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#### Generative vs. Discriminative Learning

• Generative models:

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- Example: Naive Bayes.
- · Acridictive chated assist\_predictive chated
  - Example: Decision tree, Logistic Regre
  - Instance-based Learning.
    - Example: kNN classifier.

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### Task Add We Chat edu\_assist\_pr

- Input:  $(x^{(i)}, y^{(i)})$  pairs  $(1 \le i \le n)$
- Preprocess: let  $\mathbf{x}^{(i)} = \begin{bmatrix} 1 & x^{(i)} \end{bmatrix}^{\top}$
- Output: The best  $\mathbf{w} = \begin{bmatrix} w_0 & w_1 \end{bmatrix}^{\top}$  such that  $\hat{y} = \mathbf{w}^{\top} \mathbf{x}$  best explains the observations

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#### Minimizing a Function

Taylor Series of f(x) at point a

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- close to x.
- If A(x) has low in in the edu\_assist\_property of  $f''(x^*) > 0$ .

Minimum of the local minima is the global minimum if it is smaller than the function values at all the boundary points.

• Intuitively, f(x) is almost  $f(a) + \frac{f''(a)}{2}(x-a)^2$  if a is close to  $x^*$ .

#### Find the Least Square Fit for Linear Regression

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By setting the above to 0, this essentially requires, f Add WeChat edu\_assist\_pr

$$\sum_{i=1}^{n} \hat{y}^{(i)} x_{j}^{(i)} \neq \sum_{i=1}^{n} y^{(i)} x_{j}^{(i)}$$

what the model predicts

what the data says

#### Find the Least Square Fit for Linear Regression

In the simple 1D case, we have only two parameters in  $\mathbf{w} = \begin{bmatrix} w_0 \\ w_1 \end{bmatrix}$ 

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Since  $x_0^{(i)} = 1$ , they are essentially

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$$\sum_{i=1}^{n} (w_0 + w_1 x_1^{(i)}) \cdot x_1^{(i)} = \sum_{i=1}^{n} y^{(i)} \cdot x_1^{(i)}$$

#### Example

Using the same example in https://en.wikipedia.org/wiki/

#### Generalization to *m*-dim

• Easily generalizes to more than 2-dim:

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- How to perform polynomial regression for  $A_i = A_i + A_i$ 
  - Let  $x_i^{*,'} = (x_1^{*,'})^i \Longrightarrow Polynomi$ (http://mathworld.wolfram.com/ LeastSquaresFittingPolynomial.html)

#### Probablistic Interpretation

High-level idea:

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  - If we also incorporate some prior on

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• Many models and their variants can be deemed as different ways of estimating  $P(y^{(i)} | \hat{y}^{(i)})$ 

#### Geometric Interpretation and the Closed Form Solution

Find  $\mathbf{w}$  such that  $\|\mathbf{y} - \mathbf{X}\mathbf{w}\|_2$  is minimized.

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• It is the hyperplane spanned by the d column vectors of  $\mathbf{X}$ .

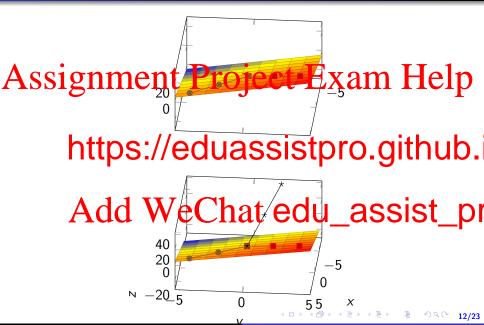
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column of X as  $X_i$ )

$$\begin{array}{cccc} Add_1^{\top} W & \text{Chat edu\_assist\_properties} \\ X_2^{\top}(\mathbf{y} - \mathbf{X} \mathbf{w}) &= 0 \\ \dots &= 0 \\ X_d^{\top}(\mathbf{y} - \mathbf{X} \mathbf{w}) &= 0 \end{array} \right\} \Longrightarrow \mathbf{X}^{\top}(\mathbf{y} - \mathbf{X} \mathbf{w}) = \mathbf{0}$$

$$\mathbf{w} = (\mathbf{X}^{\top}\mathbf{X})^{-1}\mathbf{X}^{\top}\mathbf{y} = \mathbf{X}^{+}\mathbf{y}$$

(X<sup>+</sup>: pseudo inverse of X)



#### Logistic Regression

Special case:  $y^{(i)} \in \{0, 1\}.$ 

• Not appropriate to directly regress  $y^{(i)}$ .

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- What can we say about  $p_{\mathsf{x}+\epsilon}$  w
- Aswel: we impose a linear relationship bet assist product a simple linear model (Note: all points share the same parameter w)
  - Problem: mismatch of the domains: vs
  - Solution: mean function / inverse of link function:  $g^{-1}:\Re \to \mathrm{params}$

#### Solution

• Solution: Link function  $g(parameters) \to \Re$ 

### Assignment Project, Exam Help

https://eduassistpro.github.  $\frac{1+e^{\mathbf{w}^{\mathsf{T}}\mathbf{x}}}{1+e^{\mathbf{w}^{\mathsf{T}}\mathbf{x}}}$ 

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- Decision boundary is  $p \ge 0.5$ .
  - Equivalent to whether  $\mathbf{w}^{\top}\mathbf{x} \geq 0$ . Hence, LR is a linear classifier.



#### Learning the Parameter w

- Consider a training data point  $x^{(i)}$ .
- Recall that the conditional probability ( $Pr[y^{(i)} = 1 \mid x^{(i)}]$ ) Assignment function to the likelihood of  $\mathbf{x}^{(i)}$  is denoted by the shorthand notation to th

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Log-likelihood is (assume log ≜ ln)

$$\ell(\mathbf{w}) = \sum_{i=1}^{n} y^{(i)} \log p(\mathbf{x}^{(i)}) + (1 - y^{(i)}) \log (1 - p(\mathbf{x}^{(i)}))$$
 (5)

#### Learning the Parameter w

• To maximize  $\ell$ , notice that it is concave. So take its partial

$$Assignment Project Exam Help \\ \frac{\partial \ell(\mathbf{w})}{\partial \mathbf{w}_{j}} = y^{(i)} \frac{1}{y^{(i)}} \frac{\partial p(\mathbf{x}^{(i)})}{\partial \mathbf{y}_{j}} + (1 \quad y^{(i)}) \frac{1}{y^{(i)}} \frac{\partial (1 - p(\mathbf{x}^{(i)}))}{\partial \mathbf{w}_{j}}$$

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$$\sum_{i=1}^{n} \hat{y}^{(i)} \cdot \mathbf{x}^{(i)}_{j} = \left[\sum_{i=1}^{n} p(\mathbf{x}^{(i)}) \mathbf{x}^{(i)}_{j}\right] = \left[\sum_{i=1}^{n} y^{(i)} \cdot \mathbf{x}^{(i)}_{j}\right]$$

what the model predicts

what the data says

#### Understand the Equilibrium

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  - The Ltd Stay strift we read our learned model to assessing the classification of training data, the LHS is the expected sum of
  - If this is still abstract, think of an example.

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#### (Stochastic) Gradient Ascent

- w is intialized to some random value (e.g., 0).
- Since the gradient gives the steepest direction to increase a

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### where dealing over the epochs. Where dealing over the epochs.

• Stochastic version: using the gradient on a randomly selected training instance, i.e.,

$$w_j \leftarrow w_j + \alpha(y^{(i)} - p(\mathbf{x^{(i)}}))\mathbf{x^{(i)}}_j$$

#### Newton's Method

• Gradient Ascent moves to the "right" direction a tiny step a

Assignation a good step size?

Assignation between the property of the proper

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$$A \stackrel{\Leftrightarrow}{\underset{\longrightarrow}{d}} d \stackrel{f'(a)}{\underset{\longrightarrow}{d}} \stackrel{+}{\underset{\longrightarrow}{f''(a)}} \stackrel{+}{\underset{\longrightarrow}{f''(a)}} c hat edu\_assist\_pr$$

 Can be applied to multiple dimension cases too ⇒ need to use  $\nabla$  (gradient) and Hess (Hessian).

#### Regularization

- Regularization is another method to deal with overfitting.
  - It is designed to penalize large values of the model parameters.

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• Instead of optimizing for  $\ell(\mathbf{w})$ , we optimize  $\ell(\mathbf{w}) + \lambda R(\mathbf{w})$ .

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• Grid search: http:

### Add her the fittenation of the model pa

- $R(\mathbf{w})$  quantities the "size" of the model pachoices are:
  - $L_2$  regularization (Ridge LR)  $R(\mathbf{w}) = ||\mathbf{w}||_2$
  - $L_1$  regularization (Lasso LR)  $R(\mathbf{w}) = \|w\|_1$
  - ullet  $L_1$  regularization is more likely to result in sparse models.

#### Generalizing LR to Multiple Classes

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- Z is the normalization constant.
- Let  $\mathbf{c}^*$  be the last class in C, the
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- Both belong to exponential or log

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- Tom Mitchell's book chapter: ht

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