Assignment Project Exam Help Maths Preliminaries

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Introduction

Assignment to Project Exam Help Recap relevant maths contents that you may have learned a

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Assignment Project Exam Help of linear equations, etc. We will review key concepts in LA

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- Here we emphasize more on intuitions; We deliberately skip many concepts and present some conte
- It de la company de la compa

A Common Trick in Maths I

Question

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- · Properties: WeChat:edu_assist_pr
 - f(u) * f(v) = f(u + v).
 - $f(x) = y \Leftrightarrow \ln(y) = x \ln(a) \Leftrightarrow f(x) = \exp\{x \ln a\}.$
 - $e^{ix} = cos(x) + i \cdot sin(x)$.
- The trick:
- Same in Linear algebra



Objects and Their Representations

Goal

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- A good representation helps (a lot)!
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Basic Concepts I

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constraints:

A Charles Property Plans to edu_assist_pr

- Communicative: a + b = b + a.
- Associative: (a + b) + c = a + (b + c).
- Distributive: $\lambda(a + b) = \lambda a + \lambda b$.

Basic Concepts II

Assignment Project Exam Help Tips Alwa Polyhttps://eduassistpro.github. Why these constraints are natural and useful? Add WeChat edu_assist_pr

Basic Concepts III

Representation matters?

What we represent vectors by a column of their coordinates?

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Notes Add We Chat edu_assist_p

- Informally, the objects we are concerned w are (column) vectors.
- The set of all *n*-dimensional real vectors is called \mathbb{R}^n .

(Column) Vector

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- Addition: V1+V2=Chat edu_assist_pr

Linearity I

Linear Combination: Generalization of Univariate Linear Functions

$$Assignation and projectors v_i Examine a Help $a_1v_1 + a_2v_2 + ... + a_kv_k = \sum_{i \in [k]} a_iv_i$$$

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- Span: All linear combination of a set of vector of them.
- Basis: The minimal set of vectors whose span is exactly the whole \mathbb{R}^n .

Linearity II

Assignment who in the later thank: Why uniqueness i desirable?

```
• Span of [1], [0], [2] is \mathbb{R}^2. But one o
• Decompose [4]
• Decompose [4]
```

Linearity III

Exercises

• What are the (natural) basis of all (univariate) Polynomials of

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• The "same" polynomial is mapped to two di

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Matrix I

Assignment Project Exam Help vector in \mathbb{R}^m .

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• The general We Chat edu_assist_property $\begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$ \xrightarrow{f} $\begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$ \Rightarrow $y_2 = M_{21}x_1 + M_{22}x_2$ $y_3 = M_{31}x_1 + M_{32}x_2$

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \quad \stackrel{f}{\longrightarrow} \quad \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix} \quad \Longrightarrow \quad y_2 = M_{21}x_1 + M_{22}x_2$$

$$y_3 = M_{31}x_1 + M_{32}x_2$$

Matrix II

Nonexample

Assignment
$$y_2$$
 Project $x_1 = x_2$ Help

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Why Only Linear Transformation?

- Simple and nice properties hat edu_assist_pr
 - $(\lambda f)(x) = \lambda \cdot f(x)$
 - What about f(g(x))?
- Useful

Matrix I

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• Transformation or Mapping emphasizes more on the mapping between two sets, rather than the detaile

Ampropried to the transfer of a function the true assist_propried to the true assist to the true as the

Semantic Interpretation

Matrix II

Assignment Project Exam Help https://eduassistpro.github. $y = x_1 M_{\bullet 1} + \ldots + x M$

• Example: We Chat edu_assist_properties: $\begin{bmatrix} 1 & 2 \\ -4 & 9 \\ 25 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 10 \end{bmatrix} = 1 \begin{bmatrix} 1 \\ -4 \\ 25 \end{bmatrix} + 10 \begin{bmatrix} 9 \\ 1 \end{bmatrix} = \begin{bmatrix} 86 \\ 35 \end{bmatrix}$

$$\begin{bmatrix} 1 & 2 \\ -4 & 9 \\ 25 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 10 \end{bmatrix} = 1 \begin{bmatrix} 1 \\ -4 \\ 25 \end{bmatrix} + 10 \begin{bmatrix} 9 \\ 1 \end{bmatrix} = \begin{bmatrix} 86 \\ 35 \end{bmatrix}$$

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System of Linear Equations I

Assignment Project Exam Help $M_{11} = M_{11} \times_1 + M_{12} \times_2$ https://eduassistpro.github.

- . Addio We Chatedu_assist_pr M) is exactly the given vector $y \in$
- How to solve it?

System of Linear Equations II

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A Matrix Also Specifies a (Generalized) Coordinate System

Yet another interpretation

Assignmenty Project Exam Help The vector y wrt standard coordinate system, I, is the same as

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for Add We Chat edu_assist_properties of the form of the following states of

Let
$$x = \begin{bmatrix} 1 \\ -2 \\ 3 \end{bmatrix} \implies Mx = I \begin{bmatrix} -1 \\ 13 \\ 6 \end{bmatrix}$$

Exercise I

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0 0 2 0 0 1

• The dat Weeting part C assist_property C as C as

Inner Product

THE binary operator – some kind of "similarity"

- Assignment called for each of the first section f(x,y). For certain functions, $f(y) = \int_a^b f(t)g(t) dt$. leads to the
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 - linearity in the first argument: $\langle ax + y, z = a x, z + y, z \rangle$
 - positive definitiveness: $\langle x, x \rangle \ge$
 - General of the control of the cont
 - $\langle \sin nt, \sin mt \rangle = 0$ within $[-\pi, \pi]$ $(m \neq n) \Rightarrow$ they are orthogonal to each other.
 - $\bullet \ \mathsf{C} = \mathsf{A}^{\top} \mathsf{B} \colon \ C_{ij} = \langle A_i, B_j \rangle$
 - Special case: A[⊤]A.

Eigenvalues/vectors and Eigen Decomposition

"Eigen" means "characteristic of" (German)

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- . https://eduassistpro.github.
- We can use all eigenvectors of A to construct a columns). Then $\Delta U = U A$, or equiv is the can interpret U as a transformation b is We can interpret U as a transformation b
 - systems. Note that vectors in U are not necessarily orthogonal.
 - $oldsymbol{\Lambda}$ as the scaling on each of the directions in the "new" coordinate system.

Similar Matrices

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• Let A and B be two n matrix. A is similar to B (denoted

. https://eduassistpro.github.

- Think of P as a change of basis
- Relationship with the Figen decompose Similar Outrices have the shart value of the shart (e.g., rank, trace, eigenvalues, determin

SVD

Singular Vector Decomposition

Assignment Project Exam Help Reduced SVD: $M = \hat{U}\hat{\Sigma}V^{T}$ exists for any M, such that

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V consists of a set of basis vectors v

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- Add the remaining (n-d) basis vectors to \hat{U} (thus becomes $n \times n$).
- Add the n-d rows of 0 to $\hat{\Lambda}$ (thus becomes $n \times d$).

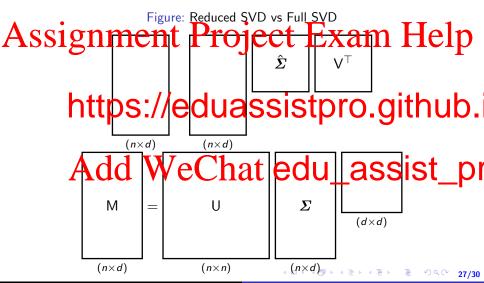
Geometric Illustration of SVD

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Graphical Illustration of SVD I



Graphical Illustration of SVD II

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Mea

- https://eduassistpro.github.
- Rows of V are the basis of \mathbb{R}

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SVD Applications I

Relationship between Singular Values and Eigenvalues

What are the eigenvalues of MTM?

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• Related to PCA (Principle Component Analysis)

References and Further Reading I

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https://www.youtube.com/watch?v=k-yUdqRXijo

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- Scipy LA tutorial. https://docs.scipy.org/doc/scipy/ reference/tutorial/linalg.htm
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