compared with **sequential search**, reduces the number of comparisons by the size of the table (a factor of m).

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- Good in a dynamic enviro keys are hard to predict. https://eduassistpro.github.io/
- The chains can be ordered, And clear that edu\_assist ppront" when accessed.
- Deletion is easy.
- However, separate chaining uses extra storage for links.

## Open-Addressing Methods

• With **open-addressing** methods (also called **closed hashing**) all records are stored in the hash table itself (not in linked lists hanging off the table).

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- There are many methods of this type edu\_assist on two:
  - linear probing
  - double hashing

• For these methods, the load factor  $\alpha \le 1$ .

## Linear probing

• In case of collision, try the next cell, then the next, and so on.

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• Assume the following ving one at the time:

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[19(19) 392(1) 179(48) 662(19at edu\_assis2\_24) 321(22) ...]

- Search proceeds in similar fashion
- If we get to the end of the table, we wrap around.
- For example, if key 20 arrives, it will be placed in cell 0.

## Linear probing

• Exercise: Add [83(14) 110(18) 497(14)] to the table

ADDRESS	0	1	2	2	3	4	<b>15</b> 851	gnŋ	nen	t P	ect <sub>1</sub>	Еx	am	He	lp <sub>5</sub>	16	17	18	19	20	21	22
LIST		392					97							359				179	19	663	639	321

https://eduassistpro.github.io/

- Again let m be the table size wand hat edu\_assist prof records stored.
- As before,  $\alpha = n/m$  is the load factor. Then, the average number of probes:
  - Successful search:  $0.5 + 1/(2(1-\alpha))$
  - Unsuccessful:  $0.5 + 1/(2(1-\alpha)^2)$

## Linear probing: advantages and disadvantages

- Space-efficient.
- Worst-case performance misesible: must be projected in the pad factor grow beyond 0.9.
- Comparative behavior, m = 111 https://eduassistpro.github.io/
   Linear probing: 5.5 probes on a

  - Binary search: 12.3 probes on average (success) hat edu\_assist\_pro
    Linear search: 5000 probes on average (success) hat edu\_assist\_pro
- Clustering (large groups of contiguous keys) is a major problem:
  - The collision handling strategy leads to clusters of contiguous cells being occupied.
- Deletion is almost impossible.

# Double Hashing

- To alleviate the clustering problem in linear probing, there are better ways of resolving collisions.
- One is **double hashing** which uses a second hash function *s* to determine an **offset** to be used in probing for a free cel <a href="https://eduassistpro.github.io/">https://eduassistpro.github.io/</a>
- For example, we may choose Ale the Chat edu\_assist\_pro
- By this we mean, if h(k) is occupied, next try h(k) + s(k), then h(k) + 2s(k), and so on.
- This is another reason why it is good to have m being a prime number. That way, using h(k) as the offset, we will eventually find a free cell if there is one.

# Rehashing

 The standard approach to avoiding performance deterioration in hashing is to keep track of the load factor and to rehash when it reaches, say, 0.9. Assignment Project Exam Help

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- Rehashing means alloc le (typically about twice the current size), revisitingle of Citet edu\_assishgoto hash address in the new table, and inserting it.
- This "stop-the-world" operation will introduce long delays at unpredictable times, but it will happen relatively infrequently.

## An exam question type

- With the hash function  $h(k) = k \mod 7$ . Draw the hash table that results after inserting in the given order, the following values Assignment Project Exam Help
- When collisions are hahttps://eduassistpro.github.io/
  - separate chaining Add WeChat edu\_assist\_pro
  - linear probing
  - double hashing using  $h'(k) = 5 (k \mod 5)$

# Solution

Index Assignn	nent <sub>o</sub>	Proj	ect J	Exan	n He	lp <sub>5</sub>	6
Separate Chaining				•	githu ssist		
Linear Probing			-		_	_ -	
Double Hashing							

## Rabin-Karp String Search

- The Rabin-Karp string search algorithm is based on string hashing.
- To search for a string position project the same hash (p) and then check every subs has the same hash value. Of course, if it has, the string https://eduassistpro.gweneed.to compare them in the usual way.

- If  $p = s_i \dots s_{i+m-1}$  then the hash values are the same; otherwise the values are almost certainly going to be different.
- Since false positives will be so rare, the O(m) time it takes to actually compare the strings can be ignored.

## Rabin-Karp String Search

#### https://eduassistpro.github.io/

• where a is the alphabet size that edu\_assist the that value, for the substring that starts at position j+1, quite cheaply:

$$hash(s, j + 1) = (hash(s, j) - a^{m-1}chr(s_j)) \times a + chr(s_{j+m})$$

• modulo m. Effectively we just subtract the contribution of  $s_j$  and add the contribution of  $s_{j+m}$ , for the cost of two multiplications, one addition and one subtraction.

## An example

- The data '31415926535'
- The hash function h(k); The

• The pattern '26'

		<u> </u>	ttns:	//edi	uass	ustoi	CO CII	thut	10/			
STRING	3	1	4	1			oig.	E	5	5	3	5
31 MOD 11		ø	Add V	WeC	hat e	edu_	ass	ist_r	oro			
14 MOD 11			3									
41 MOD 11				8								
15 MOD 11					4							
59 MOD 11						4						
92 MOD 11							4					
26 MOD 11												

# Why Not Always Use Hashing?

Some drawbacks:

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If an application calls f sorted order, a hash table is no good.
 https://eduassistpro.github.io/

- Also, unless we use separate chaining, irtually impossible.
- It may be hard to predict the volume of data, and rehashing is an expensive "stop-the-world" operation.

# When to Use Hashing?

 All sorts of information retrieval applications involving thousands to millions of keys.

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• Typical example: Symbol t The compiler hashes all (variable, function, etc.) n https://eduassistpro.gifth.com/line/d to each – no deletion in this case.

- When hashing is applicable, it is usually superior; a well-tuned hash table will outperform its competitors.
- **Unless** you let the load factor get too high, or you botch up the hash function. It is a good idea to print statistics to check that the function really does spread keys uniformly across the hash table.

## Next lecture

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• Dynamic programmin

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