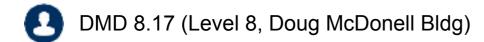


COMP90038 Algorithms and Complexity

Lecture 12: Mo https://eduassistpro.gitque.fo/Algorithms (with thanks to Hara edu_assist_pro

Toby Murray







@tobycmurray

Divide and Conquer



- In the last lecture we studied the archetypal divideand-conquer sorting algorithms: mergesort and quicksort.
- We also introduced the powerful master theorem, providing solution of recurrence relations, for free.

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- allows us to quickly determine the complexity of these divide-and-conquer algorithms
- Now we shall look at tree traversal, and then a final example of divide-and-conquer, giving a better solution to the closest-pair problem.

Binary Trees



 An example of a binary tree, with empty subtrees marked as □

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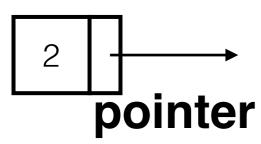
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This tree has height 4, the empty tree having height -1

Review of Linked List Terminology



node

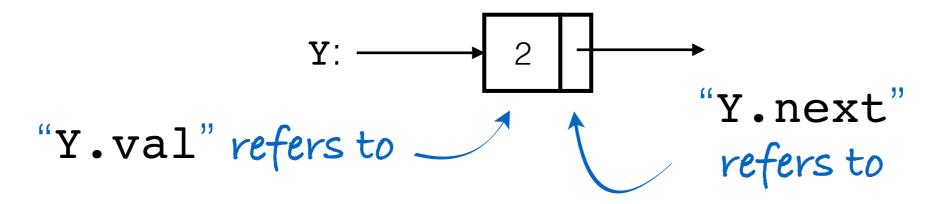


(in Java: "reference")

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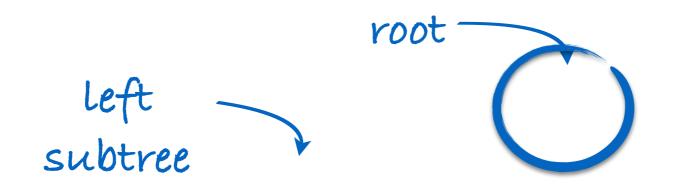


x is (a pointer to) the **head node** of the list



Tree Terminology







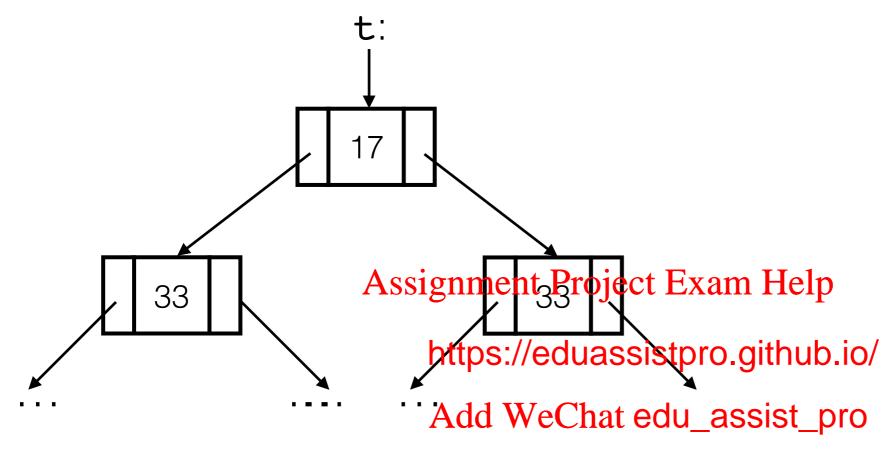
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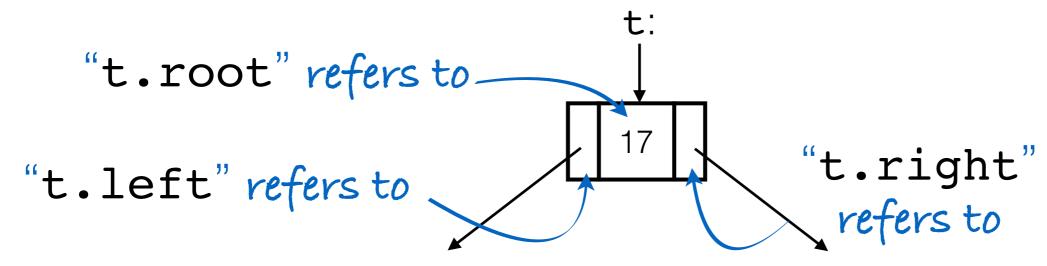
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Tree Terminology





t is (a pointer to) the root node of the tree



Binary Trees



 An example of a binary tree, with empty subtrees marked as □

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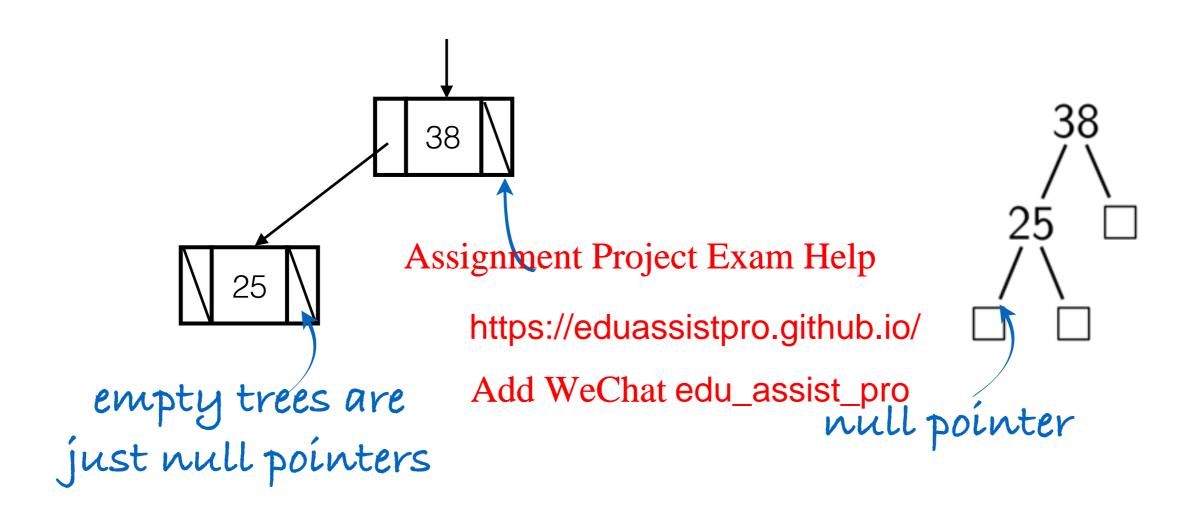
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This tree has height 4, the empty tree having height -1

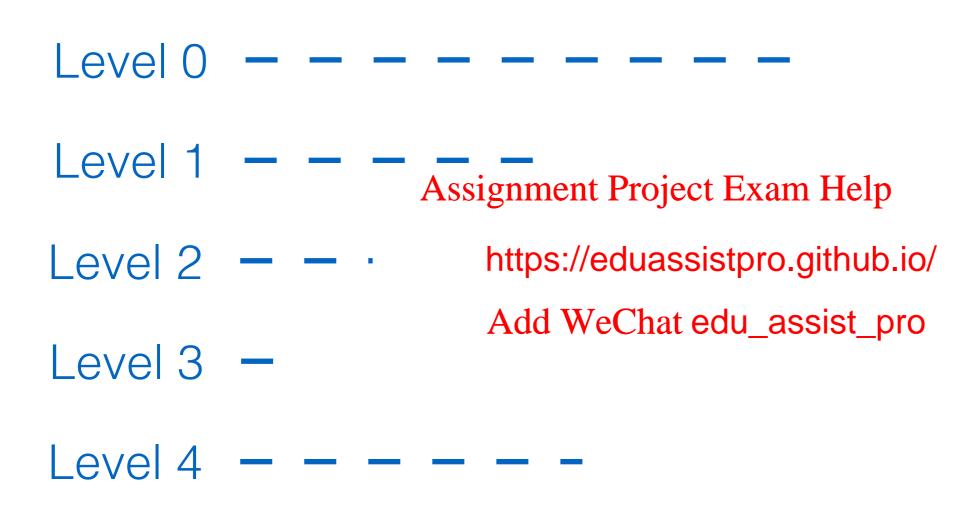
Empty Nodes





Levels and Height





So the tree has **height** 4 (its **maximum level**)

Binary Tree Concepts



 Special trees have their **external nodes** □ only at level *h* and *h*+1 for some *h*:

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A **full** binary tree: Each node has 0 or 2 (non-empty) children. A **complete** tree: Each level filled left to right.

(Every level except perhaps the last is completely filled.)

Calculating the Height



Recursion is the natural way of calculating the height:



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Height Complexity



- Input size: number n of (internal) nodes (e.g. for T n is 13)
- Number of external nodes always n+1 (e.g. for T x is 14)
- The function HEIGHT makes one tree comparison (is T null/ empty?) per nodes internal raise Externally, so altogether 2n + 1 comparisons.

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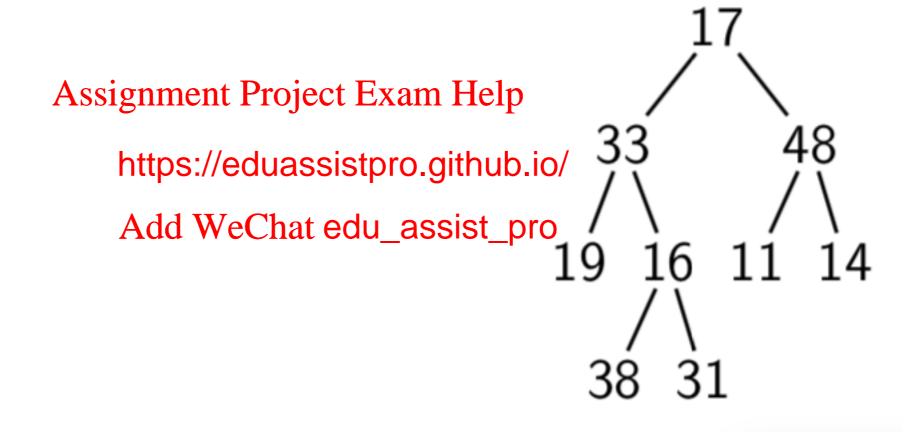
Binary Tree Traversal



- Preorder traversal visits the root, then the left subtree, and finally the right subtree.
- Inorder traversalizing the left subtree, then the root, and finally t https://eduassistpro.github.io/
- **Postorder** traversal visits t ubtree, the right subtree, and finally the root.
- Level-order traversal visits the nodes, level by level, starting from the root.



Visit order:

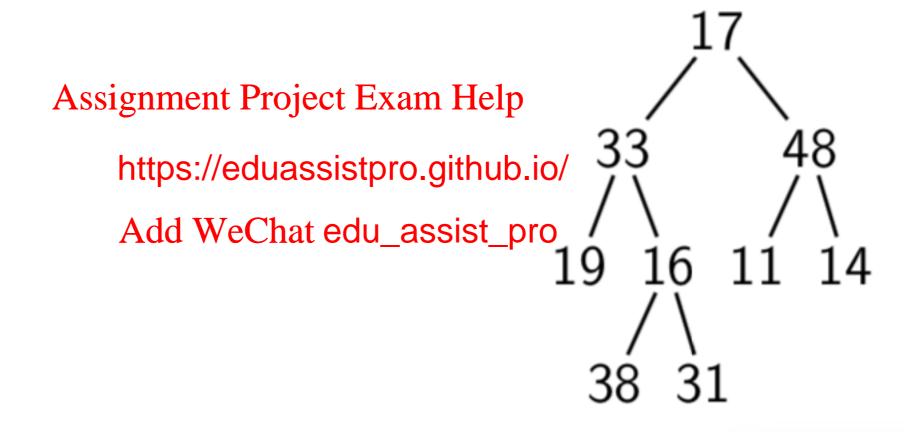


PreorderTraverse(17)

Call Stack



Visit order: 17

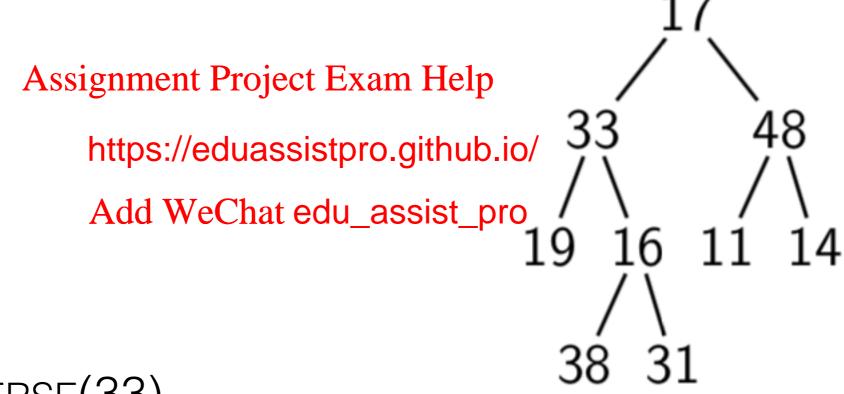


PreorderTraverse(17)

Call Stack



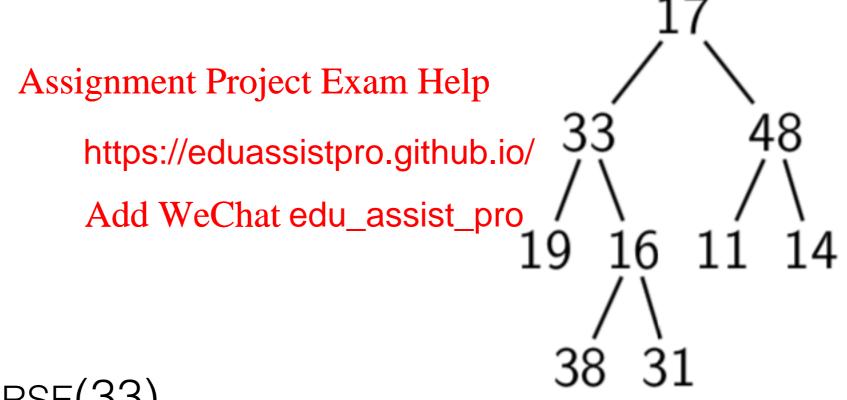
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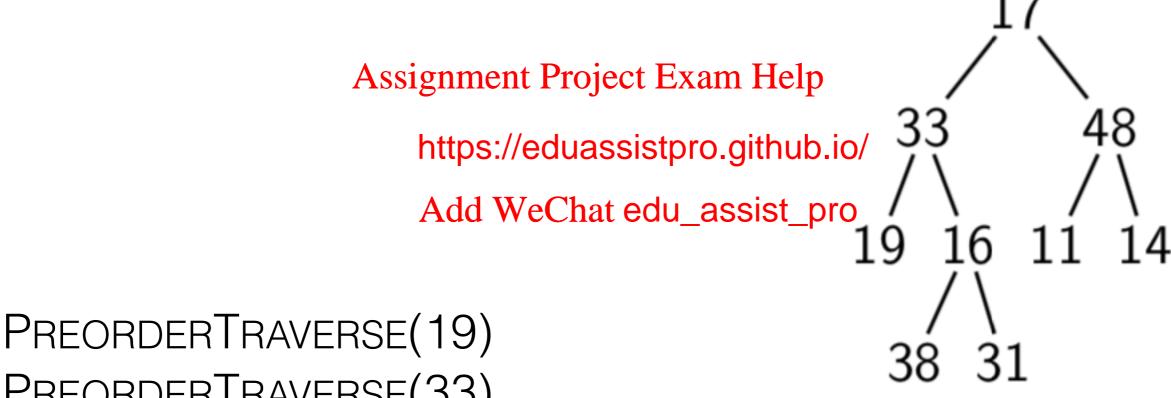
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PreorderTraverse(33)
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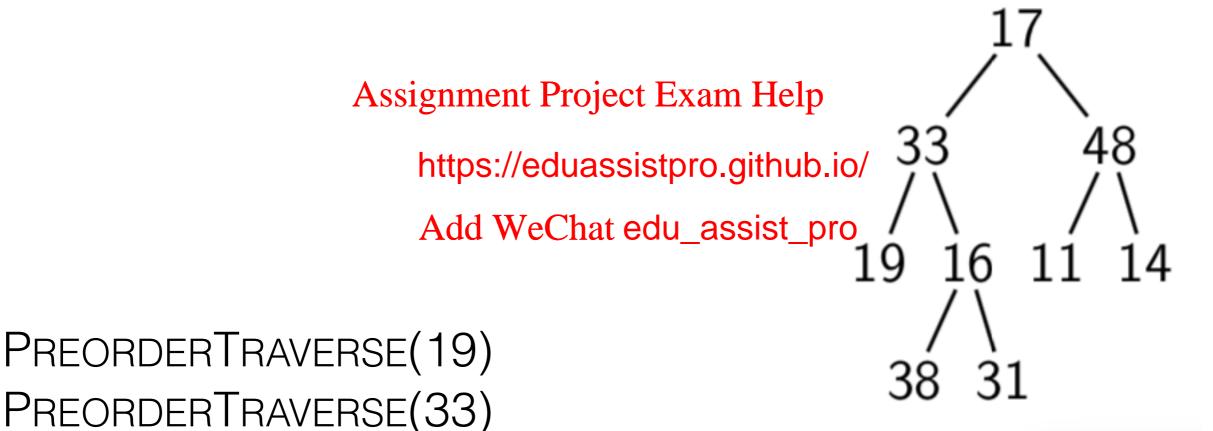
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PreorderTraverse(33)
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Visit order: 17 33 19



Call Stack

PreorderTraverse(17)

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Visit order: 17 33 19



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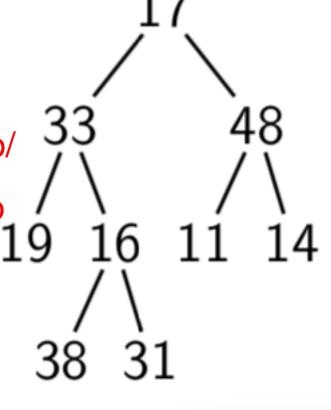
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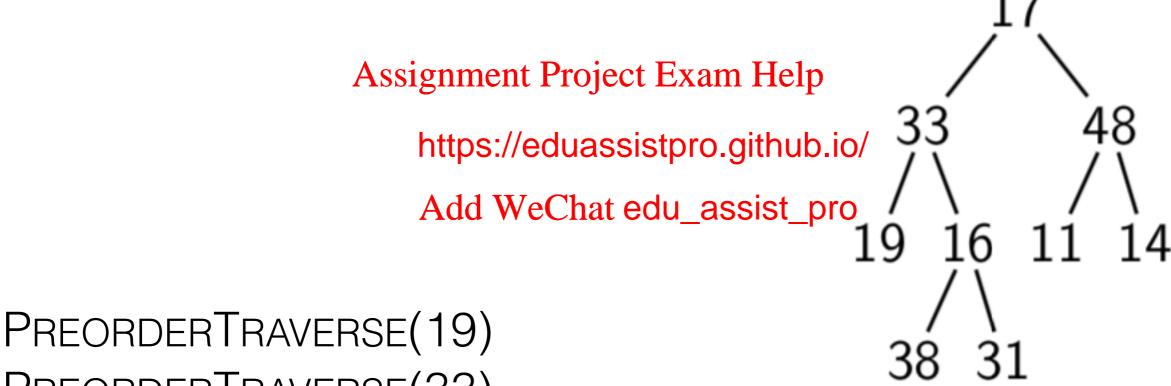
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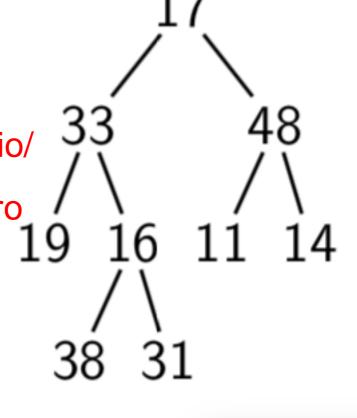
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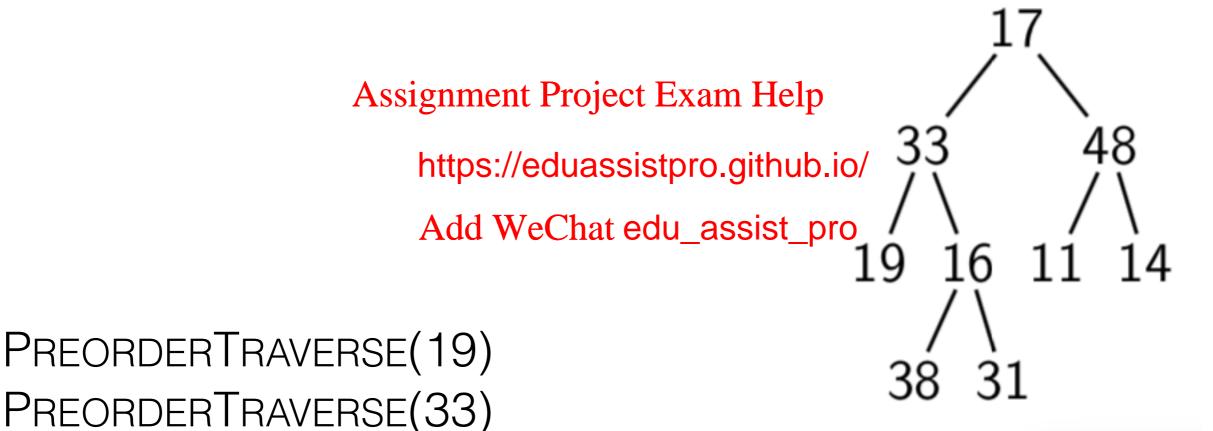
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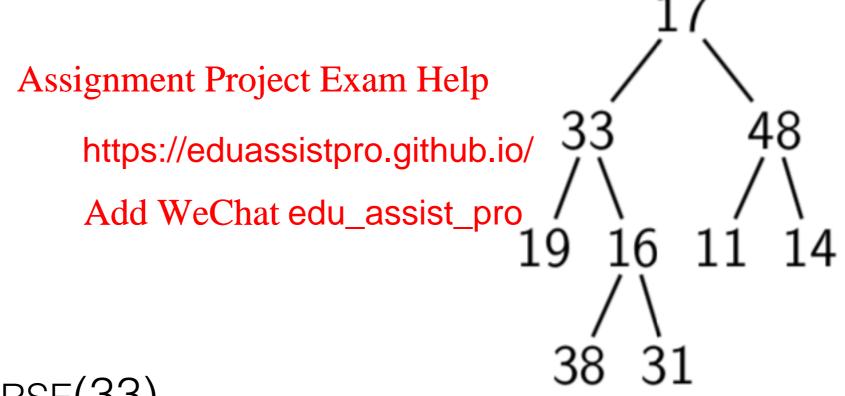


Call Stack

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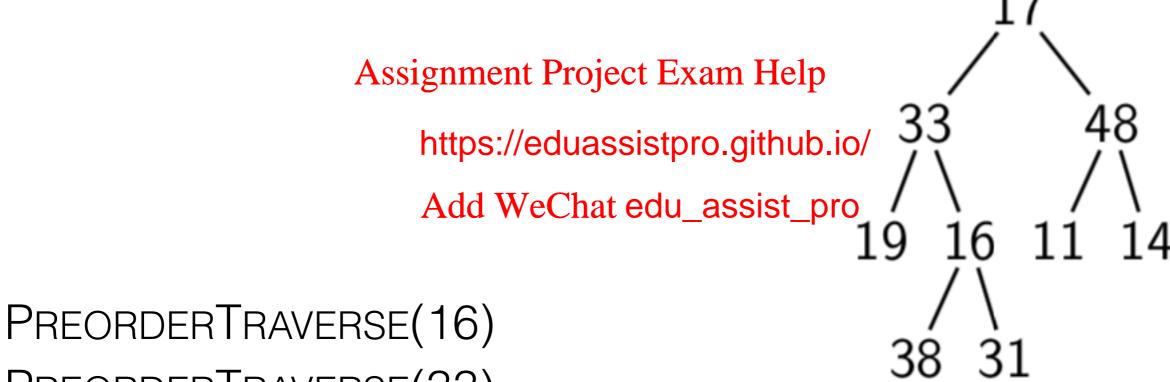
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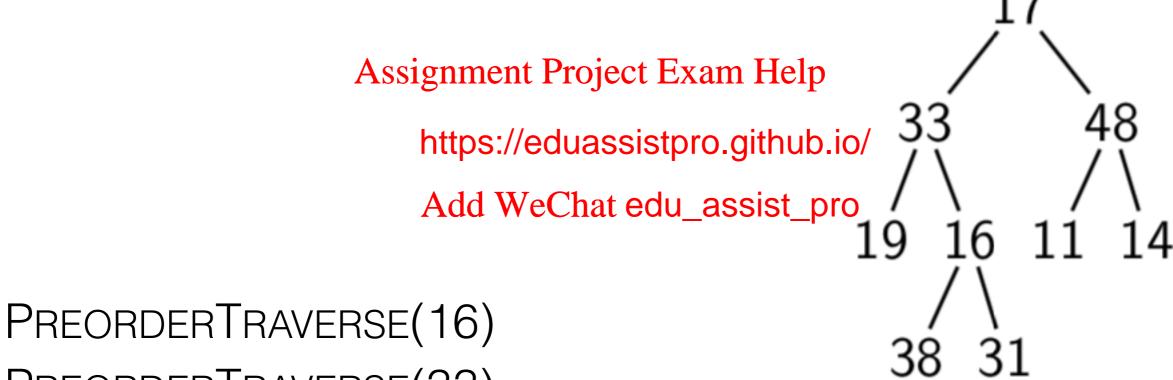
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PreorderTraverse(17)

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Visit order: 17 33 19 16



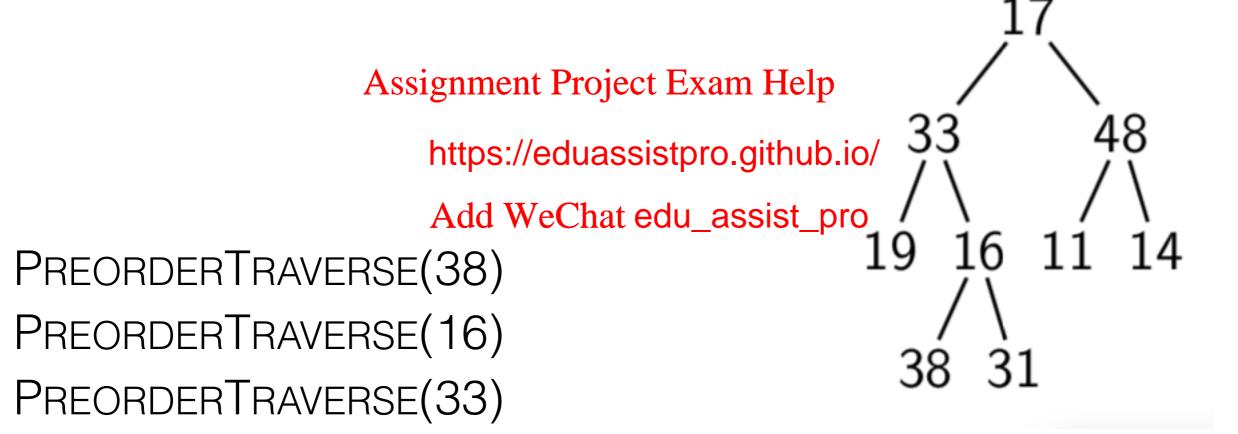
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PREORDERTRAVERSE(17)

PreorderTraverse(17)

Call Stack

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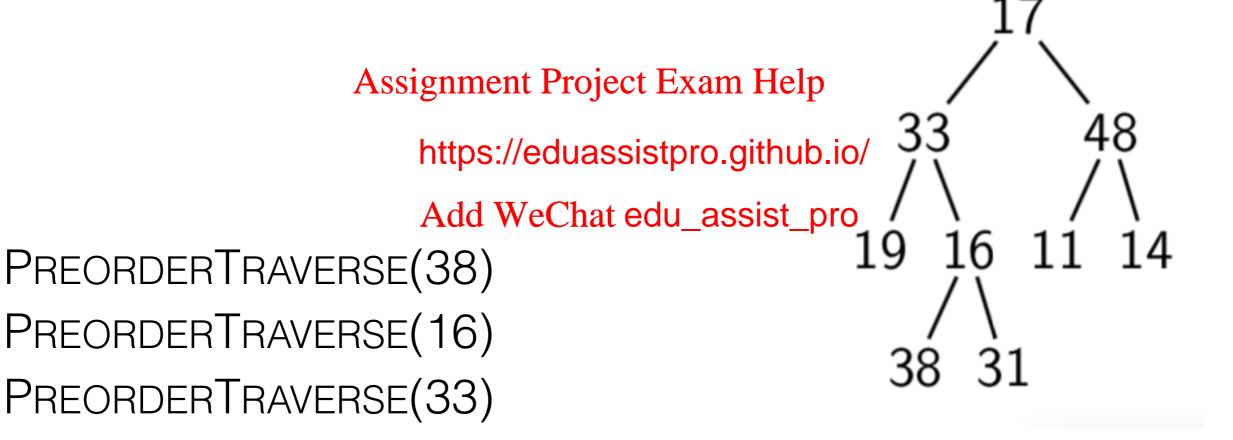


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Call Stack

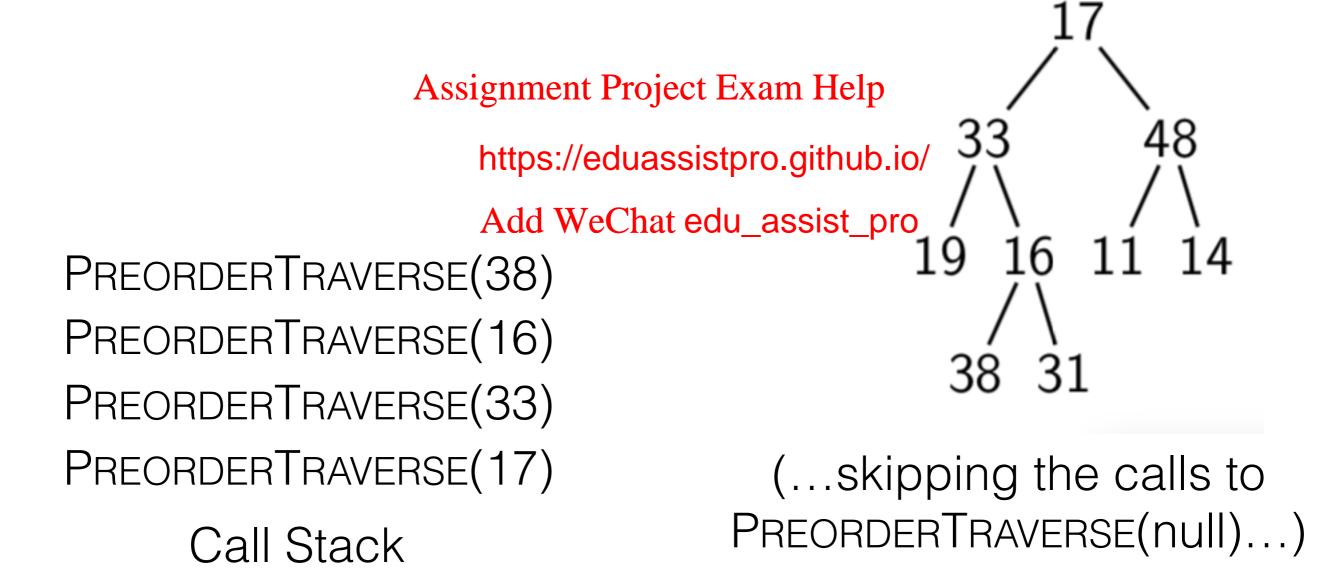


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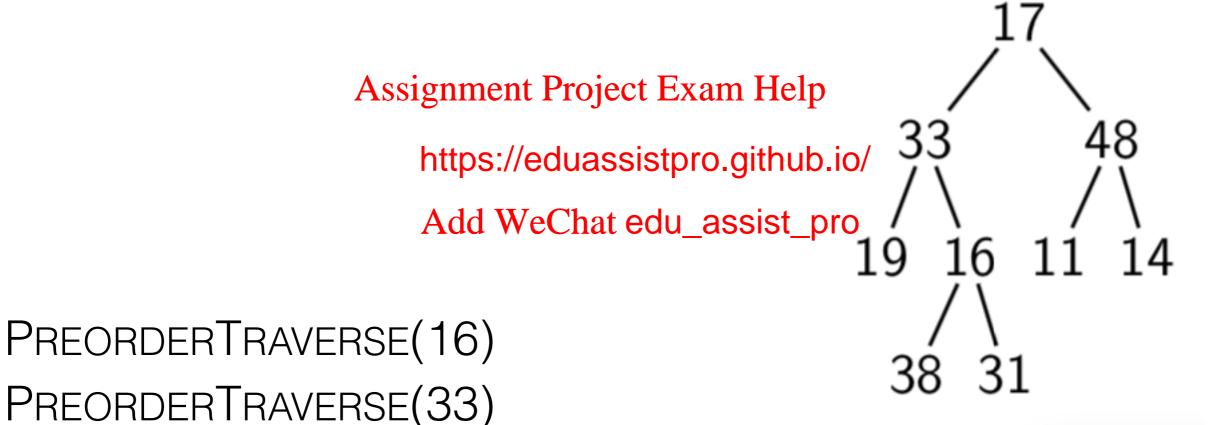


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Visit order: 17 33 19 16 38

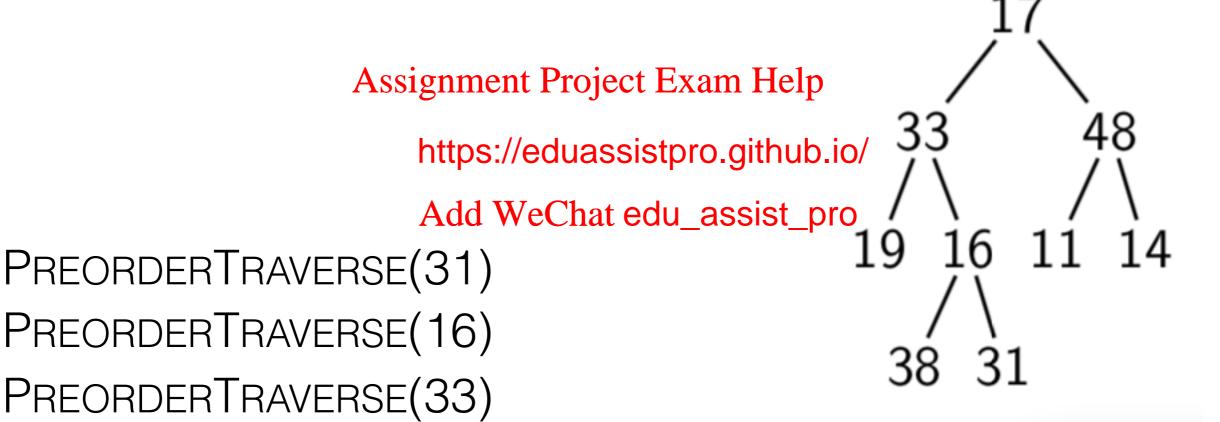


Call Stack

PreorderTraverse(17)



Visit order: 17 33 19 16 38



Call Stack

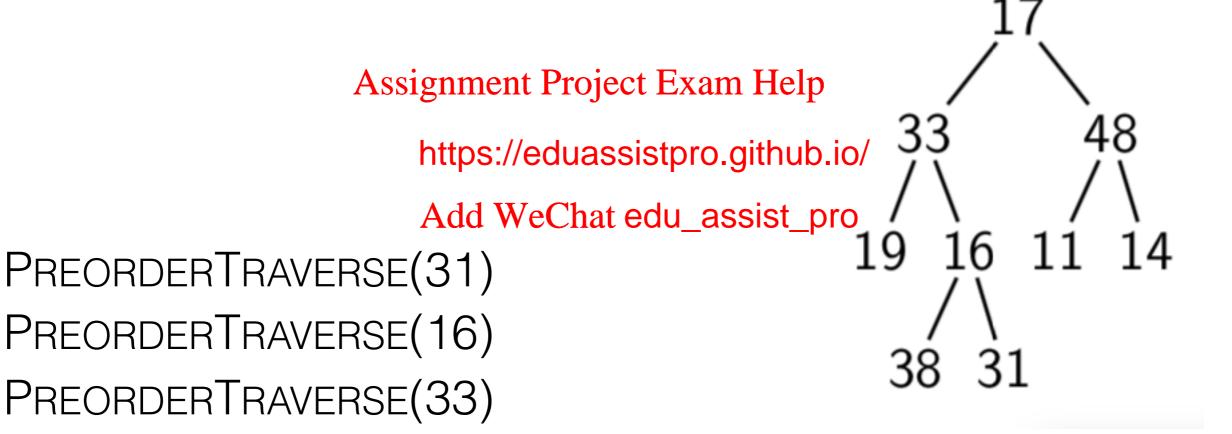
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PreorderTraverse(17)

Call Stack

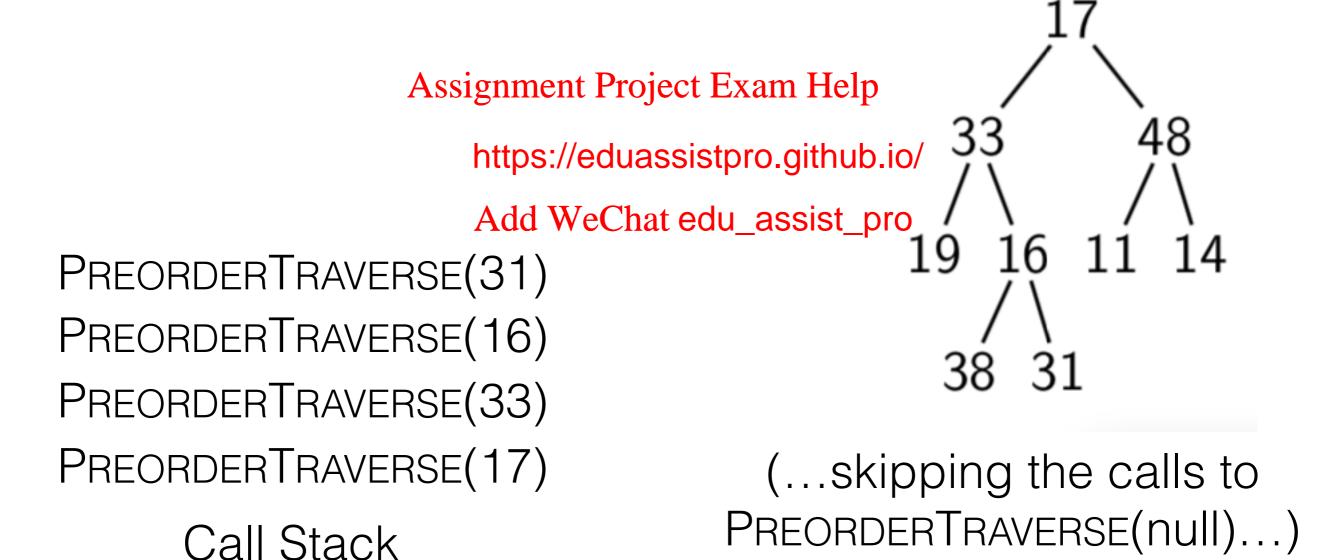


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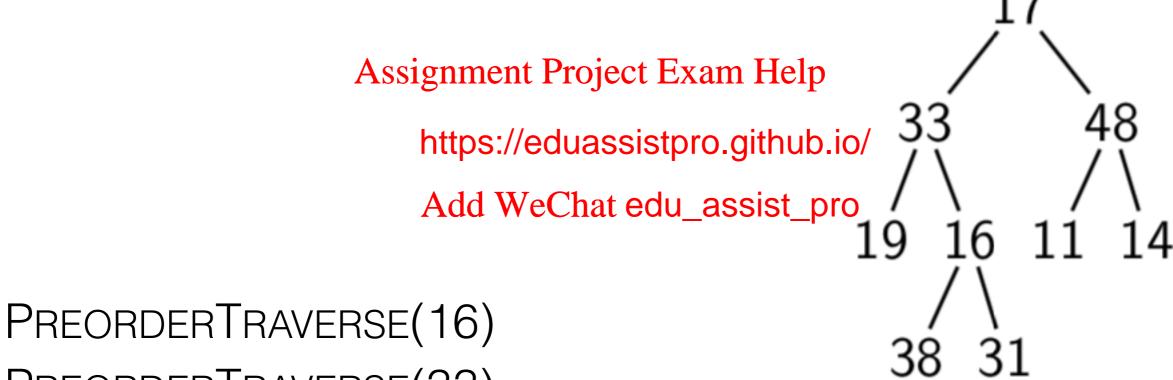


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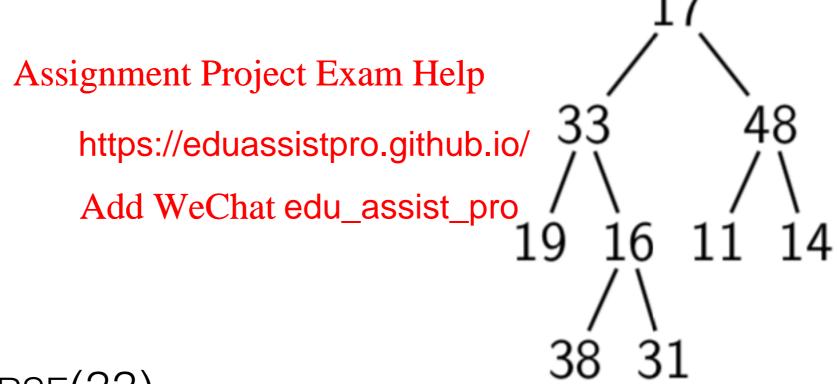
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PREORDERTRAVERSE(33)
PREORDERTRAVERSE(17)



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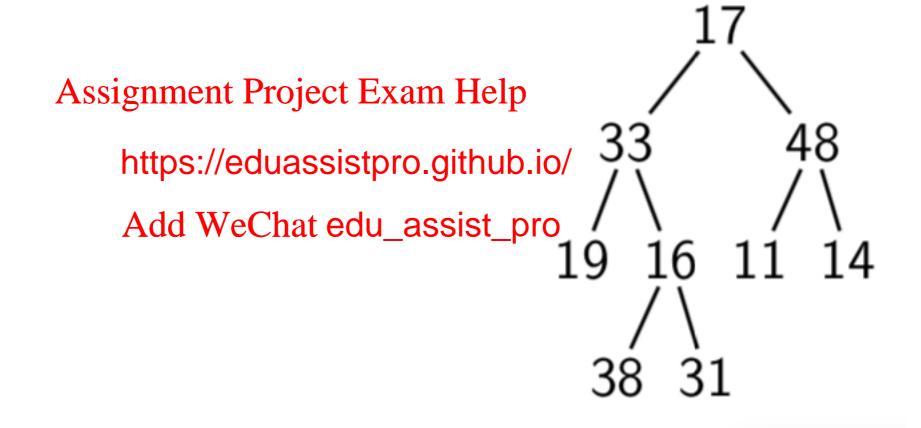


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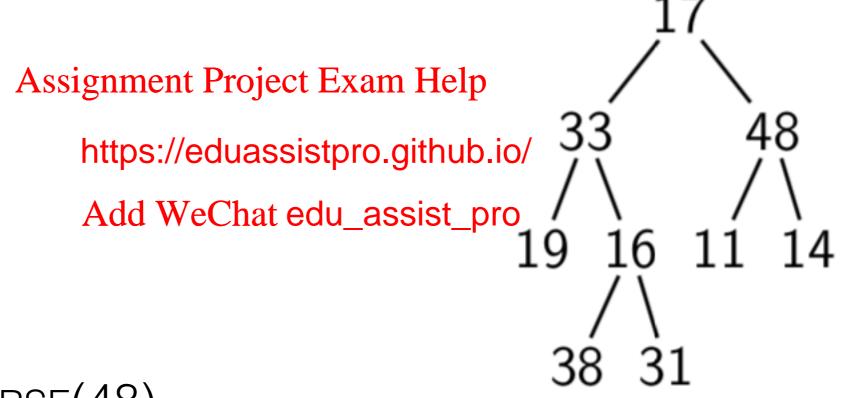


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Call Stack



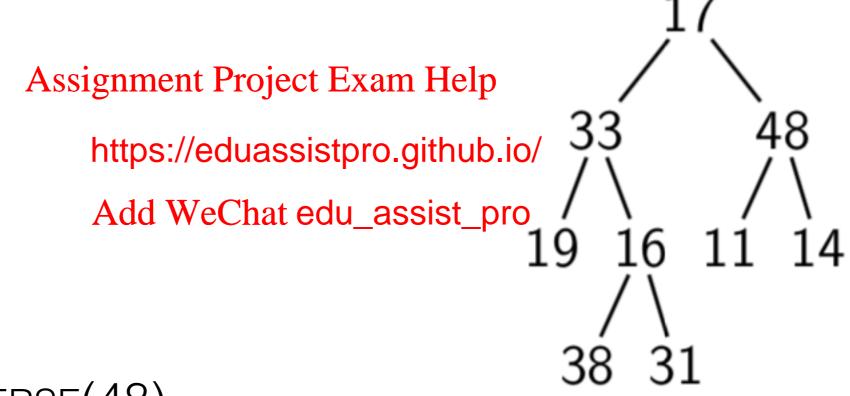
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PreorderTraverse(17)



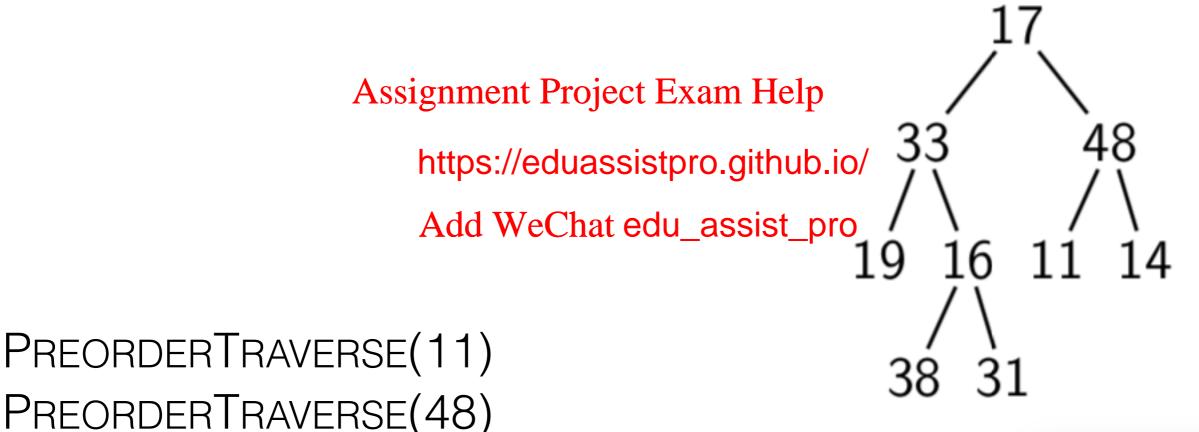
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PreorderTraverse(17)



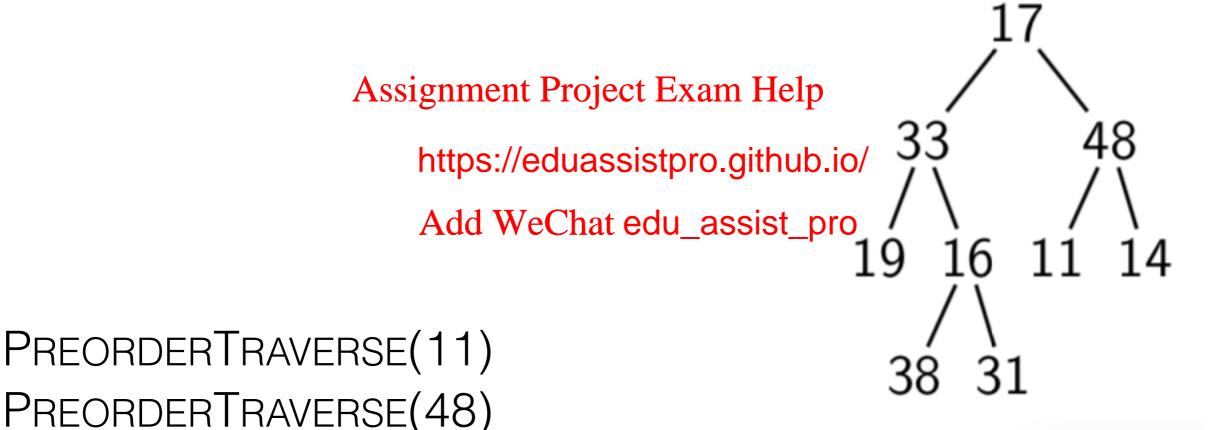
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Preorder Traverse (17)



Visit order: 17 33 19 16 38 31 48 11

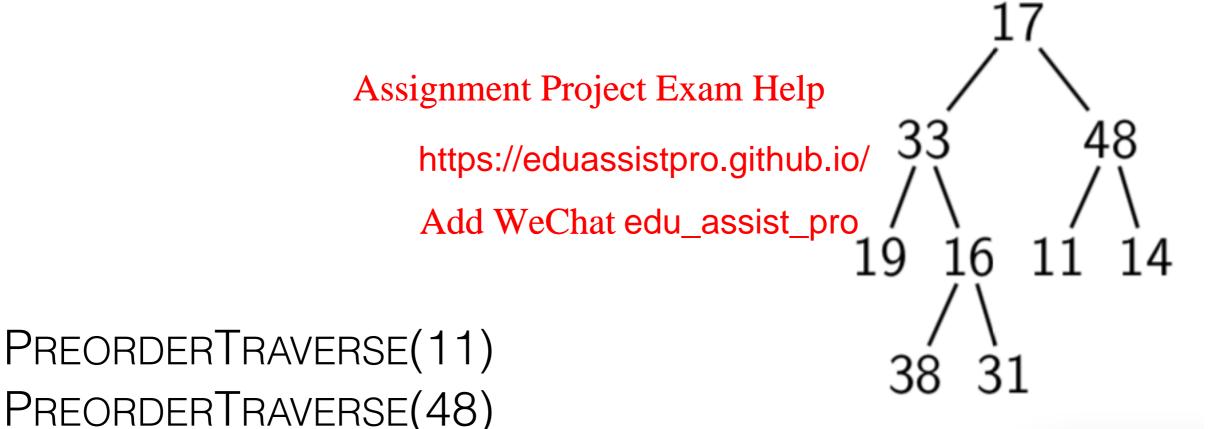


Call Stack

PreorderTraverse(17)



Visit order: 17 33 19 16 38 31 48 11



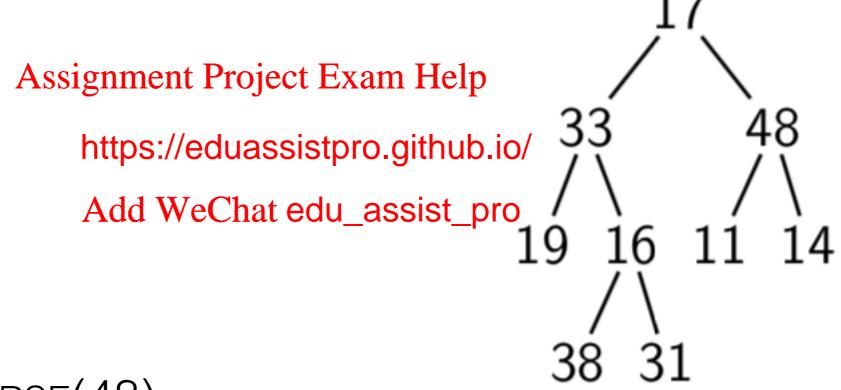
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Call Stack

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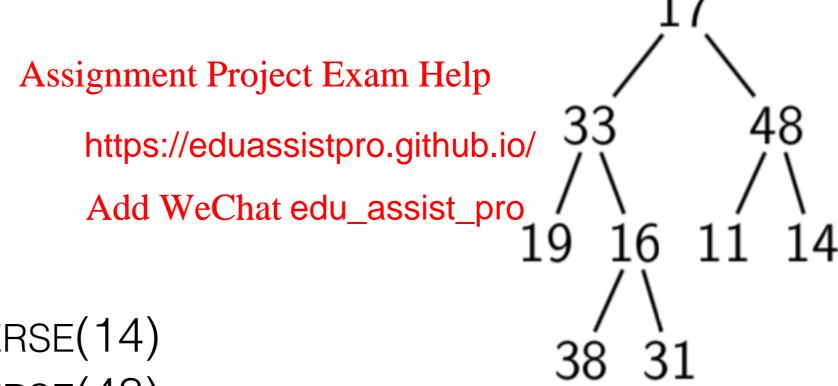
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PreorderTraverse(48)
PreorderTraverse(17)



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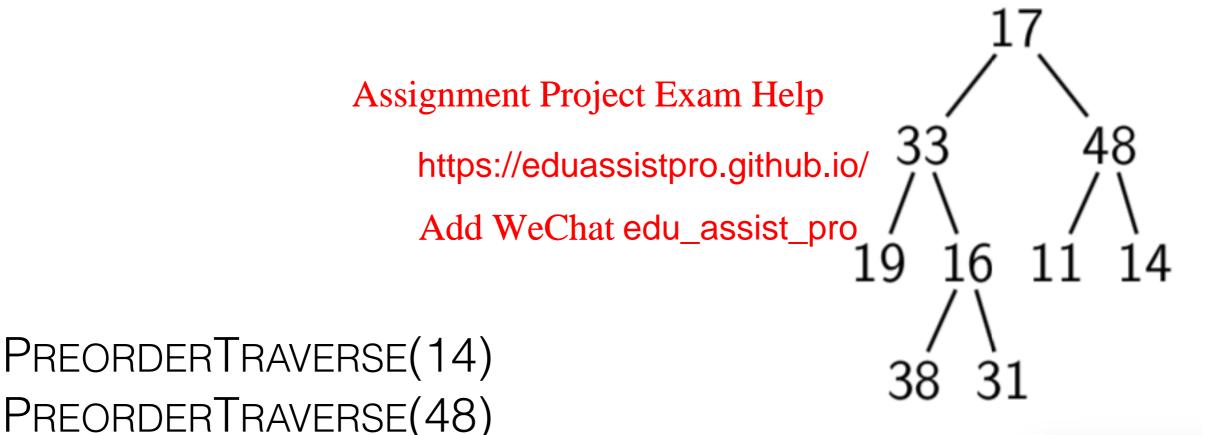


PREORDERTRAVERSE(14)
PREORDERTRAVERSE(48)

PreorderTraverse(17)



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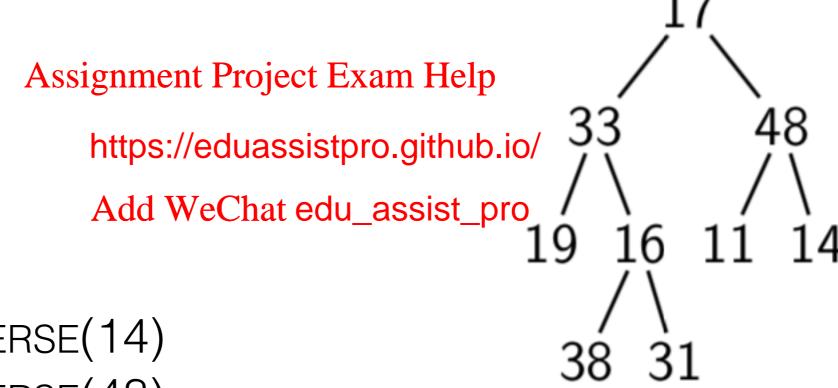


Call Stack

PreorderTraverse(17)



Visit order: 17 33 19 16 38 31 48 11 14

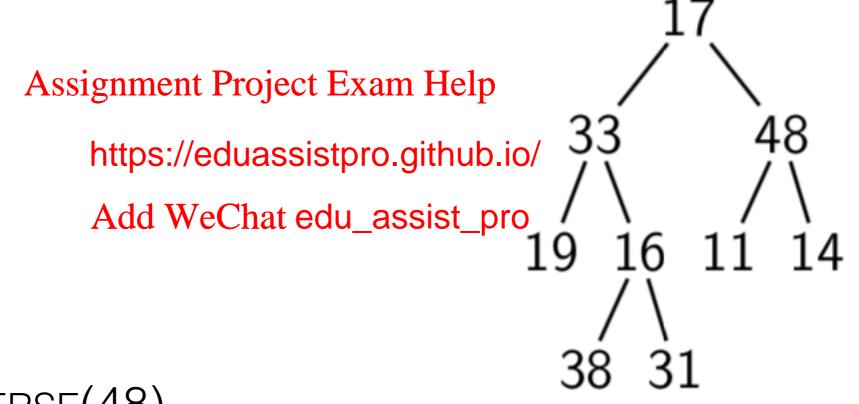


PreorderTraverse(14)
PreorderTraverse(48)
PreorderTraverse(17)
PreorderTraverse(17)
Call Stack

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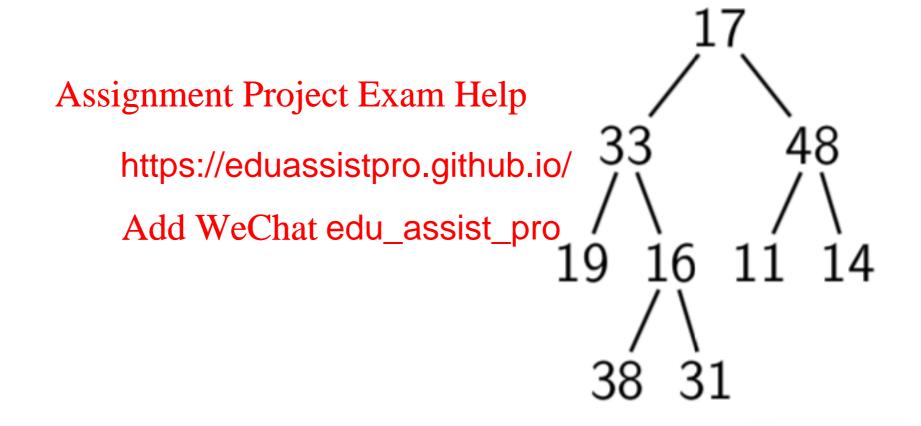
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PreorderTraverse(48)
PreorderTraverse(17)



Visit order: 17 33 19 16 38 31 48 11 14

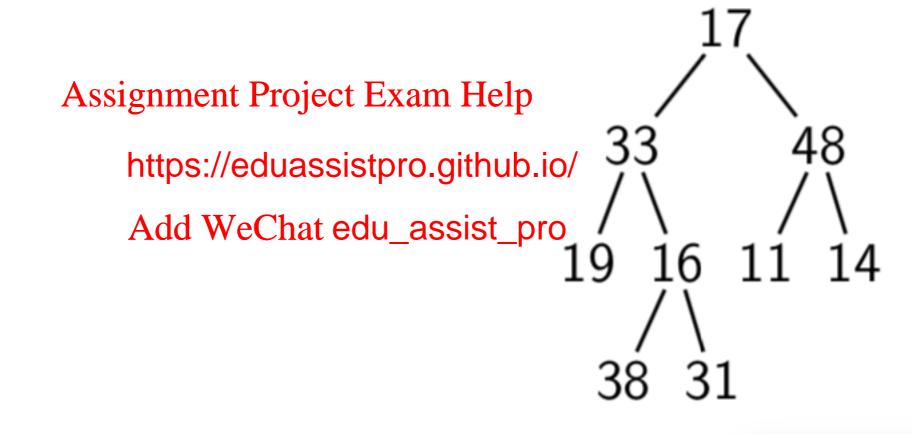


PreorderTraverse(17)

Call Stack



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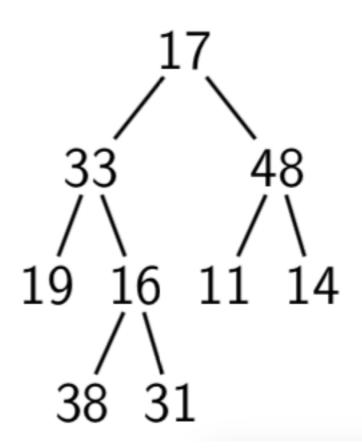


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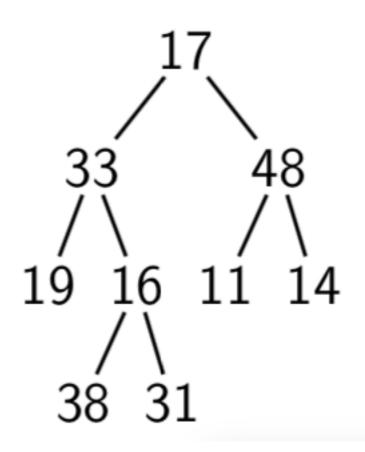


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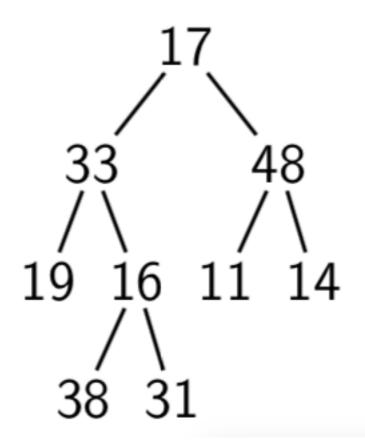


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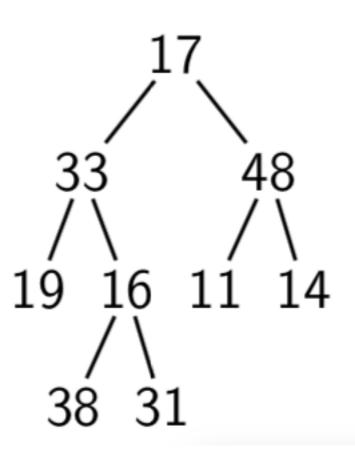
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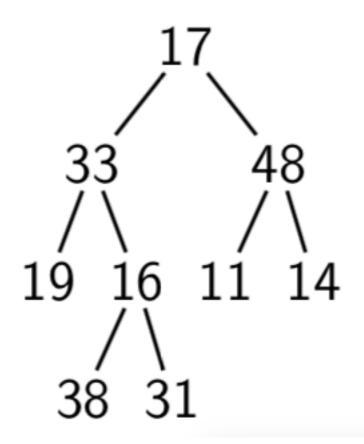


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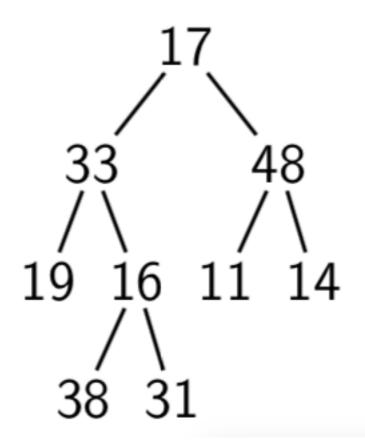


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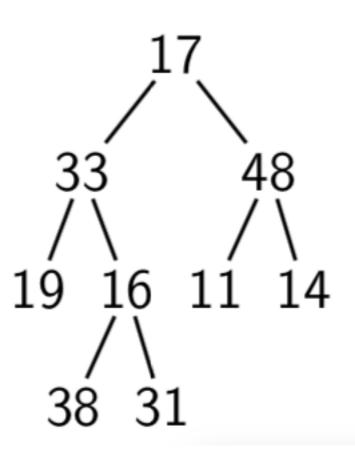
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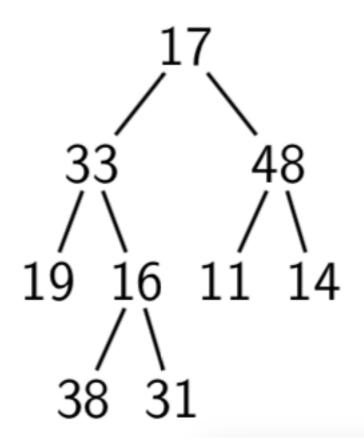


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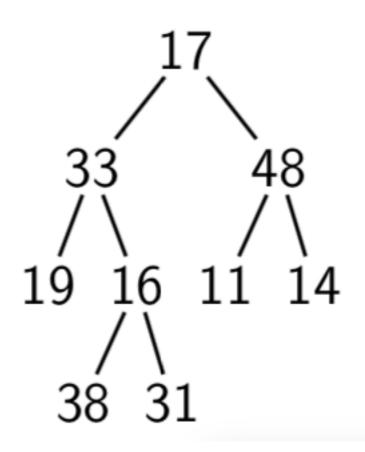


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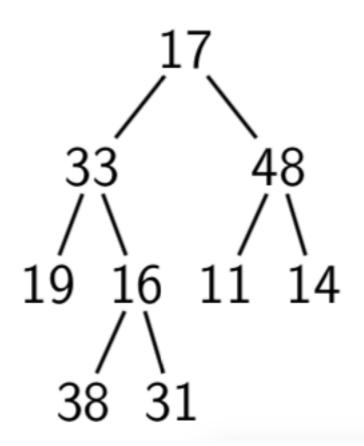


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Call Stack

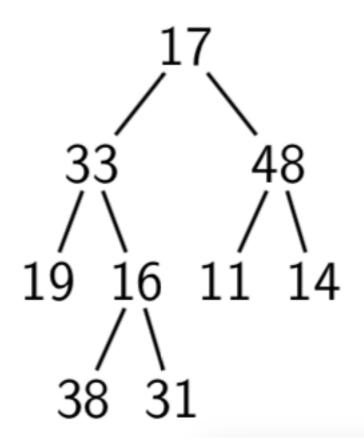


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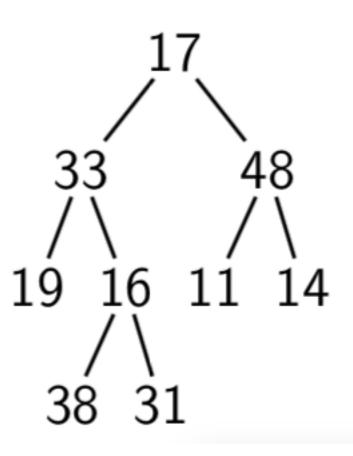
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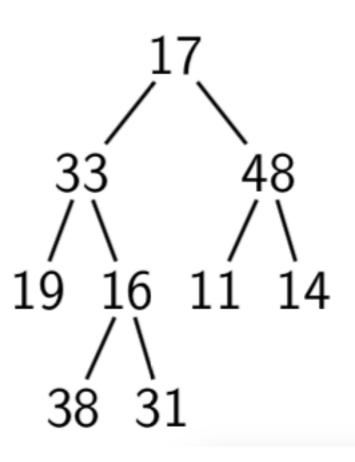
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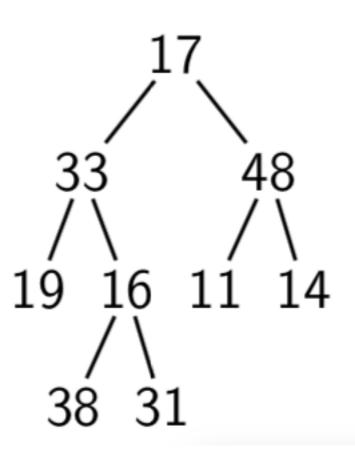
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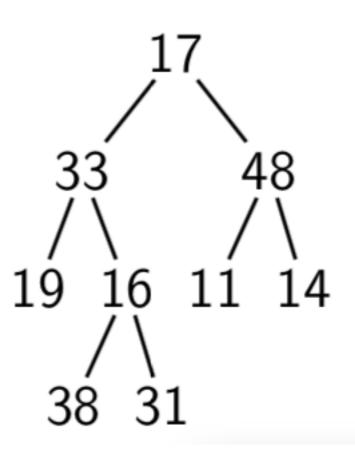
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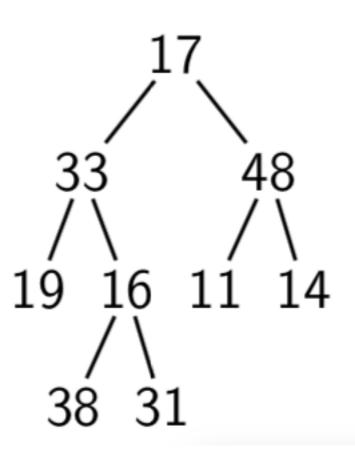
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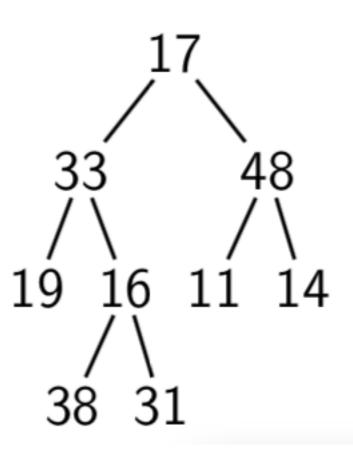
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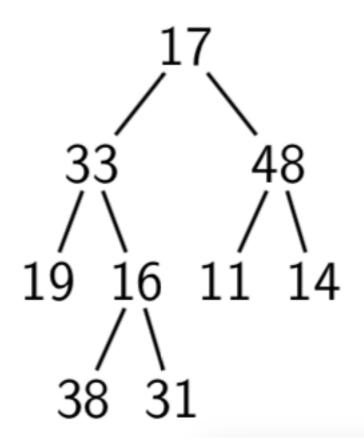


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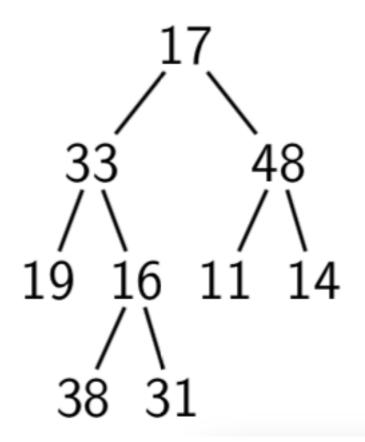


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INORDERTRAVERSE(17)



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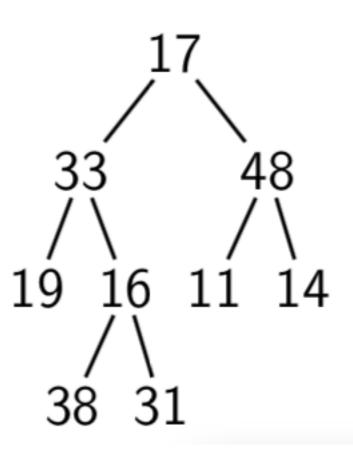
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INORDERTRAVERSE(17)





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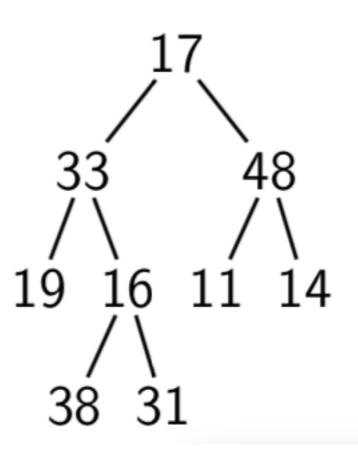
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INORDERTRAVERSE(31)

INORDERTRAVERSE(16)

INORDERTRAVERSE(33)

INORDERTRAVERSE(17)





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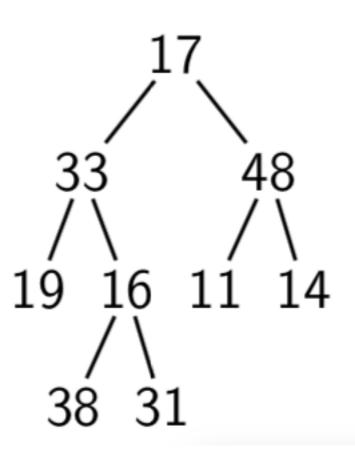
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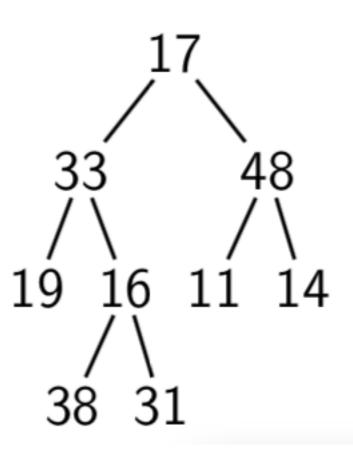
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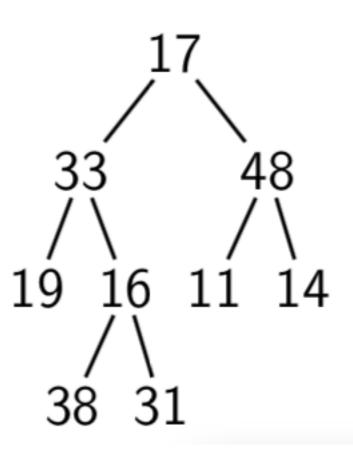
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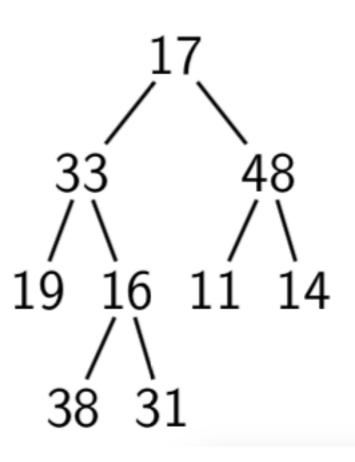
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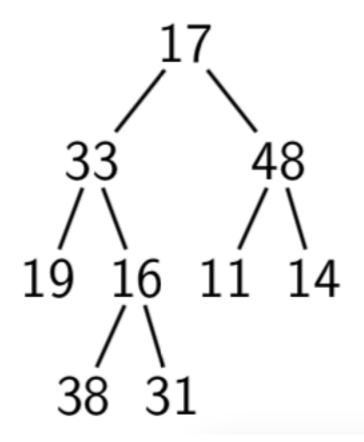


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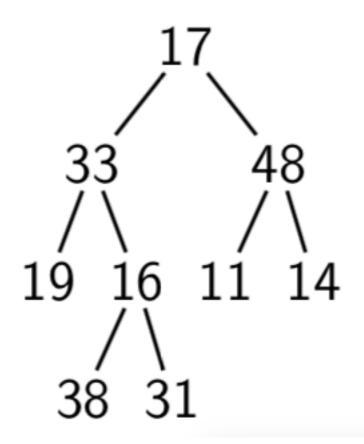


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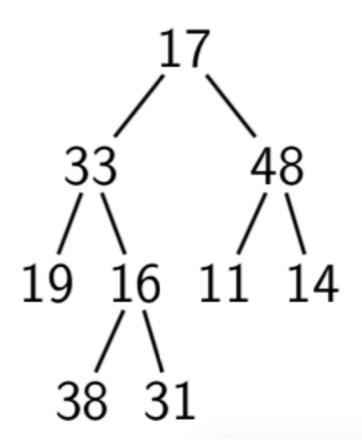


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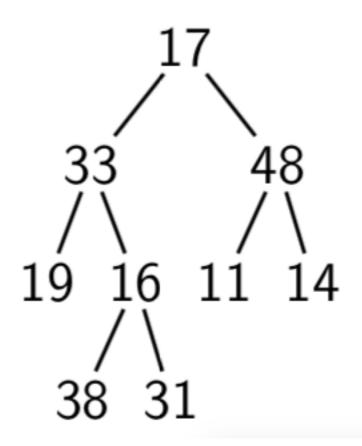


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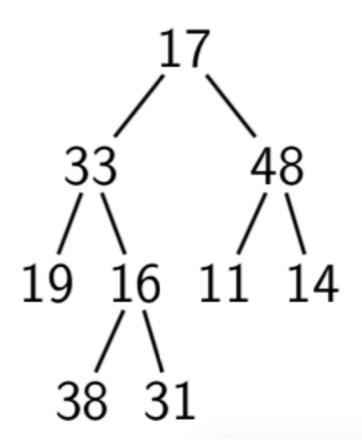


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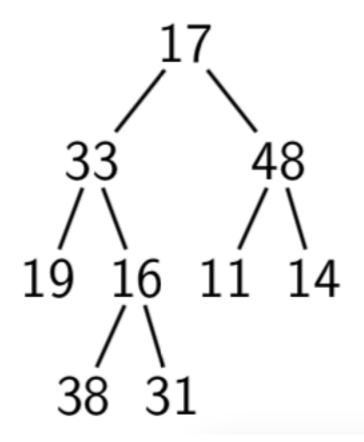


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INORDERTRAVERSE(17)



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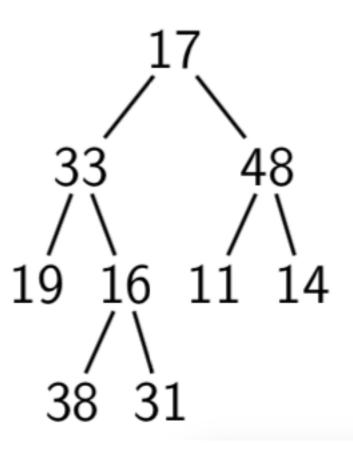
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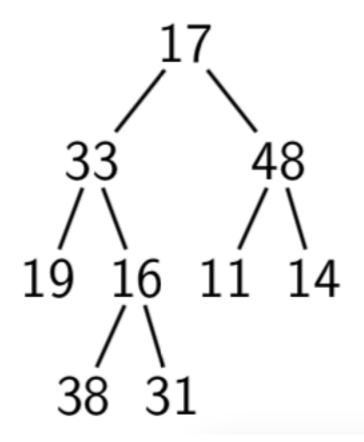


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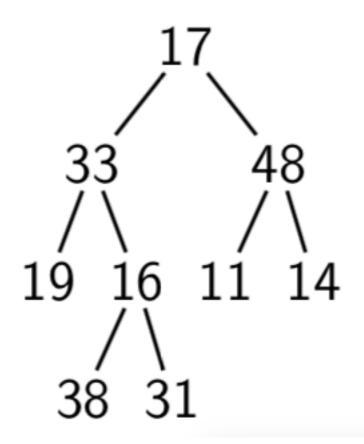


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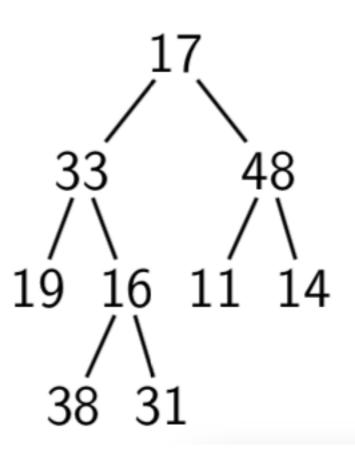
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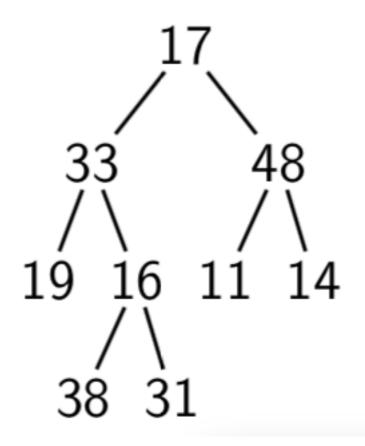


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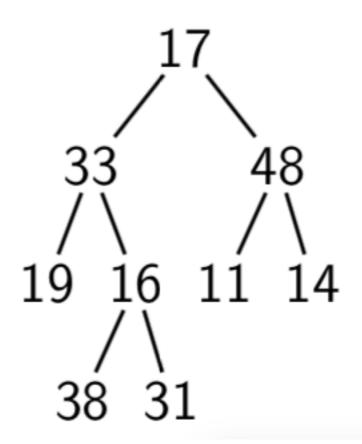


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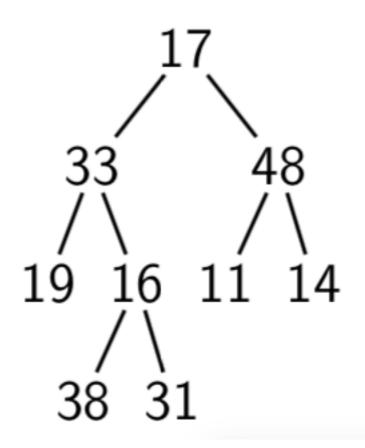


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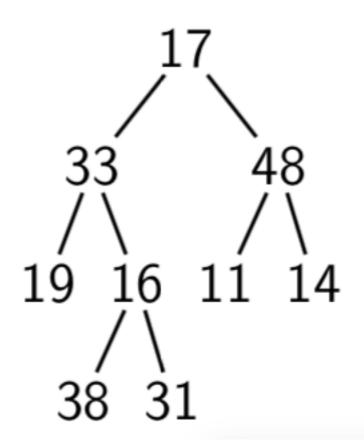


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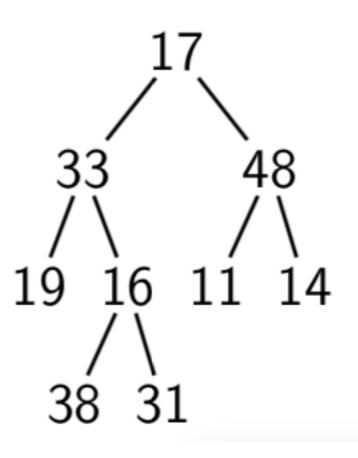
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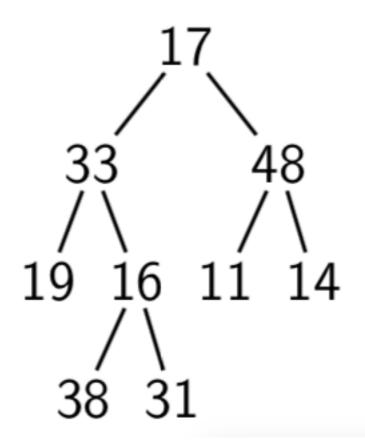


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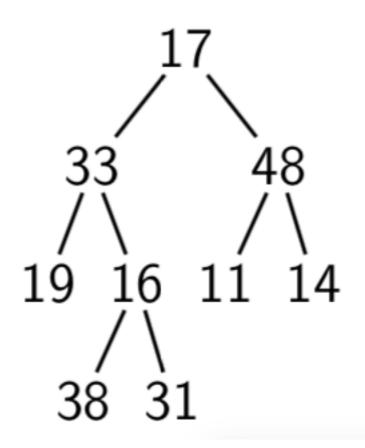


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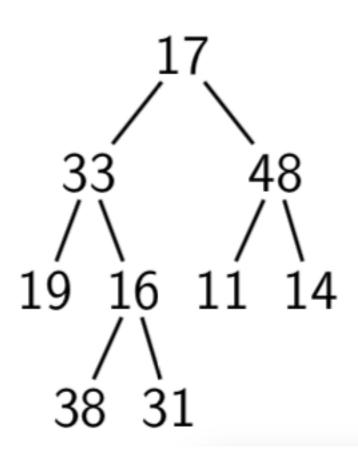
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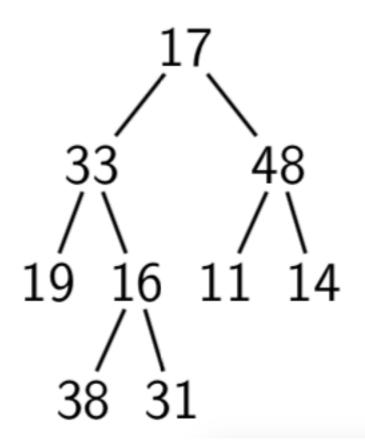


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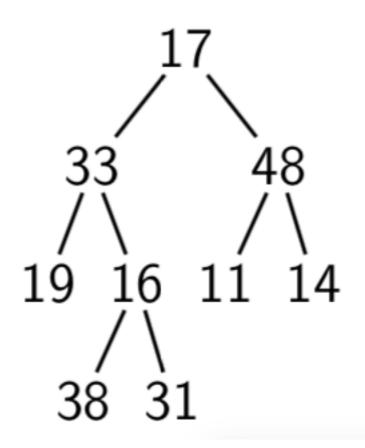


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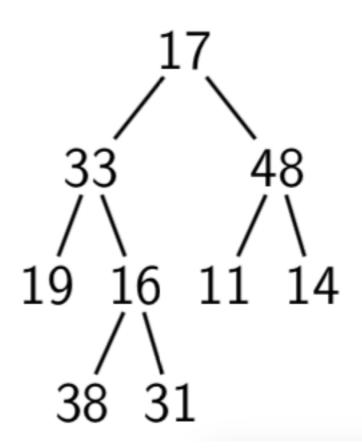


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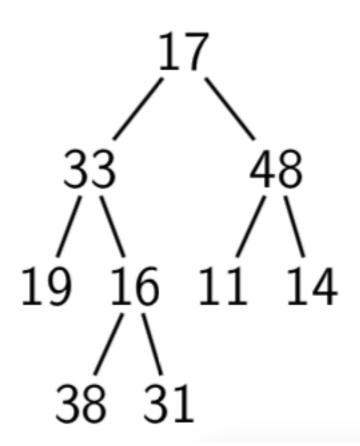


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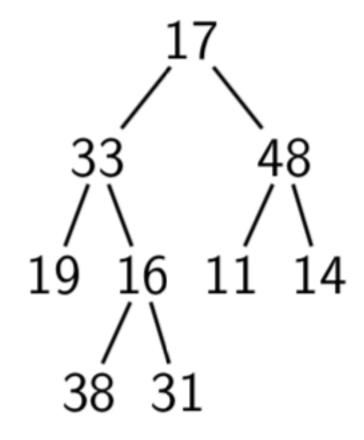


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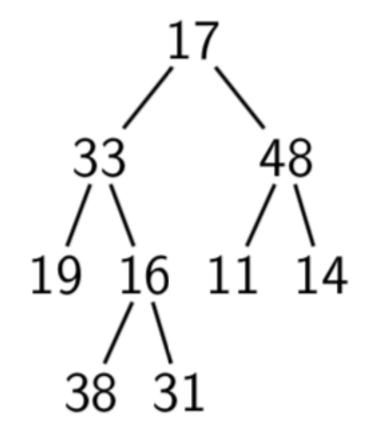


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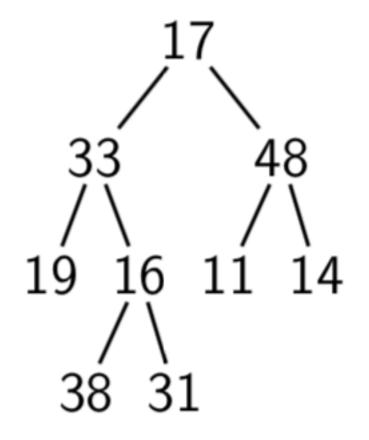


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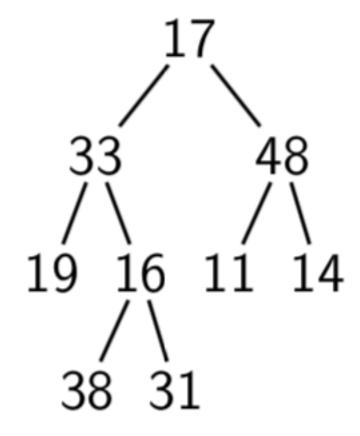


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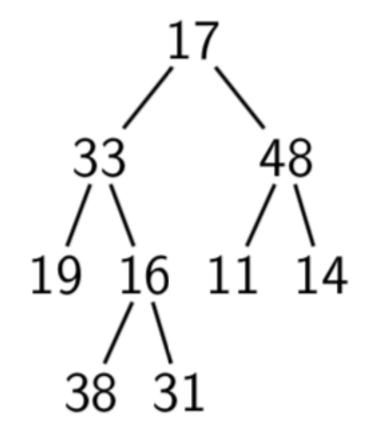


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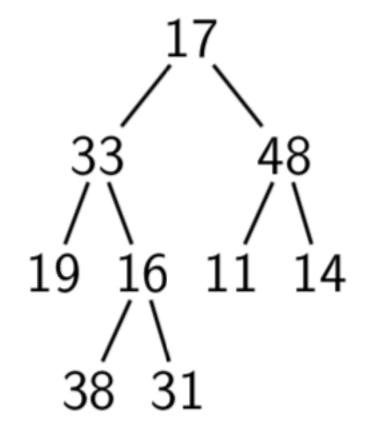


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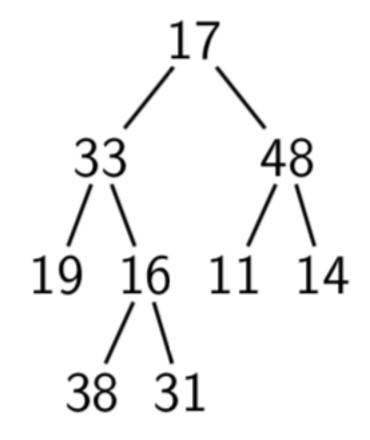


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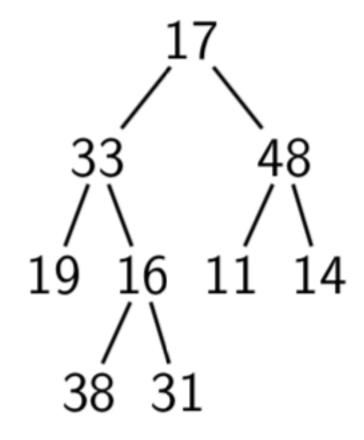


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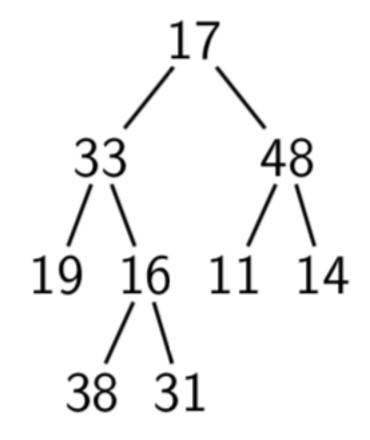


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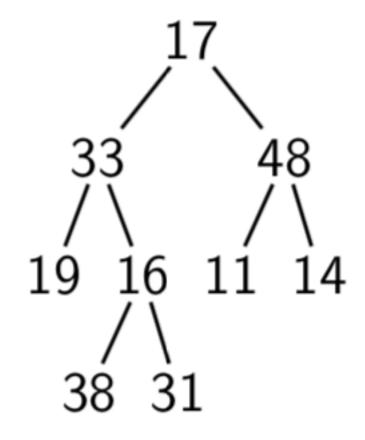


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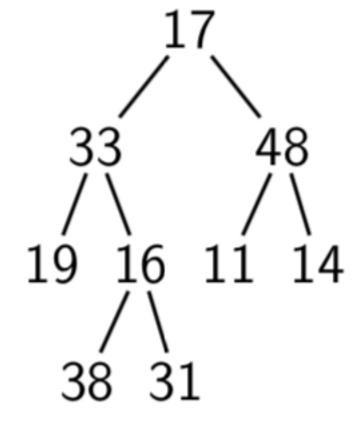


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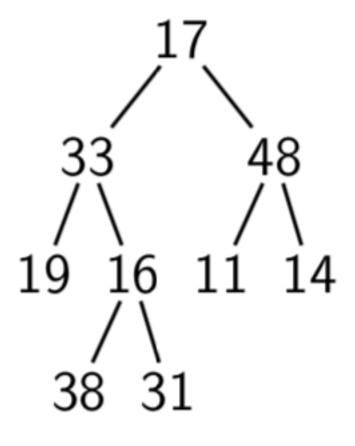
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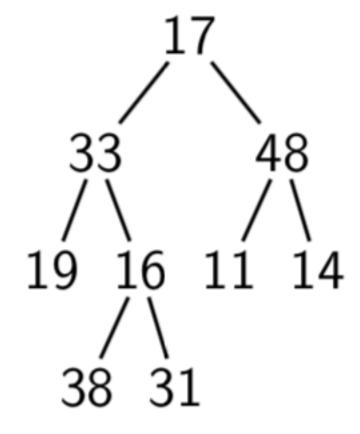


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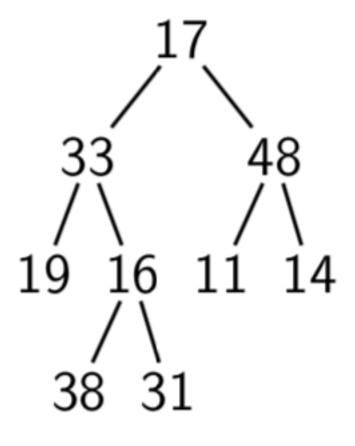
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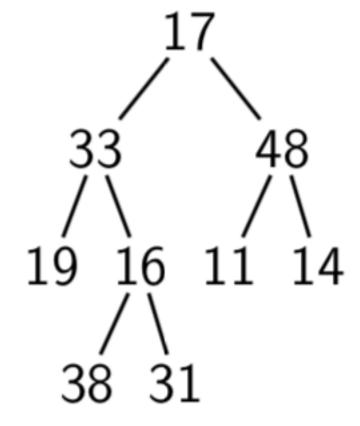


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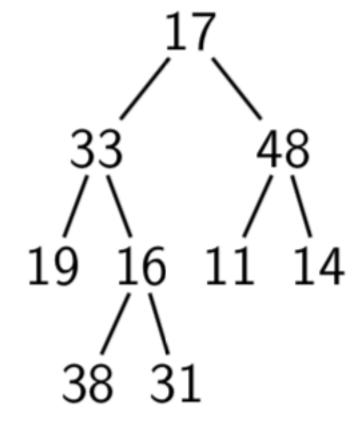


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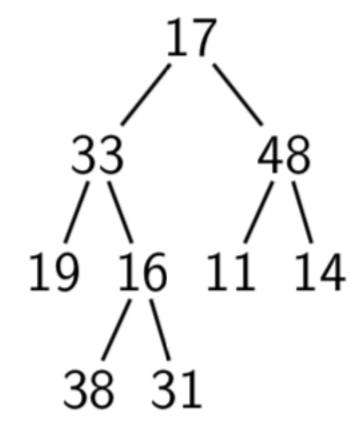


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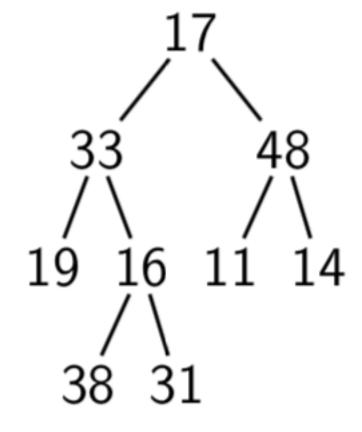


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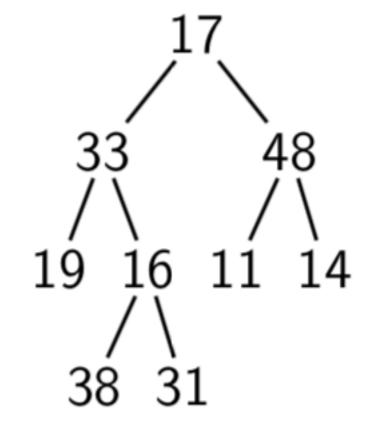


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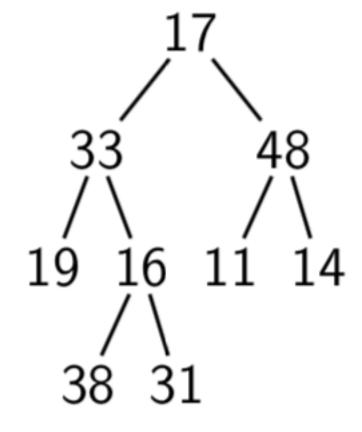


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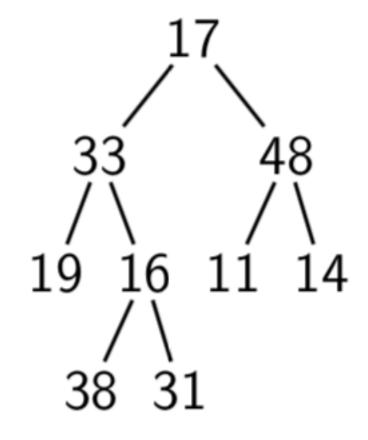


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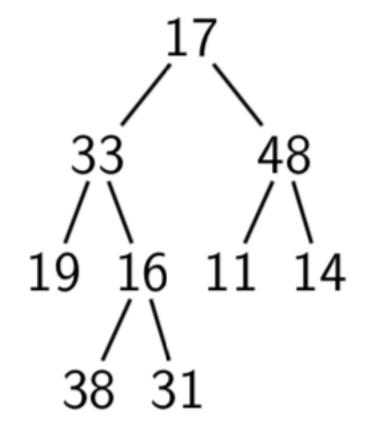


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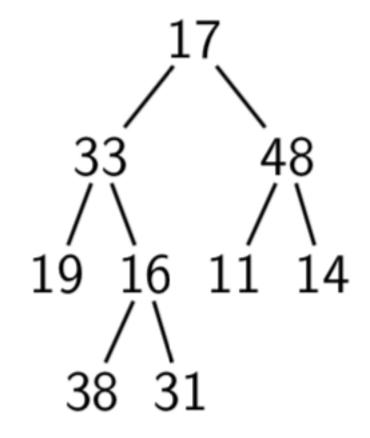


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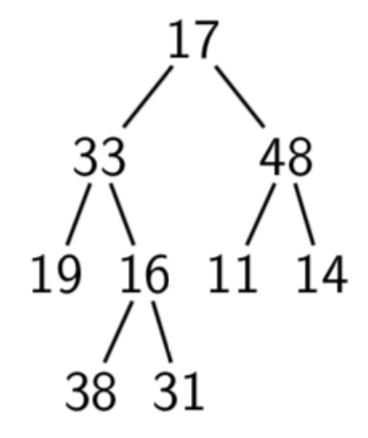


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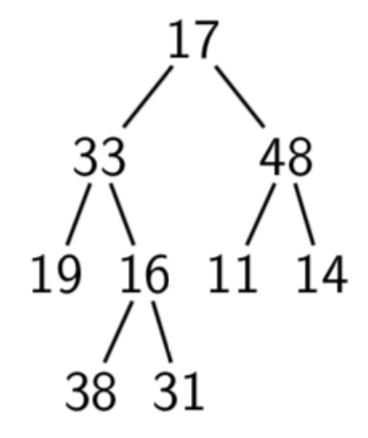


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PostorderTraverse(17)

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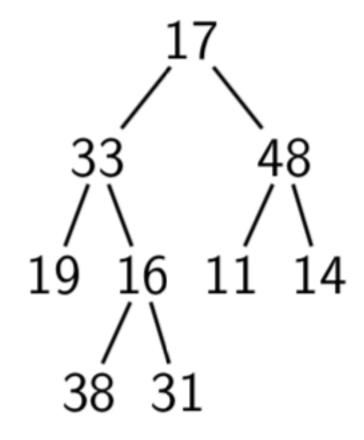


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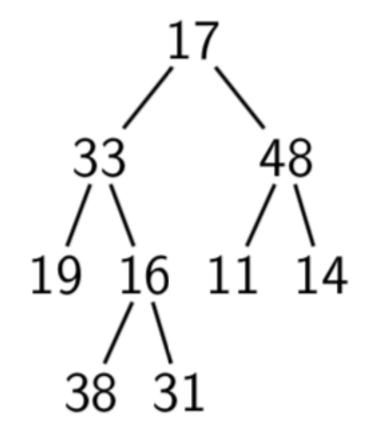


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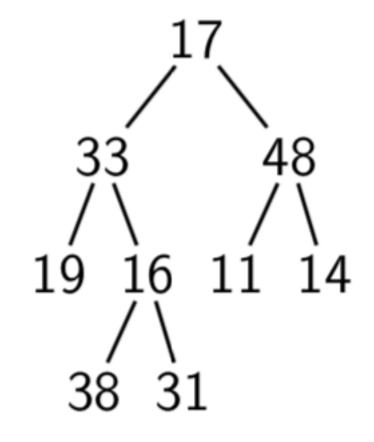


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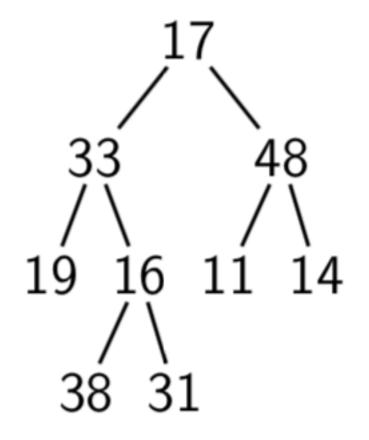


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PostorderTraverse(48)

PostorderTraverse(17)

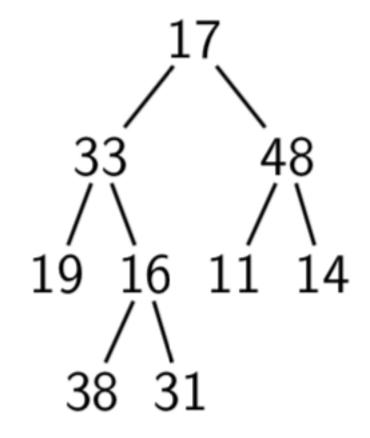


Visit order: 19 38 31 16 33 11

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PostorderTraverse(48)

PostorderTraverse(17)

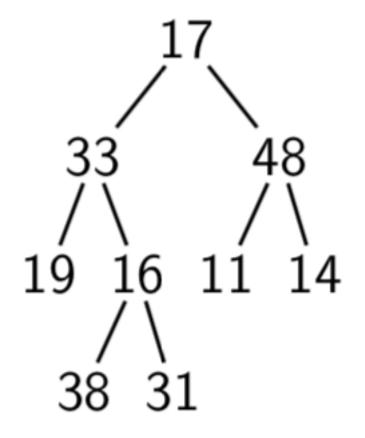


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PostorderTraverse(14)

PostorderTraverse(48)

PostorderTraverse(17)

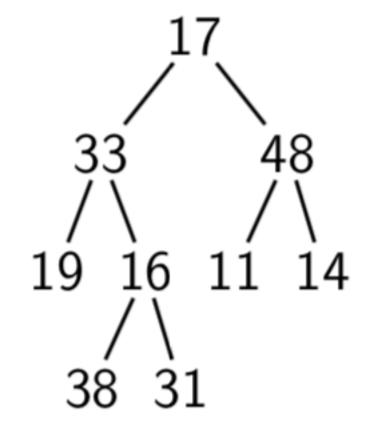


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PostorderTraverse(14)

PostorderTraverse(48)

PostorderTraverse(17)

Call Stack

(...skipping the calls to PostorderTraverse(null)...)

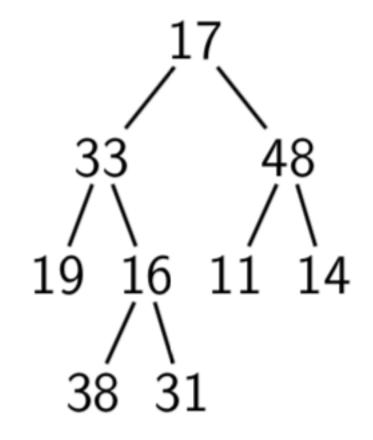


Visit order: 19 38 31 16 33 11 14

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PostorderTraverse(14)

PostorderTraverse(48)

PostorderTraverse(17)

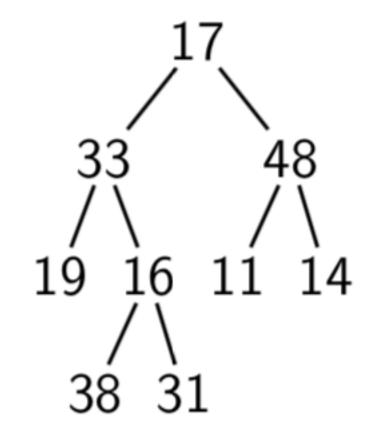


Visit order: 19 38 31 16 33 11 14

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PostorderTraverse(48) PostorderTraverse(17)

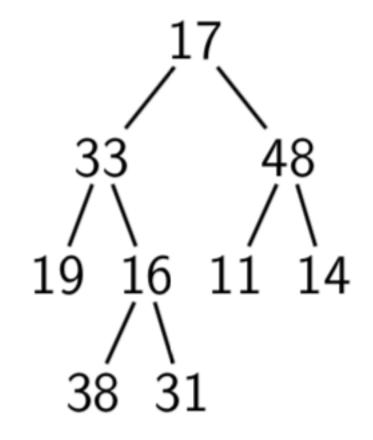


Visit order: 19 38 31 16 33 11 14 48

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PostorderTraverse(48)

PostorderTraverse(17)

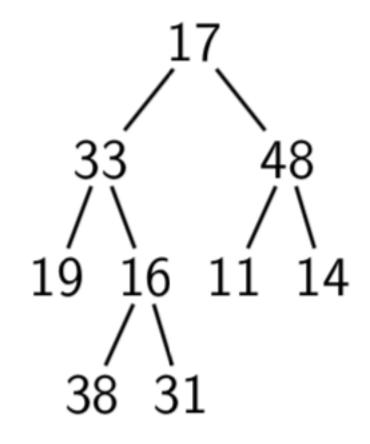


Visit order: 19 38 31 16 33 11 14 48

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PostorderTraverse(17)

Call Stack

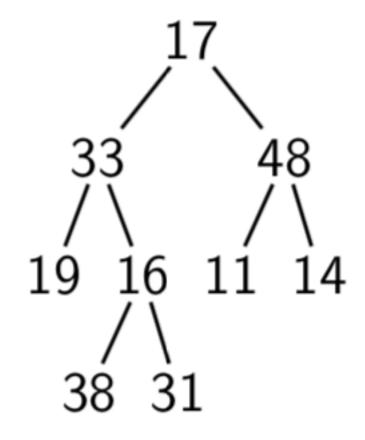


Visit order: 19 38 31 16 33 11 14 48 17

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PostorderTraverse(17)

Call Stack

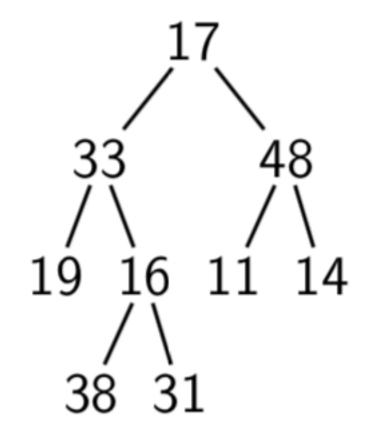


Visit order: 19 38 31 16 33 11 14 48 17

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Preorder Traversal Using a Stack



Explicitly maintain a stack of nodes

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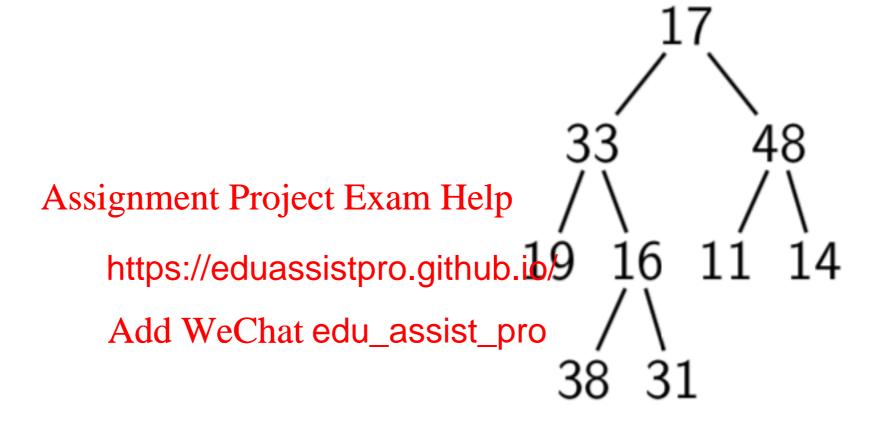
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 In an implementation, the elements placed onto the stack would not be whole trees, but **pointers** to the corresponding internal nodes



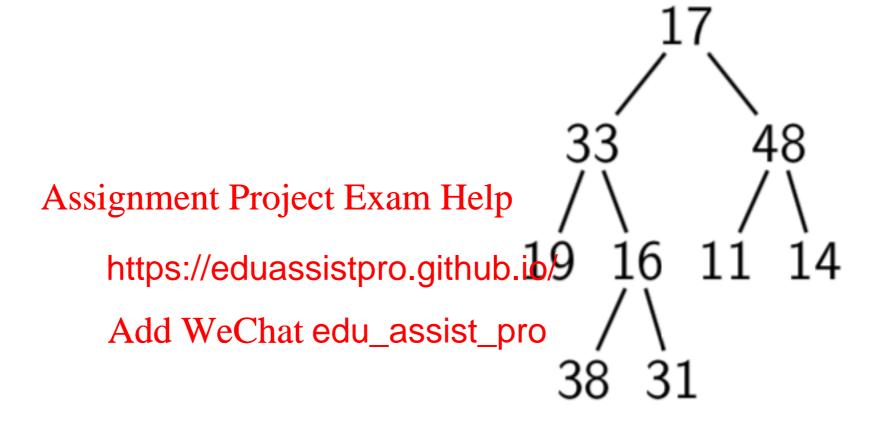
Replace the stack with a queue



Queue:



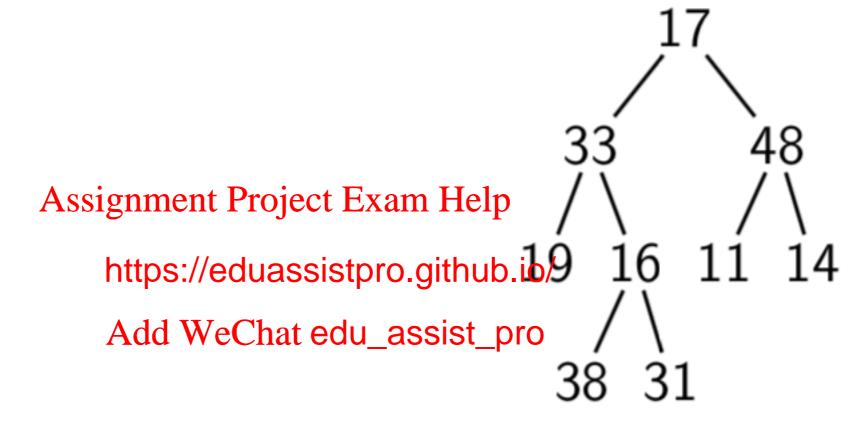
Replace the stack with a queue



Queue: 17



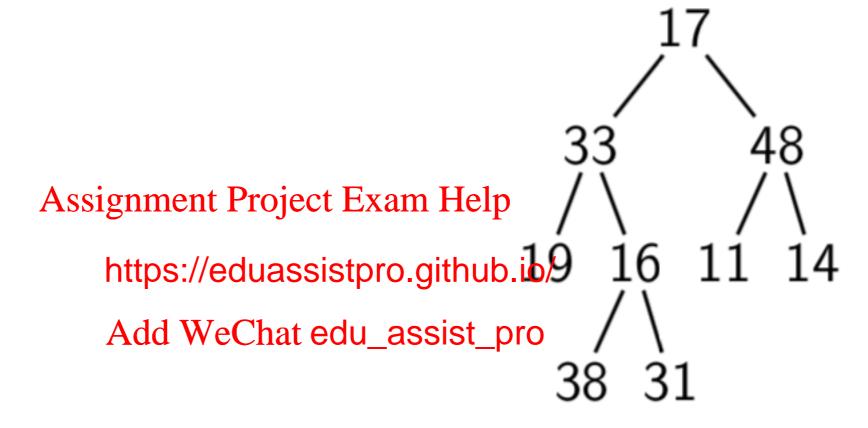
Replace the stack with a queue



Queue:



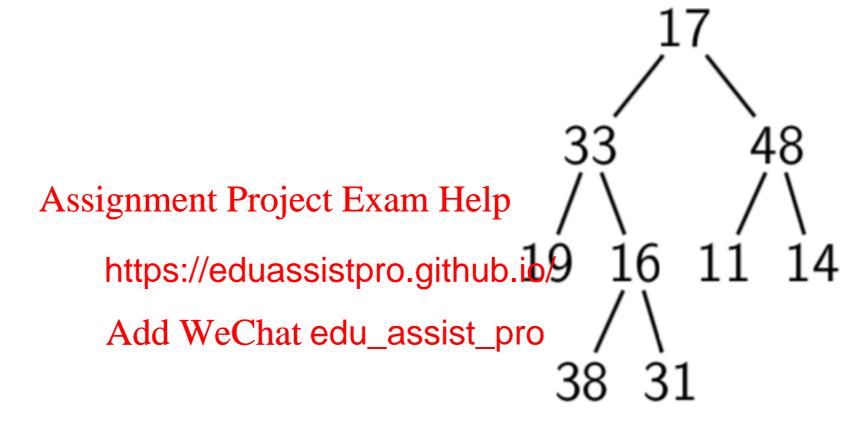
Replace the stack with a queue



Queue:



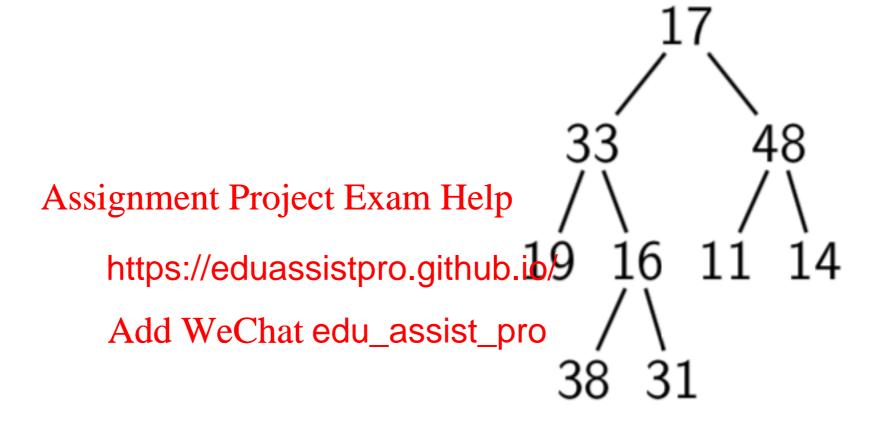
Replace the stack with a queue



Queue: 33



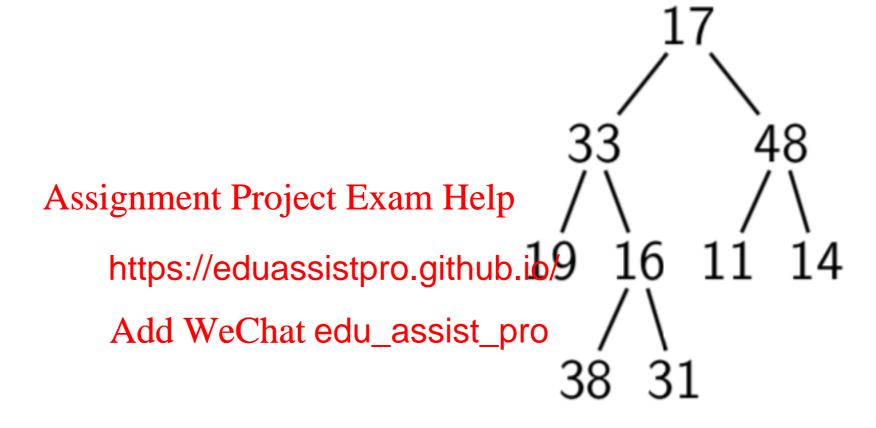
Replace the stack with a queue



Queue: 33 48



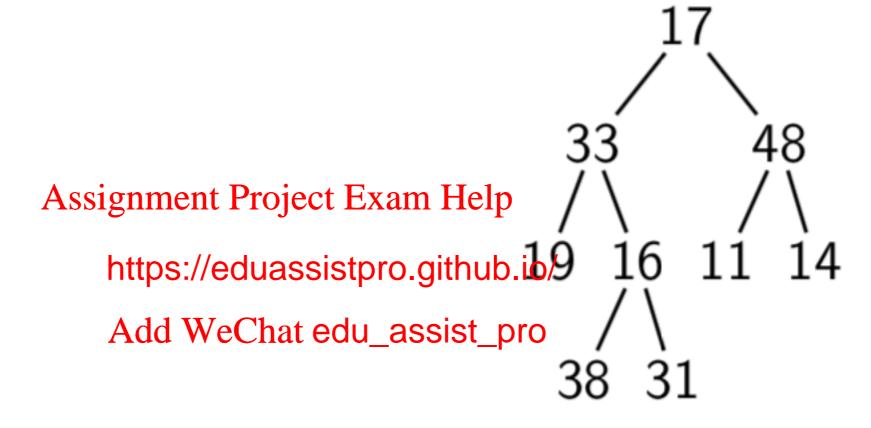
Replace the stack with a queue



Queue: 48



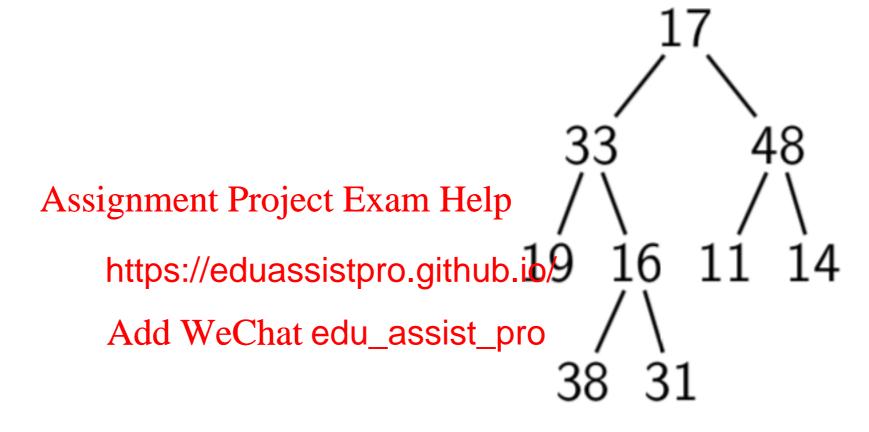
Replace the stack with a queue



Queue: 48



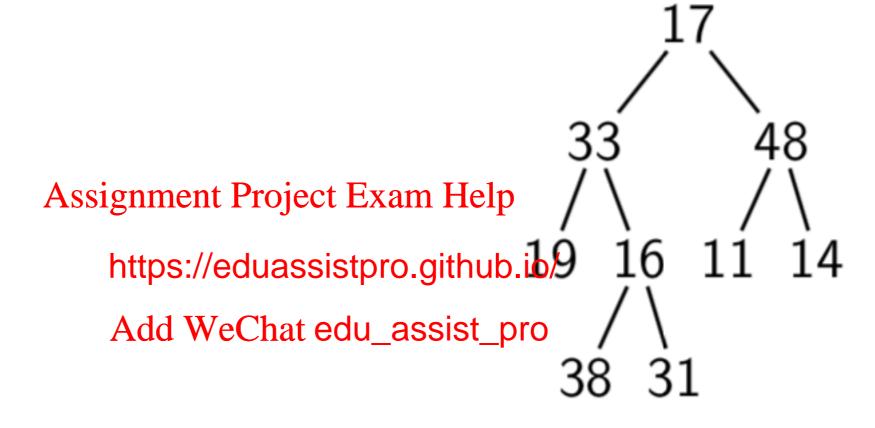
Replace the stack with a queue



Queue: 48 19



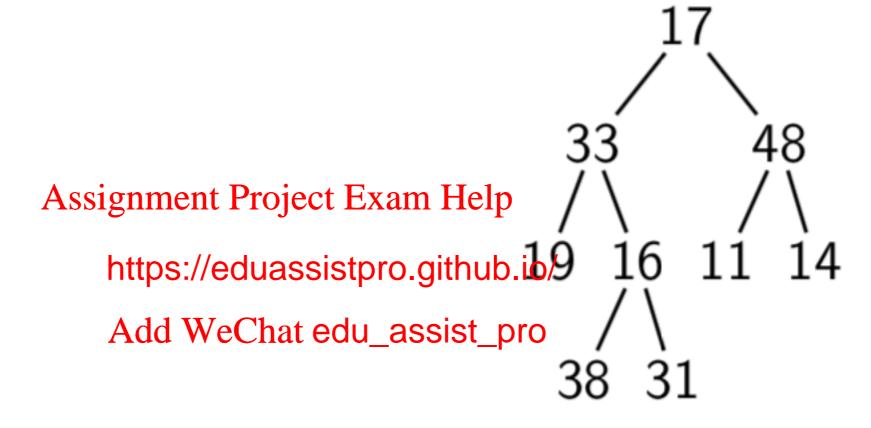
Replace the stack with a queue



Queue: 48 19 16



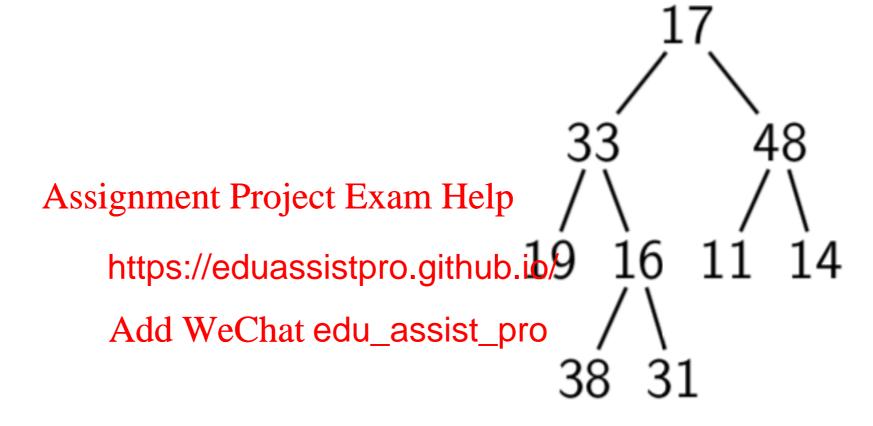
Replace the stack with a queue



Queue: 19 16



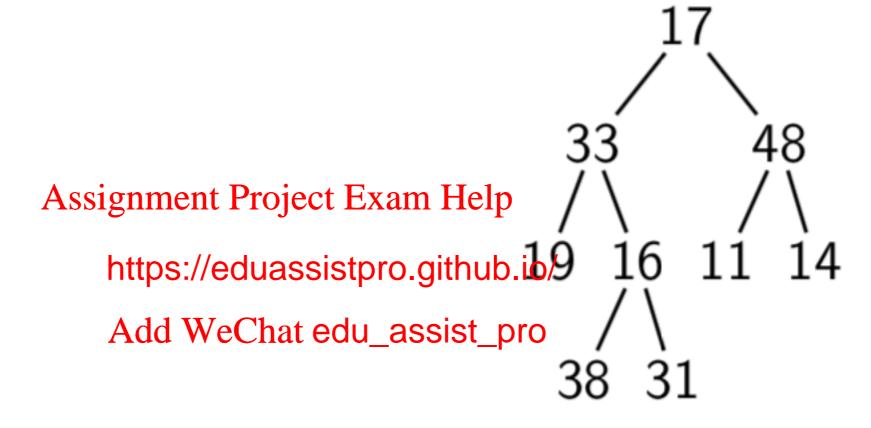
Replace the stack with a queue



Queue: 19 16



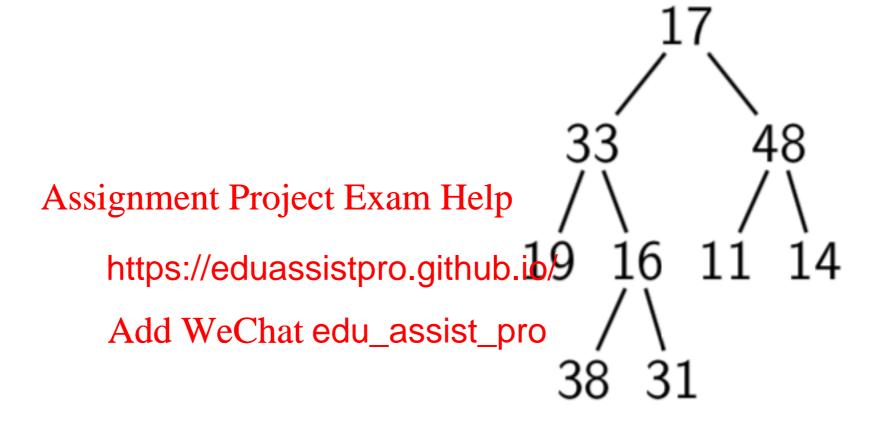
Replace the stack with a queue



Queue: 19 16 11



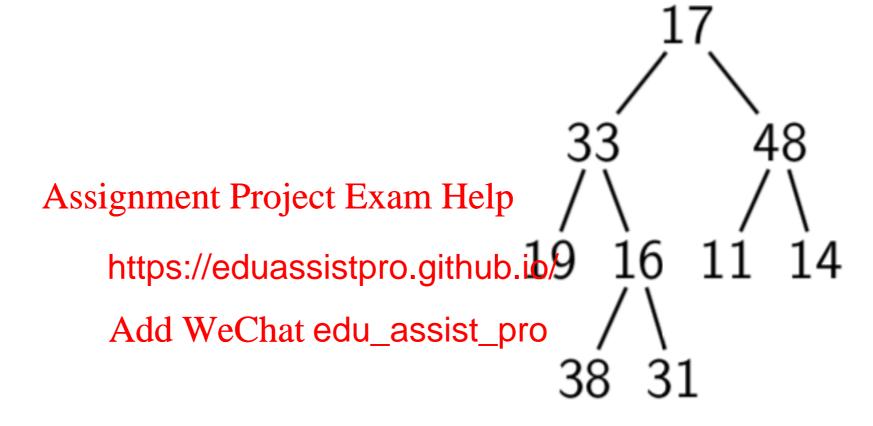
Replace the stack with a queue



Queue: 19 16 11 14



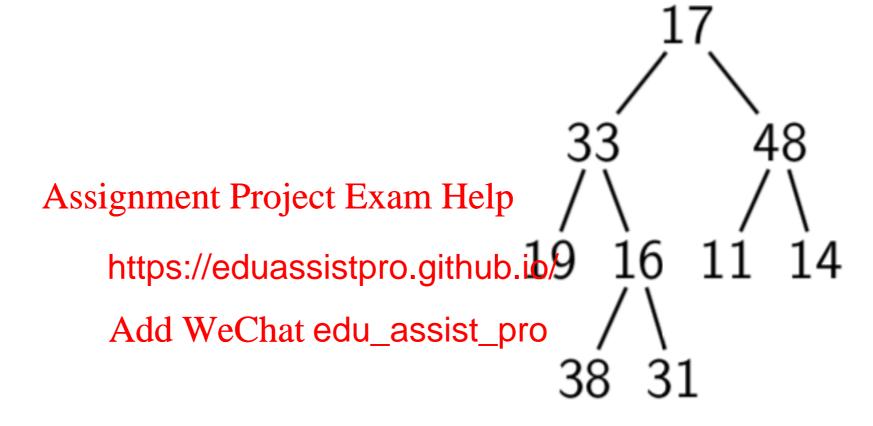
Replace the stack with a queue



Queue: 16 11 14



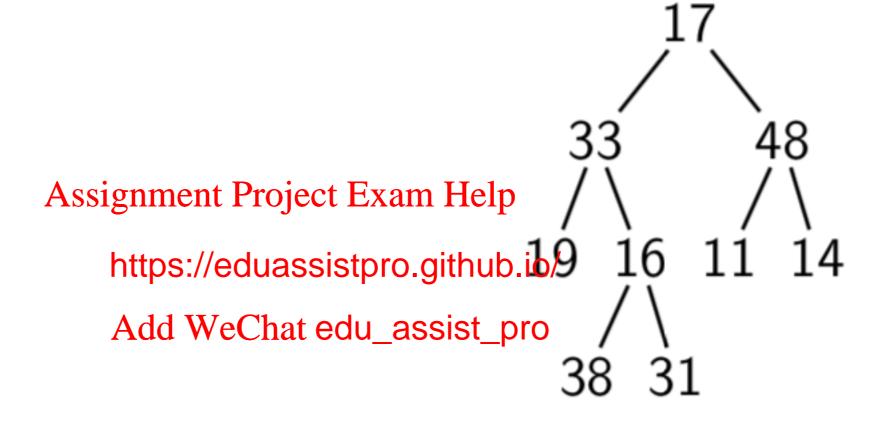
Replace the stack with a queue



Queue: 16 11 14



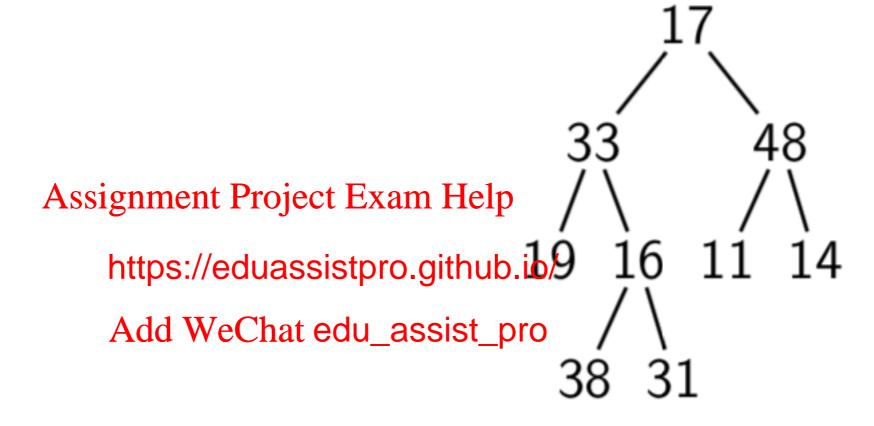
Replace the stack with a queue



Queue: 11 14



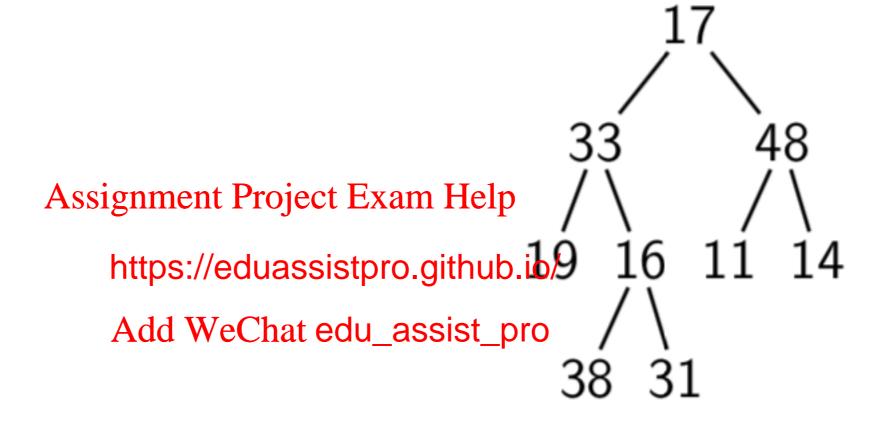
Replace the stack with a queue



Queue: 11 14



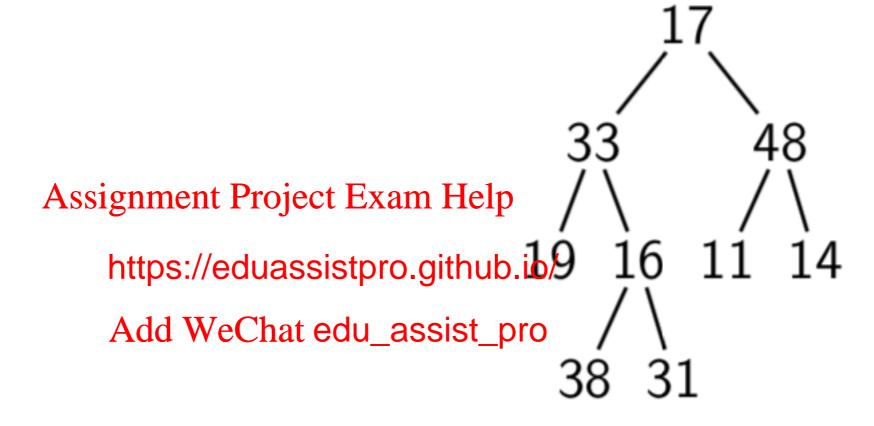
Replace the stack with a queue



Queue: 11 14 38



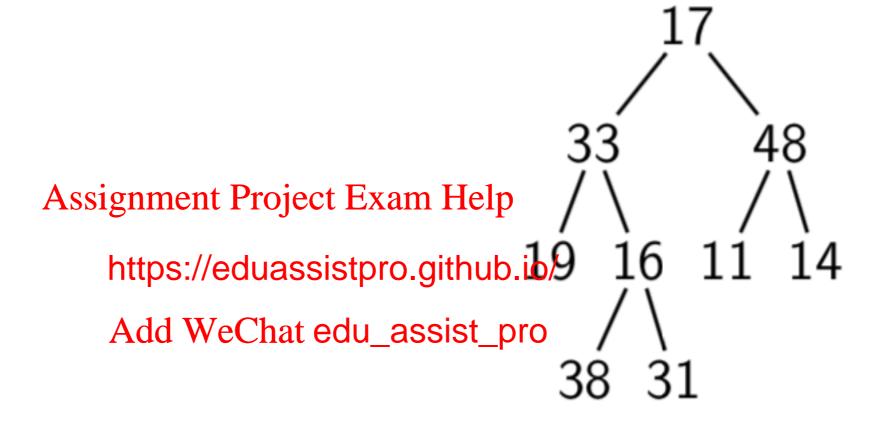
Replace the stack with a queue



Queue: 11 14 38 31



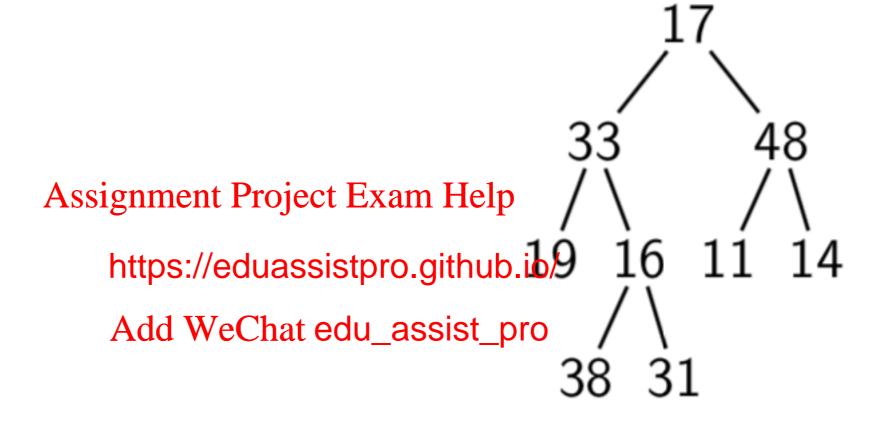
Replace the stack with a queue



Queue: 14 38 31



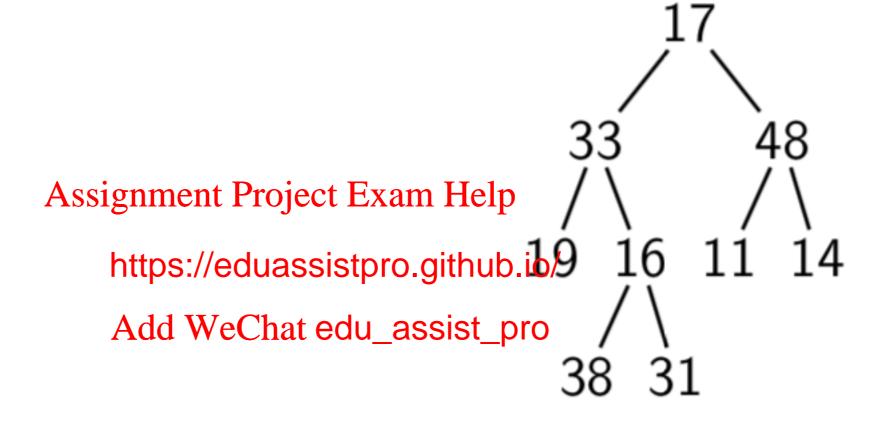
Replace the stack with a queue



Queue: 14 38 31



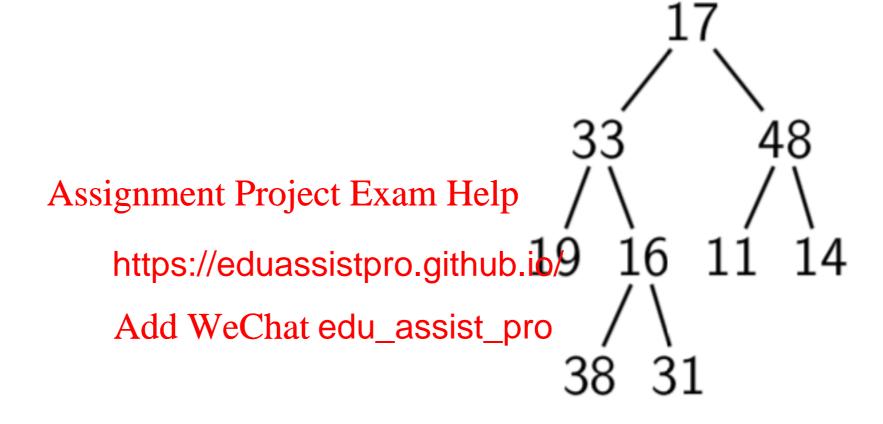
Replace the stack with a queue



Queue: 38 31



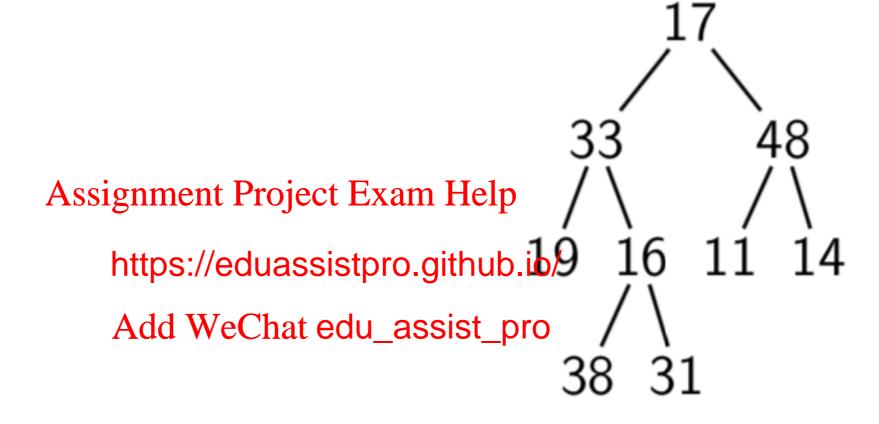
Replace the stack with a queue



Queue: 38 31



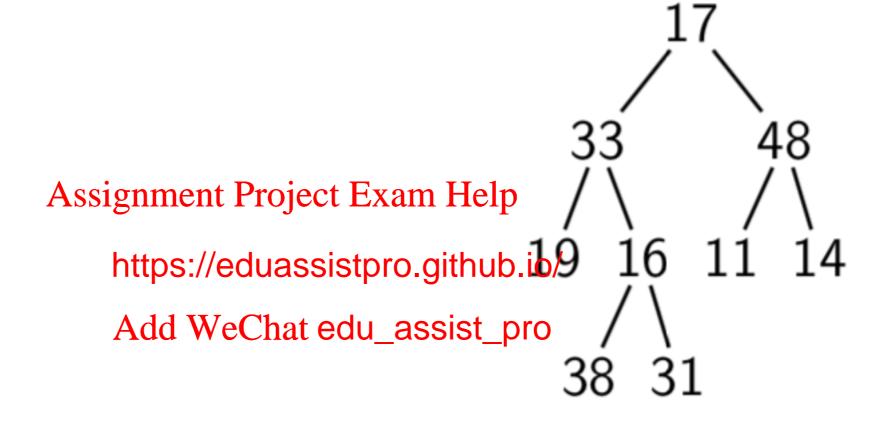
Replace the stack with a queue



Queue: 31



Replace the stack with a queue

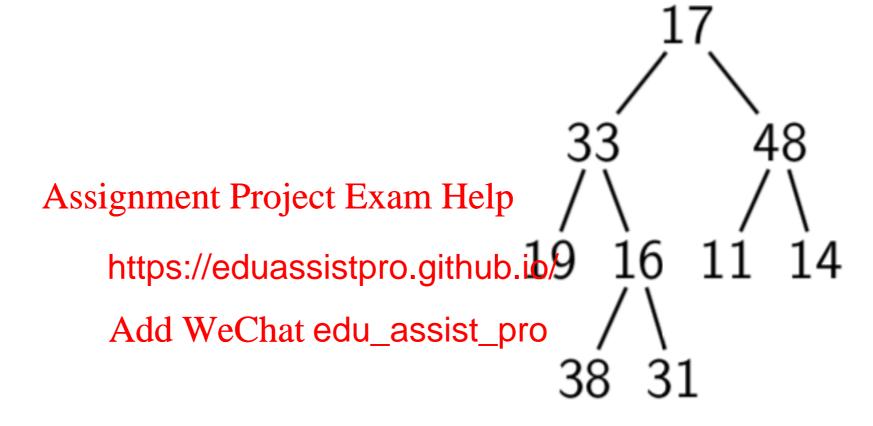


Queue: 31

Traversal order: 17 33 48 19 16 11 14 38



Replace the stack with a queue

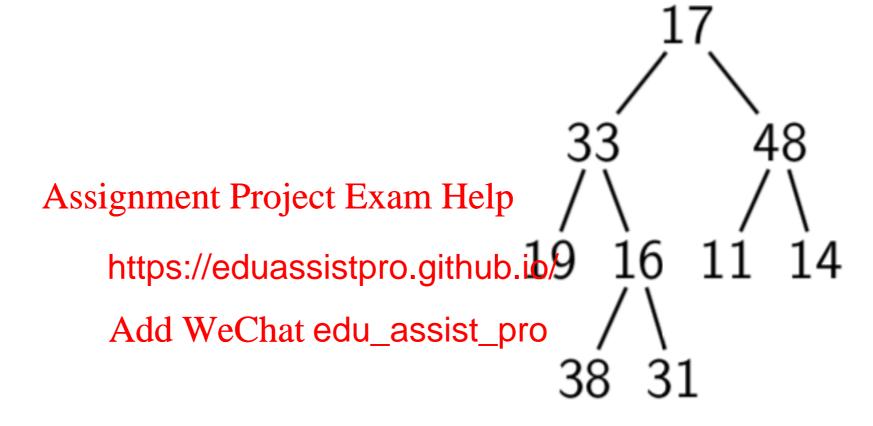


Queue:

Traversal order: 17 33 48 19 16 11 14 38



Replace the stack with a queue



Queue:

Traversal order: 17 33 48 19 16 11 14 38 31

Closest Pair Problem (2D) Revisited (see Lecture 5)



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- In Lecture 5 we gave a brute-force algorithm for the closest pair problem: Given n points in the Cartesian plane, find a pair with minimal distance.
- The brute-force method had complexity $\Theta(n^2)$. We can use divide-and-con Project Exam Help namely $\Theta(n \log n)$.

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- First, sort the points www.ahaeedu_assistrenthe result in array byX. Also sort the points by y value and store the result in array byY.
- Now we can identify the x median, and recursively process the set P_L of points with lower x values, as well as the set P_R with higher x values.



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- The recursive calls will identify d_L , the shortest distance for pairs in P_L , and d_R , the shortest distance for pairs in P_R .
- Let m be the x median and let $d = min(d_L, d_R)$. This d is a candidate for the smallest distance.

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• But d may not be the g re could be some close pair whose points are https://eduassistpro.githubile/dian line x = m.

- For candidates that may improve on d we only need to look at those in the band $m d \le x \le m + d$.
- So pick out, from array byY, each point p with x-coordinate between m-d and m+d, and keep these in array S.
- For each point in S, consider just its "close" neighbours in S.



• The following calculates the smallest distance and leaves the (square of the) result in *minsq*.

• It can be shown that the while loop can execute at most spring Earth Plalue—see diagram. https://eduassistpro.github.io/

You're Learning Heaps!



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Next up: Priority

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