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COMP90038
Algorithms and Complexity

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Lectur https://eduassistpro.github.io/ ethods

(with thanks to Hara Add WeChat edu_assist_pro ergaard)

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DMD 8.17 (Level 8, Doug McDonell Bldg)

http://people.eng.unimelb.edu.au/tobym

@tobycmurray

Compulsory Quizzes

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- **Remember:** you need to **complete** 8 of the quizzes to pass the hurdle

- By "completing" a quiz, we mean **getting all answers right (i** Assignment Project Exam Help **ting**

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- You can have as many att Add WeChat edu_assist_pro s you need, but on at least one of those attempts you need to score 100%

- The first compulsory quiz (for week 2) closes **tomorrow**

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Brute Force Algorithms

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- Straightforward problem solving approach, usually based directly on the problem's statement.

- Exhaustive search for solutions is a prime example.
  - Selection sort
  - String matching
  - Closest pair
  - Exhaustive search for combinatorial solutions
  - Graph traversal

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Example: Selection Sort

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// sw and A[min]

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Example: Selection Sort

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Time Complexity:

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Example: Selection Sort

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Time Complexity: $\Theta(n^2)$

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Example: Selection Sort

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Time Complexity: $\Theta(n^2)$

We will soon meet better sorting algorithms

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Properties of Sorting Algorithms

- A Sorting algorithm is:
  - **in-place** if it does not require additional memory except, perhap s of memory
  - **stable** if it preserves the order of elements with identical keys
  - **input-insensitive** if its running time is fairly independent of input properties other than size

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Properties of Selection Sort

- While running time is quadratic, selection sort makes only about ***n*** **exchanges**.

- So: **selection sort is a good algorithm for sorting small collection** [illegible] **ds.**

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- In-place?

- Stable?

- Input-insensitive?

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Properties of Selection Sort

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- In-place? yes
- Stable?
- Input-insensitive?

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- In-place? yes

- Stable? ?

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- In-place? yes

- Stable? ?

- Input-insensitive? yes

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Selection Sort Stability

key: 4 val: ab	key: 3 val: bc	key: 4 val: de	key: 3 val: fg
0	1	2	

↑
A[i]

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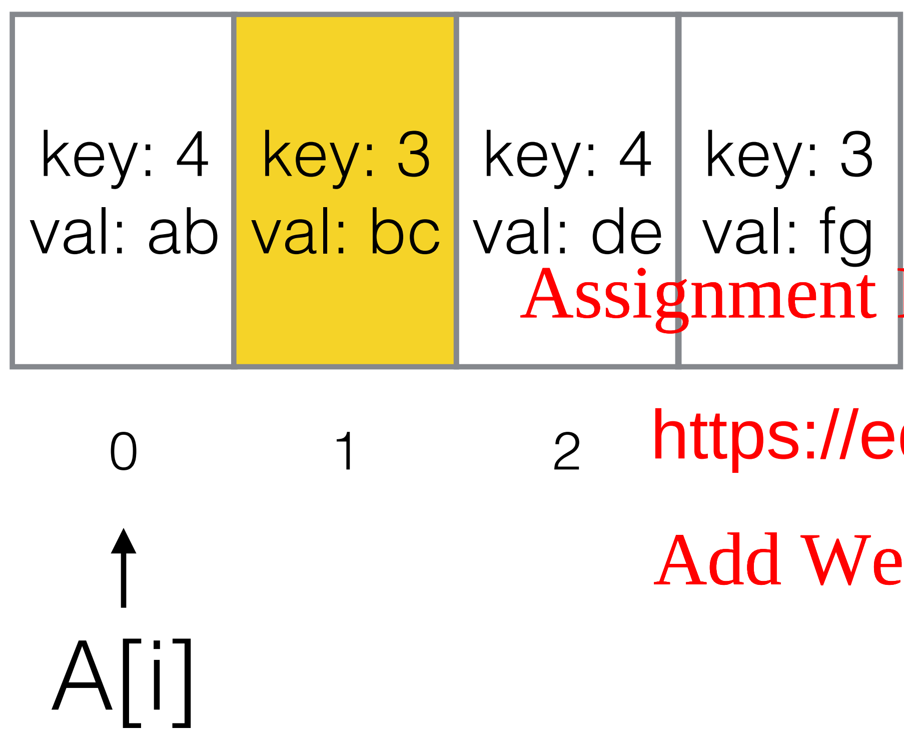
Selection Sort Stability



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A[i]

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Selection Sort Stability

0	1	2	3
key: 3 val: bc	key: 4 val: ab	key: 4 val: de	key: 3 val: fg

↑
A[i]

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Selection Sort Stability

key: 3 val: bc	key: 3 val: fg	key: 4 val: de	key: 4 val: ab
0	1	2	

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A[i]

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Selection Sort Stability

key: 3 val: bc	key: 3 val: fg	key: 4 val: de	key: 4 val: ab

0 1 2

↑
A[i]

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the relative order
of the two "4" records
has changed!

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- While running time is quadratic, selection sort makes only about ***n*** **exchanges**.

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- In-place? yes

- Stable? no

- Input-insensitive? yes

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Brute Force String Matching

- **Pattern** *p*: a string of *m* characters to search **for**
- **Text** *t*: a long string of *n* characters to search **in**
- We use *i* to run through the text and *j* to run through the pattern

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Brute Force String Matching

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t:

N	O	B	O	D	Y		K	N	O	W	S	
0	1	2	3	4	5	6	7	8	9	10	11	m

p:

N	O	T	
0	1	2	n

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Brute Force String Matching

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t[i]

↓

	0	1	2	3	4	5	6	7	8	9	10	11	m
t:	N	O	B	O	D	Y		K	N	O	W	S	

	0	1	2	n
p:	N	O	T	

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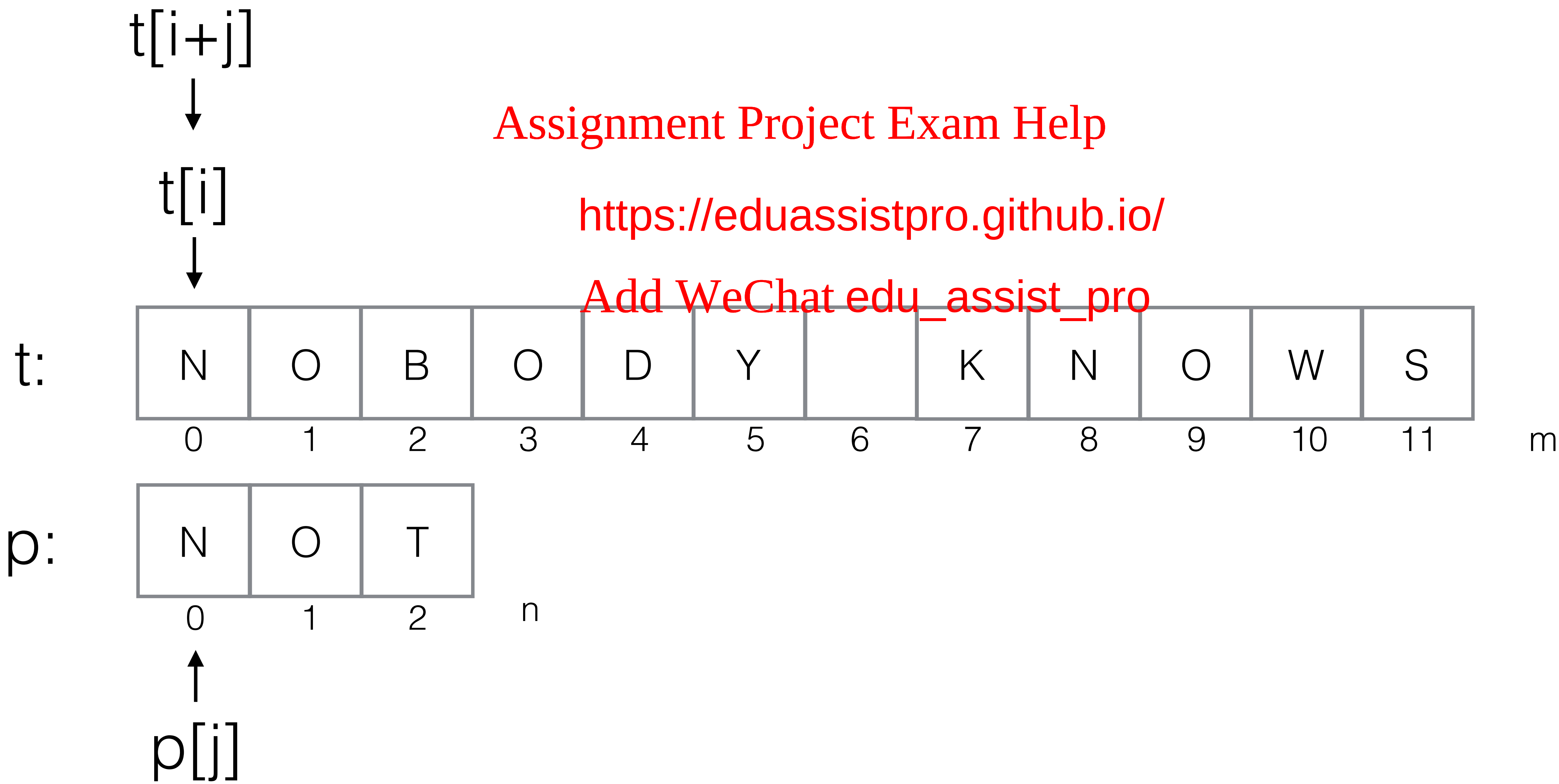
Brute Force String Matching



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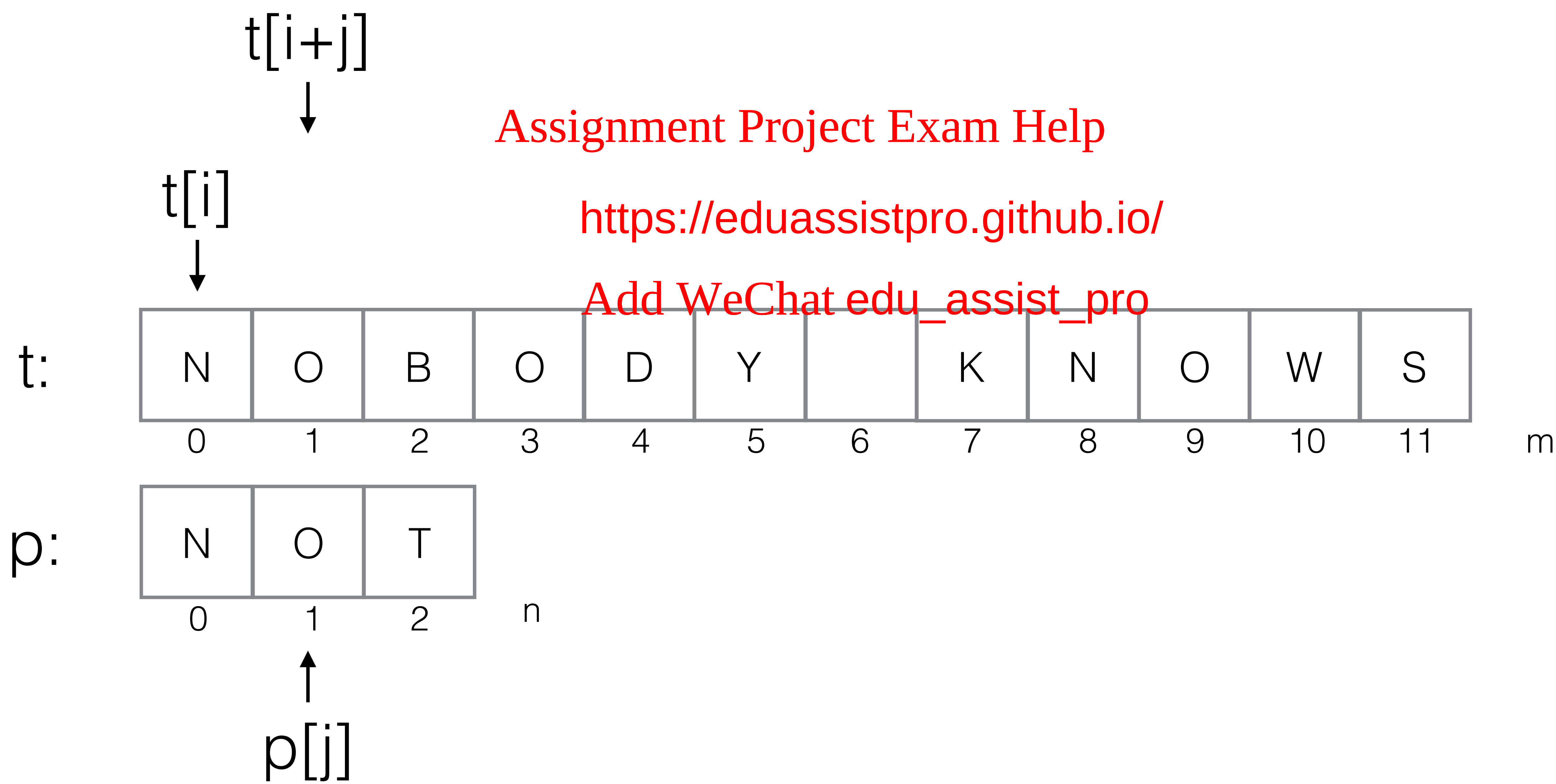

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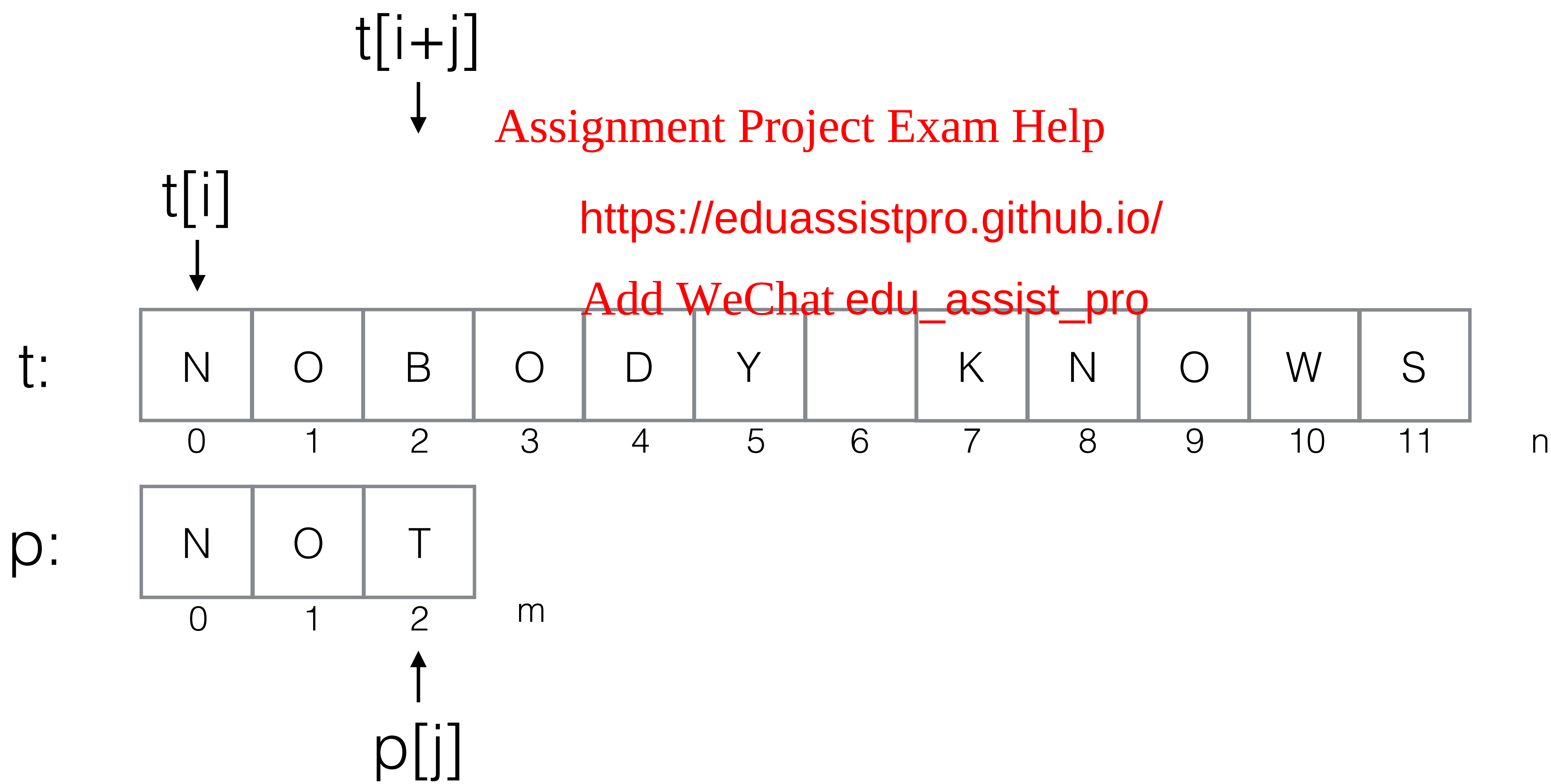
Brute Force String Matching



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Brute Force String Matching

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t[i]

↓

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	0	1	2	m

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Brute Force String Matching

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t[i]

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Brute Force String Matching

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t[i]

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0	1	2	3	4	5	6	7	8	9	10	11	n

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N	O	T	
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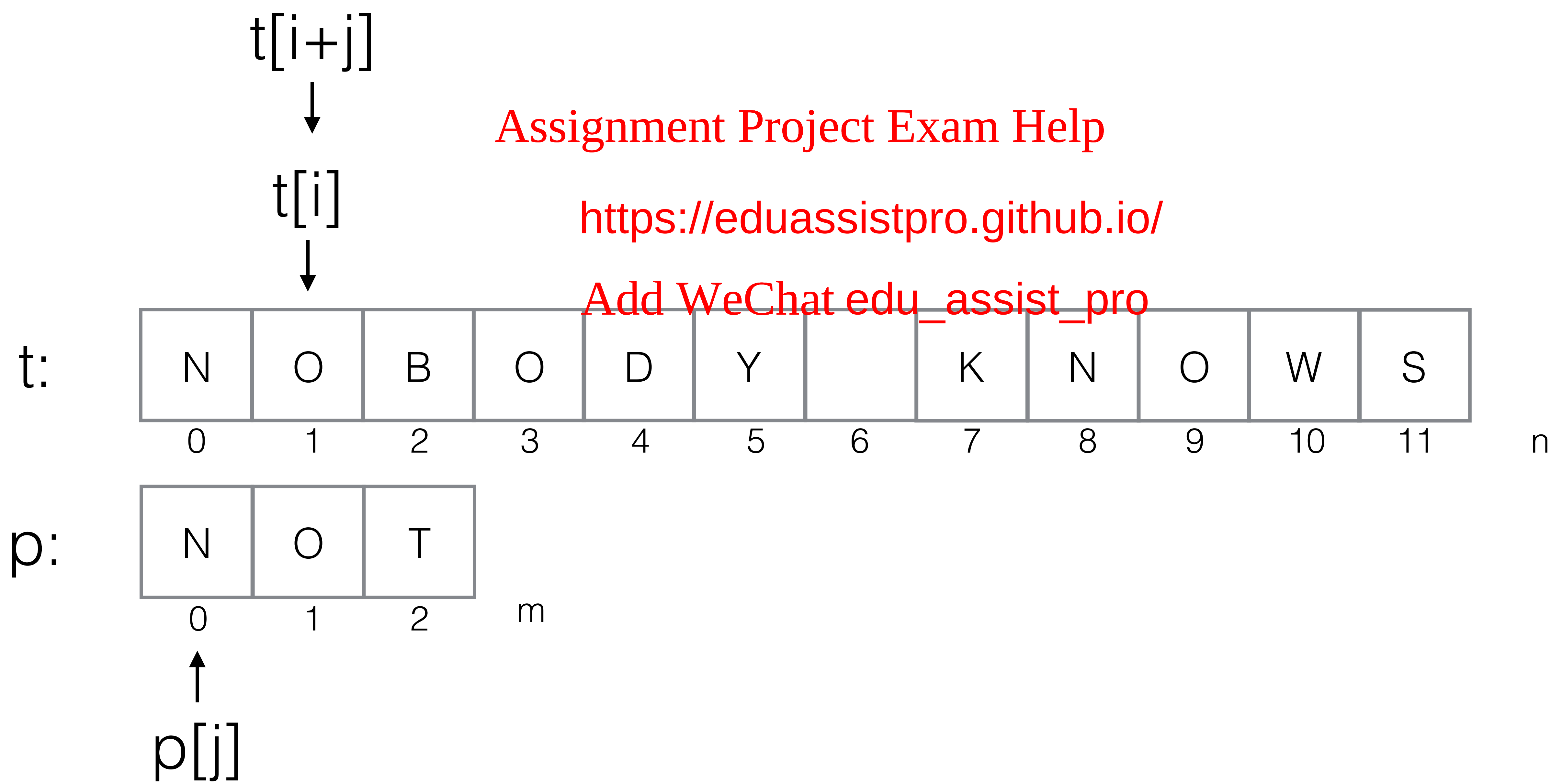
Brute Force String Matching



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Brute Force String Matching

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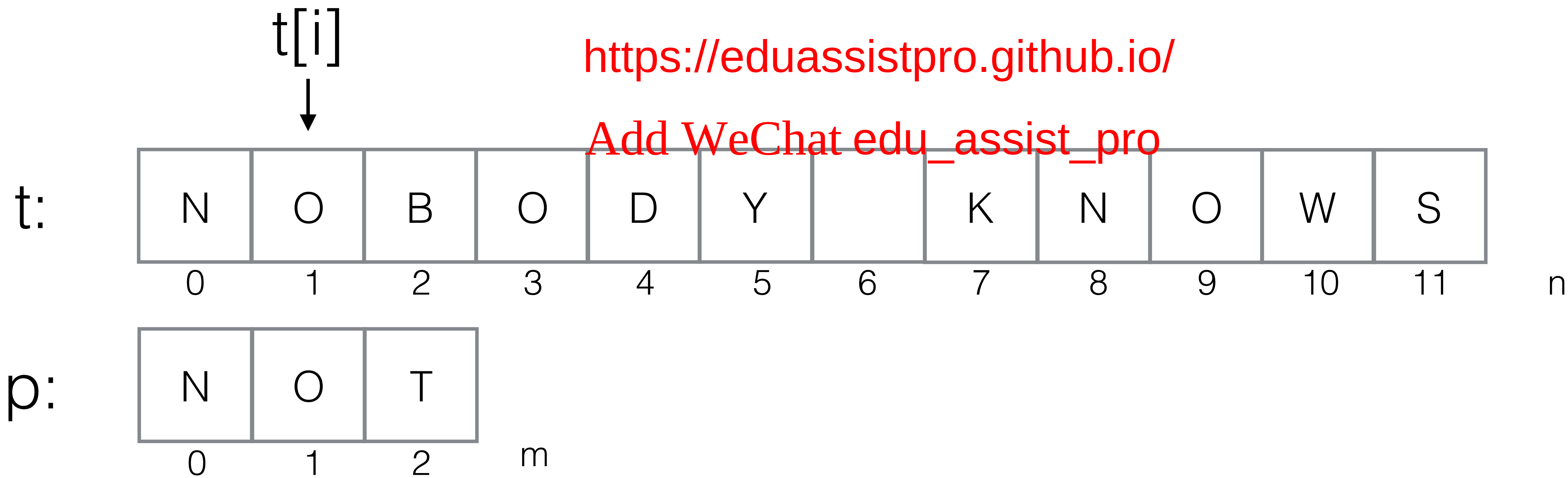

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Brute Force String Matching

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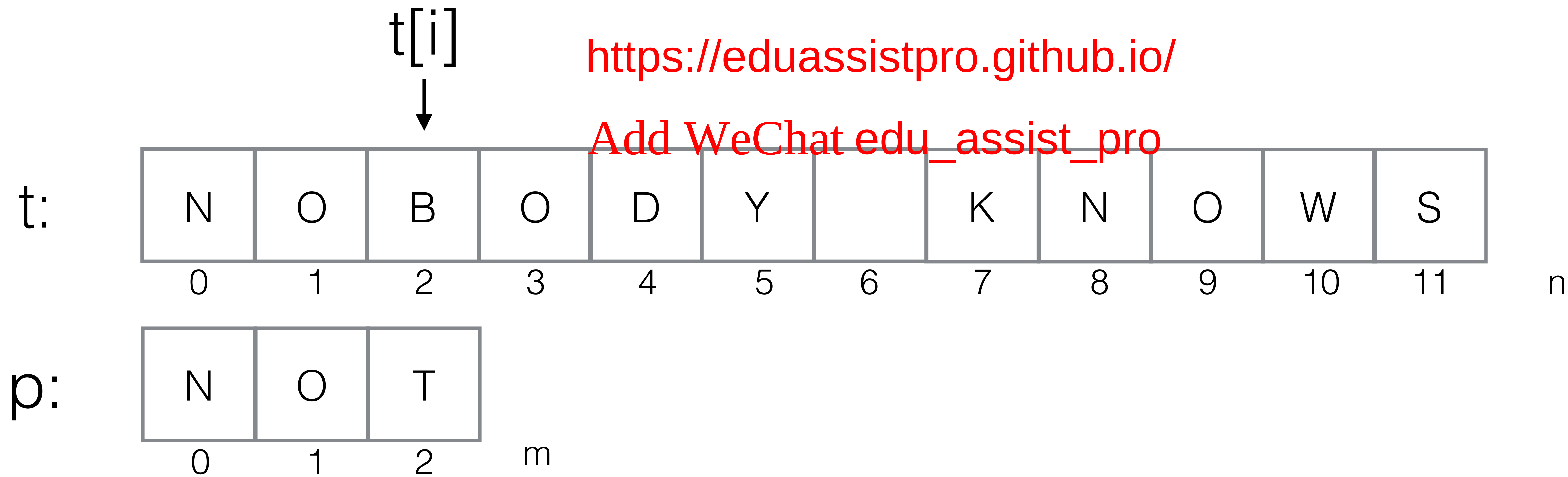

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Analysing Brute Force String Matching

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Analysing Brute Force String Matching

Basic operation:

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Analysing Brute Force String Matching

Basic operation: comparison p[j] = t[i+j]

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Analysing Brute Force String Matching

Basic operation: comparison p[j] = t[i+j]

For each n - m + 1 positions in *t*
we make up to m comparisons

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Analysing Brute Force String Matching

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Assuming m much https://eduassistpro.github.io/ (mn) comparisons.

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But for **random text** over r ly large alphabet
(e.g. English), **average** running time is linear in *n*

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Analysing Brute Force String Matching

Basic operation: comparison p[j] = t[i+j]

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But for **random text** over r ly large alphabet
(e.g. English), **average** running time is linear in *n*

There are better algorithms, for smaller alphabets such as binary strings or strings of DNA nucleobases. But for many purposes, the brute-force algorithm is acceptable.

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Brute Force Geometric Algorithms: Closest Pair

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- **Problem:** Given n points is k-dimensional space, find a pair of points with minimal separating Euclidean distance.

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- The brute force a ers each pair in turn (except that d the distance from x to y, it does not nee sider the distance from y to x).

- For simplicity, we look at the 2-dimensional case, the points being $(x_0, y_0), (x_1, y_1), \ldots, (x_{n-1}, y_{n-1})$.

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Closest Pair Problem (2D)

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Closest Pair Problem (2D)

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Brute Force Closest Pair

Try all combinations (x_i, y_i) and (x_j, y_j) with $i < j$:

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Closest Pair Problem (2D)

2

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0

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3

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1

4

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Closest Pair Problem (2D)

i=0

2

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0

3

1

4

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Closest Pair Problem (2D)

i=0 min=∞

2

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0

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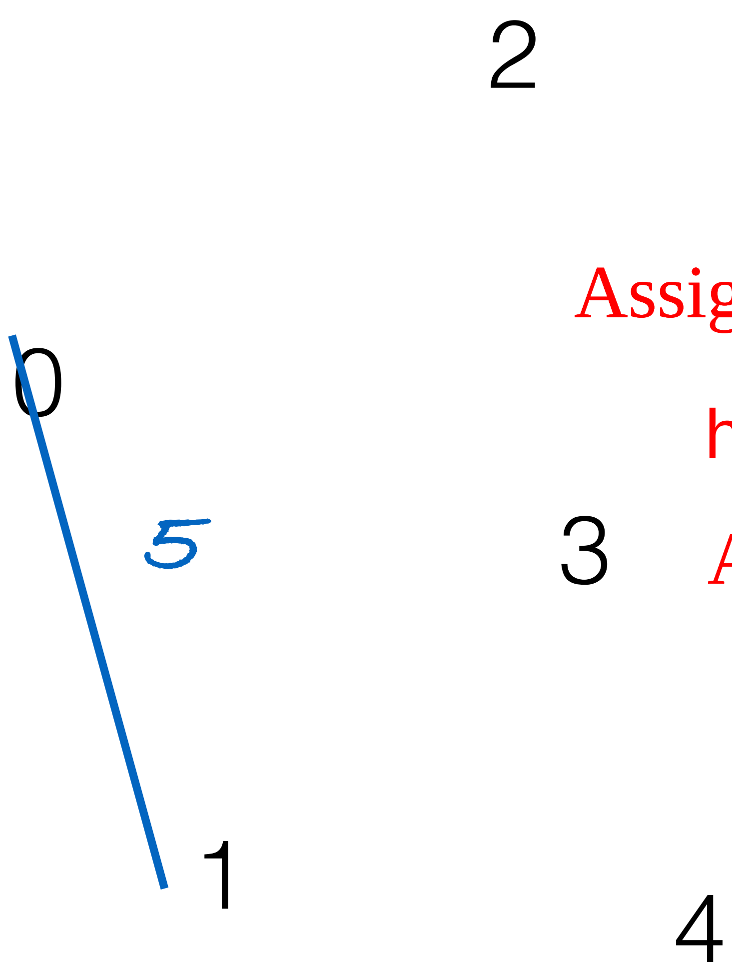
Closest Pair Problem (2D)

i=0 min=∞



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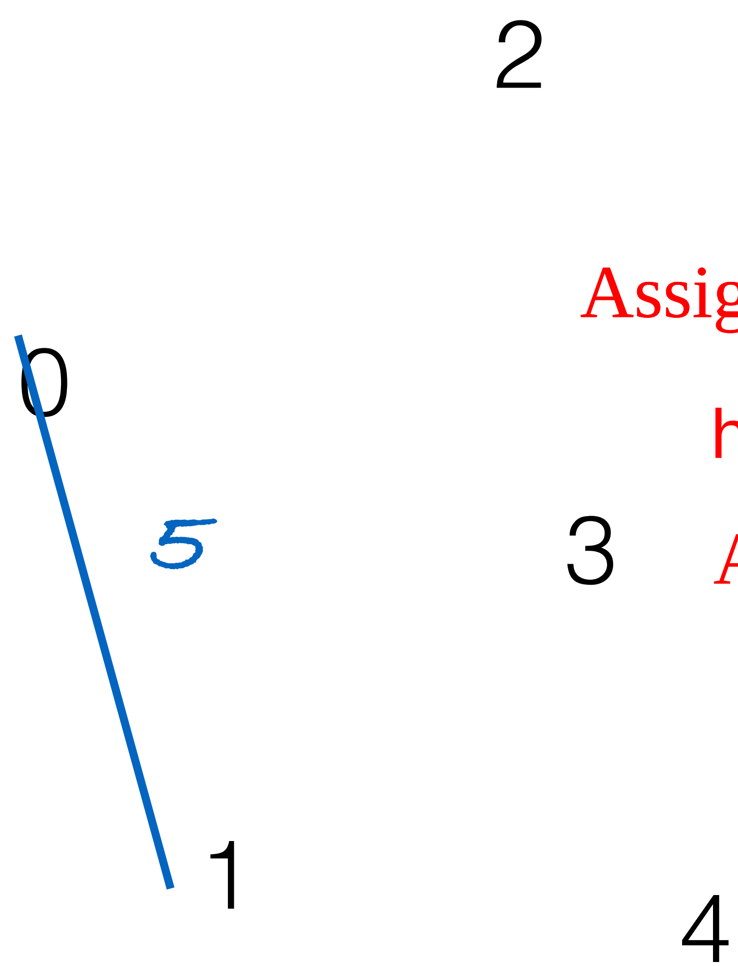
Closest Pair Problem (2D)

i=0   min=5



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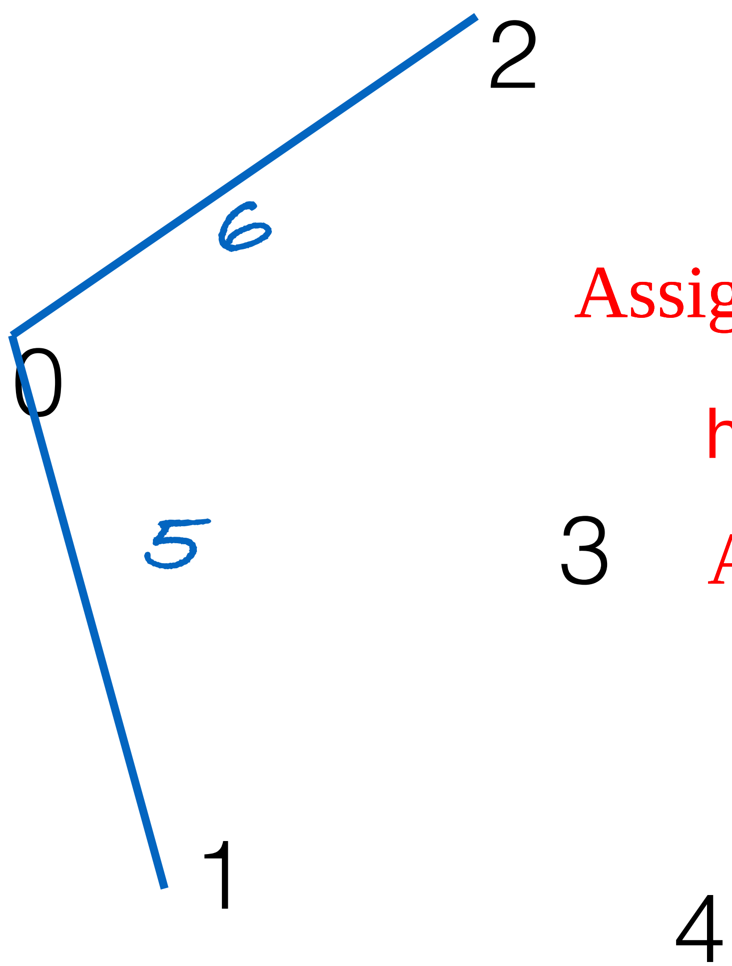
Closest Pair Problem (2D)

i=0   min=5



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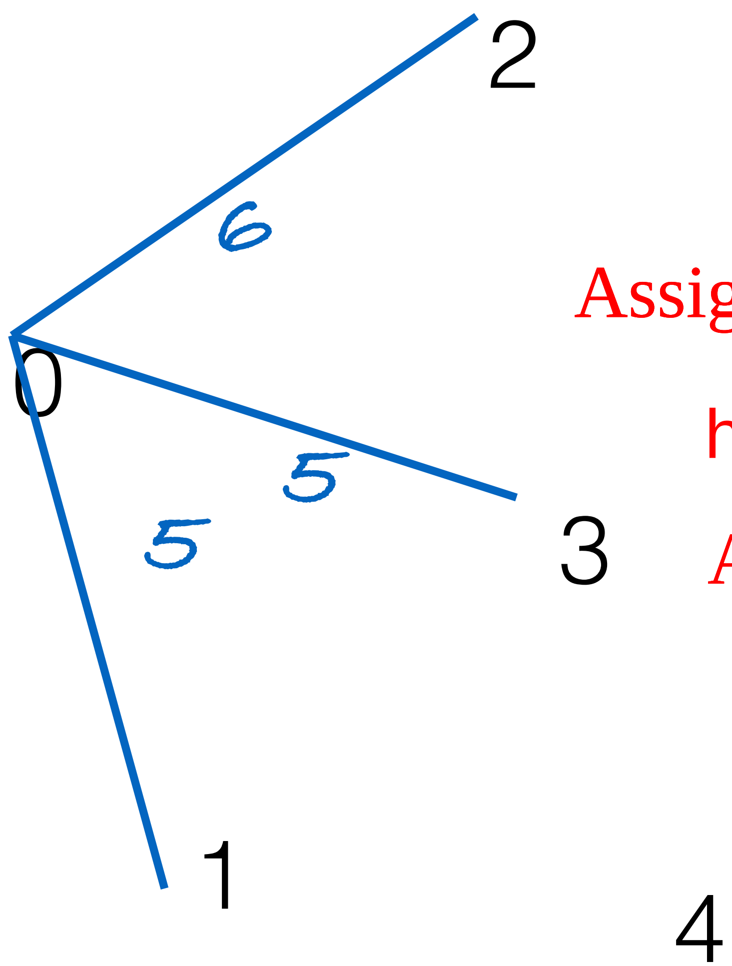
i=0 min=5



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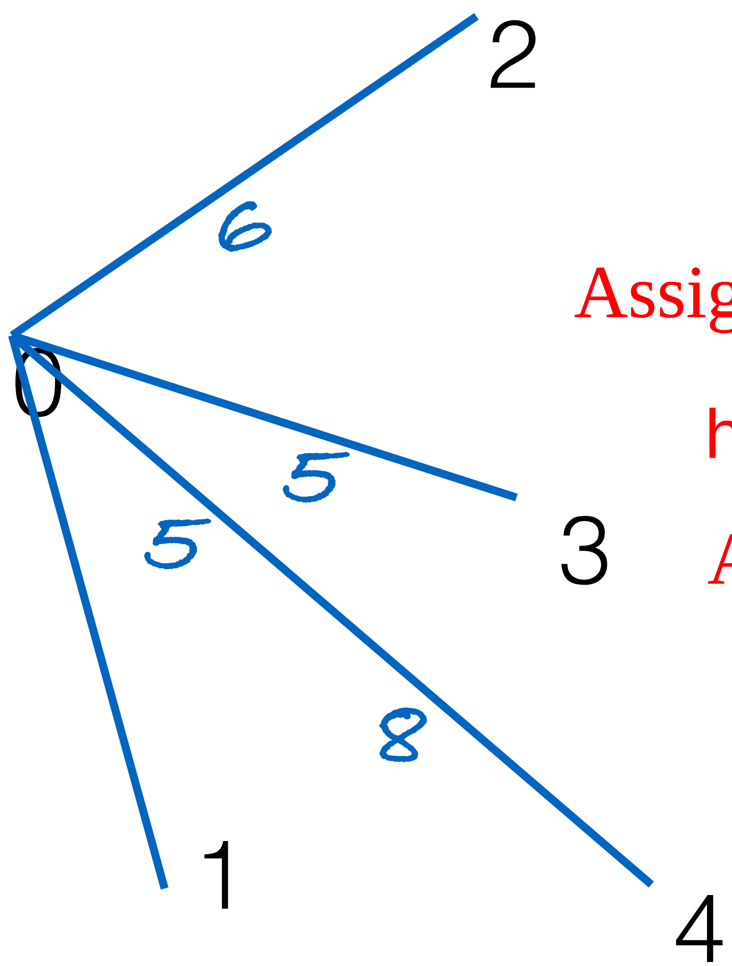
Closest Pair Problem (2D)

i=0 min=5



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Closest Pair Problem (2D)

i=1 min=5

2

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0

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1

4

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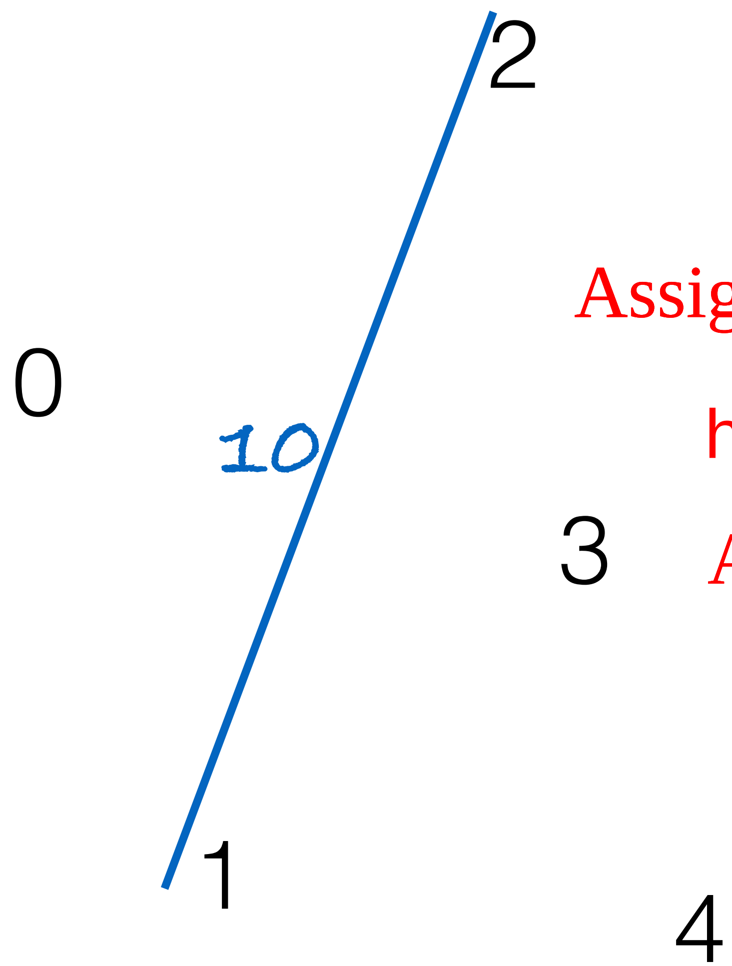
Closest Pair Problem (2D)

i=1 min=5



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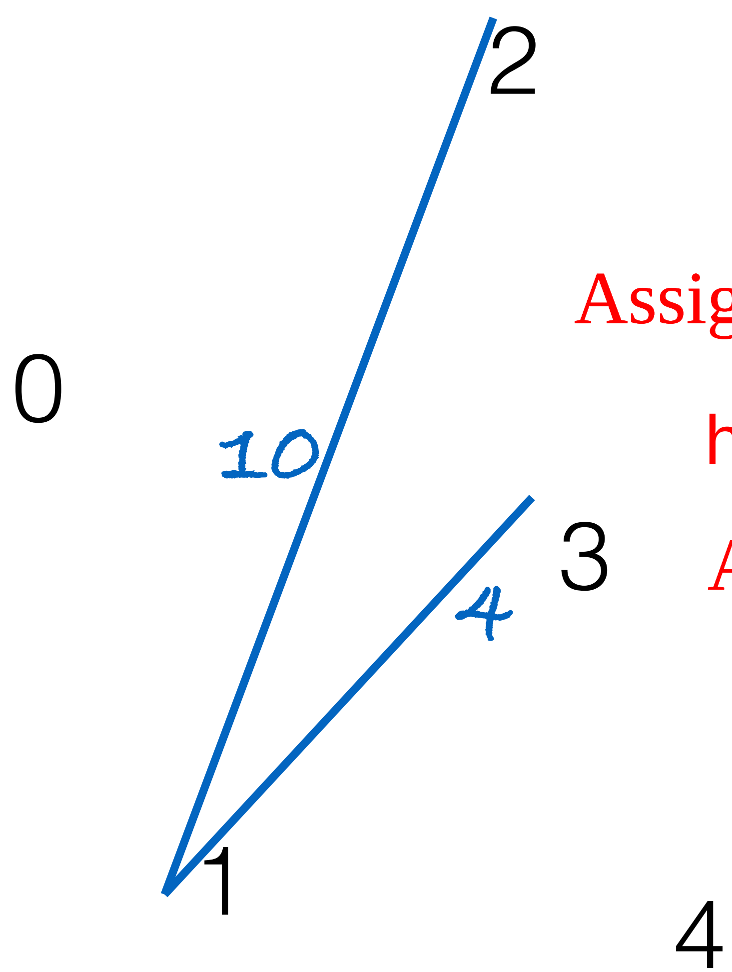
Closest Pair Problem (2D)

i=1   min=5



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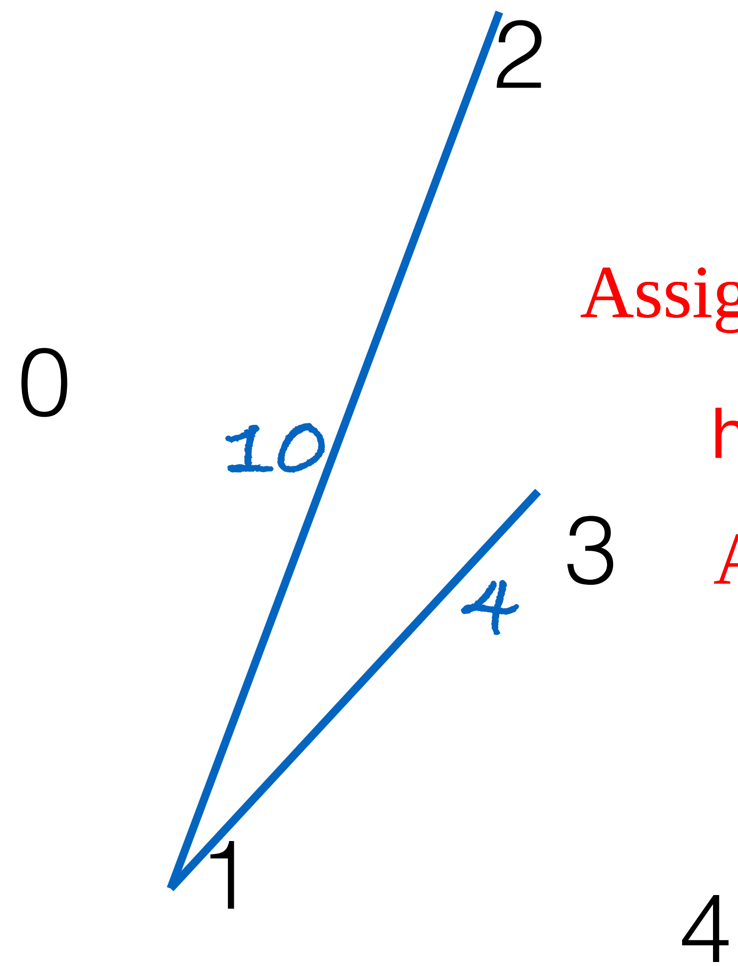
Closest Pair Problem (2D)

i=1 min=4



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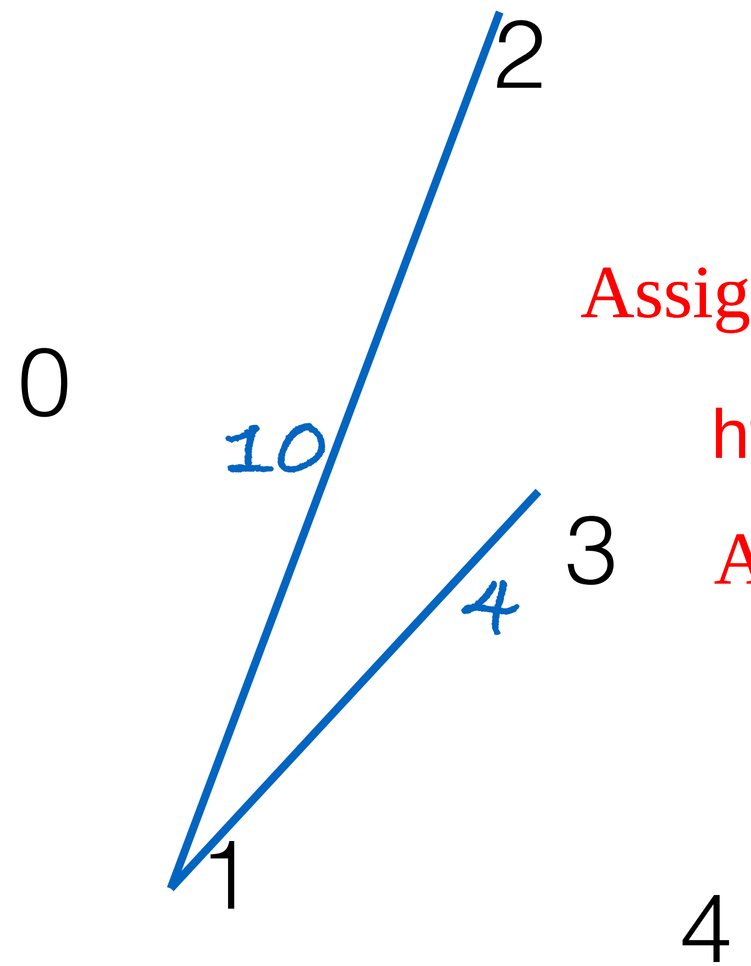
Closest Pair Problem (2D)

i=1 min=4



and so on until

3 and j=4

d the minimum here)

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Analysing Brute Force Closest Pair Algorithm

- Not hard to see that the algorithm is
- Note, however, that we can speed up the algorithm considerably, by Assignment Project Exam Help notonicity of the square root funct https://eduassistpro.github.io/

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- Does that contradict the claim?
- Later we will see a clever divide and conquer approach leads to a $\Theta(n \log n)$ algorithm

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Analysing Brute Force Closest Pair Algorithm

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- Not hard to see that the algorithm is $\Theta(n^2)$
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- Does that contradict the $\Theta(n^2)$ claim?

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Brute Force Summary

- Simple, easy to program, widely applicable.
- Standard approach for small tasks.
- Reasonable algo problems.
- **But:** Generally inefficient—does not scale well.
- Use brute force for prototyping, or when it is known that input remains small.

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Exhaustive Search

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- Problem type:
  - Combinatorial decision or optimization problems
  - Search for an element with a particular property
  - Domain grows exponentially, for example all permutations

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- The brute-force approach—generate and test:
  - Systematically construct all possible solutions
  - Evaluate each, keeping track of the best so far
  - When all potential solutions have been examined, return the best found

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Example 1: Travelling Salesperson (TSP)

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- Find the shortest **tour** (visiting each node exactly once before returning to the start) in a *weighted, undirected* graph.

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Side Note: Graph Concepts

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Side Note: Graph Concepts

a node

(aka vertex)

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Side Note: Graph Concepts

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Side Note: Graph Concepts

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a node
(aka vertex)

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an
edge

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Side Note: Graph Concepts

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a node
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an
edge

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Side Note: Graph Concepts

an edge weight

a node (aka vertex)

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an edge

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Side Note: Graph Concepts

an edge weight

a node (aka vertex)

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This graph is <u>undirected</u> since edges do not have directions associated with them.

an edge

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Example 1: Travelling Salesperson (TSP)

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- Find the shortest **tour** (visiting each node exactly once before returning to the start) in a *weighted, undirected* graph.

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Tours

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Example 2: Knapsack

- Given *n* items with
  - Weights: w_1, w_2, …, w_n
  - Values: v_1, v_2, …, v_n
  - Knapsack of c

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- find the most valuable selection of items whose combined weight does not exceed *W*

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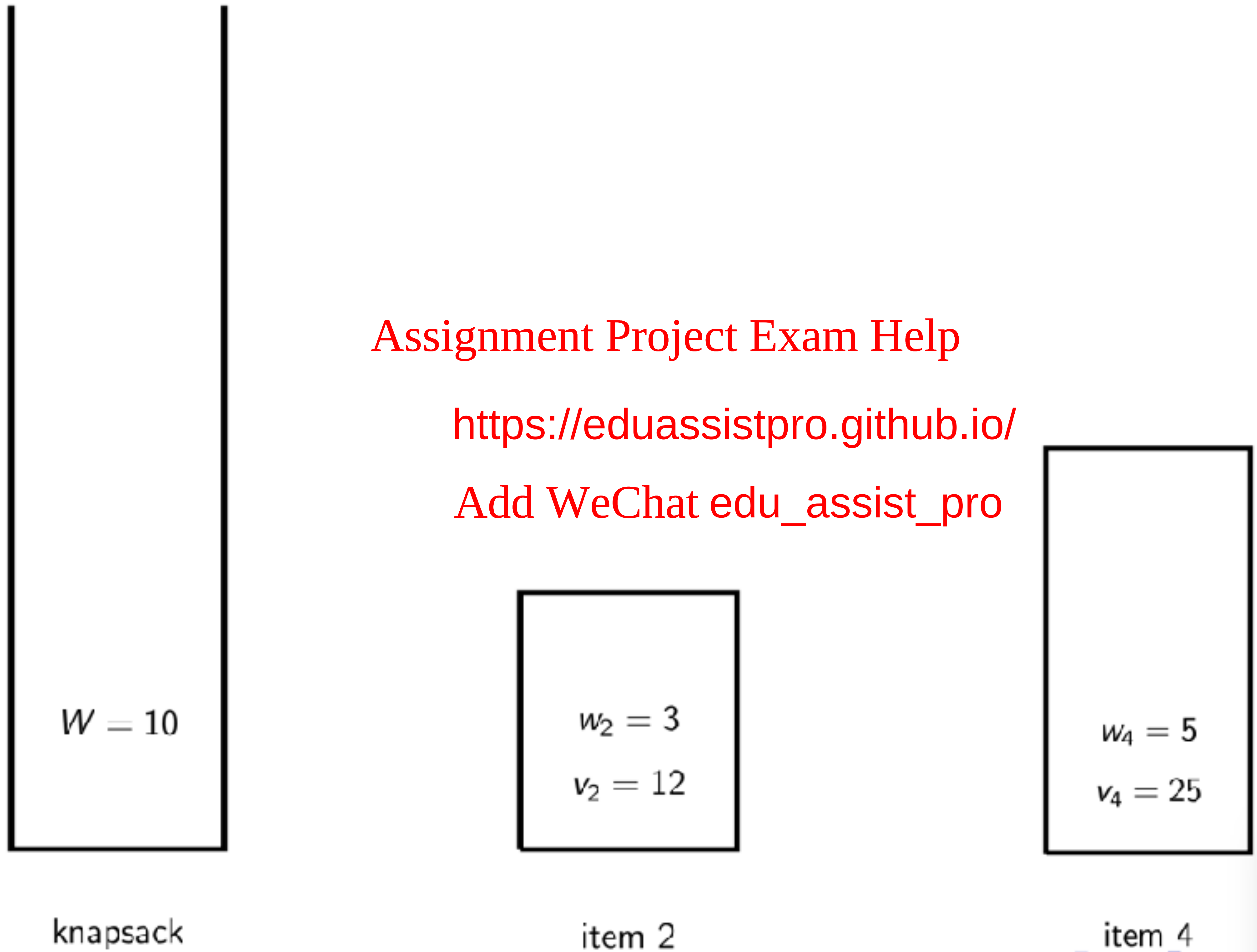
Knapsack Example



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Knapsack: Example

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NF means "not feasible": exhausts the capacity of the knapsack.

Later we'll find a better algorithm based on **dynamic programming**

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Comments on Exhaustive Search

- Exhaustive search algorithms have acceptable running times **only for very small instances.**

- In many cases there are better alternatives, for example, Eulerian tours, shortest paths, minimum spanning trees, .

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- But for some problems, it is that there is essentially no better alternative.

- For a large class of important problems, it **appears** that there is no better alternative, but we have no proof either way.

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Hamiltonian Tours

- The Hamiltonian tour problem is this:

- In a given undirected graph, is there a simple tour (a path that visits each **node** exactly once, except it returns to the starting node)?

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- Is there a Hamiltoni[illegible]ph?

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Eulerian Tours

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- The Eulerian tour problem is this:
- In a given undirected graph, is there a path which visits each **edge** exactly once?
- Is there a Euleria h?

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Hard and Easy Problems

- Recall that by a **problem** we usually mean a parametric problem: an infinite family of problem “instances”.

- Sometimes our intuition about the difficulty of problems is not very reliable. The Hamiltonian Tour problem and the Eulerian Tour problem look very similar, but one is hard and the other is easy. We shall see more exampl n later.

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- For many important **optimization** p e do not know of solutions that are essentially better ustive search (a whole raft of **NP-complete** problems, including TSP, knapsack).

- In those cases we may look for **approximation algorithms** that are fast and still find solutions that are reasonably close to the optimal.

- We plan to return to this idea in Week 12.

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Next Up

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- **Recursion** as a technique

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