

Lecture 3:
Similarity

COMP90049
Knowledge
Technologies

Comparing things
Sets of descriptors
Features, Vectors

Comparing
Documents

Distance
Measures

Lecture 3: Similarity

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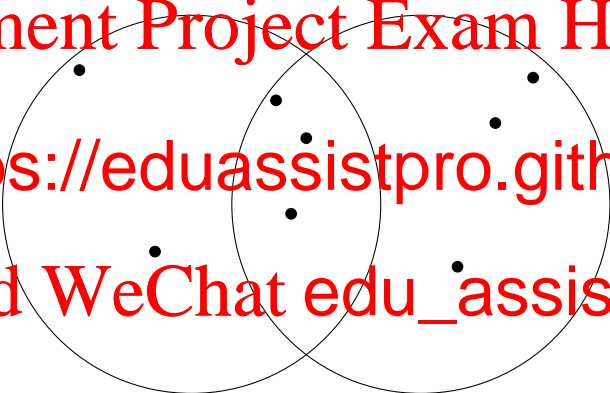
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Many similarity assessments can be framed as set intersection.

- Amazon: Book purchases



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- Rating sets (stars)

- thresholding using ratings

- different subsets for different ratings

- Categories of items

- generalisation

- book or movie genres

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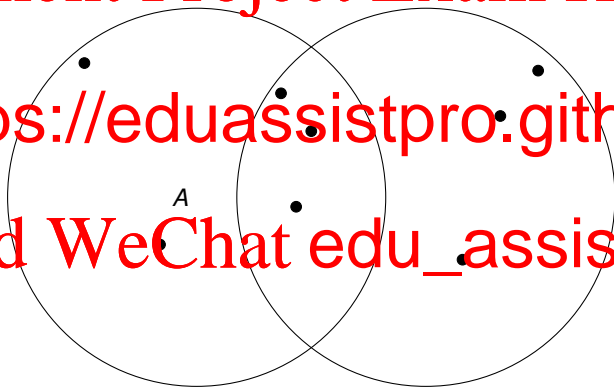
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$$\frac{|A \cap B|}{|A \cup B|}$$



$$\text{sim}(A, B) = \frac{|A \cap B|}{|A \cup B|} = \frac{3}{8}$$

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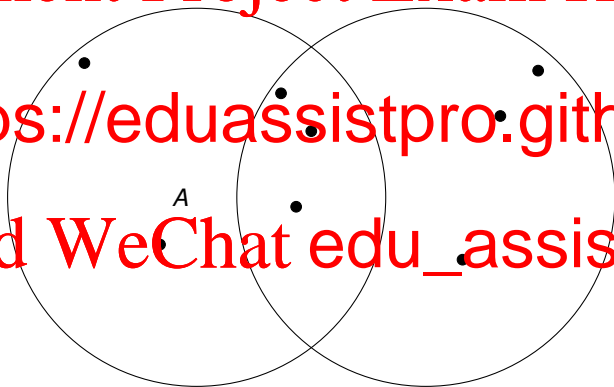
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$$\frac{2|A \cap B|}{|A| + |B|}$$



$$\text{sim}(A, B) = \frac{2|A \cap B|}{|A| + |B|} = \frac{2 * 3}{5 + 6} = \frac{6}{11}$$

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fruit above.

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A feature vector is an n -dimensional vector of *features* that represent some object.

- Features may be ordinal (e.g. cool)
- Features may be numeric/continuous

A vector locates an object (document, person, etc.) in n -space. The angle of the vector in that space is determined by the relative weight of each term.

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age	income	credit
33	8	low
58	42	low
		low
		low
		high
		high
...		

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How should we compare documents to assess their similarity?

- String-level similarity (e.g., edit distance)



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How similar are these sentences?

- 1 Mary is quicker than John.
- 2 John is quicker than Mary.
- 3 Mary is slower than John.
- 4 Jane is quicker than Mary.

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1 Mary is quicker than John.

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Sentence	"Mary"	"John"	"Jane"	"quicker"	"slower"
1	1	1	0	1	0
2	1	1	0	1	0
3	1	1	0	0	1
4	1	0	1	1	0

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One of the earliest models proposed for retrieval of documents (information retrieval in 1962) was the vector-space model.

Suppose there are n distinct indexed terms in the collection. Then each document d can be thought of as a vector

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(Most $w_{d,t}$ values will be zero, because a tiny proportion of a collection's terms.)

Intuitively, if some other document d'

$$\langle w_{d',1}, w_{d',2}, \dots, w_{d',t}, \dots, w_{d',n} \rangle$$

where the weights are close to those of d – in particular, if the non-zero w values are for much the same set of terms – then d and d' are likely to be similar in topic.

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We have discussed similarity at an intuitive and quantitative level.

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$$\text{sim}_D(A, B) = \frac{2|A \cap B|}{|A| + |B|} = \frac{2 \cdot 3}{4 + 6}$$

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What is the relationship between similarity

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A distance measure on a space is a function that takes two points in a space as arguments.

1 No negative distances.

3 Distance is symmetric.

4 The *triangle inequality* typically holds.

(Distance measures the length of the *shortest path* between two points.)

$$d(x, y) \leq d(x, z) + d(z, y)$$

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Given two items A and B , and their corresponding feature vectors \vec{a} and \vec{b} , respectively, we can calculate their similarity via their distance d in euclidean space:

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In n -dimensional space:

$$d(A, B) = \sqrt{\sum_{i=1}^n (a_i - b_i)^2}$$

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Given two items A and B , and their corresponding feature vectors \vec{a} and \vec{b} , respectively, we can calculate their similarity via their *vector cosine* (the cosine of the angle θ between the two vectors):

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$$\text{sim}(A, B) = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}| |\vec{b}|} = \frac{\sum_i a_i b_i}{\sqrt{\sum_i a_i^2} \sqrt{\sum_i b_i^2}}$$

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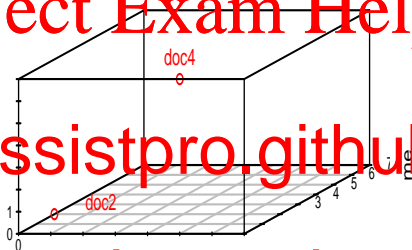
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	2
	0
	0
	7



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- Doc4, like Doc1, is all about “tea” and “two”.
- But because it is longer, it is in a space by itself.

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[“City block” distance or “Taxicab geometry” or “ L_1 distance”]

Given two items A and B , and their corresponding feature vectors \vec{a} and \vec{b} respectively, we can calculate their similarity via their distance d based on the absolute differences of their cartesian coordinates.

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In n -dimensional space:

$$d(A, B) = \sum_{i=1}^n |a_i - b_i|$$

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Relative entropy:

$$D(x \parallel y) = \sum_i x_i (\log_2 x_i - \log_2 y_i)$$

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or *Jensen-Shannon divergence*:

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where $m = \frac{1}{2}(x + y)$

NB: Probability will be reviewed next lecture!

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- How can we represent a set of objects?
- What are some methods for measuring similarity between objects?

Reading

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<http://infolab.stanford.edu/~ullman/mmds.html>

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On document representation
Chapter 6

Information Retrieval, Manning *et al.*

[http://nlp.stanford.edu/IR-book/html/htmledition/
scoring-term-weighting-and-the-vector-space-model-1.html](http://nlp.stanford.edu/IR-book/html/htmledition/scoring-term-weighting-and-the-vector-space-model-1.html)