

# Week 1

Overview Lecture

Subject Overview

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**Lecture 1**

**Introduction to cr** <https://eduassistpro.github.io/>

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**Lecture 2**

**Introduction to Numbers**

**Workshops start from Week 2**

**Quiz 1**

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Lecture 1

# Introduction to cryptography

## Lecture 1

### 1.1 Information Security

- Definitions, Role of Cryptography, Cyber Security
- Story of Cryptography since ancient times
- A story of Alice

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### 1.2 Motivating Exam

- Practical Banking
- A Communication Game:

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### 1.3 Classical example

- Diffie-Hellman Protocol

### 1.4 Basic Security Objectives

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# Information Security

## Definitions, Role of Cryptography, Cyber Security

- What is Cryptography?
  - “Secret Writing”
  - Refers to the techniques required for protecting data between authorized parties on information communication technologies in the presence of potentially malicious elements
  - Refers to a range of cryptographic techniques including encryption, signature, hash functions, assuring Privacy, data in the digital world.
- What is Information Security?
  - A broad topic of exchange and process on modern computers and networks.
  - Confidentiality, Integrity, and Availability.
- What is Cyber Security?
  - Refers to management of attacks and risks by adversarial and malicious elements on computers and networks that support modern businesses and economy involving business, government, and community.

# Information Security

## The field of Network and Internet security

- Stallings Take:

- The field of network and Internet security consists of measures to deter, prevent, and detect violations that involve the transmission of information.

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- Our Approach:

- Is to study certain basic cryptographic primitives such as symmetric and public key cryptography, hash functions, message authentication and signatures, and use them to explore the field of network and Internet security protocols.

# Story of Cryptography since ancient times



Alice

Let us  
meet in  
the  
alley  
today



Eve

Let us  
meet  
in the  
alley  
today



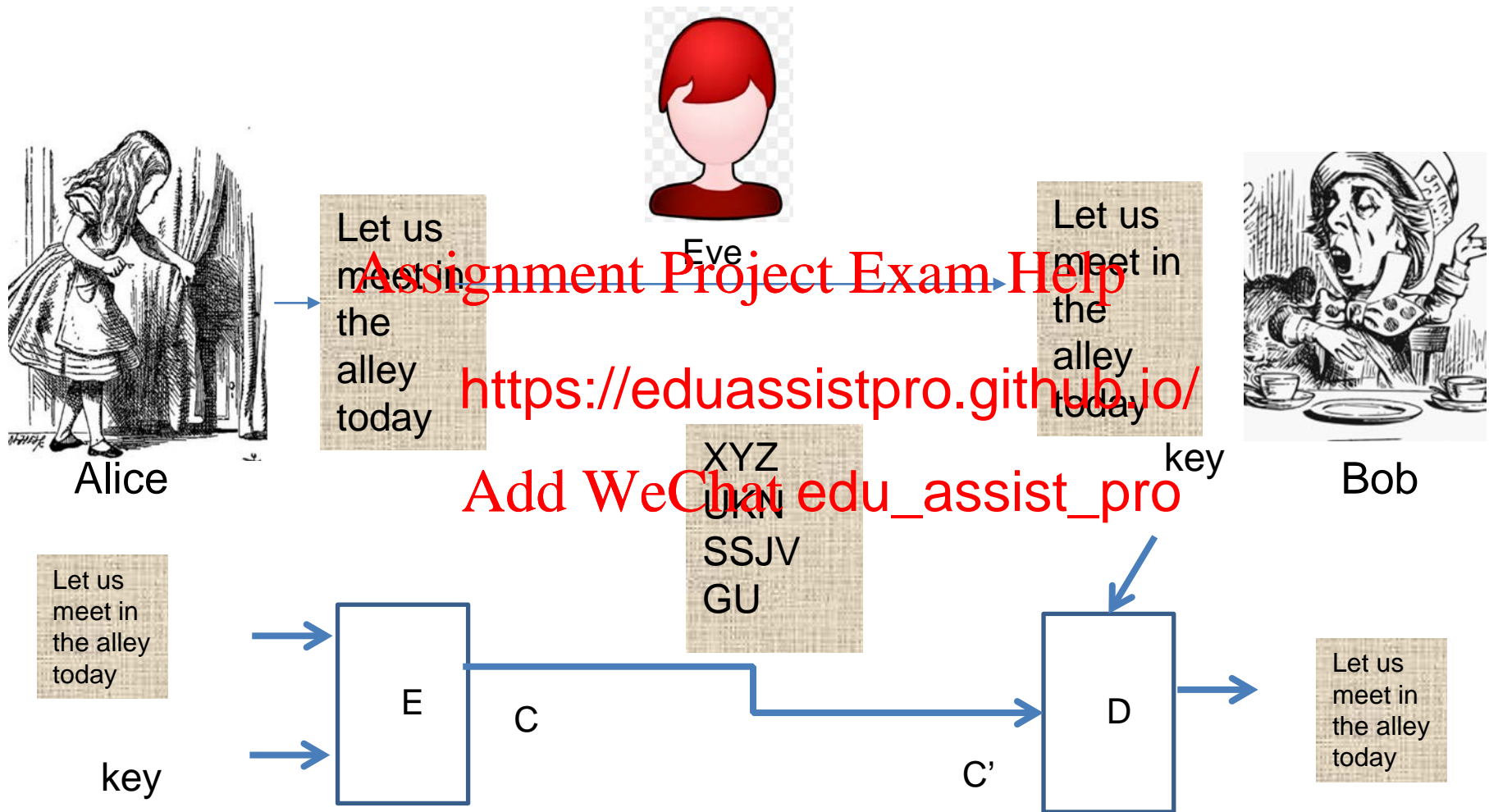
Bob

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# Story of Cryptography since ancient times



How do they agree on the "key"?

-Chicken and Egg Problem



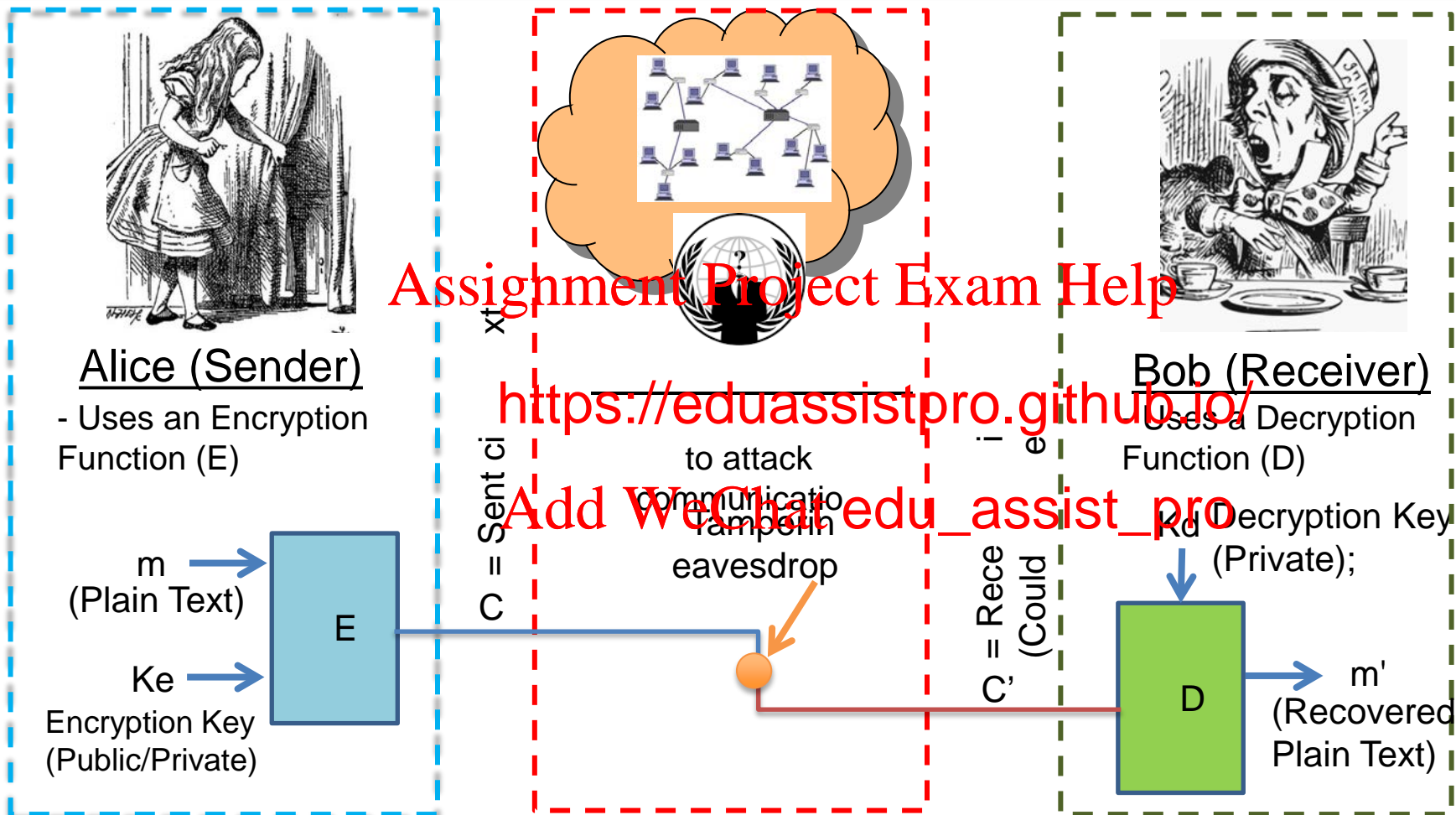
# Fast forward: In Modern times

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# Story of Alice and Bob terms and notations



$E$ ,  $D$  are public;  $c$  is the ciphertext,  $c'$  is received ciphertext; ideally  $m=m'$ ;  
Cryptography involves many conceptual ideas, we look at the basic functions

# Differences

- $K_e = K_d$  : Symmetric key also sometimes referred as private key. But we shall call always symmetric key-
  - Known since antiquity
- $K_e \neq K_d$  : Asymmetric
  - Fairly recent- since 1974 after the c by Diffie-Hellman.
  - Please read this paper. I have added a link to this page in LMS.

# 1.2 Motivating Examples

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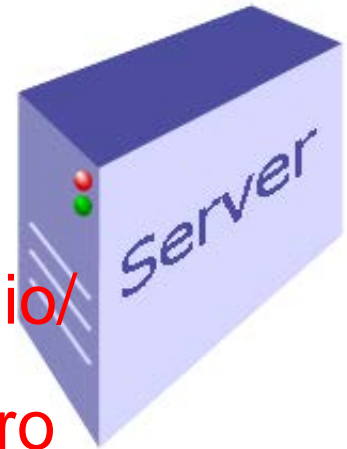
# Motivating examples

Comm bank Server

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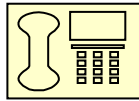
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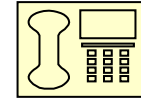
Issues in getting your money from the bank.  
Should work over Internet  
Think, who is Alice, Bob and Eve here.  
What tools Cryptography can provide here?

# A Communication Game

*Alice*



Dating Problem!



*Bob*

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Alice and Bob want

They want to decide whether to go to the Art or Cinema

They can resolve either way by tossing a coin

If they can meet together, it is a simple task.

However, they are in different offices connected by a telephone.

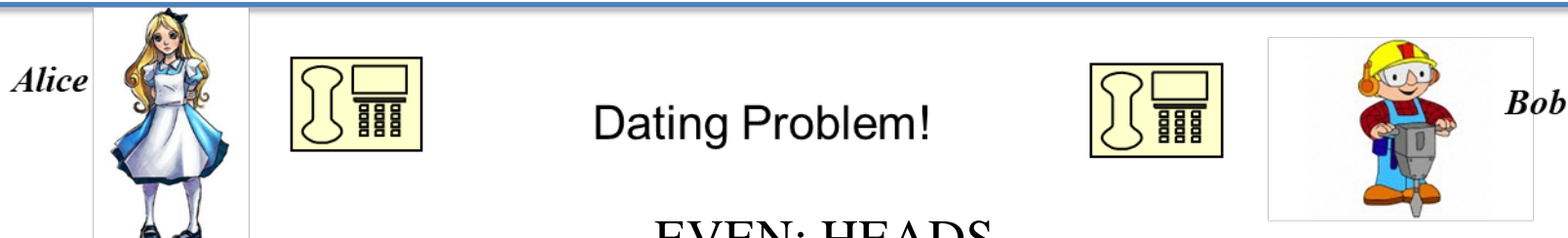
They need to book the program in advance and want to make a decision over the phone.

Can you help them?

# A Cryptographic Solution Using Mathematics!

- Assume we have a magic function with
  - A. For every integer  $x$ , it is EASY to compute  $f(x)$  from  $x$ , however given a value for  $x$  which is the pre-image of  $f(x)$ , eg <https://eduassistpro.github.io/>  
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  - A. It is impossible to find a pair of in  $x$  not equal to  $y$  and  $f(x) = f(y)$
- Even number  $x$  in  $f(x)$  denotes EVEN and the other case denotes ODD.

# A protocol



EVEN: HEADS

ODD: TAILS

Choose a random  $x$  and  
compute  $f(x)$

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es  $x$  is even or Odd

Send  $x$

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$= f(x)$   
his guess  
t or not

Whoever wins the game decides the venue of the meeting!

Is this protocol correct and fair (unbiased)?  
Can you modify so that both Alice and Bob



# If the line is not secure: Some questions

- They need to introduce traditional cryptography to secure the line
- Symmetric key or Asymmetric key?

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- Or Use Different methods of communication where intruder cannot read the channel.
- We will discuss cry

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# Models for Information Security

- Traditional Communication Model:
  - Alice and Bob is connected by insecure channel. Marvin, an adversary can listen to their conversation and modify if needed.
- Modern Network <https://eduassistpro.github.io/>
  - Network itself is an adversary. No participants. A valid participant also can be an adversary to others. Many models exist.

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# One-Way functions

- Does One Way functions exist?

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- This simple question has many issues.  
Cryptographers who claim to have come up with many practical one-way functions.  
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- Do they have a clear cut proof for these claims?
- On the other hand, cryptanalysts believe in the opposite and work towards breaking the claims of cryptographers.

## 1.3 Classical example

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# Diffie-Hellman Idea: Basics

- Two users want to share a common secret over a public network, Is this possible? Think!

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- For a moment assume that we have a one way function.

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- What is one way fu

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- Given  $x$  in domain it is easy to co
- Given  $y$  in range, it is difficult find  $x$  in domain such that  $f(x)=y$

# DH Continued

- Alice can create  $x$  in a domain (agreed in advance) –keep it secret,
- Compute  $f(x)$ – Send it to Bob over public channel
- Bob can create  $y$  and also computes  $f(y)$  –  
Send it back to Alice
- Now both of them have  $f(x)$  and  $f(y)$
- If  $f$  is such that they can workout a common function of their secrets which others who observed  $f(x)$  and  $f(y)$  cannot compute, then one can attempt to have a solution to this problem.
- Diffie-Hellman in their 1974 paper give one such concrete solution!  
Please read it, you will love the idea.

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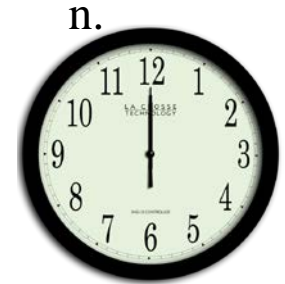
# Prime Numbers

- A number is said to be a prime number if  $p > 1$  and  $p$  has no positive divisors except 1 and  $p$ .
- Example:  $p = 2, 3, 5, 7, 11, 13$
- The numbers which are not prime numbers are referred as composite numbers.
- For any integer  $n, n > 1$ , let  $\mathbb{Z}_n = \{0, 1, 2, \dots, n-1\}$  be a set of numbers. This set is called the set of remainders of integers divided by the number  $n$ .
- We define the following

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- Example:  $(6 + 7) \bmod 12 = 1$  ;  $5 \times 4 \bmod 12 = 8$ ;
- In this lecture,  $n$  will only be a prime number.

# Modular Inverse

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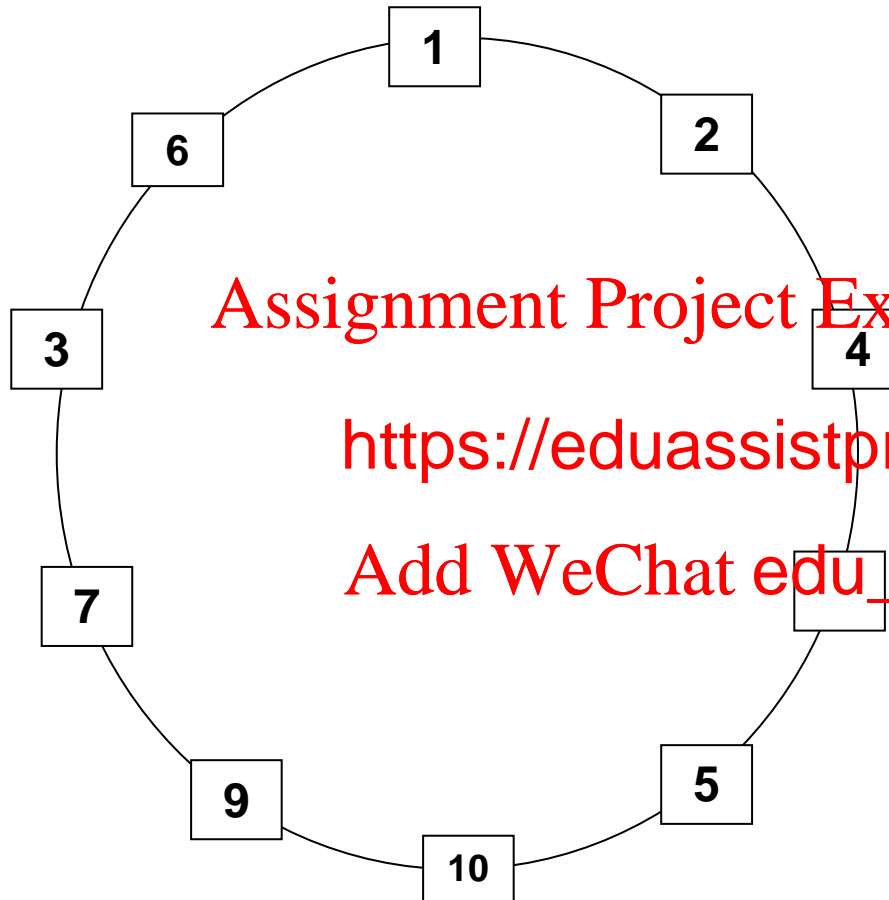
We can now define a cyclic group over nonzero elements of  $Z_p$  when  $p$  is prime.

Let  $Z_p^* = \{1, 2, 3, \dots, (p-1)\}$ . Let  $g$  be an element of  $Z_p^*$  such that

$Z_p^* = \{g, g^2, g^3, \dots, g^{p-1}=1\}$ , (\*you can always find such an element  $g$ )

\*We do not cover this idea here, it requires more study; those interested can see the textbook

# An example



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$g^i$	$g^i \bmod p$	$Dlog(g^i)$
$2^1$	2	1
$2^2$	4	2
$2^3$	8	3
$2^4$	5	4
$2^5$	10	5
$2^6$	9	6
$2^7$	7	7
$2^8$	3	8
$2^9$	6	9
$2^{10}$	1	10

Example of a Cyclic group modulo  $p = 11$

$g$  : generator = 2

Order(size) of  $G = 10$

# The Example of One Way Function

X	$2^x \bmod 11$
0	1
1	2
2	4
3	8
4	5
5	10 Or -1
6	9
7	7
8	3
9	6
10	1
11	2

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# Discrete Logarithm Problem (DLP)

Let ‘ $g$ ’ and ‘ $h$ ’ be elements of the group  $G$ . Then the discrete logarithm (DL) problem is the problem of finding ‘ $x$ ’ such that  $g^x = h$ .

For example, the solution to  $x$  in the problem:

$$3^x = 13 \pmod{17} \rightarrow 17).$$

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- o The discrete log problem is believed to be hard to solve. It has become the basis of several public key schemes, for example.
- o Next, we will consider the Diffie-Hellman protocol, the first public key algorithm.
- o The protocol is defined over a cyclic group:  $Z_p^* = \{g, g^2, g^3, \dots, g^{p-1}=1\}$ ,

# Diffie-Hellman Key Establishment Protocol

- Alice
  - Choose  $N_a=2$
  - $g^{N_a} = 2^2 = 4 = M_a$
- Bob
- Choose  $N_b=6$
- 
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- $M_b = 9$
  - Compute
  - $K_{ab} = M_b^{N_a}$
  - $= 9^2 = 4$
- 
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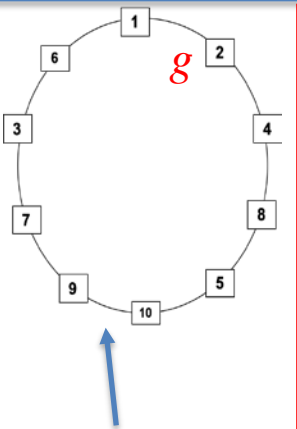
- $K_{ba} = M_a^{N_b}$
- $= 4^6 = 4$

Compute

$K_{ba} = M_a^{N_b} = 4^6 = 4$

$$K_{ab} = K_{ba} = 4$$

# Diffie-Hellman Protocol



All arithmetic  
under  $mod$   
 $p=11$

<p><b>Alice</b></p> <p>Choose <math>N_a=2</math> Choose <math>N_b=6</math></p> <p><math>g^{N_a} = 2^2 = 4 = M_a</math></p> <p>Compute <math>K_{ab} = M_b^{N_a} = (g^{N_b})^{N_a}</math> <math>= 9^2 = 4</math></p>	<p><math>p=11, g=2</math></p> <p>Eve</p> <p><math>\longleftrightarrow</math></p>	<p><b>Bob</b></p> <p><math>g^{N_b} = 2^6 = 9 = M_b</math></p> <p>Compute <math>K = M_a^{N_b} = (g^{N_a})^{N_b}</math> <math>= 4^6 = 4</math></p>
<p><math>K_{ab} = K_{ba} = 4</math></p>		



Whitfield Diffie  
and  
Martin Hellman

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**CDH PROBLEM**

Problem for Eve in the above  
protocol

Clearly a solution to DL  
implies a solution to  
CDH

Is the converse True?\*

\* Open Problem

Let  $G$  be a cyclic group of size  $q$  and  $g$  be a generator of the group  $G$ .  
Given  $g^a$  and  $g^b$ , two arbitrary elements of the group  $G$  for some integers  
 $a$  and  $b$  in the range:  $0 \leq a, b \leq q$ , then find  $g^{ab}$   
Normally  $G$  is a multiplicative group in a suitable finite field.

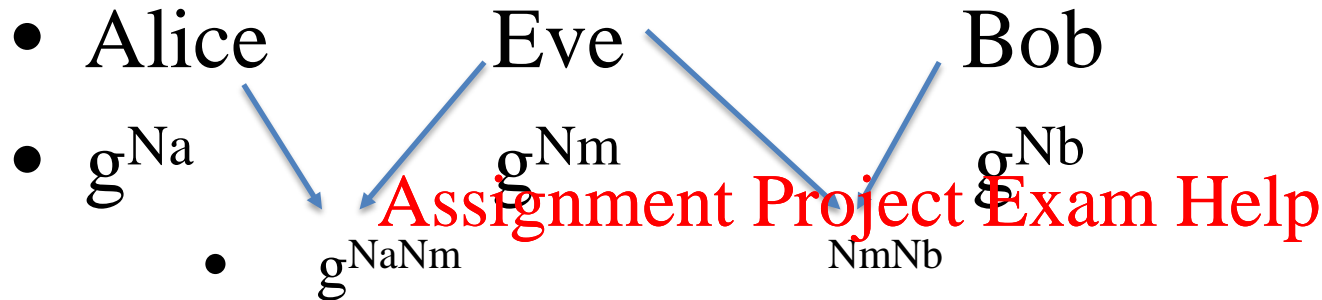
New directions in Cryptography, IEEE Trans. Inf. Theory 22(6): 644-654 (1976)

# Issues with this Protocol: Secure?

- Exchanged data -only  $g^{N_a}$  and  $g^{N_b}$
- So Alice cannot guess  $N_b$  nor Bob can guess  $N_a$
- So their secrets are safe from each other
- But also none can guess  $N_a$  and  $N_b$  for the same reason
- Both Alice and Bob can see  $g^{N_a N_b}$  secret  $g^{N_a N_b}$
- It is also believed that  $g^{N_a N_b}$  cannot be guessed by others who can only see  $g^{N_a}$  and  $g^{N_b}$
- The later problem is known as Computational Diffie-Hellman problem (Hard!)



# Man in the Middle Attack



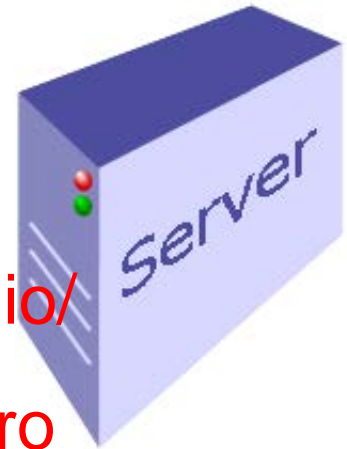
- Marvin comes in between Alice and Bob and creates two secrets one with Alice and the other with Bob.
- This is possible because when Bob receives a message from Alice, there is no way for him to determine if it indeed came from Alice, in other words, the messages are not authenticated.
- A way to solve this problem is by using digital signatures! –We will revisit these ideas when we visit Public Key topics later in the semester.

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## 1.4 Basic Security Objectives

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# Three important concerns of Information security

- Confidentiality

- In simple terms, confidentiality of information or data ensures that the access is given only to authorized individuals.

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- Integrity

- Information exists so that authorized individual changes to the information by intentional means will be detected.

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- Availability

- Information or data availability ensures that the information is authorized available to the users.

From the textbook definitions

# OSI Security Architecture

- How to define the requirements for security in networked world and characterizing the approaches to satisfy those requirements?

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- Refer to ITU-T X.800 “Security Architecture for OSI”
  - It defines a systemaity requirements

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- Three main aspects:
  - Security attacks
  - Security Mechanisms.
  - Security services.

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# Security Attack

- *Attack* is any action that compromises the security of information owned by an organization
- *Threat* is a possible potential for violation of security,
- Information security attacks, or failing that, to detect attacks,
- often *threat* & *attack* used to mean the same thing (threat is attack in waiting)
- Generally we have a wide range of attacks:
- Some generic types of attacks:
  - passive
  - active

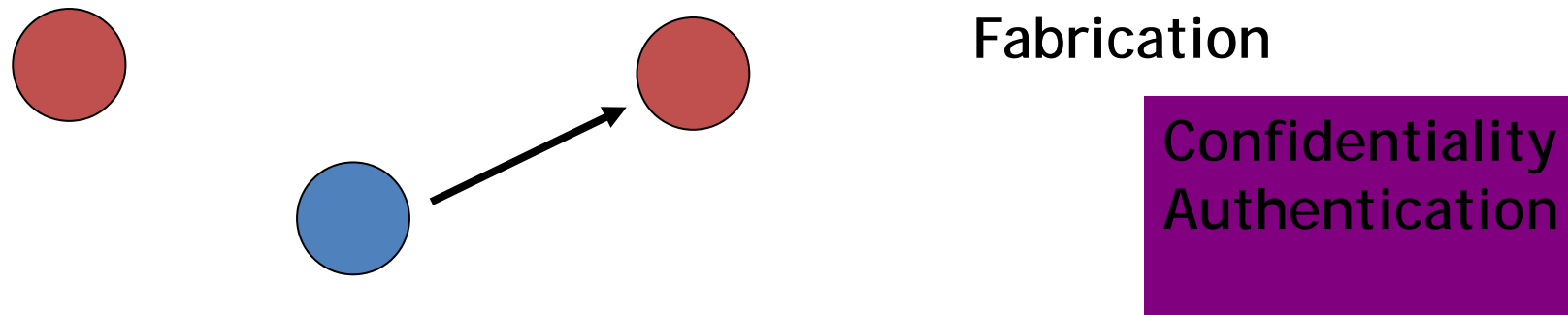
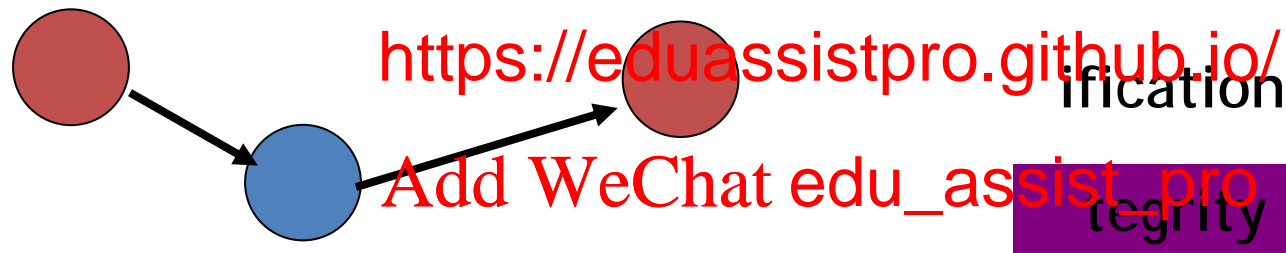
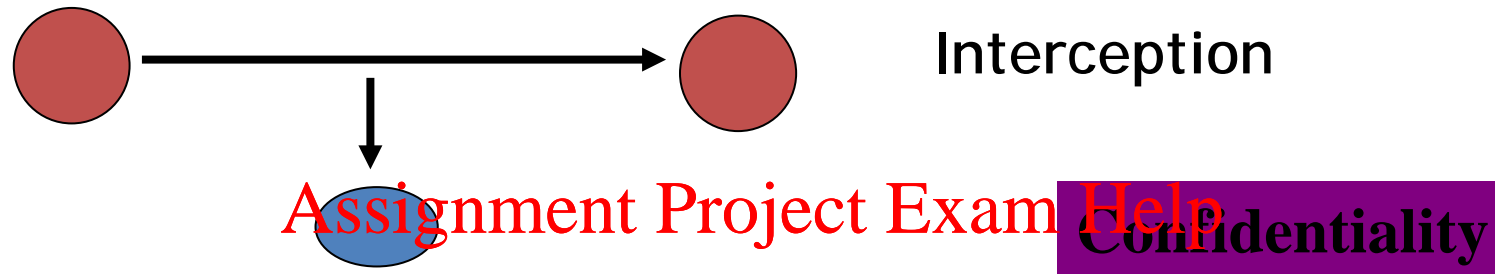
# Basics Security Services

We concentrate on Implementation and Mechanism aspects of Information Security.

- Authentication
  - Confidentiality
  - Integrity
  - Nonrepudiation
  - Availability
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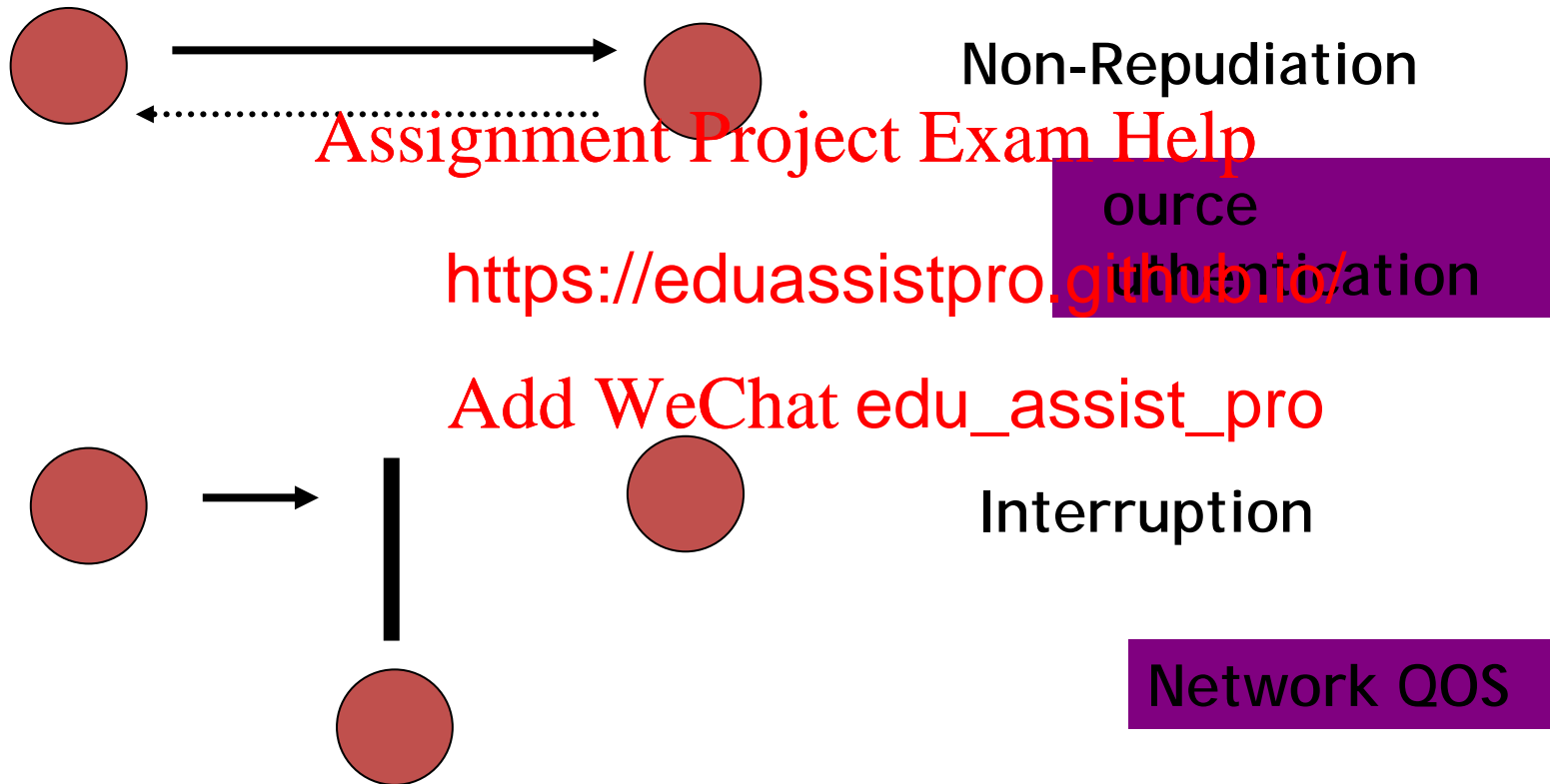
# Security Threats in Networked World

- Security services are defined to address or withstand threats





# Security Threats in Networked World



# Model for Network Security (Textbook)

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Source: William Stallings, Cryptograph and Security

# Network Access Security Model

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Source: William Stallings, Cryptograph and Security

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**Lecture 1**

**Introduction to crypt**

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Lecture 2

Introduction to Numbers

Workshops start from Week 2

Quiz 1