Solution to COMP9334 Revision Questions for Week 7A_1

Question 1

Let us first compute the second moment of each customer type. Let us use C_a , σ_a , $E[S_a]$ and $E[S_a^2]$ to denote, respectively, the coefficient of variation, standard deviation, mean and second moment of the service time of customer of type a. Recall that the coefficient of variation of a random variable is its standard deviation divided by mean, i.e $C_a = \frac{\sigma_a}{E[S_a]}$. By using the relation:

$$E[S_a^2] = E[S_a]^2 + \sigma_a^2, (1)$$

it can be showed that

$$E[S_a^2] = E[S_a]^2 (1 + C_a^2) (2)$$

Since we know $E[S_a] = 0.1$ and $C_a = 1.5$, we can compute $E[S_a^2]$ using the above equation.

Similarly, let C_b , σ_b , $E[S_b]$ and $E[S_b^2]$ to denote, respectively, the coefficient of variation, standard delisibility and each temperature and afficient of the period of t

$_{\text{With }E[S_b]=0.08}$ https://eduassistpro.github.io/

Requests of type a and b-have equal prigrities. This is an M/G/1 quest virtually in the Thankiv facts 10 assist D D λ). Since 30% of the request are type a and the remaining are type b, we have time E[S] and second moment $E[S^2]$ of the aggregate are, respectively,

$$E[S] = 0.3E[S_a] + 0.7E[S_b] \tag{4}$$

$$E[S^2] = 0.3E[S_a^2] + 0.7E[S_b^2]$$
 (5)

The mean response time is therefore $E[S] + \frac{\lambda E[S^2]}{2(1-\rho)}$ where $\rho = \lambda E[S]$.

 $\frac{\text{Requests of type b have non-preemptive priority over type a}}{\text{Let}}$

$$R = \frac{1}{2}(0.3\lambda E[S_a^2] + 0.7\lambda E[S_b^2]) \tag{6}$$

$$\rho_a = 0.3\lambda E[S_a] \tag{7}$$

$$\rho_b = 0.7\lambda E[S_b] \tag{8}$$

Response time of type b is

$$E[S_b] + \frac{R}{1 - \rho_b} \tag{9}$$

Response time of type a is

$$E[S_a] + \frac{R}{(1 - \rho_b)(1 - \rho_a - \rho_b)} \tag{10}$$

Requests of type b have preemptive priority over type a Let

$$R_b = \frac{1}{2}(0.7\lambda E[S_b^2]) \tag{11}$$

$$R_a = \frac{1}{2}(0.3\lambda E[S_a^2] + 0.7\lambda E[S_b^2])$$
 (12)

$$\rho_a = 0.3\lambda E[S_a] \tag{13}$$

$$\rho_b = 0.7\lambda E[S_b] \tag{14}$$

Response time of type b is

$$E[S_b] + \frac{R_b}{1 - \rho_b} \tag{15}$$

Response time of type a is

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The numerical answers are summarised in the following table.

Mean response time				
type a	ttns	•//_	dua	ssistpro.github.io/
type b	upo	-// -	uuu	bolotpro.gittidb.io/

Observe that the response time for type b customers have beco a higher priority, this is of course at the expense of type a customers which h priority.

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