13 Text classification and Naive Bayes

Thus far, this book has mainly discussed the process of ad hoc retrieval, where users have transient information needs that they try to address by posing one or more queries to search engine. However, many users have ongoing for introduced. For example for meht xeed of track developments in multicore computer chips. One way of doing this is to issue the query multie e articles each

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DING QUERY

pt that it nts are incre-

is periodically executed on a collection to w mentally added over time.

A colic tanking the cry in a full COU assistivou will tend to miss many relevant new articles which u as multicore

processors. To achieve good recall, standing queries thus have to be refined over time and can gradually become quite complex. In this example, using a Boolean search engine with stemming, you might end up with a query like (multicore OR multi-core) AND (chip OR processor OR microprocessor).

To capture the generality and scope of the problem space to which standing queries belong, we now introduce the general notion of a *classification* problem. Given a set of *classes*, we seek to determine which class(es) a given object belongs to. In the example, the standing query serves to divide new newswire articles into the two classes: documents about multicore computer chips and documents not about multicore computer chips. We refer to this as *two-class classification*. Classification using standing queries is also called *routing* or *filtering* and will be discussed further in Section 15.3.1 (page 335).

A class need not be as narrowly focused as the standing query *multicore computer chips*. Often, a class is a more general subject area like *China* or *coffee*. Such more general classes are usually referred to as *topics*, and the classification task is then called *text classification*, *text categorization*, *topic classification*, or *topic spotting*. An example for *China* appears in Figure 13.1. Standing queries and topics differ in their degree of specificity, but the methods for

STANDING QUERY

CLASSIFICATION

ROUTING FILTERING

TEXT CLASSIFICATION

solving routing, filtering, and text classification are essentially the same. We therefore include routing and filtering under the rubric of text classification in this and the following chapters.

The notion of classification is very general and has many applications within and beyond information retrieval (IR). For instance, in computer vision, a classifier may be used to divide images into classes such as *landscape*, *portrait*, and *neither*. We focus here on examples from information retrieval such as:

 Several of the preprocessing steps necessary for indexing as discussed in Chapter 2: detecting a document's encoding (ASCII, Unicode UTF-8 etc; page 20); word segmentation (Is the white space between two letters a word boundary or not? page 24); truecasing (page 30); and identifying the language of a document (page 46).

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SENTIMENT DETECTION

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EMAIL SORTING

Personal email sorting. A user may hav
 nouncements, electronic bills, email from family and friends, and so on, and may want a classifier to classify each incoming email and automatically move it to the appropriate folder. It is easier to find messages in sorted folders than in a very large inbox. The most common case of this application is a spam folder that holds all suspected spam messages.

VERTICAL SEARCH ENGINE

- Topic-specific or *vertical* search. *Vertical search engines* restrict searches to a particular topic. For example, the query computer science on a vertical search engine for the topic *China* will return a list of Chinese computer science departments with higher precision and recall than the query computer science China on a general purpose search engine. This is because the vertical search engine does not include web pages in its index that contain the term china in a different sense (e.g., referring to a hard white ceramic), but does include relevant pages even if they do not explicitly mention the term China.
- Finally, the ranking function in ad hoc information retrieval can also be based on a document classifier as we will explain in Section 15.4 (page 341).

This list shows the general importance of classification in IR. Most retrieval systems today contain multiple components that use some form of classifier. The classification task we will use as an example in this book is text classification.

A computer is not essential for classification. Many classification tasks have traditionally been solved manually. Books in a library are assigned Library of Congress categories by a librarian. But manual classification is expensive to scale. The *multicore computer chips* example illustrates one alternative approach: classification by the use of standing queries – which can be thought of as *rules* – most commonly written by hand. As in our example (multicore OR multi-core) AND (chip OR processor OR microprocessor), rules are sometimes equivalent to Boolean expressions.

RULES IN TEXT CLASSIFICATION

A rule captures a certain combination of keywords that indicates a class. Hand-coded rules have good scaling properties, but creating and maintaining them over time in labor intensive. A technically skilled person (e.g., a contain expert violation good at writing regular expressions can be tended.

gen aid expert who it good at writing regular expressions, land tente rule sets that will rival or exceed the accuracy of the automatically generated classomeone with

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cation. It is the approach that we focus on in the n chapters. In machine learning, the set of rules or, more sion criterion of that a classific true practical under the chapters. In sion criterion of that a classification is also called statistical text classification.

STATISTICAL TEXT CLASSIFICATION

LABELING

In statistical text classification, we require a number of good example documents (or training documents) for each class. The need for manual classification is not eliminated because the training documents come from a person who has labeled them – where *labeling* refers to the process of annotating each document with its class. But labeling is arguably an easier task than writing rules. Almost anybody can look at a document and decide whether or not it is related to China. Sometimes such labeling is already implicitly part of an existing workflow. For instance, you may go through the news articles returned by a standing query each morning and give relevance feedback (cf. Chapter 9) by moving the relevant articles to a special folder like *multicore-processors*.

We begin this chapter with a general introduction to the text classification problem including a formal definition (Section 13.1); we then cover Naive Bayes, a particularly simple and effective classification method (Sections 13.2–13.4). All of the classification algorithms we study represent documents in high-dimensional spaces. To improve the efficiency of these algorithms, it is generally desirable to reduce the dimensionality of these spaces; to this end, a technique known as *feature selection* is commonly applied in text clas-

sification as discussed in Section 13.5. Section 13.6 covers evaluation of text classification. In the following chapters, Chapters 14 and 15, we look at two other families of classification methods, vector space classifiers and support vector machines.

13.1 The text classification problem

DOCUMENT SPACE CLASS In text classification, we are given a description $d \in \mathbb{X}$ of a document, where \mathbb{X} is the *document space*; and a fixed set of *classes* $\mathbb{C} = \{c_1, c_2, \ldots, c_J\}$. Classes are also called *categories* or *labels*. Typically, the document space \mathbb{X} is some type of high-dimensional space, and the classes are human defined for the needs of an application, as in the examples *China* and *documents that talk about multicore computer chips* above. We are given a *training set* \mathbb{D} of labeled documents $\langle d, c \rangle$, where $\langle d, c \rangle \in \mathbb{X} \times \mathbb{C}$. For example:

TRAINING SET

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ganization and

LEARNING METHOD

CLASSIFIER

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(13.1)

SUPERVISED LEARNING

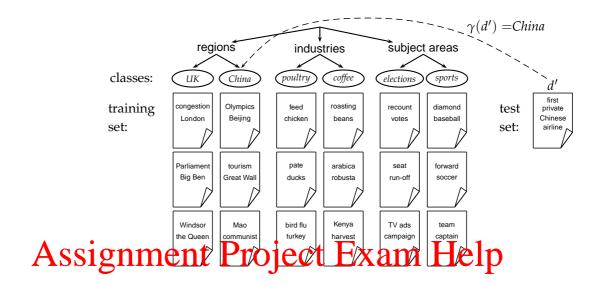
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human who defines the classes and labels training documents) serves as a teacher directing the learning process. We denote the supervised learning method by Γ and write $\Gamma(\mathbb{D}) = \gamma$. The learning method Γ takes the training set \mathbb{D} as input and returns the learned classification function γ .

Most names for learning methods Γ are also used for classifiers γ . We talk about the Naive Bayes (NB) *learning method* Γ when we say that "Naive Bayes is robust," meaning that it can be applied to many different learning problems and is unlikely to produce classifiers that fail catastrophically. But when we say that "Naive Bayes had an error rate of 20%," we are describing an experiment in which a particular NB *classifier* γ (which was produced by the NB learning method) had a 20% error rate in an application.

Figure 13.1 shows an example of text classification from the Reuters-RCV1 collection, introduced in Section 4.2, page 69. There are six classes (UK, China, ..., sports), each with three training documents. We show a few mnemonic words for each document's content. The training set provides some typical examples for each class, so that we can learn the classification function γ . Once we have learned γ , we can apply it to the test set (or test data), for example, the new document test test

TEST SET



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In Figure 13.1, the classification function of the China, Which the Operator U_assistant of the China, Which the China (China) (China

as the hierarchy in Figure 13.1. There are two instances each of region categories, industry categories, and subject area categories. A hierarchy can be an important aid in solving a classification problem; see Section 15.3.2 for further discussion. Until then, we will make the assumption in the text classification chapters that the classes form a set with no subset relationships between them.

Definition (13.1) stipulates that a document is a member of exactly one class. This is not the most appropriate model for the hierarchy in Figure 13.1. For instance, a document about the 2008 Olympics should be a member of two classes: the *China* class and the *sports* class. This type of classification problem is referred to as an *any-of* problem and we will return to it in Section 14.5 (page 306). For the time being, we only consider *one-of* problems where a document is a member of exactly one class.

Our goal in text classification is high accuracy on test data or *new data* – for example, the newswire articles that we will encounter tomorrow morning in the multicore chip example. It is easy to achieve high accuracy on the training set (e.g., we can simply memorize the labels). But high accuracy on the training set in general does not mean that the classifier will work well on

new data in an application. When we use the training set to learn a classifier for test data, we make the assumption that training data and test data are similar or from *the same distribution*. We defer a precise definition of this notion to Section 14.6 (page 308).

13.2 Naive Bayes text classification

MULTINOMIAL NAIVE
BAYES

The first supervised learning method we introduce is the *multinomial Naive Bayes* or *multinomial NB* model, a probabilistic learning method. The probability of a document d being in class c is computed as

(13.2)
$$P(c|d) \propto P(c) \prod_{1 \le k \le n_d} P(t_k|c)$$

Assumer $P(t_k c)$ is the conditional probability of term to occurring the document of class c. We interpret $P(t_k | c)$ as a measure of how much pridence t_k contributes that c is the correct class. P(c) is the prior probability of a declar

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example, $\langle t_1, t_2, \dots, t_{n_d} \rangle$ for the one-se g and Taipei join the WTO might be Beijing Taipei, join around the as solve Fords Π at the terms around the as solve Fords Π at Π and Π at Π

MAXIMUM A POSTERIORI CLASS In text classification, our goal is to find the ument. The best class in NB classification is the most likely or *maximum a posteriori* (MAP) class c_{map} :

(13.3)
$$c_{\text{map}} = \underset{c \in \mathbb{C}}{\arg \max} \, \hat{P}(c|d) = \underset{c \in \mathbb{C}}{\arg \max} \, \hat{P}(c) \prod_{1 < k < n_d} \hat{P}(t_k|c).$$

We write \hat{P} for P because we do not know the true values of the parameters P(c) and $P(t_k|c)$, but estimate them from the training set as we will see in a moment.

In Equation (13.3), many conditional probabilities are multiplied, one for each position $1 \le k \le n_d$. This can result in a floating point underflow. It is therefore better to perform the computation by adding logarithms of probabilities instead of multiplying probabilities. The class with the highest log probability score is still the most probable; $\log(xy) = \log(x) + \log(y)$ and the logarithm function is monotonic. Hence, the maximization that is

^{1.} We will explain in the next section why P(c|d) is proportional to (∞) , not equal to the quantity on the right.

actually done in most implementations of NB is:

(13.4)
$$c_{\text{map}} = \underset{c \in \mathbb{C}}{\arg \max} \left[\log \hat{P}(c) + \sum_{1 \le k \le n_d} \log \hat{P}(t_k|c) \right].$$

Equation (13.4) has a simple interpretation. Each conditional parameter $\log \hat{P}(t_k|c)$ is a weight that indicates how good an indicator t_k is for c. Similarly, the prior $\log \hat{P}(c)$ is a weight that indicates the relative frequency of c. More frequent classes are more likely to be the correct class than infrequent classes. The sum of log prior and term weights is then a measure of how much evidence there is for the document being in the class, and Equation (13.4) selects the class for which we have the most evidence.

We will initially work with this intuitive interpretation of the multinomial NB model and defer a formal derivation to Section 13.4.

How do we estimate the parameters $\hat{P}(c)$ and $\hat{P}(t_k|c)$? We first try the maximum likelihood estimate (MLE; Section 11.3.2, page 22), which is simply likely required for the parameter given the training data. For the priors this estimate is:

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We estimate the conditional probabil requency of team and occurrent shelonging to cool assist_pro

$$\hat{P}(t|c) = \frac{1}{\sum_{t' \in V} T_{ct'}}$$

where T_{ct} is the number of occurrences of t in training documents from class c, including multiple occurrences of a term in a document. We have made the positional independence assumption here, which we will discuss in more detail in the next section: T_{ct} is a count of occurrences in all positions k in the documents in the training set. Thus, we do not compute different estimates for different positions and, for example, if a word occurs twice in a document, in positions k_1 and k_2 , then $\hat{P}(t_{k_1}|c) = \hat{P}(t_{k_2}|c)$.

The problem with the MLE estimate is that it is zero for a term—class combination that did not occur in the training data. If the term WTO in the training data only occurred in *China* documents, then the MLE estimates for the other classes, for example *UK*, will be zero:

$$\hat{P}(WTO|UK) = 0.$$

Now, the one-sentence document *Britain is a member of the WTO* will get a conditional probability of zero for *UK* because we are multiplying the conditional probabilities for all terms in Equation (13.2). Clearly, the model should

```
TrainMultinomialNB(\mathbb{C},\mathbb{D})
  1 V \leftarrow \text{EXTRACTVOCABULARY}(\mathbb{D})
 2 N \leftarrow \text{CountDocs}(\mathbb{D})
 3 for each c \in \mathbb{C}
  4 do N_c \leftarrow \text{COUNTDOCSINCLASS}(\mathbb{D}, c)
           prior[c] \leftarrow N_c/N
 6
           text_c \leftarrow ConcatenateTextOfAllDocsInClass(\mathbb{D}, c)
 7
           for each t \in V
 8
           do T_{ct} \leftarrow \text{COUNTTOKENSOFTERM}(text_c, t)
 9
           \quad \text{for each } t \in V
    do condprob[t][c] \leftarrow \frac{T_{ct}+1}{\sum_{t'}(T_{ct'}+1)}

return V, prior, condprob
10
```

APPLYMULTINOMIALNB(\mathbb{C} , V, prior, cond prob, d)

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assign a high probability to the *UK* class because the term Britain occurs. The problem is that the zero probability for WTO cannot be "conditioned away," no matter how strong the evidence for the class *UK* from other features. The estimate is 0 because of *sparseness*: The training data are never large enough to represent the frequency of rare events adequately, for example, the frequency of WTO occurring in *UK* documents.

SPARSENESS

ADD-ONE SMOOTHING

To eliminate zeros, we use *add-one* or *Laplace smoothing*, which simply adds one to each count (cf. Section 11.3.2):

(13.7)
$$\hat{P}(t|c) = \frac{T_{ct} + 1}{\sum_{t' \in V} (T_{ct'} + 1)} = \frac{T_{ct} + 1}{(\sum_{t' \in V} T_{ct'}) + B'}$$

where B = |V| is the number of terms in the vocabulary. Add-one smoothing can be interpreted as a uniform prior (each term occurs once for each class) that is then updated as evidence from the training data comes in. Note that this is a prior probability for the occurrence of a *term* as opposed to the prior probability of a *class* which we estimate in Equation (13.5) on the document level.

► **Table 13.1** Data for parameter estimation examples.

	docID	words in document	in $c = China$?
training set	1	Chinese Beijing Chinese	yes
	2	Chinese Chinese Shanghai	yes
	3	Chinese Macao	yes
	4	Tokyo Japan Chinese	no
test set	5	Chinese Chinese Tokyo Japan	?

► **Table 13.2** Training and test times for NB.

mode	time complexity
training	$\Theta(\mathbb{D} L_{\text{ave}} + \mathbb{C} V)$
testing	$\Theta(L_{\mathbf{a}} + \mathbb{C} M_{\mathbf{a}}) = \Theta(\mathbb{C} M_{\mathbf{a}})$

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ing an NB classifier. The complete algorithm is described in Figure 13.2.



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Add: We can be a to a constant and a

$$\hat{P}(\mathsf{Chinese}|\overline{c}) = (1 \ 1 \ / \ 3 \ 6 \ 2/9$$

$$\hat{P}(\mathsf{Tokyo}|\overline{c}) = \hat{P}(\mathsf{Japan}|\overline{c}) = (1+1)/(3+6) = 2/9$$

The denominators are (8+6) and (3+6) because the lengths of $text_c$ and $text_{\overline{c}}$ are 8 and 3, respectively, and because the constant B in Equation (13.7) is 6 as the vocabulary consists of six terms.

We then get:

$$\hat{P}(c|d_5) \propto 3/4 \cdot (3/7)^3 \cdot 1/14 \cdot 1/14 \approx 0.0003.$$

 $\hat{P}(\overline{c}|d_5) \propto 1/4 \cdot (2/9)^3 \cdot 2/9 \cdot 2/9 \approx 0.0001.$

Thus, the classifier assigns the test document to c = China. The reason for this classification decision is that the three occurrences of the positive indicator Chinese in d_5 outweigh the occurrences of the two negative indicators Japan and Tokyo.

What is the time complexity of NB? The complexity of computing the parameters is $\Theta(|\mathbb{C}||V|)$ because the set of parameters consists of $|\mathbb{C}||V|$ conditional probabilities and $|\mathbb{C}|$ priors. The preprocessing necessary for computing the parameters (extracting the vocabulary, counting terms, etc.) can be done in one pass through the training data. The time complexity of this

component is therefore $\Theta(|\mathbb{D}|L_{ave})$, where $|\mathbb{D}|$ is the number of documents and L_{ave} is the average length of a document.

We use $\Theta(|\mathbb{D}|L_{\text{ave}})$ as a notation for $\Theta(T)$ here, where T is the length of the training collection. This is nonstandard; $\Theta(.)$ is not defined for an average. We prefer expressing the time complexity in terms of \mathbb{D} and L_{ave} because these are the primary statistics used to characterize training collections.

The time complexity of APPLYMULTINOMIALNB in Figure 13.2 is $\Theta(|\mathbb{C}|L_a)$. L_a and M_a are the numbers of tokens and types, respectively, in the test document. APPLYMULTINOMIALNB can be modified to be $\Theta(L_a + |\mathbb{C}|M_a)$ (Exercise 13.8). Finally, assuming that the length of test documents is bounded, $\Theta(L_a + |\mathbb{C}|M_a) = \Theta(|\mathbb{C}|M_a)$ because $L_a < b|C|M_a$ for a fixed constant b.²

Table 13.2 summarizes the time complexities. In general, we have $|\mathbb{C}||V| < |\mathbb{D}|L_{ave}$, so both training and testing complexity are linear in the time it takes to scan the data. Because we have to look at the data at least once, NB can be said to have optimal time complexity. Its efficiency is one reason why NB is

Assign the tastification be to the complexity. Its efficiency is one teason why NB is

13.2.1 Relati

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a special case of Equation (12.12) fro

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(13.8)

The document d in text classification (Equation (13.2)) takes the role of the query in language modeling (Equation (13.8)) and the classes c in text classification take the role of the documents d in language modeling. We used Equation (13.8) to rank documents according to the probability that they are relevant to the query q. In NB classification, we are usually only interested in the top-ranked class.

We also used MLE estimates in Section 12.2.2 (page 243) and encountered the problem of zero estimates owing to sparse data (page 244); but instead of add-one smoothing, we used a mixture of two distributions to address the problem there. Add-one smoothing is closely related to add- $\frac{1}{2}$ smoothing in Section 11.3.4 (page 228).

2 Exercise 13.1

Why is $|\mathbb{C}||V| < |\mathbb{D}|L_{\text{ave}}$ in Table 13.2 expected to hold for most text collections?

^{2.} Our assumption here is that the length of test documents is bounded. L_a would exceed $b|C|M_a$ for extremely long test documents.

```
TrainBernoulliNB(\mathbb{C},\mathbb{D})
             1 V \leftarrow \text{EXTRACTVOCABULARY}(\mathbb{D})
             2 N \leftarrow \text{CountDocs}(\mathbb{D})
             3 for each c \in \mathbb{C}
                do N_c \leftarrow \text{COUNTDOCSINCLASS}(\mathbb{D}, c)
             5
                     prior[c] \leftarrow N_c/N
             6
                     for each t \in V
             7
                     do N_{ct} \leftarrow \text{COUNTDOCSINCLASSCONTAININGTERM}(\mathbb{D}, c, t)
             8
                         condprob[t][c] \leftarrow (N_{ct}+1)/(N_c+2)
                 return V , prior , condprob
             APPLYBERNOULLINB(\mathbb{C}, V, prior, condprob, d)
                 V_d \leftarrow \text{EXTRACTTERMSFROMDOC}(V, d)
                 for each c \in \mathbb{C}
Assignment Project Exam Help
                     do if t \in V_d
```

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```
Figure 13.3 NB algorithm (Bernoulli dd-one smoothing in Tint 8 (top is it analogy to Ecolati assist pro
```

13.3 The Bernoulli model

There are two different ways we can set up an NB classifier. The model we introduced in the previous section is the multinomial model. It generates one term from the vocabulary in each position of the document, where we assume a generative model that will be discussed in more detail in Section 13.4 (see also page 237).

BERNOULLI MODEL

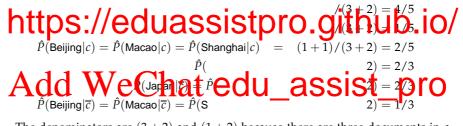
An alternative to the multinomial model is the *multivariate Bernoulli model* or *Bernoulli model*. It is equivalent to the binary independence model of Section 11.3 (page 222), which generates an indicator for each term of the vocabulary, either 1 indicating presence of the term in the document or 0 indicating absence. Figure 13.3 presents training and testing algorithms for the Bernoulli model. The Bernoulli model has the same time complexity as the multinomial model.

The different generation models imply different estimation strategies and different classification rules. The Bernoulli model estimates $\hat{P}(t|c)$ as the *fraction of documents* of class c that contain term t (Figure 13.3, TRAINBERNOULLI-

NB, line 8). In contrast, the multinomial model estimates $\hat{P}(t|c)$ as the *fraction of tokens* or *fraction of positions* in documents of class c that contain term t (Equation (13.7)). When classifying a test document, the Bernoulli model uses binary occurrence information, ignoring the number of occurrences, whereas the multinomial model keeps track of multiple occurrences. As a result, the Bernoulli model typically makes many mistakes when classifying long documents. For example, it may assign an entire book to the class *China* because of a single occurrence of the term China.

The models also differ in how nonoccurring terms are used in classification. They do not affect the classification decision in the multinomial model; but in the Bernoulli model the probability of nonoccurrence is factored in when computing P(c|d) (Figure 13.3, APPLYBERNOULLINB, Line 7). This is because only the Bernoulli NB model models absence of terms explicitly.

Example 13.2: Appling the Bernoulli middle to the example in Table 13.1, we have the sum estimates for the process before: \hat{\hat{L}} & \hat{L} & \hat{L}



The denominators are (3+2) and (1+2) because there are three documents in c and one document in \overline{c} and because the constant B in Equation (13.7) is 2 – there are two cases to consider for each term, occurrence and nonoccurrence.

The scores of the test document for the two classes are

$$\begin{array}{ll} \hat{P}(c|d_5) & \propto & \hat{P}(c) \cdot \hat{P}(\mathsf{Chinese}|c) \cdot \hat{P}(\mathsf{Japan}|c) \cdot \hat{P}(\mathsf{Tokyo}|c) \\ & \qquad \cdot (1 - \hat{P}(\mathsf{Beijing}|c)) \cdot (1 - \hat{P}(\mathsf{Shanghai}|c)) \cdot (1 - \hat{P}(\mathsf{Macao}|c)) \\ & = & 3/4 \cdot 4/5 \cdot 1/5 \cdot 1/5 \cdot (1 - 2/5) \cdot (1 - 2/5) \cdot (1 - 2/5) \\ & \approx & 0.005 \end{array}$$

and, analogously,

$$\hat{P}(\overline{c}|d_5) \propto 1/4 \cdot 2/3 \cdot 2/3 \cdot 2/3 \cdot (1-1/3) \cdot (1-1/3) \cdot (1-1/3)$$

 ≈ 0.022

Thus, the classifier assigns the test document to $\overline{c} = not$ -China. When looking only at binary occurrence and not at term frequency, Japan and Tokyo are indicators for \overline{c} (2/3 > 1/5) and the conditional probabilities of Chinese for c and \overline{c} are not different enough (4/5 vs. 2/3) to affect the classification decision.

13.4 Properties of Naive Bayes

To gain a better understanding of the two models and the assumptions they make, let us go back and examine how we derived their classification rules in Chapters 11 and 12. We decide class membership of a document by assigning it to the class with the maximum a posteriori probability (cf. Section 11.3.2, page 226), which we compute as follows:

$$c_{\text{map}} = \underset{c \in C}{\operatorname{arg max}} P(c|d)$$

$$= \underset{c \in C}{\operatorname{arg max}} \frac{P(d|c)P(c)}{P(d)}$$

$$= \underset{c \in C}{\operatorname{arg max}} P(d|c)P(c),$$

$$= \underset{c \in C}{\operatorname{arg max}} P(d|c)P(c),$$

Assignment Project Exam Hep the denominator in the last step because P(d) is the same for all classes and

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13.4 and 13.5). The e generation of

two models differ in the formalization of the dodument given the tiles, correspond assist_production of the dodument given the tiles, correspond assist_production.

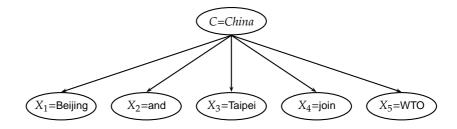
(13.11) **Multinomial**
$$P(d|c) = P(\langle t_1, ..., t_k, ..., t_{n_d} \rangle | c)$$

(13.12) **Bernoulli** $P(d|c) = P(\langle e_1, ..., e_i, ..., e_M \rangle | c)$

where $\langle t_1,\ldots,t_{n_d}\rangle$ is the sequence of terms as it occurs in d (minus terms that were excluded from the vocabulary) and $\langle e_1,\ldots,e_i,\ldots,e_M\rangle$ is a binary vector of dimensionality M that indicates for each term whether it occurs in d or not.

It should now be clearer why we introduced the document space \mathbb{X} in Equation (13.1) when we defined the classification problem. A critical step in solving a text classification problem is to choose the document representation. $\langle t_1, \ldots, t_{n_d} \rangle$ and $\langle e_1, \ldots, e_M \rangle$ are two different document representations. In the first case, \mathbb{X} is the set of all term sequences (or, more precisely, sequences of term tokens). In the second case, \mathbb{X} is $\{0,1\}^M$.

We cannot use Equations (13.11) and (13.12) for text classification directly. For the Bernoulli model, we would have to estimate $2^M |\mathbb{C}|$ different parameters, one for each possible combination of M values e_i and a class. The number of parameters in the multinomial case has the same order of magni-



► Figure 13.4 The multinomial NB model.

tude.³ This being a very large quantity, estimating these parameters reliably is infeasible.

CONDITIONAL CINDEPENDENCE ASSUMPTION

Toppedace the number of parameters, we make the Naive Blyes conditional independence assumption. We assume that attribute values are independent of each other given the class:

(13.13)

https://eduassistpro.github.io/
Bernoulli $P(d|c) = P(\langle e_1, ..., e_M \rangle | c) = P(U_i = e_i | c).$

(13.14)

What in the generative models explicit. X_k is the

RANDOM VARIABLE X

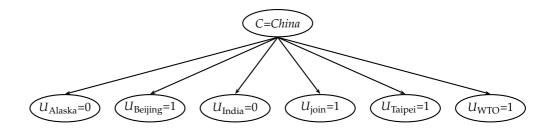
random variable U

document and takes as values terms from the vocabulary. $P(X_k = t|c)$ is the probability that in a document of class c the term t will occur in position k. U_i is the random variable for vocabulary term i and takes as values 0 (absence) and 1 (presence). $\hat{P}(U_i = 1|c)$ is the probability that in a document of class c the term t_i will occur – in any position and possibly multiple times.

We illustrate the conditional independence assumption in Figures 13.4 and 13.5. The class *China* generates values for each of the five term attributes (multinomial) or six binary attributes (Bernoulli) with a certain probability, independent of the values of the other attributes. The fact that a document in the class *China* contains the term Taipei does not make it more likely or less likely that it also contains Beijing.

In reality, the conditional independence assumption does not hold for text data. Terms *are* conditionally dependent on each other. But as we will discuss shortly, NB models perform well despite the conditional independence assumption.

In fact, if the length of documents is not bounded, the number of parameters in the multinomial case is infinite.



► Figure 13.5 The Bernoulli NB model.

Even when assuming conditional independence, we still have too many parameters for the multinomial model if we assume a different probability distribution for each position f in the document. The position of a term in a accumentably treat does not draw information about the dass. Athough there is a difference between *China sues France* and *France sues China*, the

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Also, if we assumed different term distriction would have to estimate a different set of participating is the first term of the from it appearing as the second term, and so in estimation owing to data sparseness.

POSITIONAL INDEPENDENCE

For these reasons, we make a second independence assumption for the multinomial model, *positional independence*: The conditional probabilities for a term are the same independent of position in the document.

$$P(X_{k_1} = t|c) = P(X_{k_2} = t|c)$$

for all positions k_1 , k_2 , terms t and classes c. Thus, we have a single distribution of terms that is valid for all positions k_i and we can use X as its symbol. Positional independence is equivalent to adopting the bag of words model, which we introduced in the context of ad hoc retrieval in Chapter 6 (page 117).

With conditional and positional independence assumptions, we only need to estimate $\Theta(M|C|)$ parameters $P(t_k|c)$ (multinomial model) or $P(e_i|c)$ (Bernoulli

^{4.} Our terminology is nonstandard. The random variable *X* is a categorical variable, not a multinomial variable, and the corresponding NB model should perhaps be called a *sequence model*. We have chosen to present this sequence model and the multinomial model in Section 13.4.1 as the same model because they are computationally identical.

► Table 13.3 Multinomial ve	ersus Bernoulli model. multinomial model	Bernoulli model
event model	generation of token	generation of document
random variable(s)	X = t iff t occurs at given pos	$U_t = 1$ iff t occurs in doc
document representation	$d = \langle t_1, \ldots, t_k, \ldots, t_{n_d} \rangle, t_k \in V$	$d = \langle e_1, \dots, e_i, \dots, e_M \rangle,$ $e_i \in \{0, 1\}$
parameter estimation	$\hat{P}(X=t c)$	$\hat{P}(U_i = e c)$
decision rule: maximize	$\hat{P}(c) \prod_{1 \le k \le n_d} \hat{P}(X = t_k c)$	$\hat{P}(c) \prod_{t_i \in V} \hat{P}(U_i = e_i c)$
multiple occurrences	taken into account	ignored
length of docs	can handle longer docs	works best for short docs
# features	can handle more	works best with fewer
estimate for term the	$\hat{P}(X = \text{the} c) \approx 0.05$	$\hat{P}(U_{\mathrm{the}} = 1 c) \approx 1.0$

Assignmental Proceeding ion Xaturtian a length that is at least exponential in M, the size of the vocabulary. The independence by several

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random variable C

taking values from $\mathbb C$ as values. Next $\mathbb C$ osition $\mathbb C$ with $P(X_k = t_k | c)$ for each of the n_d position $\mathbb C$ and $\mathbb C$ the angular form $\mathbb C$ of the $\mathbb C$ osition $\mathbb C$ we show the generation of $\mathbb C$ of $\mathbb C$ or $\mathbb C$ or $\mathbb C$ or $\mathbb C$ of $\mathbb C$ or $\mathbb C$ of $\mathbb C$ or $\mathbb C$ or

For a completely specified document generation model, we would also have to define a distribution $P(n_d|c)$ over lengths. Without it, the multinomial model is a token generation model rather than a document generation model.

We generate a document in the Bernoulli model (Figure 13.5) by first picking a class C=c with P(c) and then generating a binary indicator e_i for each term t_i of the vocabulary ($1 \le i \le M$). In the example in Figure 13.5, we show the generation of $\langle e_1, e_2, e_3, e_4, e_5, e_6 \rangle = \langle 0, 1, 0, 1, 1, 1 \rangle$, corresponding, again, to the one-sentence document *Beijing and Taipei join WTO* where we have assumed that and is a stop word.

We compare the two models in Table 13.3, including estimation equations and decision rules.

Naive Bayes is so called because the independence assumptions we have just made are indeed very naive for a model of natural language. The conditional independence assumption states that features are independent of each other given the class. This is hardly ever true for terms in documents. In many cases, the opposite is true. The pairs hong and kong or london and en-

▶ Table 13.4 Correct estimation implies accurate prediction, but accurate prediction does not imply correct estimation.

	c_1	c_2	class selected
true probability $P(c d)$	0.6	0.4	c_1
$\hat{P}(c) \prod_{1 \le k \le n_d} \hat{P}(t_k c)$ (Equation (13.13))	0.00099	0.00001	
NB estimate $\hat{P}(c d)$	0.99	0.01	c_1

glish in Figure 13.7 are examples of highly dependent terms. In addition, the multinomial model makes an assumption of positional independence. The Bernoulli model ignores positions in documents altogether because it only cares about absence or presence. This bag-of-words model discards all information that is communicated by the order of words in natural language Shiender. The Man NB 60 that text dass Niervillen it indeed in natural language is so oversimplified?

s of NB are of low sider a document

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 c_1 and many terms that are negative indicators for c. Thus, when using the multinomial model in Equation (1 1) will be much like that \hat{p} (1) will be much vision by 0.001 to get well-formed probability that is close to 1.0 and one that is close to 0.0. This is common: The winning class in NB classification usually has a much larger probability than the other classes and the estimates diverge very significantly from the true probabilities. But the classification decision is based on which class gets the highest score. It does not matter how accurate the estimates are. De-

spite the bad estimates, NB estimates a higher probability for c_1 and therefore assigns d to the correct class in Table 13.4. Correct estimation implies accurate prediction, but accurate prediction does not imply correct estimation. NB classifiers estimate badly, but often classify well.

Even if it is not the method with the highest accuracy for text, NB has many virtues that make it a strong contender for text classification. It excels if there are many equally important features that jointly contribute to the classification decision. It is also somewhat robust to noise features (as defined in the next section) and *concept drift* – the gradual change over time of the concept underlying a class like *US president* from Bill Clinton to George W. Bush (see Section 13.7). Classifiers like kNN (Section 14.3, page 297) can be carefully tuned to idiosyncratic properties of a particular time period. This will then hurt them when documents in the following time period have slightly

CONCEPT DRIFT

- ► **Table 13.5** A set of documents for which the NB independence assumptions are problematic.
 - (1) He moved from London, Ontario, to London, England.
 - (2) He moved from London, England, to London, Ontario.
 - He moved from England to London, Ontario.

different properties.

The Bernoulli model is particularly robust with respect to concept drift. We will see in Figure 13.8 that it can have decent performance when using fewer than a dozen terms. The most important indicators for a class are less likely to change. Thus, a model that only relies on these features is more likely to maintain a certain level of accuracy in concept drift.

Assignment ength sits efficiency fra eing and classifection can be accomplished with one pass over the data. because it combines efficiency with good accuracy it is often used as a baseline in text classification research. I

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ifier on a smaller training set, or (iii) if its robustness to concep oited.

In this book we discuss NB as a classifier for the semplant do not look for the UH when the classifier (in the sense of minimal er

OPTIMAL CLASSIFIER

where the independence assumptions do hold.

13.4.1 A variant of the multinomial model

An alternative formalization of the multinomial model represents each document d as an M-dimensional vector of counts $\langle \mathsf{tf}_{t_1,d},\ldots,\mathsf{tf}_{t_M,d} \rangle$ where $\mathsf{tf}_{t_i,d}$ is the term frequency of t_i in d. P(d|c) is then computed as follows (cf. Equation (12.8), page 243);

(13.15)
$$P(d|c) = P(\langle \mathsf{tf}_{t_1,d}, \dots, \mathsf{tf}_{t_M,d} \rangle | c) \propto \prod_{1 \le i \le M} P(X = t_i | c)^{\mathsf{tf}_{t_i,d}}$$

Note that we have omitted the multinomial factor. See Equation (12.8) (page 243). Equation (13.15) is equivalent to the sequence model in Equation (13.2) as $P(X = t_i | c)^{tf_{t_i,d}} = 1$ for terms that do not occur in d ($tf_{t_i,d} = 0$) and a term that occurs $tf_{t_i,d} \ge 1$ times will contribute $tf_{t_i,d}$ factors both in Equation (13.2) and in Equation (13.15).

13.5 Feature selection 271

```
SELECTFEATURES(\mathbb{D}, c, k)

1 V \leftarrow \text{EXTRACTVOCABULARY}(\mathbb{D})

2 L \leftarrow []

3 for each t \in V

4 do A(t, c) \leftarrow \text{ComputeFeatureUtility}(\mathbb{D}, t, c)

5 APPEND(L, \langle A(t, c), t \rangle)

6 return FeaturesWithLargestValues(L, k)
```

▶ **Figure 13.6** Basic feature selection algorithm for selecting the k best features.

?
Which of the documents in Table 13.5 have identical and different bag of words representations for (i) the Broulli model (ii) the multinomial model? If there are different project Exam Help

Exercise 13.3

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Exercise 13.4

Table 13.3 gives Bernoulli and multinomia the. Explain the difference WeChat edu_assist_pro

13.5 Feature selection

FEATURE SELECTION

Feature selection is the process of selecting a subset of the terms occurring in the training set and using only this subset as features in text classification. Feature selection serves two main purposes. First, it makes training and applying a classifier more efficient by decreasing the size of the effective vocabulary. This is of particular importance for classifiers that, unlike NB, are expensive to train. Second, feature selection often increases classification accuracy by eliminating noise features. A *noise feature* is one that, when added to the document representation, increases the classification error on new data. Suppose a rare term, say arachnocentric, has no information about a class, say *China*, but all instances of arachnocentric happen to occur in *China* documents in our training set. Then the learning method might produce a classifier that misassigns test documents containing arachnocentric to *China*. Such an incorrect generalization from an accidental property of the training set is called *overfitting*.

OVERFITTING

NOISE FEATURE

We can view feature selection as a method for replacing a complex classifier (using all features) with a simpler one (using a subset of the features).

It may appear counterintuitive at first that a seemingly weaker classifier is advantageous in statistical text classification, but when discussing the biasvariance tradeoff in Section 14.6 (page 308), we will see that weaker models are often preferable when limited training data are available.

The basic feature selection algorithm is shown in Figure 13.6. For a given class c, we compute a utility measure A(t,c) for each term of the vocabulary and select the k terms that have the highest values of A(t,c). All other terms are discarded and not used in classification. We will introduce three different utility measures in this section: mutual information, $A(t,c) = I(U_t; C_c)$; the χ^2 test, $A(t,c) = X^2(t,c)$; and frequency, A(t,c) = N(t,c).

Of the two NB models, the Bernoulli model is particularly sensitive to noise features. A Bernoulli NB classifier requires some form of feature selection or else its accuracy will be low.

This section mainly addresses feature selection for two-class classification tasks like China versup of China. Section 13.5.5 briefly discusses optimizations for sylvers with more than the dasks.

Mutua 13.5.1

MUTUAL INFORMATION

(13.16)

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formation the presence/absence of a term

classification decision on c. Formally:

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where *U* is a random variable that takes values $e_t = 1$ (the document contains term t) and $e_t = 0$ (the document does not contain t), as defined on page 266, and *C* is a random variable that takes values $e_c = 1$ (the document is in class c) and $e_c = 0$ (the document is not in class c). We write U_t and C_c if it is not clear from context which term *t* and class *c* we are referring to.

ForMLEs of the probabilities, Equation (13.16) is equivalent to Equation (13.17):

(13.17)
$$I(U;C) = \frac{N_{11}}{N} \log_2 \frac{NN_{11}}{N_{1.}N_{.1}} + \frac{N_{01}}{N} \log_2 \frac{NN_{01}}{N_{0.}N_{.1}} + \frac{N_{10}}{N} \log_2 \frac{NN_{10}}{N_{1.}N_{0}} + \frac{N_{00}}{N} \log_2 \frac{NN_{00}}{N_{0.}N_{0}}$$

where the Ns are counts of documents that have the values of e_t and e_c that are indicated by the two subscripts. For example, N_{10} is the number of doc-

^{5.} Take care not to confuse expected mutual information with pointwise mutual information, which is defined as $\log N_{11}/E_{11}$ where N_{11} and E_{11} are defined as in Equation (13.18). The two measures have different properties. See Section 13.7.

13.5 Feature selection 273

uments that contain t ($e_t = 1$) and are not in c ($e_c = 0$). $N_1 = N_{10} + N_{11}$ is the number of documents that contain t ($e_t = 1$) and we count documents independent of class membership ($e_c \in \{0,1\}$). $N = N_{00} + N_{01} + N_{10} + N_{11}$ is the total number of documents. An example of one of the MLE estimates that transform Equation (13.16) into Equation (13.17) is $P(U = 1, C = 1) = N_{11}/N$.



Example 13.3: Consider the class *poultry* and the term export in Reuters-RCV1. The counts of the number of documents with the four possible combinations of indicator values are as follows:

After plugging these values into Equation (13.17) we get:

Assignment Project 8 (49+27,652) (49+141) Help

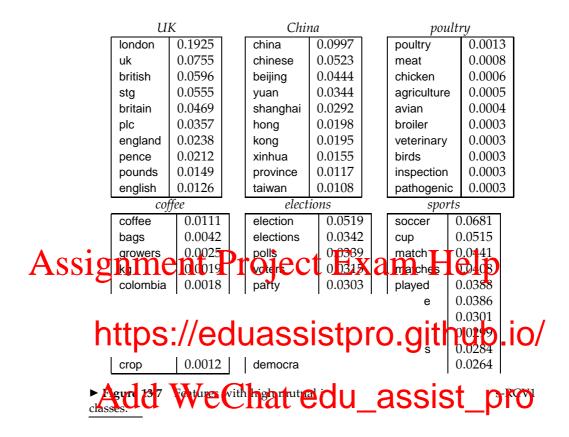
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To select k terms t_1, \ldots, t_k for a given class, we use the feature selection algorithm in Figure 13.6: We compute the utility measure as $A(t,c) = I(U_t, C_c)$ and select the k terms with the largest values.

Mutual information measures how much information – in the information-theoretic sense – a term contains about the class. If a term's distribution is the same in the class as it is in the collection as a whole, then I(U;C)=0. MI reaches its maximum value if the term is a perfect indicator for class membership, that is, if the term is present in a document if and only if the document is in the class.

Figure 13.7 shows terms with high mutual information scores for the six classes in Figure 13.1.⁶ The selected terms (e.g., london, uk, british for the class UK) are of obvious utility for making classification decisions for their respective classes. At the bottom of the list for UK we find terms like peripherals and tonight (not shown in the figure) that are clearly not helpful in deciding

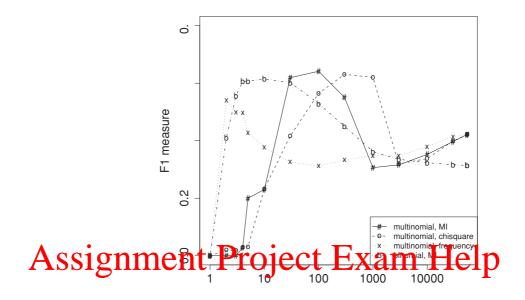
⁶. Feature scores were computed on the first 100,000 documents, except for *poultry*, a rare class, for which 800,000 documents were used. We have omitted numbers and other special words from the top ten lists.



whether the document is in the class. As you might expect, keeping the informative terms and eliminating the non-informative ones tends to reduce noise and improve the classifier's accuracy.

Such an accuracy increase can be observed in Figure 13.8, which shows F_1 as a function of vocabulary size after feature selection for Reuters-RCV1.⁷ Comparing F_1 at 132,776 features (corresponding to selection of all features) and at 10–100 features, we see that MI feature selection increases F_1 by about 0.1 for the multinomial model and by more than 0.2 for the Bernoulli model. For the Bernoulli model, F_1 peaks early, at ten features selected. At that point, the Bernoulli model is better than the multinomial model. When basing a classification decision on only a few features, it is more robust to consider binary occurrence only. For the multinomial model (MI feature selection), the peak occurs later, at 100 features, and its effectiveness recovers somewhat at

^{7.} We trained the classifiers on the first 100,000 documents and computed F_1 on the next 100,000. The graphs are averages over five classes.



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the number of occurrences into account in parameter estimation and classification and therefore better exploits a larger number of features than the Bernoulli model. Regardless of the differences between the two methods, using a carefully selected subset of the features results in better effectiveness than using all features.

13.5.2 χ^2 Feature selection

 χ^2 FEATURE SELECTION

INDEPENDENCE

Another popular feature selection method is χ^2 . In statistics, the χ^2 test is applied to test the independence of two events, where two events A and B are defined to be *independent* if P(AB) = P(A)P(B) or, equivalently, P(A|B) = P(A) and P(B|A) = P(B). In feature selection, the two events are occurrence of the term and occurrence of the class. We then rank terms with respect to the following quantity:

(13.18)
$$X^{2}(\mathbb{D}, t, c) = \sum_{e_{t} \in \{0,1\}} \sum_{e_{c} \in \{0,1\}} \frac{(N_{e_{t}e_{c}} - E_{e_{t}e_{c}})^{2}}{E_{e_{t}e_{c}}}$$

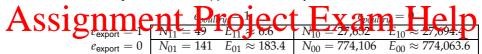
where e_t and e_c are defined as in Equation (13.16). N is the *observed* frequency in \mathbb{D} and E the *expected* frequency. For example, E_{11} is the expected frequency of t and c occurring together in a document assuming that term and class are independent.



Example 13.4: We first compute E_{11} for the data in Example 13.3:

$$E_{11} = N \times P(t) \times P(c) = N \times \frac{N_{11} + N_{10}}{N} \times \frac{N_{11} + N_{01}}{N}$$
$$= N \times \frac{49 + 141}{N} \times \frac{49 + 27652}{N} \approx 6.6$$

where N is the total number of documents as before. We compute the other $E_{e_t e_c}$ in the same way:



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deviate from each other. A high value of X^2 indicates that the hypothesis of independence, which implies that expected and observed counts are similar, is incorrect. In our example, $X^2 \approx 284 > 10.83$. Based on Table 13.6, we can reject the hypothesis that poultry and export are independent with only a 0.001 chance of being wrong. Equivalently, we say that the outcome $X^2 \approx$ 284 > 10.83 is *statistically significant* at the 0.001 level. If the two events are dependent, then the occurrence of the term makes the occurrence of the class more likely (or less likely), so it should be helpful as a feature. This is the rationale of χ^2 feature selection.

STATISTICAL SIGNIFICANCE

An arithmetically simpler way of computing X^2 is the following:

(13.19)
$$X^{2}(\mathbb{D},t,c) = \frac{(N_{11} + N_{10} + N_{01} + N_{00}) \times (N_{11}N_{00} - N_{10}N_{01})^{2}}{(N_{11} + N_{01}) \times (N_{11} + N_{10}) \times (N_{10} + N_{00}) \times (N_{01} + N_{00})}$$

This is equivalent to Equation (13.18) (Exercise 13.14).

^{8.} We can make this inference because, if the two events are independent, then $X^2 \sim \chi^2$, where χ^2 is the χ^2 distribution. See, for example, Rice (2006).

▶ **Table 13.6** Critical values of the χ^2 distribution with one degree of freedom. For example, if the two events are independent, then $P(X^2 > 6.63) < 0.01$. So for $X^2 >$ 6.63 the assumption of independence can be rejected with 99% confidence.

p	χ^2 critical value
0.1	2.71
0.05	3.84
0.01	6.63
0.005	7.88
0.001	10.83

Assessing χ^2 as a feature selection method

From a statistical point of view, χ^2 feature selection is problematic. For a S1Qthiline naree of fiestper the so-called this correction should be used (see Section 13.7), which makes it harder to reach statistical significance. en the probability

are rejected, each

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few additional terms are added to the feature set or removed from it. Rather, ² feature selecthe relative importance of features is im tion or ly analyteatmes with respect to the assists nopule of ce of variables, make statements about statistical depen we need not be overly concerned that it does not adhere strictly to statistical theory.

13.5.3 Frequency-based feature selection

A third feature selection method is frequency-based feature selection, that is, selecting the terms that are most common in the class. Frequency can be either defined as document frequency (the number of documents in the class c that contain the term t) or as collection frequency (the number of tokens of t that occur in documents in c). Document frequency is more appropriate for the Bernoulli model, collection frequency for the multinomial model.

Frequency-based feature selection selects some frequent terms that have no specific information about the class, for example, the days of the week (Monday, Tuesday, ...), which are frequent across classes in newswire text. When many thousands of features are selected, then frequency-based feature selection often does well. Thus, if somewhat suboptimal accuracy is acceptable, then frequency-based feature selection can be a good alternative to more complex methods. However, Figure 13.8 is a case where frequencybased feature selection performs a lot worse than MI and χ^2 and should not be used.

13.5.4 Feature selection for multiple classifiers

In an operational system with a large number of classifiers, it is desirable to select a single set of features instead of a different one for each classifier. One way of doing this is to compute the X^2 statistic for an $n \times 2$ table where the columns are occurrence and nonoccurrence of the term and each row corresponds to one of the classes. We can then select the k terms with the highest X^2 statistic as before.

More commonly, feature selection statistics are first computed separately

for each class on the two-class classification task c versus \overline{c} and then combined. One combination method computes a single figure of merit for each feature, for example, by averaging the values A(t,c) for frature t and then selected that callures with highest figures of marit. Mother frequently used combination method selects the top k/n features for each of n classifiers and

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may be worth the loss in accuracy.

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Mutual information and χ^2 represent rather different feature selection methods. The independence of term t and class c can sometimes be rejected with high confidence even if t carries little information about membership of a document in c. This is particularly true for rare terms. If a term occurs once in a large collection and that one occurrence is in the *poultry* class, then this is statistically significant. But a single occurrence is not very informative according to the information-theoretic definition of information. Because its criterion is significance, χ^2 selects more rare terms (which are often less reliable indicators) than mutual information. But the selection criterion of mutual information also does not necessarily select the terms that maximize classification accuracy.

Despite the differences between the two methods, the classification accuracy of feature sets selected with χ^2 and MI does not seem to differ systematically. In most text classification problems, there are a few strong indicators and many weak indicators. As long as all strong indicators and a large number of weak indicators are selected, accuracy is expected to be good. Both methods do this.

Figure 13.8 compares MI and χ^2 feature selection for the multinomial model.

Peak effectiveness is virtually the same for both methods. χ^2 reaches this peak later, at 300 features, probably because the rare, but highly significant features it selects initially do not cover all documents in the class. However, features selected later (in the range of 100–300) are of better quality than those selected by MI.

GREEDY FEATURE SELECTION All three methods – MI, χ^2 and frequency based – are *greedy* methods. They may select features that contribute no incremental information over previously selected features. In Figure 13.7, kong is selected as the seventh term even though it is highly correlated with previously selected hong and therefore redundant. Although such redundancy can negatively impact accuracy, non-greedy methods (see Section 13.7 for references) are rarely used in text classification due to their computational cost.

2 Exercise 13.5
Consider the following Toppencies for the class of the four terms in the first 100,000 EXAM HELD

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13.6 Evaluation of text classification

] Historically, the classic Reuters-21578 collection was the main benchmark for text classification evaluation. This is a collection of 21,578 newswire articles, originally collected and labeled by Carnegie Group, Inc. and Reuters, Ltd. in the course of developing the CONSTRUE text classification system. It is much smaller than and predates the Reuters-RCV1 collection discussed in Chapter 4 (page 69). The articles are assigned classes from a set of 118 topic categories. A document may be assigned several classes or none, but the commonest case is single assignment (documents with at least one class received an average of 1.24 classes). The standard approach to this *any-of* problem (Chapter 14, page 306) is to learn 118 two-class classifiers, one for each class, where the *two-class classifier* for class c is the classifier for the two classes c and its complement \overline{c} .

TWO-CLASS CLASSIFIER

MODAPTE SPLIT

For each of these classifiers, we can measure recall, precision, and accuracy. In recent work, people almost invariably use the *ModApte split*, which includes only documents that were viewed and assessed by a human indexer,

► **Table 13.7** The ten largest classes in the Reuters-21578 collection with number of documents in training and test sets.

class	# train	# testclass	# train	# test
earn	2877	1087 trade	369	119
acquisitions	1650	179 interest	347	131
money-fx	538	179 ship	197	89
grain	433	149 wheat	212	71
crude	389	189 <i>corn</i>	182	56

and comprises 9,603 training documents and 3,299 test documents. The distribution of documents in classes is very uneven, and some work evaluates systems on only documents in the ten largest classes. They are listed in Tatle 10.0 Ten and 1

ble 13.7. A typical document with topics is shown in Figure 16.9. 1

Solution of Classification error on test data. Classification error is 1.0 minus classification to the control of classification error on test data.

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because always saying no, a strategy that de e of building a classifier, will achieve high accuracy. The 99% accurate for classifier measures. Sign, recall and F_1 are better measures.

EFFECTIVENESS

PERFORMANCE EFFICIENCY

MACROAVERAGING
MICROAVERAGING

We will use *effectiveness* as a generic term for measures that evaluate the quality of classification decisions, including precision, recall, F_1 , and accuracy. *Performance* refers to the computational efficiency of classification and IR systems in this book. However, many researchers mean effectiveness, not efficiency of text classification when they use the term performance.

When we process a collection with several two-class classifiers (such as Reuters-21578 with its 118 classes), we often want to compute a single aggregate measure that combines the measures for individual classifiers. There are two methods for doing this. *Macroaveraging* computes a simple average over classes. *Microaveraging* pools per-document decisions across classes, and then computes an effectiveness measure on the pooled contingency table. Table 13.8 gives an example.

The differences between the two methods can be large. Macroaveraging gives equal weight to each class, whereas microaveraging gives equal weight to each per-document classification decision. Because the F_1 measure ignores true negatives and its magnitude is mostly determined by the number of true positives, large classes dominate small classes in microaveraging. In the example, microaveraged precision (0.83) is much closer to the precision of

C

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► Figure 13.9 A sample document from t

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 c_2 (0.9) than to the precision of c_1 (0.5) because c_2 is five times larger than c_1 . Microaveraged results are therefore really a measure of effectiveness on the large classes in a test collection. To get a sense of effectiveness on small classes, you should compute macroaveraged results.

In one-of classification (Section 14.5, page 306), microaveraged F_1 is the same as accuracy (Exercise 13.6).

Table 13.9 gives microaveraged and macroaveraged effectiveness of Naive Bayes for the ModApte split of Reuters-21578. To give a sense of the relative effectiveness of NB, we compare it with linear SVMs (rightmost column; see Chapter 15), one of the most effective classifiers, but also one that is more expensive to train than NB. NB has a microaveraged F_1 of 80%, which is 9% less than the SVM (89%), a 10% relative decrease (row "micro-avg-L (90 classes)"). So there is a surprisingly small effectiveness penalty for its simplicity and efficiency. However, on small classes, some of which only have on the order of ten positive examples in the training set, NB does much worse. Its macroaveraged F_1 is 13% below the SVM, a 22% relative decrease (row "macro-avg (90 classes)").

The table also compares NB with the other classifiers we cover in this book:

▶ **Table 13.8** Macro- and microaveraging. "Truth" is the true class and "call" the decision of the classifier. In this example, macroaveraged precision is [10/(10+10)+90/(10+90)]/2 = (0.5+0.9)/2 = 0.7. Microaveraged precision is $100/(100+20) \approx 0.83$.

	class 1			class 2		po	ooled tal	ole
	truth:	truth:		truth:	truth:		truth:	truth:
	yes	no		yes	no		yes	no
call: yes	10	10	call: yes	90	10	call: yes	100	20
call: no	10	970	call: no	10	890	call: no	20	1860

▶ **Table 13.9** Text classification effectiveness numbers on Reuters-21578 for F₁ (in percent). Results from Li and Yang (2003) (a), Joachims (1998) (b: kNN) and Dumais

Assign Menter Project Exam Helpvm micro-avg-L (90 classes) 80 85 86 89

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		96	93	97	98	98
	acq	88	65	92	90	94
A -	money-fx7	57	47	78	66	75
A	mener we Chat	₩ O		SSI	3 {	910
	crude	80	70	86	85	89
	trade	64	65	77	73	76
	interest	65	63	74	67	78
	ship	85	49	79	74	86
	wheat	70	69	77	93	92
	corn	65	48	78	92	90
-	micro-avg (top 10)	82	65	82	88	92
	micro-avg-D (118 classes)	75	62	n/a	n/a	87

DECISION TREES

Rocchio and kNN. In addition, we give numbers for *decision trees*, an important classification method we do not cover. The bottom part of the table shows that there is considerable variation from class to class. For instance, NB beats kNN on *ship*, but is much worse on *money-fx*.

Comparing parts (a) and (b) of the table, one is struck by the degree to which the cited papers' results differ. This is partly due to the fact that the numbers in (b) are break-even scores (cf. page 161) averaged over 118 classes, whereas the numbers in (a) are true F_1 scores (computed without any know-

ledge of the test set) averaged over ninety classes. This is unfortunately typical of what happens when comparing different results in text classification: There are often differences in the experimental setup or the evaluation that complicate the interpretation of the results.

These and other results have shown that the average effectiveness of NB is uncompetitive with classifiers like SVMs when trained and tested on *independent and identically distributed* (*i.i.d.*) data, that is, uniform data with all the good properties of statistical sampling. However, these differences may often be invisible or even reverse themselves when working in the real world where, usually, the training sample is drawn from a subset of the data to which the classifier will be applied, the nature of the data drifts over time rather than being stationary (the problem of concept drift we mentioned on page 269), and there may well be errors in the data (among other problems). Many practitioners have had the experience of being unable to build a fancy

ASSI Sold For a certain problem that consistently performs before than NB. Sold For the Sold from the sold Cirl Table X aid that, although thost researchers believe that an SVM is better than kNN and kNN better than NB,

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When performing evaluations like th maintain a strict separation between the test set. We can exclipinate cover elessification described as a good predictor in the test set, such articular term is a good predictor in the test set (even though this is not the case in the training set). A more subtle example of using knowledge about the test set is to try a large number of values of a parameter (e.g., the number of selected features) and select the value that is best for the test set. As a rule, accuracy on new data – the type of data we will encounter when we use the classifier in an application – will be much lower than accuracy on a test set that the classifier has been tuned for. We discussed the same problem in ad hoc retrieval

In a clean statistical text classification experiment, you should never run any program on or even look at the test set while developing a text classification system. Instead, set aside a *development set* for testing while you develop your method. When such a set serves the primary purpose of finding a good value for a parameter, for example, the number of selected features, then it is also called *held-out data*. Train the classifier on the rest of the training set with different parameter values, and then select the value that gives best results on the held-out part of the training set. Ideally, at the very end, when all parameters have been set and the method is fully specified, you run one final experiment on the test set and publish the results. Because no informa-

DEVELOPMENT SET

HELD-OUT DATA

in Section 8.1 (page 153).

▶]	Table 13.10	Data for	parameter	estimation	exercise.
-----	-------------	----------	-----------	------------	-----------

	docID	words in document	in $c = China$?
training set	1	Taipei Taiwan	yes
	2	Macao Taiwan Shanghai	yes
	3	Japan Sapporo	no
	4	Sapporo Osaka Taiwan	no
test set	5	Taiwan Taiwan Sapporo	?

tion about the test set was used in developing the classifier, the results of this experiment should be indicative of actual performance in practice.

This ideal often cannot be met; researchers tend to evaluate several systems on the same test set over a period of several years. But it is neverthesess highly important part look at the telt data and to rule systems on it as springly as possible. Beginners often violate this rule, and their regults lose validity because they have implicitly tuned their system to the test data simthe system.

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Assume a situation where every document in the t een assigned exactly one class and that a classifier also assign that a classifier also assign that a classifier also assign that in the classification (i) the total number of false positive and (ii) microaveraged F_1 and accuracy are identical.

Exercise 13.7

The class priors in Figure 13.2 are computed as the fraction of *documents* in the class as opposed to the fraction of *tokens* in the class. Why?

Exercise 13.8

The function APPLYMULTINOMIALNB in Figure 13.2 has time complexity $\Theta(L_a + |\mathbb{C}|L_a)$. How would you modify the function so that its time complexity is $\Theta(L_a + |\mathbb{C}|M_a)$?

Exercise 13.9

Based on the data in Table 13.10, (i) estimate a multinomial Naive Bayes classifier, (ii) apply the classifier to the test document, (iii) estimate a Bernoulli NB classifier, (iv) apply the classifier to the test document. You need not estimate parameters that you don't need for classifying the test document.

Exercise 13.10

Your task is to classify words as English or not English. Words are generated by a source with the following distribution:

event	word	English?	probability
1	ozb	no	4/9
2	uzu	no	4/9
3	zoo	yes	1/18
4	bun	ves	1/18

(i) Compute the parameters (priors and conditionals) of a multinomial NB classifier that uses the letters b, n, o, u, and z as features. Assume a training set that reflects the probability distribution of the source perfectly. Make the same independence assumptions that are usually made for a multinomial classifier that uses terms as features for text classification. Compute parameters using smoothing, in which computed-zero probabilities are smoothed into probability 0.01, and computed-nonzero probabilities are untouched. (This simplistic smoothing may cause $P(A) + P(\overline{A}) > 1$. Solutions are not required to correct this.) (ii) How does the classifier classify the word zoo? (iii) Classify the word zoo using a multinomial classifier as in part (i), but do not make the assumption of positional independence. That is, estimate separate parameters for each position in a word. You only need to compute the parameters you need for classifying zoo.

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What are the values of $I(U_t; C_c)$ and $X^2(\mathbb{D}, t, c)$ if term and class are completely inde-

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model. Why? How could one modify it for the multinomial model?

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$$IG(\mathbb{D}, t, c) = H(p_{\mathbb{D}}) - \sum_{x \in \{\mathbb{D}_{t+t}, \mathbb{D}_{t-t}\}} \frac{|x|}{|\mathbb{D}|} H(p_x)$$

where H is entropy, $\mathbb D$ is the training set, and $\mathbb D_{t^+}$, and $\mathbb D_{t^-}$ are the subset of $\mathbb D$ with term t, and the subset of $\mathbb D$ without term t, respectively. p_A is the class distribution in (sub)collection A, e.g., $p_A(c)=0.25$, $p_A(\overline c)=0.75$ if a quarter of the documents in A are in class c.

Show that mutual information and information gain are equivalent.

Exercise 13.14

Show that the two X^2 formulas (Equations (13.18) and (13.19)) are equivalent.

Exercise 13.15

In the χ^2 example on page 276 we have $|N_{11}-E_{11}|=|N_{10}-E_{10}|=|N_{01}-E_{01}|=|N_{00}-E_{00}|$. Show that this holds in general.

Exercise 13.16

 χ^2 and mutual information do not distinguish between positively and negatively correlated features. Because most good text classification features are positively correlated (i.e., they occur more often in c than in \overline{c}), one may want to explicitly rule out the selection of negative indicators. How would you do this?

13.7 References and further reading

General introductions to statistical classification and machine learning can be found in (Hastie et al. 2001), (Mitchell 1997), and (Duda et al. 2000), including many important methods (e.g., decision trees and boosting) that we do not cover. A comprehensive review of text classification methods and results is (Sebastiani 2002). Manning and Schütze (1999, Chapter 16) give an accessible introduction to text classification with coverage of decision trees, perceptrons and maximum entropy models. More information on the superlinear time complexity of learning methods that are more accurate than Naive Bayes can be found in (Perkins et al. 2003) and (Joachims 2006a).

Maron and Kuhns (1960) described one of the first NB text classifiers. Lewis (1998) focuses on the history of NB classification. Bernoulli and multinomial models and their accuracy for different collections are discussed by McCal-

ASS models Indiving Land Phazer 1007, Fried Xad (1917), and Gand and Yu (2001) analyze why NB performs well although its probability estimates are independence

opose a modified

https://eduassistpro.github.io e tendency of NB

probability estimates to be close to either 0 or 1 to t t of document length. Ng and Jordan (2001) show th Siches it forth an be tuned for superior o distributative in the is seen mal error rate. The basic NB model present better effectiveness (Rennie et al. 2003; Kołcz and Yih 2007). The problem of concept drift and other reasons why state-of-the-art classifiers do not always excel in practice are discussed by Forman (2006) and Hand (2006). Early uses of mutual information and χ^2 for feature selection in text clas-

sification are Lewis and Ringuette (1994) and Schütze et al. (1995), respectively. Yang and Pedersen (1997) review feature selection methods and their impact on classification effectiveness. They find that pointwise mutual information is not competitive with other methods. Yang and Pedersen refer to expected mutual information (Equation (13.16)) as information gain (see Exercise 13.13, page 285). (Snedecor and Cochran 1989) is a good reference for the χ^2 test in statistics, including the Yates' correction for continuity for 2 × 2 tables. Dunning (1993) discusses problems of the χ^2 test when counts are small. Nongreedy feature selection techniques are described by Hastie et al.

(2001). Cohen (1995) discusses the pitfalls of using multiple significance tests and methods to avoid them. Forman (2004) evaluates different methods for feature selection for multiple classifiers.

David D. Lewis defines the ModApte split at www.daviddlewis.com/resources/testcollections/reuters219 based on Apté et al. (1994). Lewis (1995) describes utility measures for the

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UTILITY MEASURE

evaluation of text classification systems. Yang and Liu (1999) employ significance tests in the evaluation of text classification methods.

Lewis et al. (2004) find that SVMs (Chapter 15) perform better on Reuters-RCV1 than kNN and Rocchio (Chapter 14).

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