COMP9334 Capacity Planning for Computer Systems and Networks

Assignment Project Exam Help

Week 2Ahttps://eduassistpro.gitsisb(2).

Workload A Chartiedu_assist_pro

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Last lecture

- Modelling a computer system as a queueing network
- Operational analysis on queueing networks
- We have derived these operational laws p
 - Utilisation law https://eduassistpro.github.io/
 - Forced flow la
 - Service demand that the edu_assist (p) ro
 - Little's law N = X R

This lecture

- Operational analysis (Continued)
 - Using operational law for
 - Performance analysis
 - Bottleneck analysis
- Workload characterisation

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 - Poisson proce https://eduassistpro.github.io/

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Interactive systems

M users

 An interactive system is used to model the interaction between Assignment Project Exam Help Computers

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Add WeChat edu_assisstem consists of

A number of users

A computer system

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Interactive systems (Cont'd)

M users

Interactions

 Users send jobs to computer systems

After finishing

Assignment Project Examples ing a job, the

https://eduassistpro.github.io/ urns the result to the

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 A user, after inspecting the results from the computer system, will send another job to the system

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Interactive systems: Modelling assumptions

M users

 Analyze interactive systems with specific assumptions

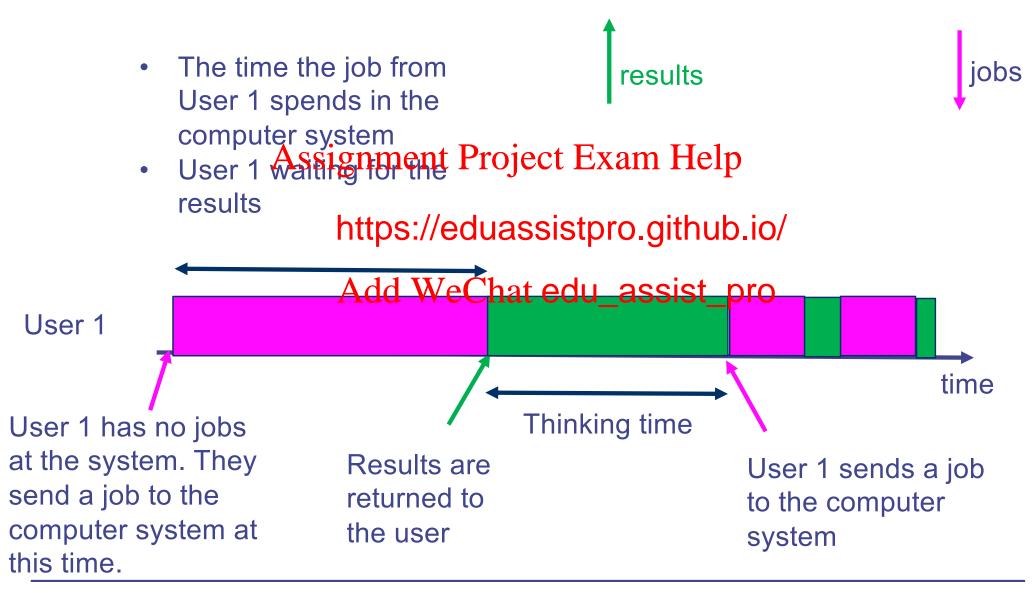
• Fixed number of users Assignment Project Exam Help by M

https://eduassistpro.githubspr/can have at at the AddoWeChat edu_assistupepsystem

results

- Each user goes through a cycle consisting of
 - Thinking time
 - Waiting for result time

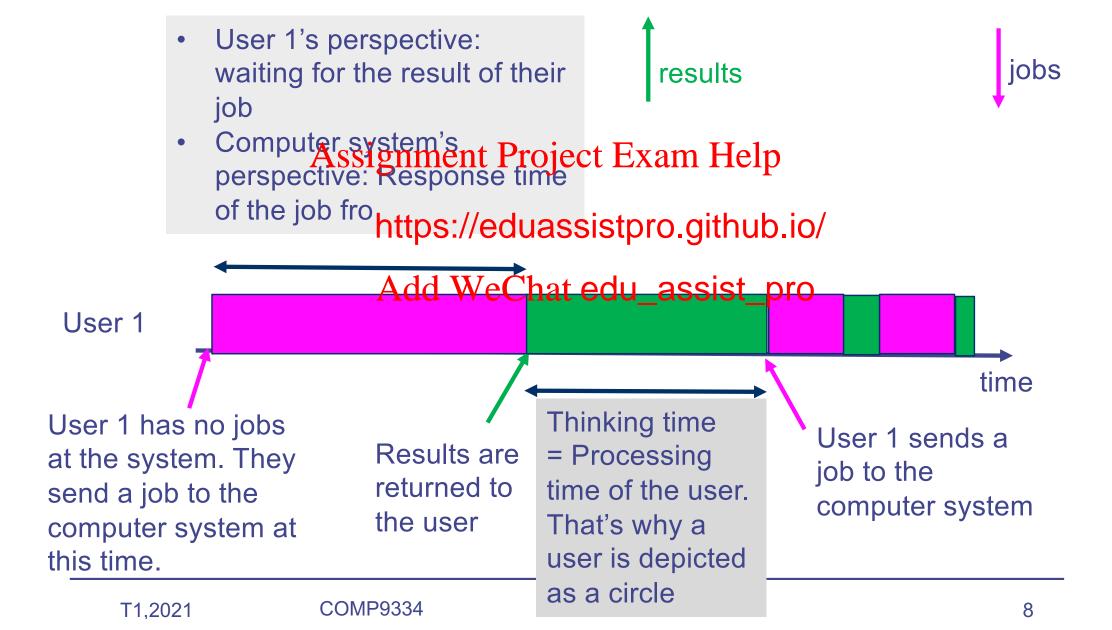
Interactive cycle



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Interactive cycle



Quiz

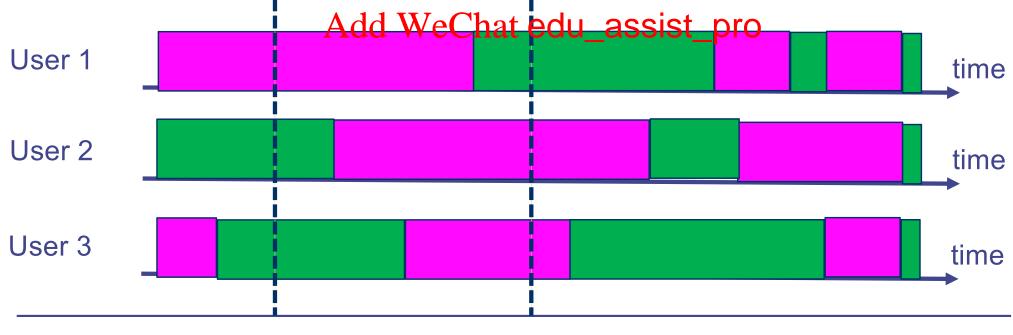
 Question: At any time, what is the sum of the number of busy users and the number of jobs at the computer system?

results

jobs

Job at computations Project Exam Help

Busy user (= t https://eduassistpro.github.io/



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Interactive system: Parameters

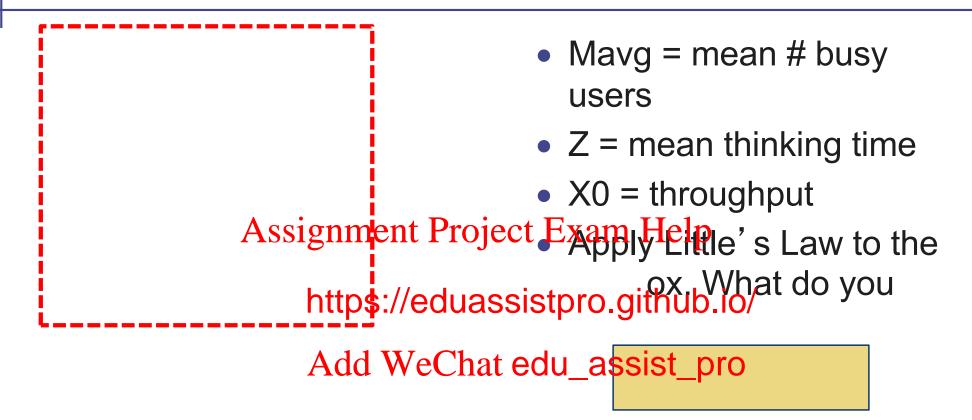
- M interactive users
- Z = mean thinking time
- R = mean response time

Assignment Project Extatme Holpmputer system

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Analyzing interactive system: Quiz 1



Analyzing interactive system: Quiz 2

- Navg = average # jobs in the computer system
- R = mean response time

Assignment Project Exam Help throughput

https://eduassistpro.githittleios/ Law to the er system (i.e. the Add-WeChat edu_assistx)prohat do you

get?

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Analyzing interactive system: Quiz 3

- Quiz 1: Quiz 2:
- Assignment Project Exhat Helpavg + Navg?

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The operational laws

- These are the operational laws
 - Utilisation law U(j) = X(j) S(j)
 - Forced flow law X(j) = V(j) X(0)
 - Service demand law D(j) = V(j) S(j) = U(j) / X(0)

 - Little's law N = X R
 Assignment Project Exam Help
 Interactive response time M = X(0) (R+Z)
- Applications https://eduassistpro.github.io/
 - Mean value anal.
 - Bottleneck analys Add WeChat edu_assist_pro
 - Modification analysis

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Bottleneck analysis - motivation

		D(j)	Utilisation
	Disk 1	79ms	0.30
	Disk 2	108ms	0.41
Assignment Pro	j e gt _k Ezxam	Helps	0.54
https://edua	ssistpro.	gRAWB.io/	0.35

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Service demand law: D(j) = U(j) / X(0) ==> U(j) = D(j) X(0) Utilisation increases with increasing throughput and service demand

Utilisation vs. throughput plot U(j) = D(j) X(0)

Disk 3

Disk 2 CPU

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Disk 1

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What determines this order?

Observation: For all system throughput: Utilisation of Disk 3 > Utilisation of Disk 2 > Utilisation of CPU COMP SIJIIII is ation of Disk 1

Bottleneck analysis

- Recall that utilisation is the busy time of a device divided by measurement time
 - What is the maximum value of utilisation?
- Based on the example on the previous slide, which device will reach the maximum willisetion first Help

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Bottleneck (1)

- Disk 3 has the highest service demand
- It is the bottleneck of the whole system

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Operational law: https://eduassistpro.github.io/
$$X(0) \leq \frac{1}{D(i)}$$

Utilisation limit: $U(j) \leq 1$ edu_assist_pro D(j) = D(j)

Bottleneck (2)

$$X(0) \leq \frac{1}{D(j)}$$
 Should hold for all K devices in the system Assignment Project Exam Help

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$$\Rightarrow X(0) \le \min \frac{1}{D(j)}$$

$$\Rightarrow X(0) \le \frac{1}{\max D(j)}$$

Bottleneck throughput is limited by the maximum service demand

Bottleneck exercise

		D(j)	Utilisation
	Disk 1	79ms	0.30
	Disk 2	108ms	0.41
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The system throughput is upper bounded by $\frac{1}{0.142}$ = 7.04 jobs/s If we upgrade Disk 3 by a new disk which is 2 times faster, which device will be the bottleneck after the upgrade? You can assume that service time is inversely proportional to disk speed.

Another throughput bound

Little's law

$$N = R \times X(0) \ge (\sum_{i=1}^{K} D_i) \times X(0)$$

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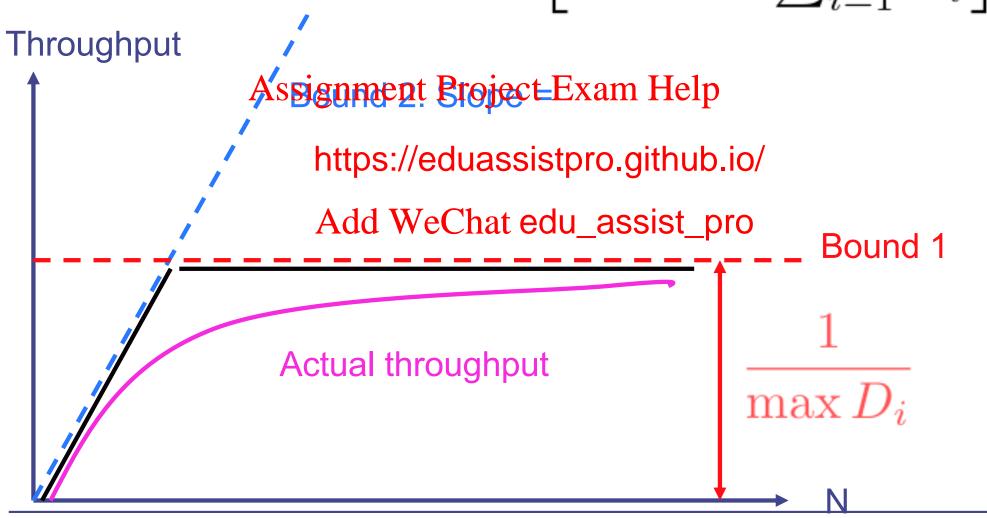
Previously, we have
$$X(0) \leq \frac{1}{\max D(j)}$$

Therefore:
$$X(0) \leq \min \left[\frac{1}{\max D_i}, \frac{N}{\nabla^K D_i} \right]$$

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Throughput bounds

$$X(0) \le \min \left[\frac{1}{\max D_i}, \frac{N}{\sum_{i=1}^K D_i} \right]$$



Bottleneck analysis

- Simple to use
 - Needs only utilisation of various components
- Assumes service demand is load independent

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Modification analysis (1)

- (Reference: Lazowska Section 5.3.1)
- A company currently has a system (3790) and is considering switching to a new system (8130). The service demands for these two systems are given below:

Assignment Project Exam Help				
System	1100151	ment i reject Zne	sk	
3790	htt	ps://eduassistpro	o.gothub.io/	
8130	A	da WeChat edu a	essist pro	

- The company uses the system for interactive application with a think time of 60s.
- Given the same workload, should the company switch to the new system?
- Exercise: Answer this question by using bottleneck analysis. For each system, plot the upper bound of throughput as a function of the number of interactive users.

Modification analysis (2)

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Operational analysis

- Operational analysis allows you to bound the system performance but it does NOT allow you to find the throughput and response time of a system
- To order to find the throughput and response time, we need to use auginarial write Exam Help
- To order to use workload
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Workload analysis

- Performance depends on workload
 - When we look at the performance bound earlier, the bounds depend on number of users and service demand
 - Queue response time depends on the job arrival probability distribution and job service time distribution

 - Recall from entire the Project Exam Help
 Uniform arrival times and uniform processing times result in zero waiting time
 - But non-u https://eduassistpro.githயுக் ip/e

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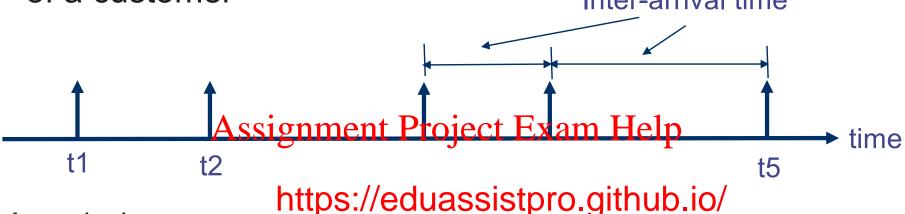
- Need to specify workload by ability distribution.
- We will look at a well-known arrival process called Poisson process today.

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Arrival process

 Each vertical arrow in the time line below depicts the arrival of a customer

Inter-arrival time

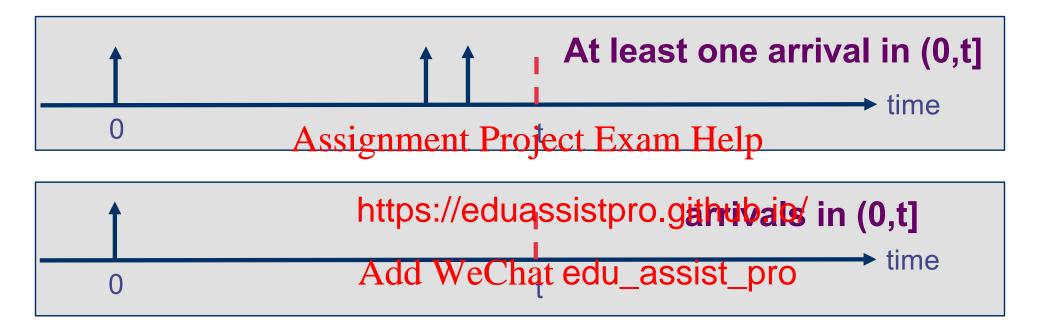


An arrival can mean

- A telephone call arriving a long telephone call a
- A transaction arriving at a computer system
- A customer arriving at a checkout counter
- An HTTP request arriving at a web server
- The inter-arrival time distribution will impact on the response time.
- We will study an inter-arrival distribution that results from a large number of independent customers.

Describing arrivals probabilistically

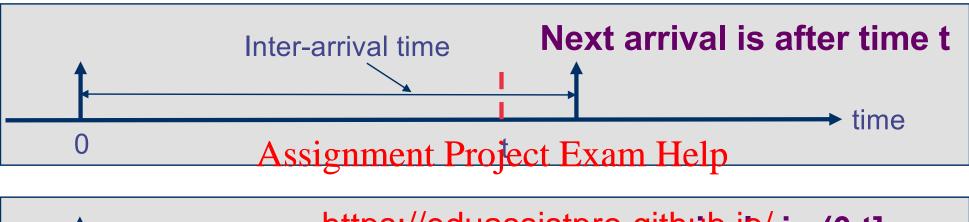
Assume a customer arrives at time 0



- Quiz: What is the relation between the following two probabilities?
 - Prob[at least one arrival in (0,t]]
 - Prob[no arrivals in (0,t]]
- Answer:
- Moral: "No arrivals" is not boring, it tells you something

Inter-arrival probability

Assume a customer arrives at time 0





- Quiz: What is the relation between the following two probabilities?
 - Prob[Inter-arrival time is >= t]
 - Prob[no arrivals in (0,t]]
- Answer:
- Next step: Find Prob[no arrivals in (0,t]] for independent customers

Many independent arrivals (1)

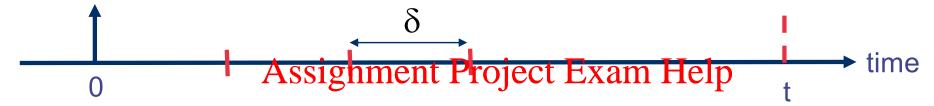
- Problem set up:
 - An arrival at time 0
 - A large pool of N independent customers
 - Behaviour of each customer: Within a small time interval of δ , a customer sends a request (or arrives) with a probability of $p\delta$
 - p is a constant

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Ouiz: If there are 2 (= N) customers, what is the probability that both of them do not send https://eduassistpro.github.io/

Many independent arrivals (2)

- Aim: Want to find the probability of no arrivals in (0,t)
- Divide the time t into intervals of width δ



- No arrival in (0,t] https://eduassistpro.gitfy@b.oofrom N users
- Probability of no arrival in δ = Add WeChat edu_assist_pro
- There are t / δ intervals
- Probability of no arrival in (0,t) is

$$(1 - Np\delta)^{\frac{t}{\delta}} \rightarrow e^{-Npt} \text{ as } \delta \rightarrow 0$$

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Exponential inter-arrival time

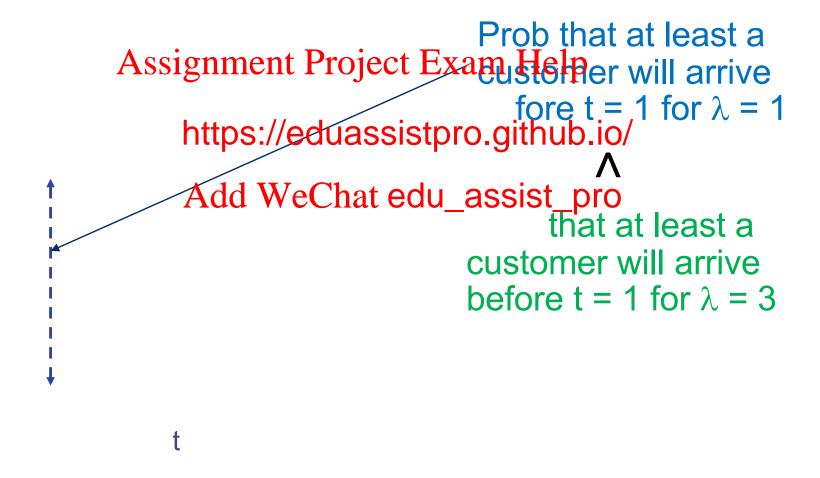
- We have showed Probability(no arrival in (0,t]) = $\exp(-Npt)$
- Probability(inter-arrival time > t) = $\exp(-Npt)$ Assignment Project Exam Help
- This means
 Probability(i https://eduassistpro.github.io/

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- What this shows is the inter-arrival time distribution for independent arrival is exponentially distributed
- Define: $\lambda = Np$
 - λ is the mean arrival rate of customers

Exponential distribution - cumulative distribution

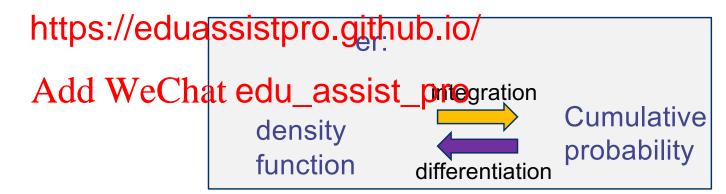
- Cumulative distribution of inter-arrival time with customer arrival rate λ
 - Prob(inter-arrival time \leq t) = 1 exp(- λ t)



Exponential distribution

• A continuous random variable is exponentially distributed with rate λ if it has probability density function

$$f(t) = \begin{cases} \lambda \exp(-\lambda t) & \text{for } t \ge 0\\ \text{Assignment Project Examfed } t < 0 \end{cases}$$



$$1 - \exp(-\lambda t)$$

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Probability density function (PDF)

Reminder: PDF f(t)

Probability($t \le T \le t + \delta t$)

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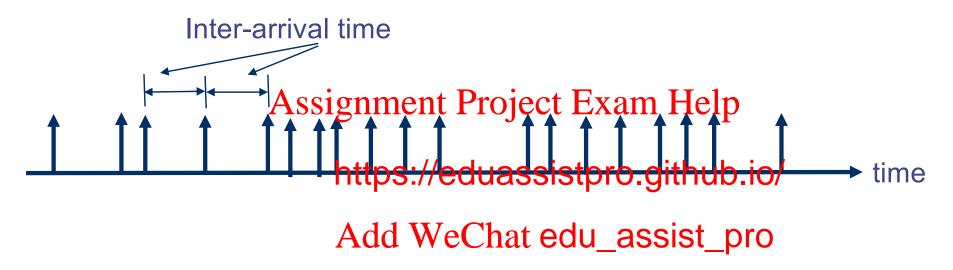
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Red area = probability that inter-arrival time is in the interval [0,0.2] Blue area = probability that the inter-arrival is in the interval [1,1.2]

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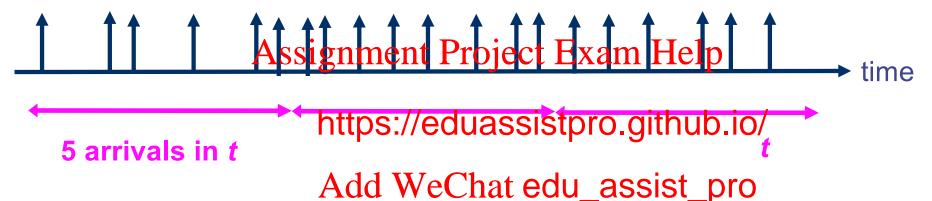
Two different methods to describe arrivals

Method 1: Continuous probability distribution of inter-arrival time



Two different methods to describe arrivals

Method 2: Use a fixed time interval (say *t*), and count the number of arrivals within *t*.



- The number of arrivals in t is ra
- The number of arrivals must be a non-negative integer
- We need a discrete probability distribution:
 - Prob[#arrivals in t = 0]
 - Prob[#arrivals in t = 1]
 - etc.

Poisson process (1)

• Definition: An arrival process is Poisson with parameter λ if the probability that n customer arrive in any time interval t is

 $(\lambda t)^n e^{-\lambda t}$

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Note: Poisson is a discrete probability distribution.

Poisson process (2)

- Theorem: An exponential inter-arrival time distribution with parameter λ gives rise to a Poisson arrival process with parameter λ
- How can you prove this theorem? Exam Help
 - A possible methatips://eduassistpro.github.io/ me intervals of width δ . A fini stribution and with $\delta \rightarrow 0$, we get a Poissor distribution assist pro

Customer arriving rate

• Given a Poisson process with parameter λ , we know that the probability of n customers arriving in a time interval of t is given by:

 $(\lambda t)^n e^{-\lambda t}$

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What is the meahttps://eduassistpro.githabritong in a time interval of t?
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• That's why λ is called the arrival rate.

Customer inter-arrival time

- You can also show that if the inter-arrival time distribution is exponential with parameter λ , then the mean inter-arrival time is $1/\lambda$
- Quite nicely, we have
 Mean arrival Areaties mule/ntmleanjeiotterxa.mivaletime

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Application of Poisson process

- Poisson process has been used to model the arrival of telephone calls to a telephone exchange successfully
- Queueing networks with Poisson arrival is tractable
 - We will see that in the next few weeks.
- Beware that Astigh arcintal priocesse arrival processe today are not Poisson. We will https://eduassistpro.github.io/

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References

- Operational analysis
 - Lazowska et al, Quantitative System Performance, Prentice Hall, 1984.
 (Classic text on performance analysis. Now out of print but can be download from http://www.cs.washington.edu/homes/lazowska/qsp/
 - Chapters 3 and 5 (For Chapter 5, up to Section 5.3 only)
 - Alternative 1: You can read Menasce et al. "Performance by design", Chapter 3. Note that Menasce doesn't cover certain aspects of performance bounds.
 So, you will also ne Lazowska.
 - Alternative 2: You c https://eduassistpro.github.io/. The treatment is more rigorous. You can gross over the https://eduassist_pro.mentioning ergodicity.

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- Poisson process: Harcol-Balter Chapter 11