

Hash-Based Indexes

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu_assist_pro

Introduction

As for any index, 3 alternatives for data entries k^ :*

1. Data record with key value k
2. $\langle k, \text{rid of data record with search key value } k \rangle$
3. $\langle k, \text{list of } \dots \text{ with search key } k \rangle$

■ Choice of x *ique*

■ Hash-based indexes are *t for equality selections. Cannot* support range searches.

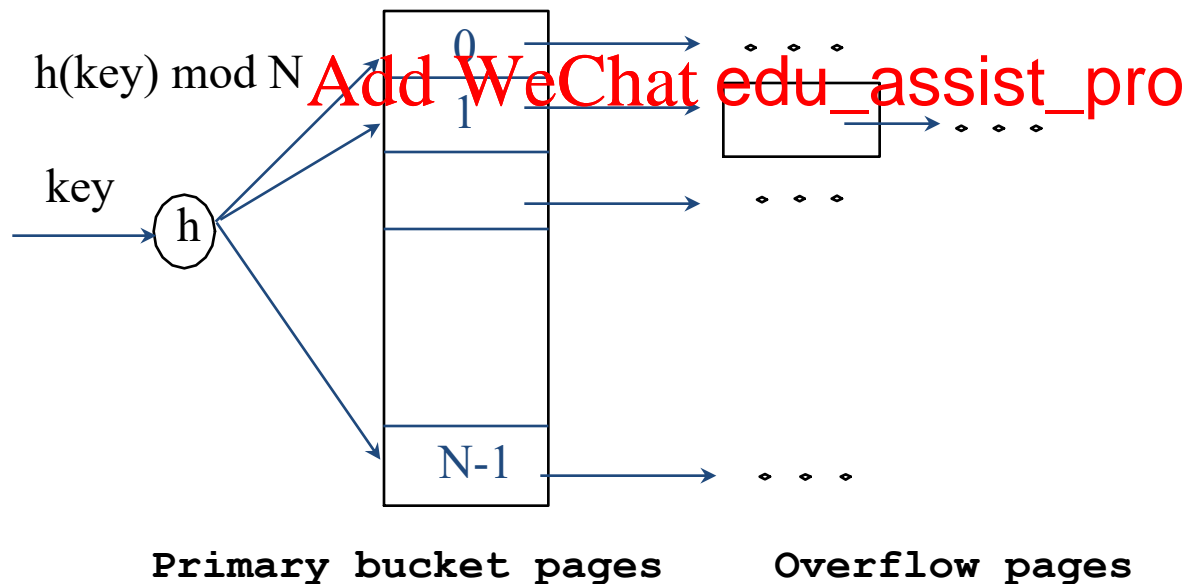
■ Static and dynamic hashing techniques exist; trade-offs similar to ISAM vs. B+ trees.

Static Hashing

- # primary pages (index data entry pages) fixed, allocated sequentially, never de-allocated; overflow pages if needed.
- $h(k) \bmod M = \text{bucket to which data entry with key } k \text{ belongs}$

Assignment Project Exam Help

<https://eduassistpro.github.io/>



Static Hashing (Contd.)

- Buckets contain *data entries*.
- Hash function works on *search key* field of record *r*. Must distribute values over range 0 ... M-1.
 - $h(key) = (a * key + b) \bmod M$ works well.
 - **a** and **b** are <https://eduassistpro.github.io/> about how to tune **h**.
Add WeChat edu_assist_pro
- Long overflow chains can occur and degrade performance.
 - Keep 80% full initially and/or re-hashing
 - *Extendible* and *Linear Hashing*: Dynamic techniques to fix this problem.

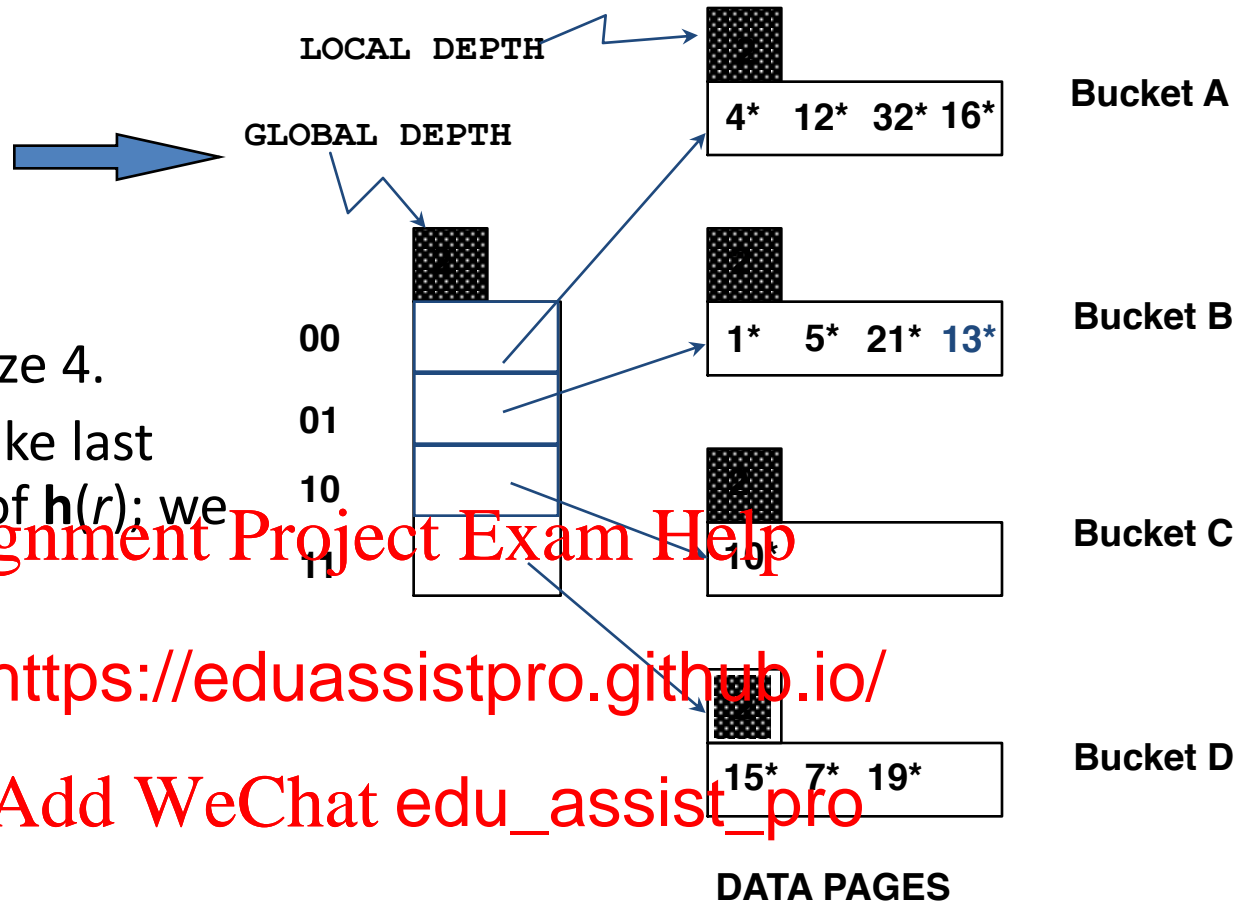
Extendible Hashing

- Situation: Bucket (primary page) becomes full. Why not re-organize file by *doubling* # of buckets?
 - Reading and writing all pages is expensive!
 - Idea: Use d buckets, double # of buckets $2d$, splitting just the bucket that overflowed
 - Directory much smaller than file, so doubling it is much cheaper. Only one page of data entries is split. *Ensure no overflow page!*
 - Trick lies in how hash function is adjusted!

Example

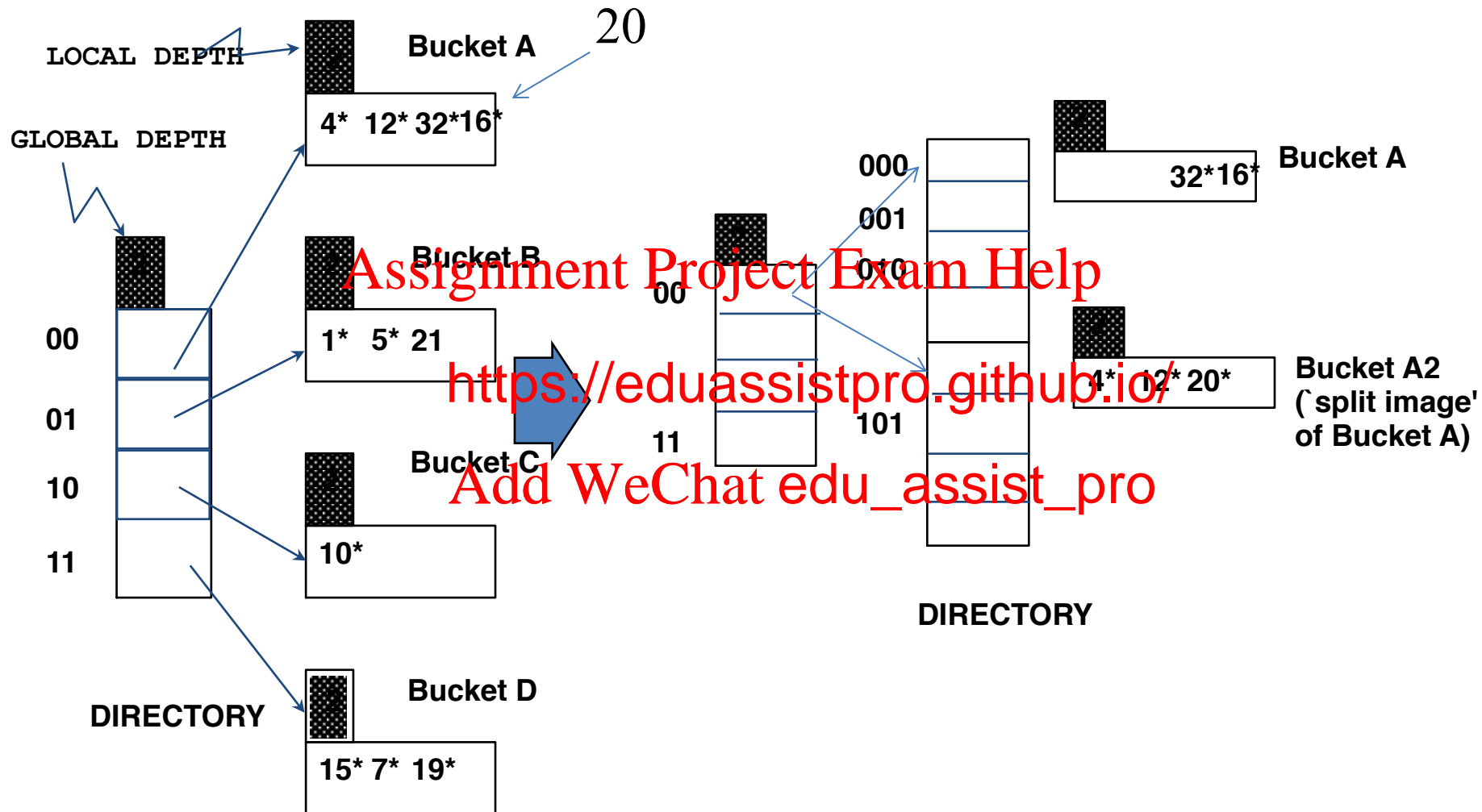
- Directory is array of size 4.
- To find bucket for r , take last '*global depth*' # bits of $h(r)$; we denote r by $h(r)$.

– If $h(r) = 5 = \text{bin } 01$ is in bucket po 01.

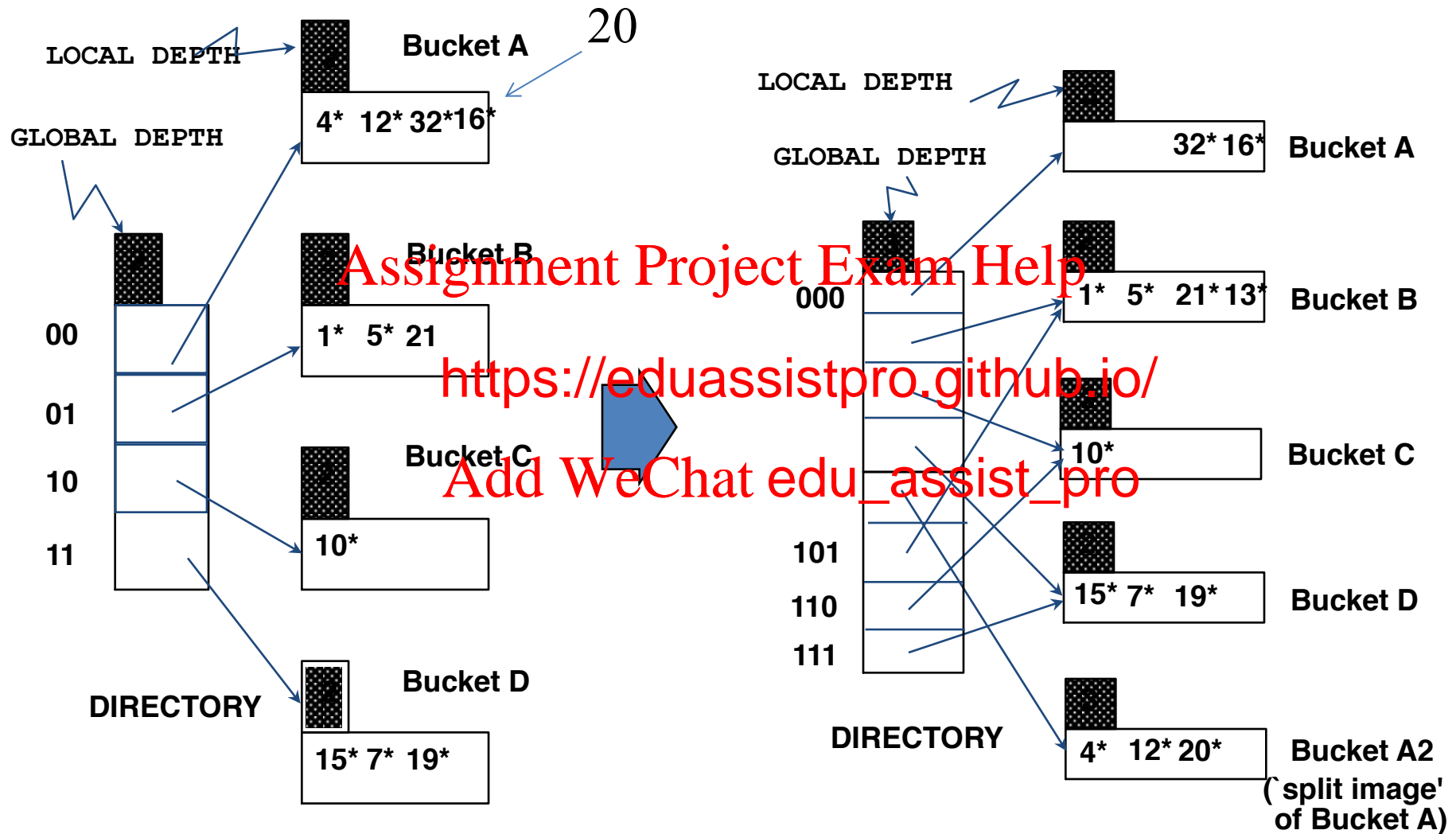


- ❖ **Insert:** If bucket is full, *split* it (allocate new page, re-distribute).
- ❖ *If necessary*, double the directory. (As we will see, splitting a bucket does not always require doubling; we can tell by comparing *global depth* with *local depth* for the split bucket.)

Insert $h(r)=20$ (Causes Doubling)



After inserting $h(r)=20$

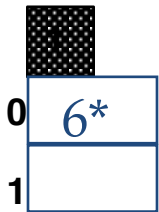


Points to Note

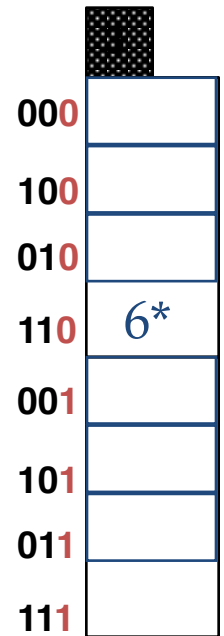
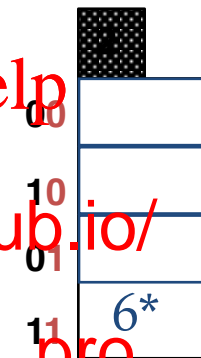
- 20 = binary 10100. Last **2** bits (00) cannot tell us r belongs in A or A2. Last **3** bits can tell us the which bucket.
 - *Global depth of directory*: Max # of bits needed to tell which bucket
 - *Local depth of* <https://eduassistpro.github.io/> to determine if an entry belongs to this bucket.
- When does bucket split cause directory doubling?
 - Before insert, *local depth* of bucket = *global depth*. Insert causes *local depth* to become $>$ *global depth*; directory is doubled by *copying it over* and 'fixing' pointer to split image page. (Use of least significant bits enables efficient doubling via copying of directory!)

Directory Doubling

6 = 110



6 = 110



Least Significant

vs.

Most Significant

Why use least significant bits in directory?

- Hard to decide where to start
- Quite biased in the most significant bids

Comments on Extendible Hashing

- If directory fits in memory, equality search answered with one disk access; else two.
 - 100MB file, 100 bytes/rec, 4K pages contains 1,000,000 records (as data entries) and 25,000 directory elements; chances are it in memory.
<https://eduassistpro.github.io/>
 - Directory growth distribution of hash values is skewed, directory size.
[Add WeChat edu_assist_pro](#)
 - Multiple entries with same hash value cause problems!
- **Delete**: If removal of data entry makes bucket empty, can be merged with 'split image'. If each directory element points to same bucket as its split image, can halve directory.

$$2^N, 2^{N+1}, 2^{N+2}, 2^{N+4}, 2^{N+5}$$

$$N = 100$$

Assignment Project Exam Help

00, 000, 0000, <https://eduassistpro.github.io/>

Add WeChat edu_assist_pro

$$2^{101}$$

Linear Hashing

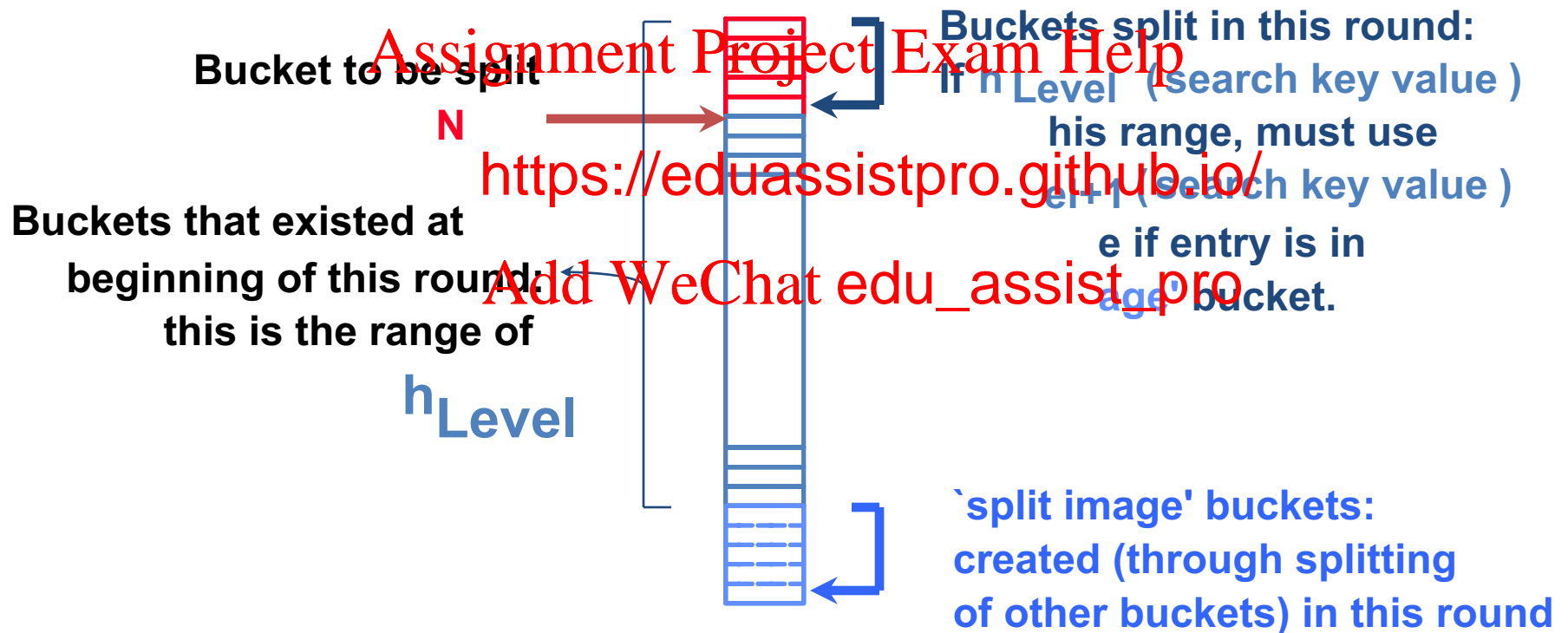
- This is another dynamic hashing scheme, an alternative to Extendible Hashing.
- LH handles the problem of long overflow chains without using a directory, and handles duplicates.
- Idea: Use a function h_0, h_1, h_2, \dots
 - $h_i(\text{key}) = h(\text{key}) \bmod (2^i N)$; buckets
 - h is some hash function (range 0 to $N-1$)
 - If $N = 2^{d_0}$, for some d_0 , h_i consists of applying h and looking at the last d_i bits, where $d_i = d_0 + i$.
 - h_{i+1} doubles the range of h_i (similar to directory doubling)

Linear Hashing (Contd.)

- Directory avoided in LH by using overflow pages, and choosing bucket to split round-robin.
 - Splitting proceeds in rounds. Round ends when all N_R initial (for r initial) buckets 0 to $N_R - 1$ have been split. Buckets 0 to $N_R - 1$ have been split. Buckets 0 to $N_R - 1$ have been split.
 - Current round number is r .
 - **Search:** To find bucket for data entry r , find $h_{Level}(r)$:
 - If $h_{Level}(r)$ in range 'Next to N_R ', r belongs here.
 - Else, r could belong to bucket $h_{Level}(r)$ or bucket $h_{Level}(r) + N_R$; must apply $h_{Level+1}(r)$ to find out.

Overview of LH File

In the middle of a round.



Linear Hashing (Contd.)

- **Insert:** Find bucket by applying $h_{Level} / h_{Level+1}$:
 - If bucket to insert into is full:
 - Add overflow page and insert data entry.
 - (Maybe) Split Next bucket and increment Next.
- Can choose any cr
- Since buckets are split round-robin low chains don't develop!
- Doubling of directory in Extendible Hashing is similar; switching of hash functions is *implicit* in how the # of bits examined is increased.

Usually, when a new overflow page is created.

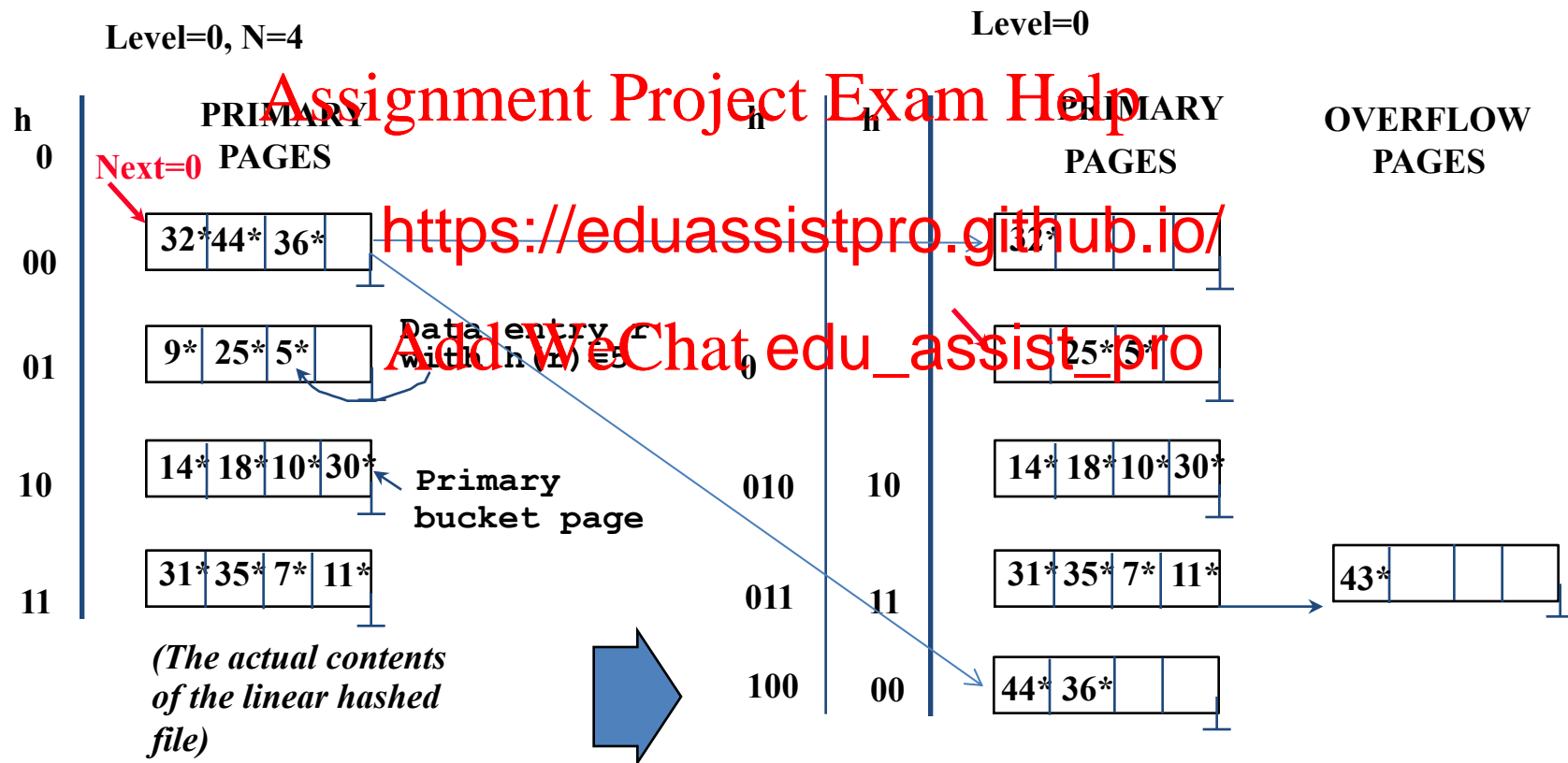
~~Assignment Project Exam Help~~

<https://eduassistpro.github.io/>

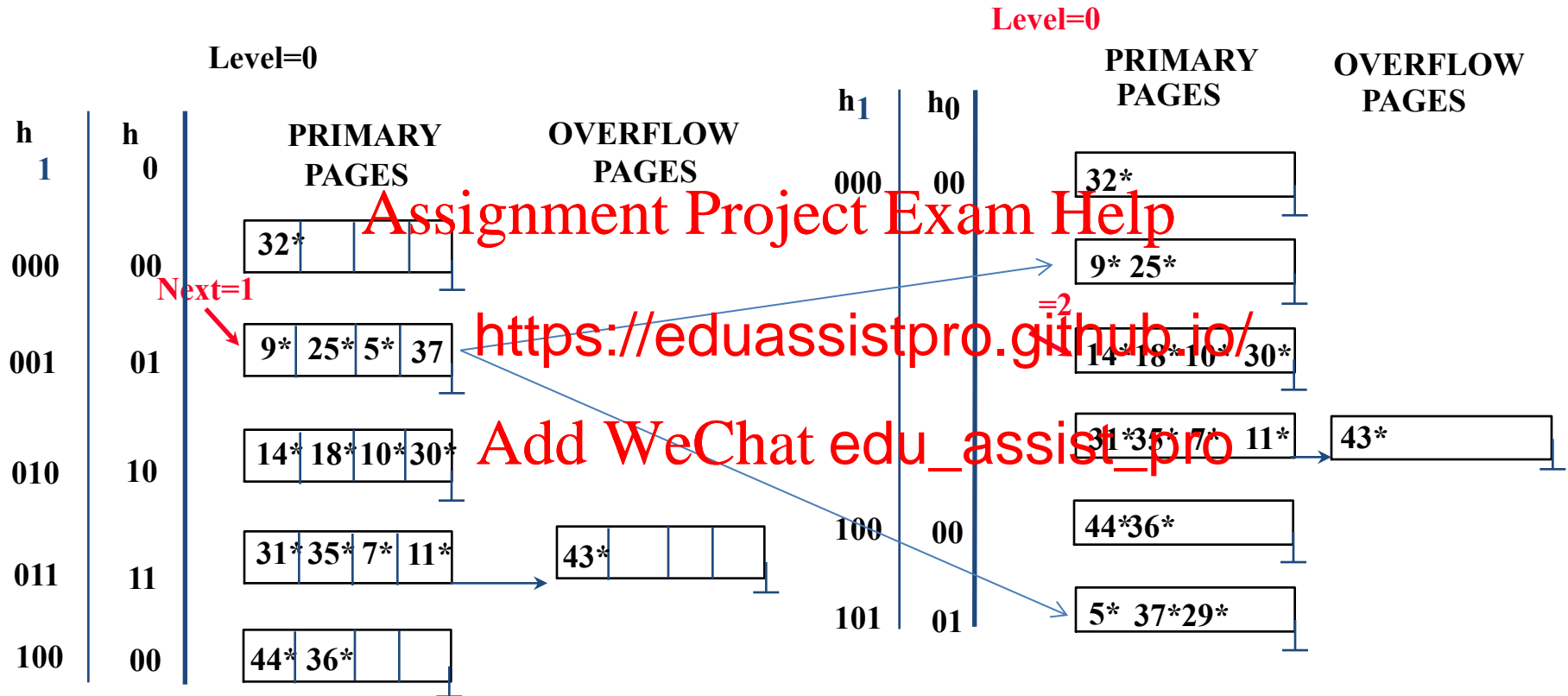
Add WeChat edu_assist_pro

Example of Linear Hashing

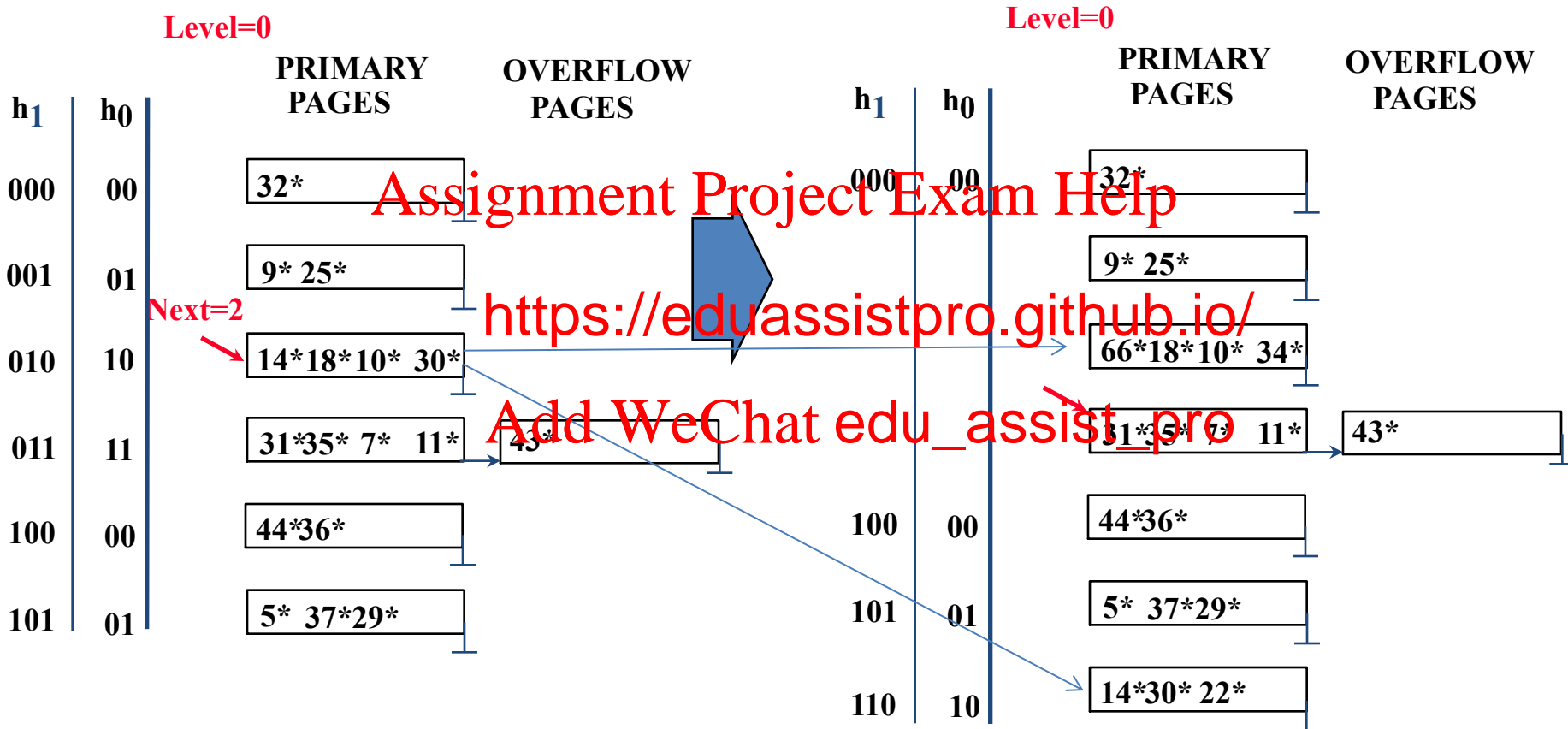
- Insert 43*



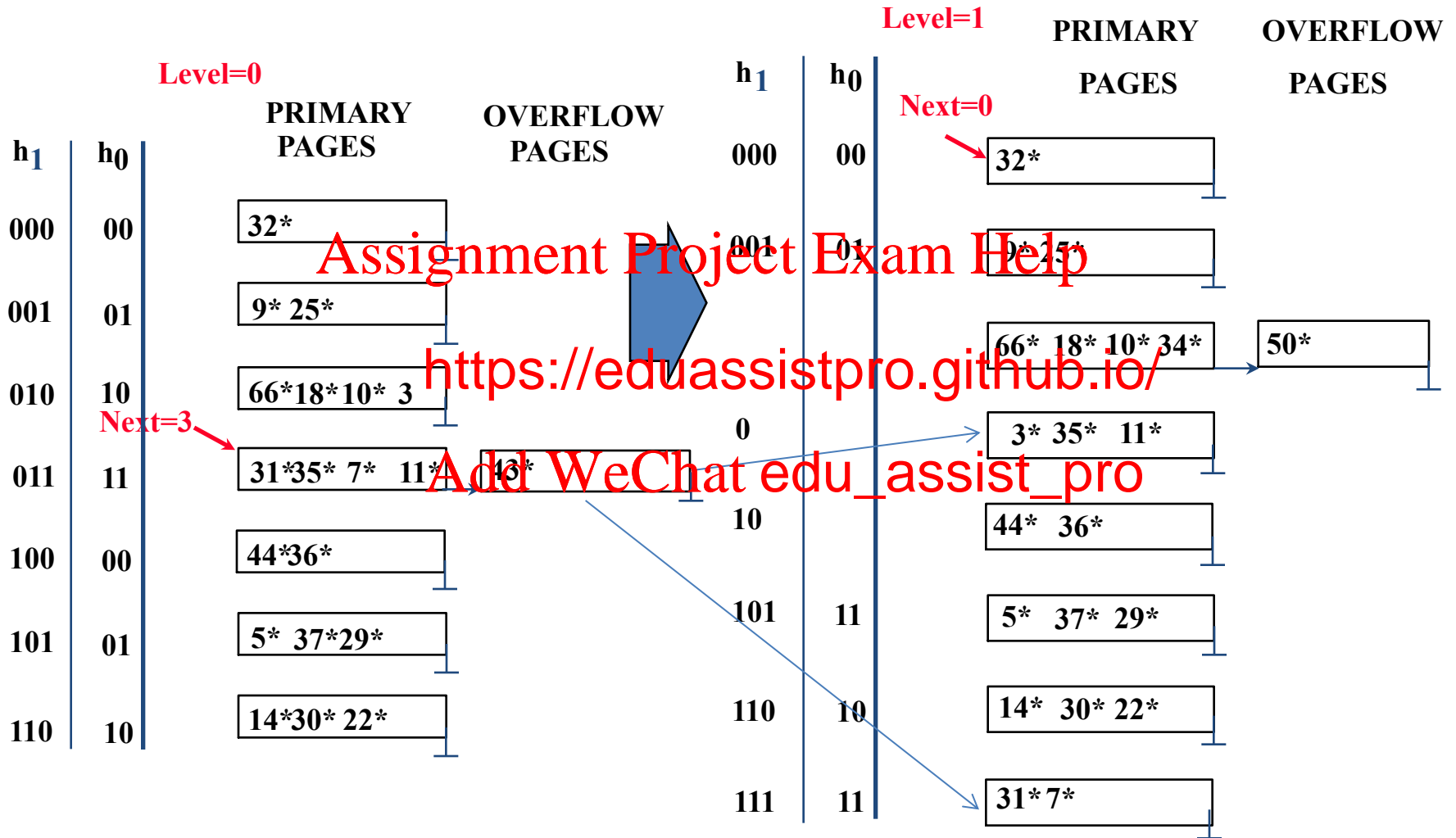
Insert 37 29



Insert 34 66 22



Insert 50



LH Described as a Variant of EH

- The two schemes are actually quite similar:
 - Begin with an EH index where directory has N elements.
 - Use overflow und-robin.
 - First split is at $\text{https://eduassistpro.github.io/}$ directory being doubled at this point.) But $\text{Add WeChat edu_assist_pro}$ $\langle 1, N+1 \rangle, \langle 2, N+2 \rangle, \dots$ are the same. So, need only create directory element N , which differs from 0, now.
 - When bucket 1 splits, create directory element $N+1$, etc.
- So, directory can double gradually. Also, primary bucket pages are created in order. If they are allocated in sequence too (so that finding 'this

Summary

- Hash-based indexes: best for equality searches, cannot support range searches.
- Static Hashing can lead to long overflow chains.
- Extendible Hashing: new pages by splitting a full bucket. A new entry is to be added to it. (Duplicate pages.)
 - Directory to keep track of buckets, doubles periodically.
 - Can get large with skewed data; additional I/O if this does not fit in main memory.

Summary (Contd.)

- Linear Hashing avoids directory by splitting buckets round-robin, and using overflow pages.
 - Overflow pages not likely to be long.
 - Duplicates handled easily.
 - Space utilization is an Extendible Hashing, since buckets are split on 'dense' data areas.
 - Can tune criterion for triggering splits to trade-off slightly longer chains for better space utilization.
- For hash-based indexes, a *skewed* data distribution is one in which the *hash values* of data entries are not uniformly distributed!

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu_assist_pro