

Assignment Project Exam Help

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COMP9517: Co Add WeChat edu_assist_pro sion

Image Formation

Image Formation



- « Image formation occurs when a **sensor** registers **radiation** that has interacted with **physical objects** » Ballard & Brown

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scene

Geometry of image formation

Mapping **world coordinates** to **image coordinates**

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- Pinhole camera

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- Projective geometry

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- Projection matrix

Image formation

Film

Object

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Idea 1: Put a piece of film in front of an object

Do we get a reasonable image?

Image formation

Film

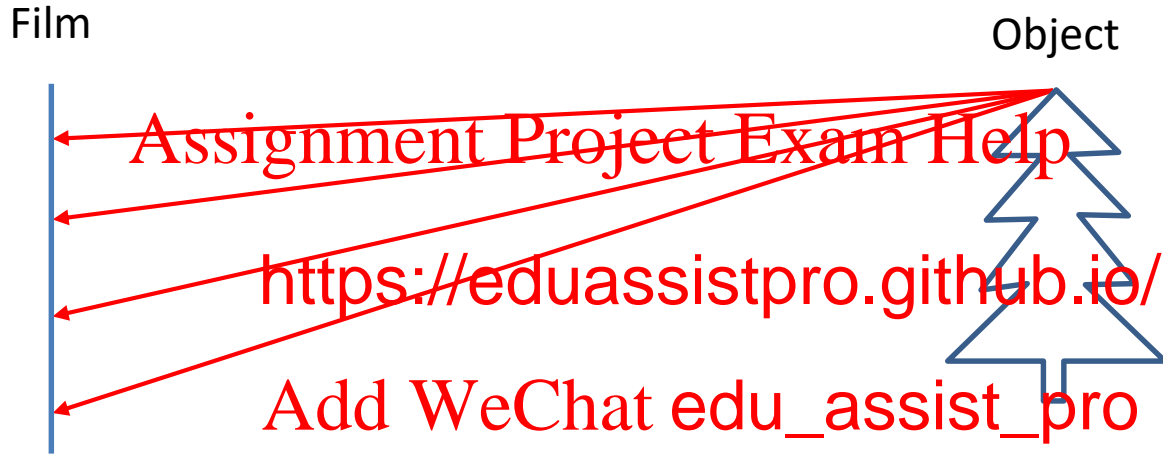
Object



Idea 1: Put a piece of film in front of an object

Do we get a reasonable image?

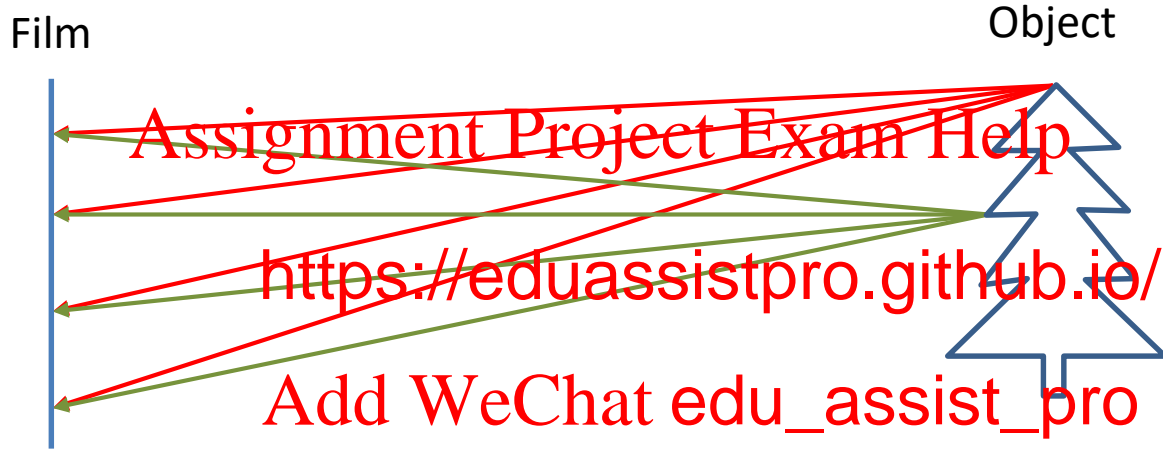
Image formation



Idea 1: Put a piece of film in front of an object

Do we get a reasonable image?

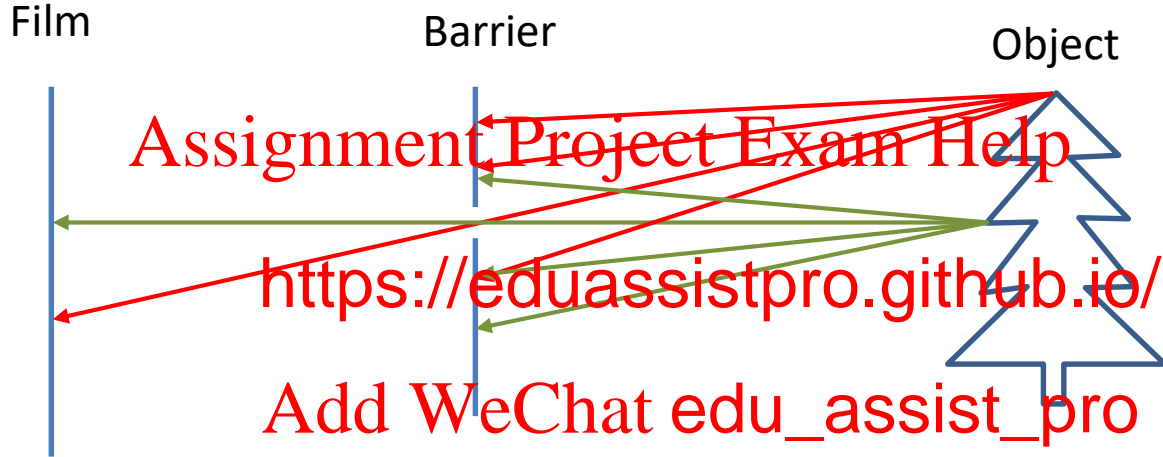
Image formation



Idea 1: Put a piece of film in front of an object

Do we get a reasonable image?

Image formation

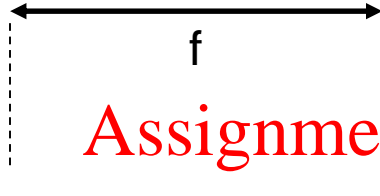


Idea 2: Add a barrier to block off most of the rays

This reduces blurring significantly

Opening known as the **pinhole** or **aperture**

Pinhole camera model



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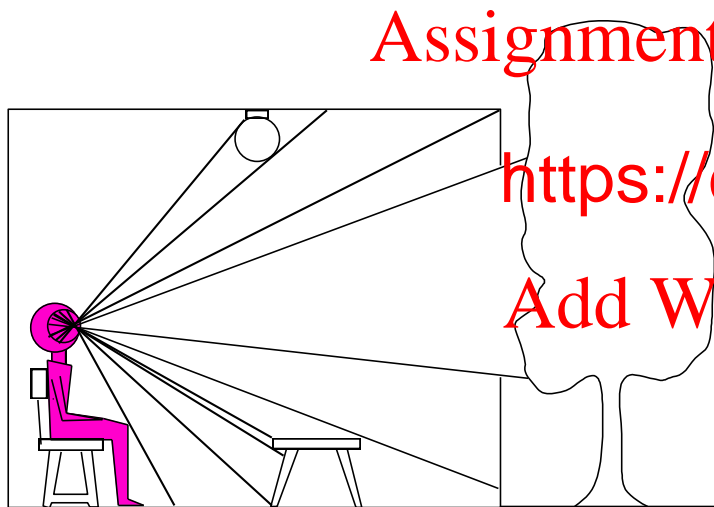
f = focal length

c = centre of the camera

Dimensionality reduction machine

3D world

2D image



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Point of o

bservation

Projection can be tricky...

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Projection can be tricky...

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Projective geometry

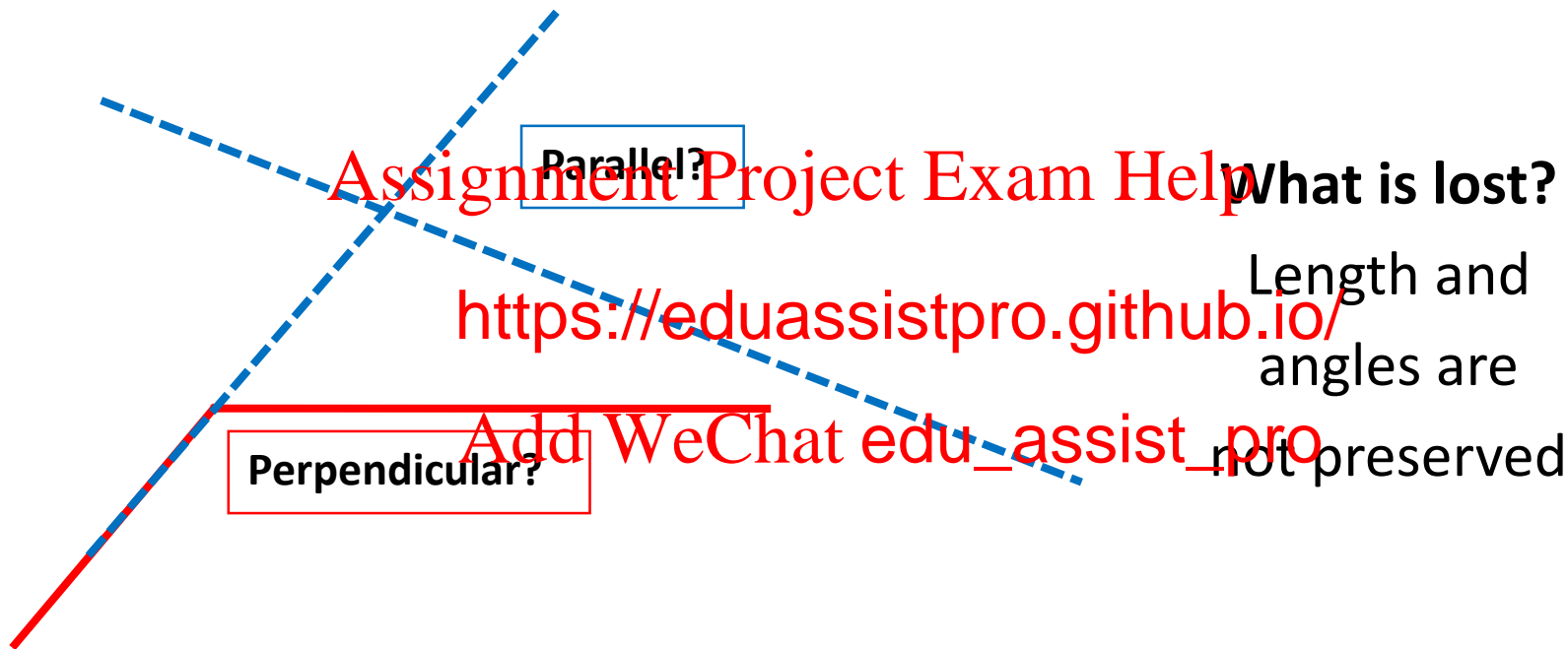
Assignment Project Exam Help Length and
area are not
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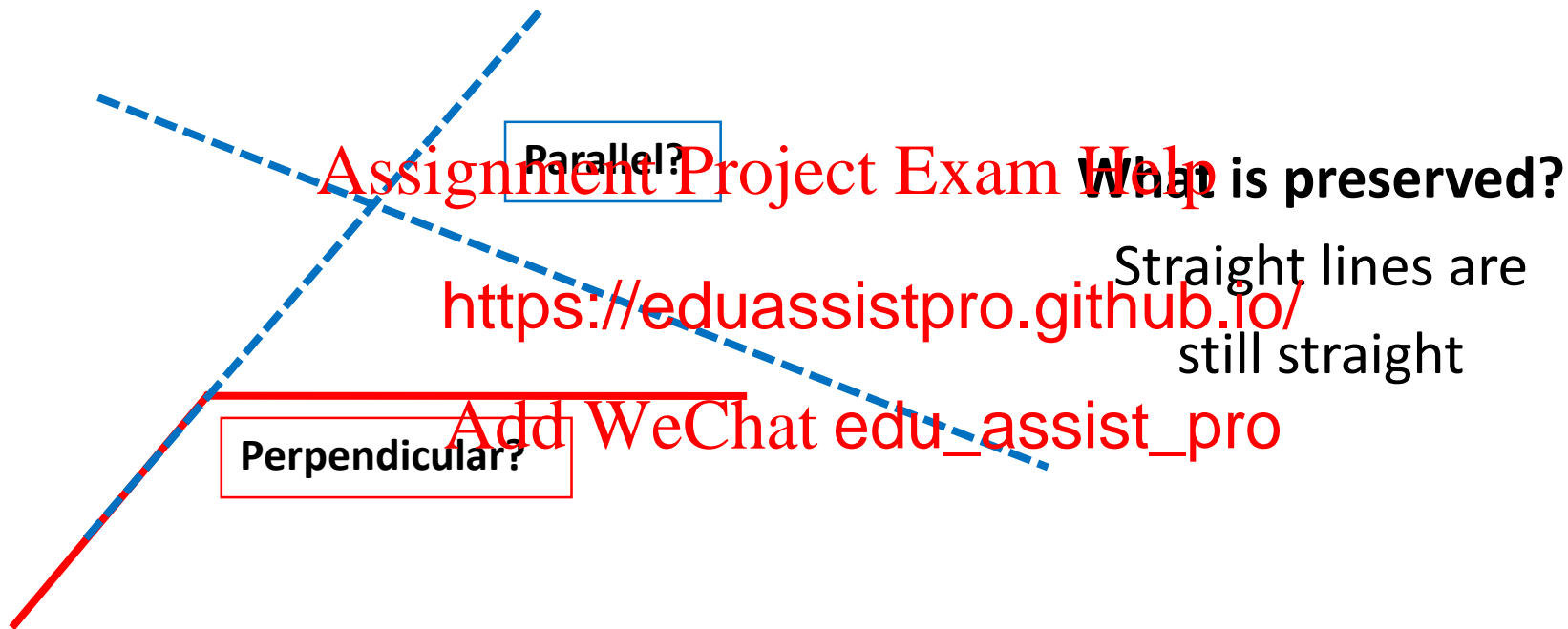
C'

B'

Projective geometry



Projective geometry



Vanishing points and lines

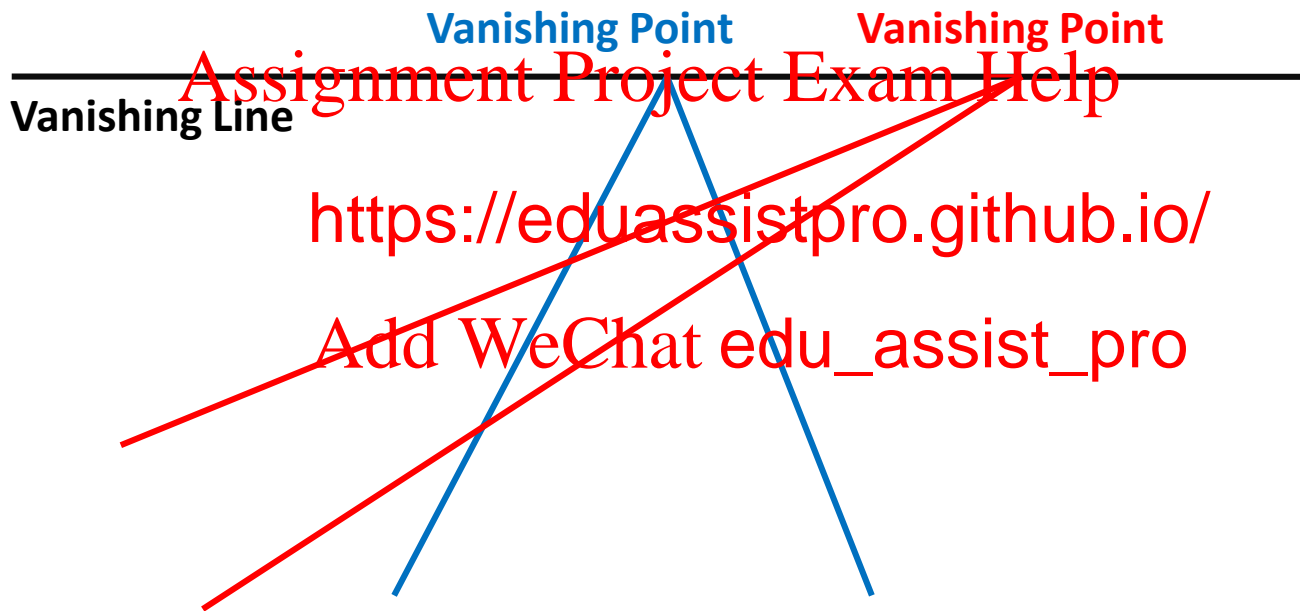
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es in the world

<https://eduassistpro.github.io/> the image at a

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Vanishing points and lines



Vanishing points and lines

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Vanishing points and lines

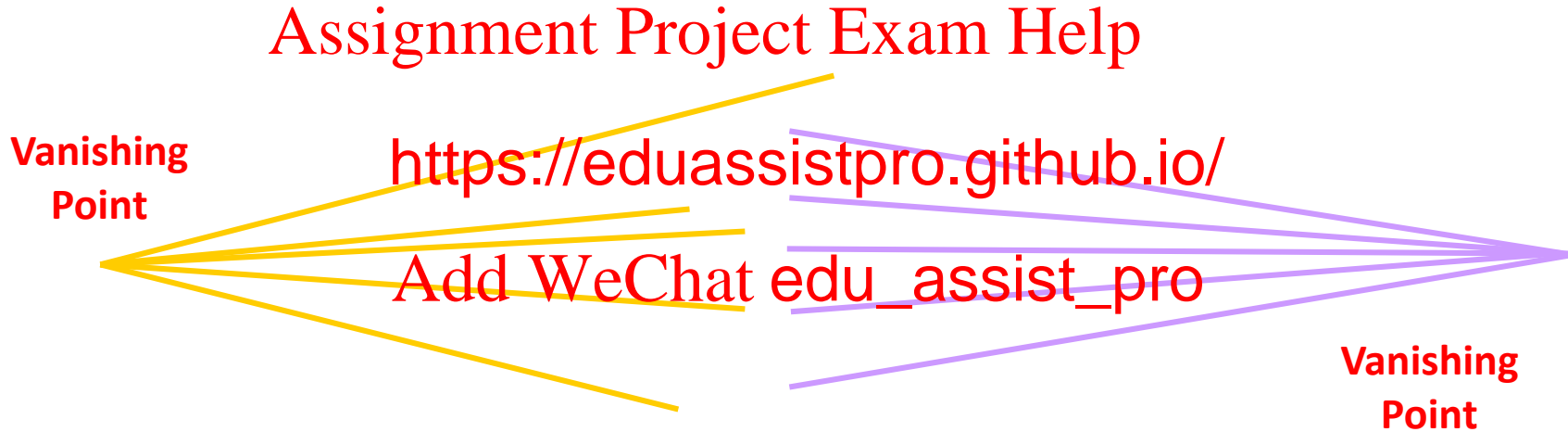
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Vanishing
Point

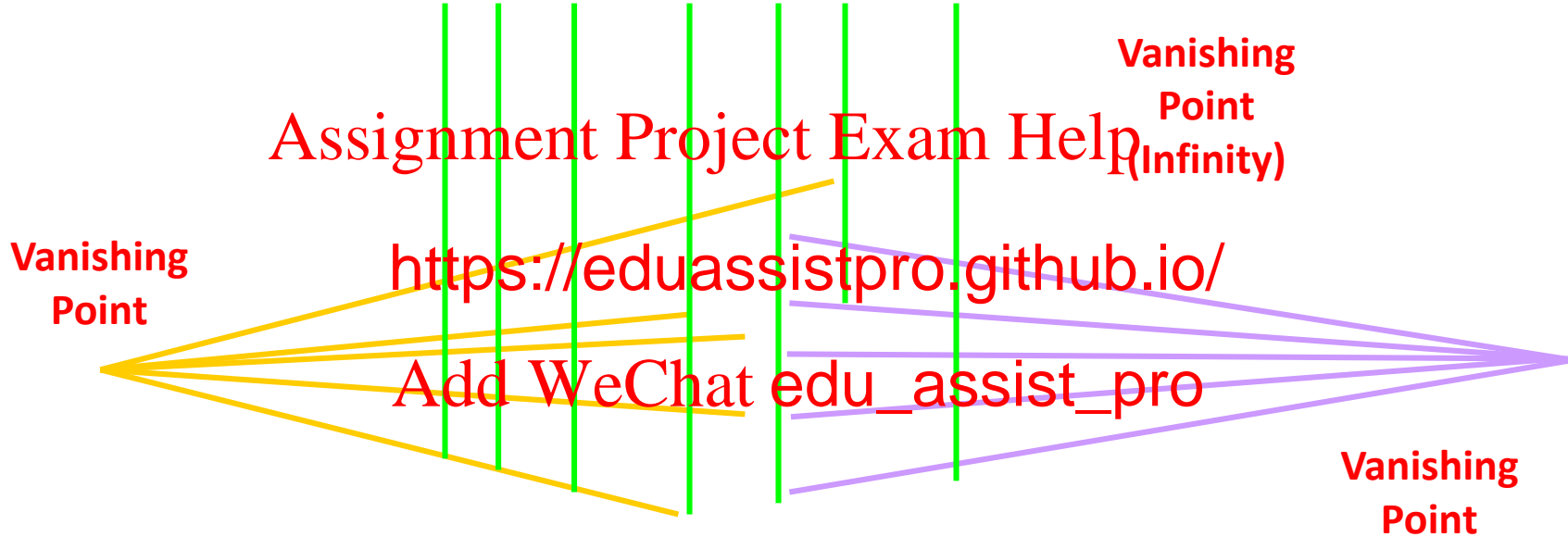
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Vanishing points and lines

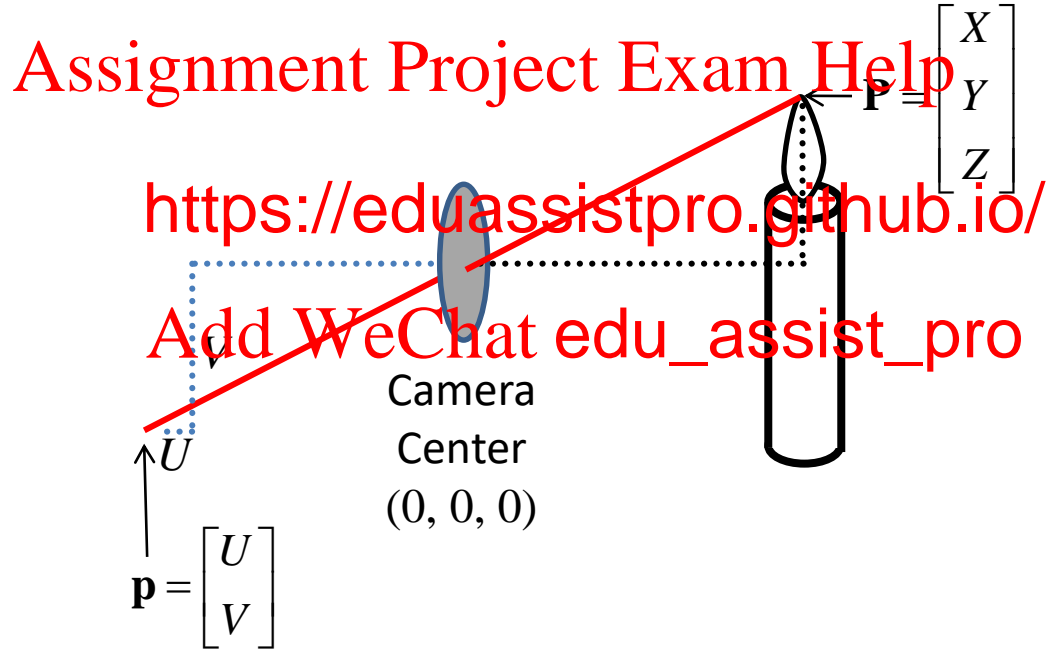


Vanishing points and lines



Projection maths

world coordinates => image coordinates



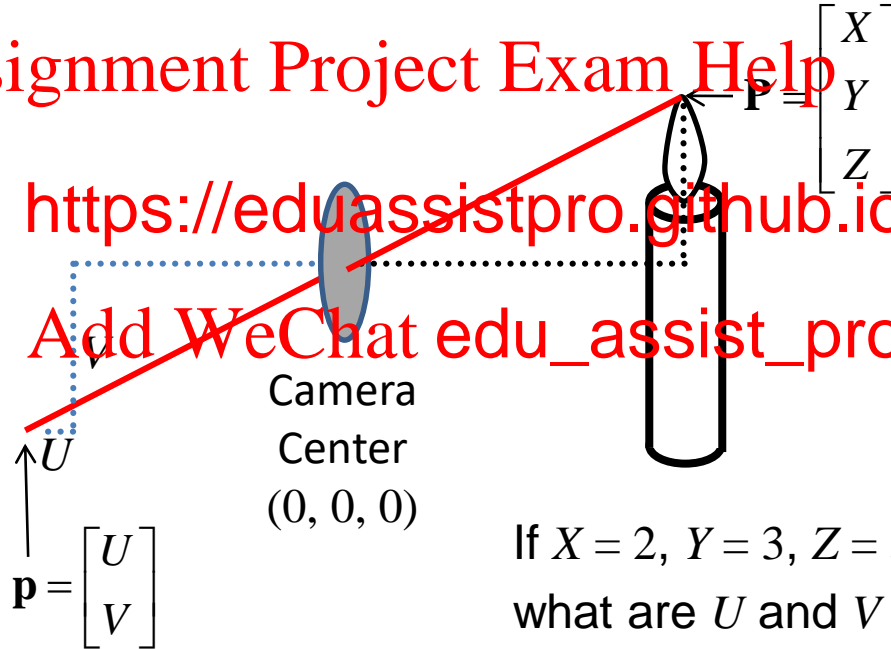
Projection maths

world coordinates => image coordinates

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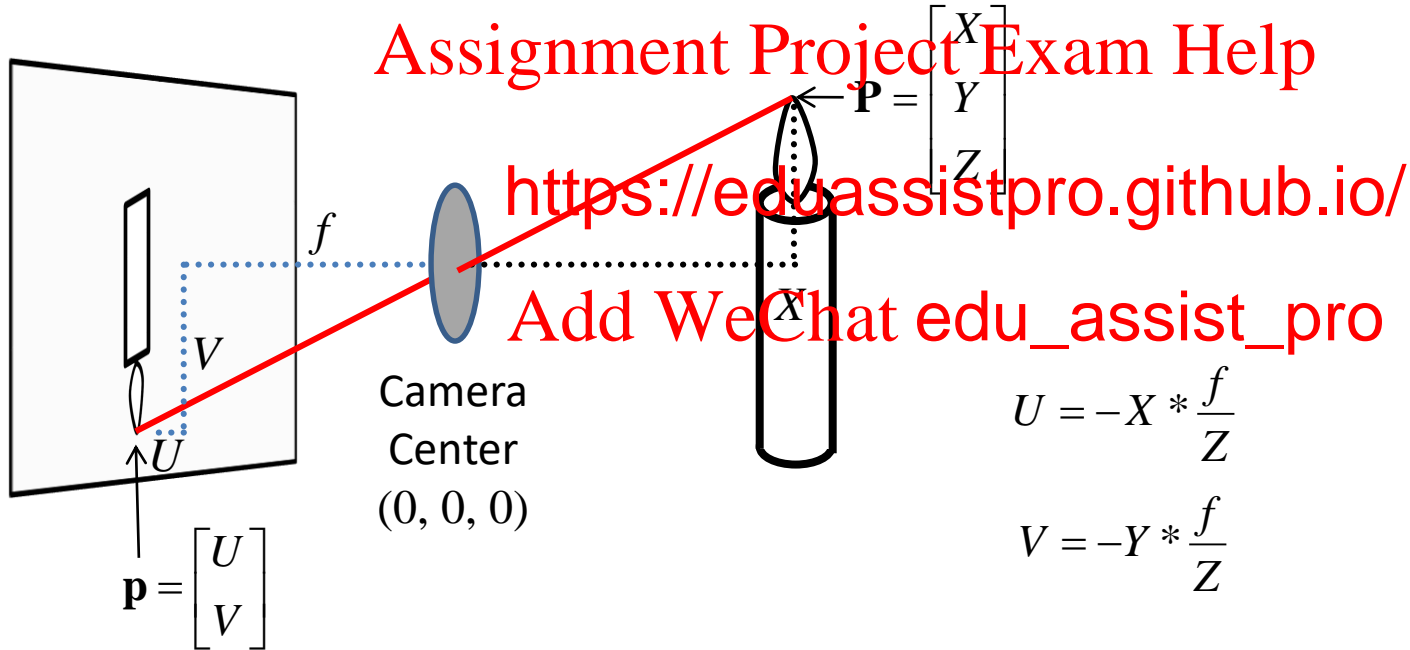
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If $X = 2$, $Y = 3$, $Z = 5$, and $f = 2$,
what are U and V ?

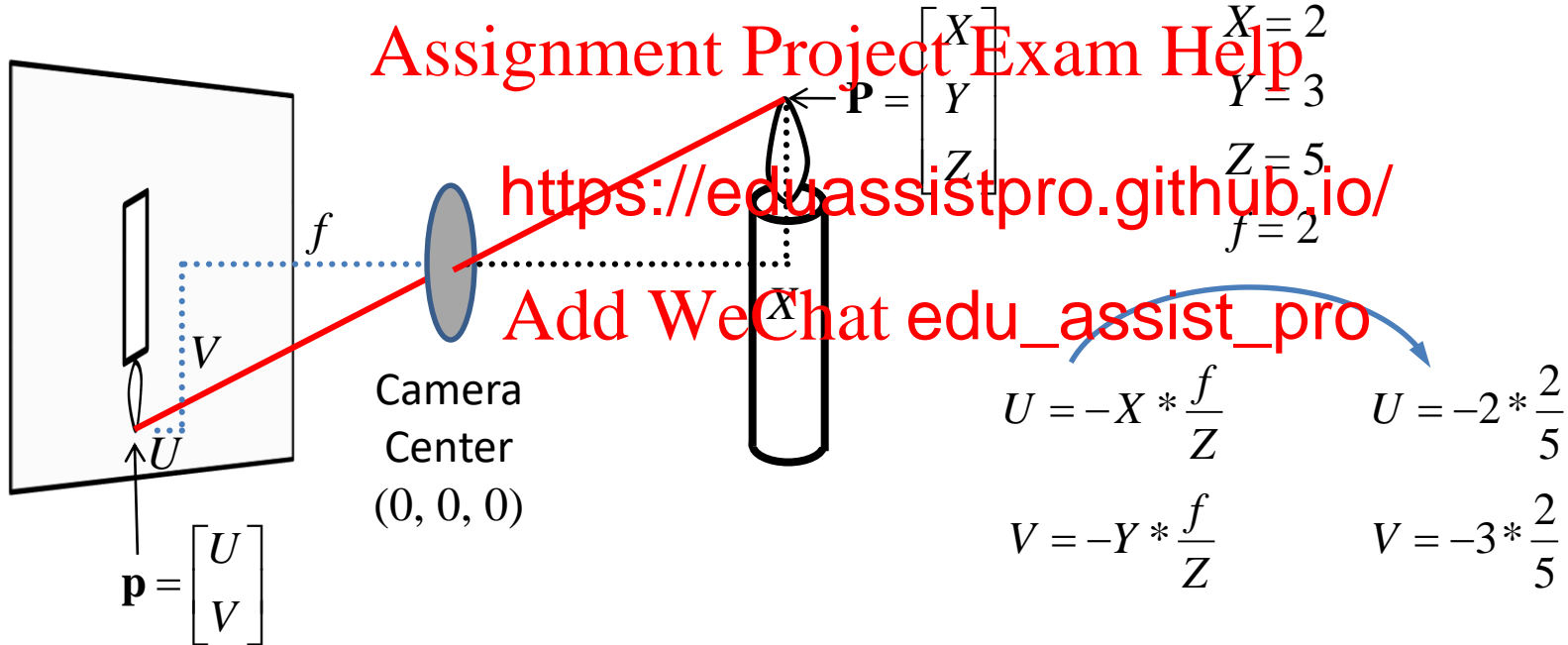
Projection maths

world coordinates => image coordinates



Projection maths

world coordinates > image coordinates



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Perspective projection

- Apparent size of object depends on its distance:
far objects appear

- By similar triangles

$$(x', y', z') = \left(f \frac{x}{z}, f \frac{y}{z}, -f\right)$$

- Ignore the third coordinate

$$(x', y') = \left(f \frac{x}{z}, f \frac{y}{z}\right)$$

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Affine projection

- Suitable when scene depth is small relative to the average distance from the camera
- Let magnification $m = -f' / z_0$ constant, treat all points in the scene as if they are at distance z_0 from camera
- Leads to weak perspective projection

$$(x', y') = (-mx, -my)$$

Affine projection

- Camera always remains at roughly constant distance from the scene

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- Orthographic projection is used to - 1
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$$(x', y') = (x, y)$$

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Beyond pinholes: radial distortions

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Corrected barrel distortion

Comparing with human vision

- Cameras imitate the frequency response of the human eye, so it is good to know some

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- Computer vision probably would not get as much attention if biological vision (especially human vision) had not proven that it is possible to make important judgements from 2D images

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The Eye

Electromagnetic spectrum

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<https://sites.google.com/site/chempendix/em-spectrum>

Normalized responsivity spectra of
human cone cells (S, M, L types)

Colour represented by RGB images

Red

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Green

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Blue

Colour spaces: RGB

Default colour space



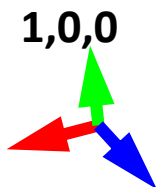
R
(G=0,B=0)

0,1,0
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G
(R=0,B=0)

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0,0,1

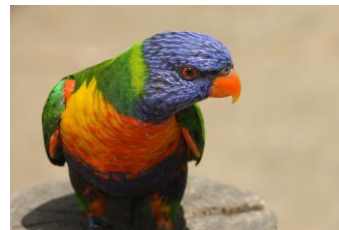
B
(R=0,G=0)

Drawback: strongly correlated channels



Colour spaces: HSV

Intuitive colour space



H
(S=1,V=1)

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S
(H=1,V=1)

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V
(H=1,S=0)

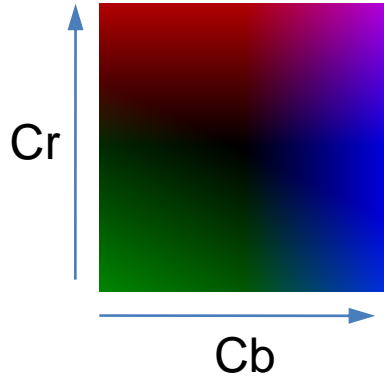
Colour spaces: YCbCr

Fast to compute, good for
compression, used by TV



Y
(Cb=0.5,Cr=0.5)

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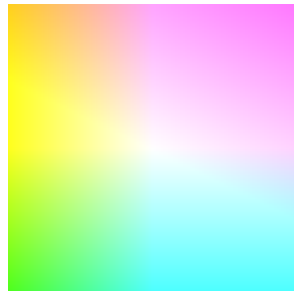


Y=0

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Cb
(Y=0.5,Cr=0.5)



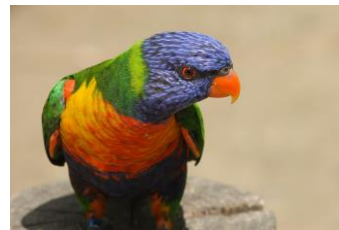
Y=1



Cr
(Y=0.5,Cb=0.5)

Colour spaces: $L^*a^*b^*$

“Perceptually uniform” colour space



L

(a=0,b=0)

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a

(L=65,b=0)

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b

(L=65,a=0)

Digital image formation

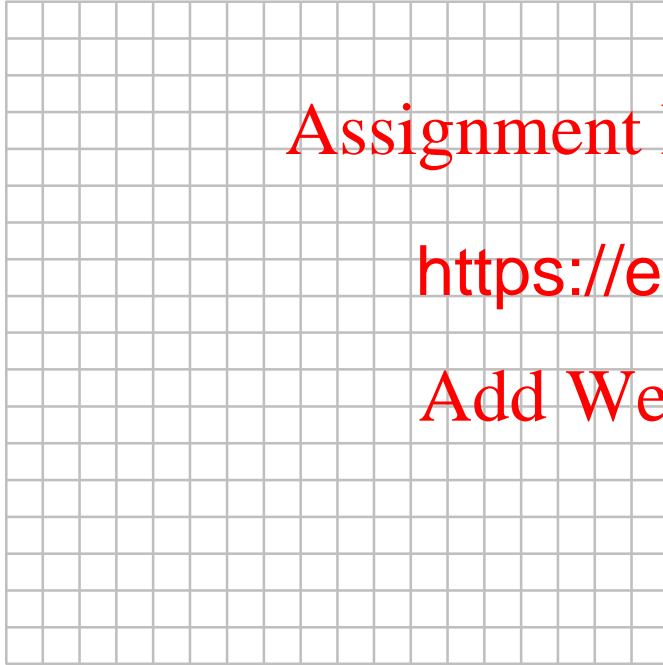
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Digital image

Digital image formation



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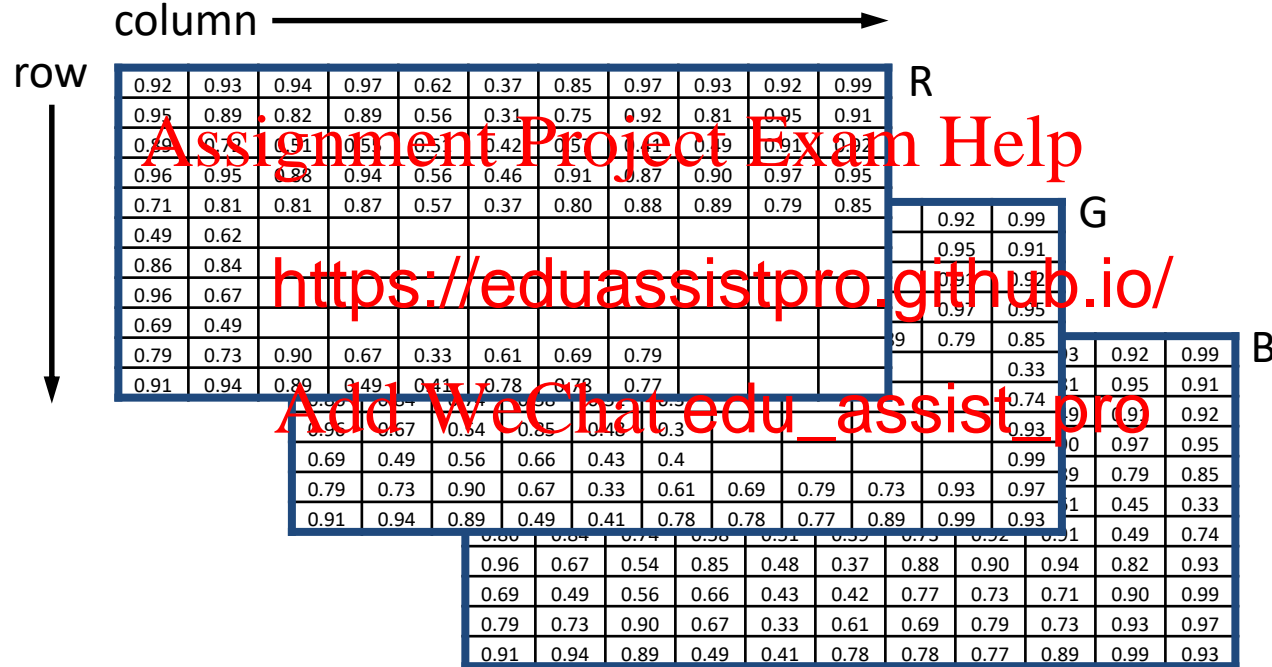


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Digitisation by spatial sampling

- **Digitisation** converts an analog image to a digital image by sampling the image space
- Sampling digitise
 - Spatial discretisation of a picture f
 - Uses a (typically rectangular) grid of sampling points:
$$x = j\Delta x, y = k\Delta y \quad | \quad j = 1 \dots M, k = 1 \dots N$$
 - The $\Delta x, \Delta y$ are called the **sampling intervals**

Digital colour images



Spatial resolution

- Spatial resolution: number of pixels per unit of length

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- Example: resolution decreases by one half each time (

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- Human faces can be recognized in 64 x 64 pixels images

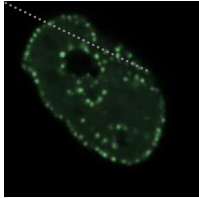
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- Appropriate resolution is essential:
 - Too little resolution, poor recognition
 - Too much resolution, slow and wastes memory

Quantisation

- Quantisation digitises the intensity or amplitude values $F(x,y)$
 - Called intensity or gray level quantisation
 - Gray-level resolution
 - For example 1 <https://eduassistpro.github.io/>
 - Number of levels should be high and perception of shading details... requires 100 levels for a realistic image

Quantisation and bits/pixel



Pixel (picture element)

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er pixel:

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$2^8 = 256$

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$2^2 = 4,096$

16 bits = $2^{16} = 65,536$

24 bits = $2^{24} = 16,777,216$

Further reading

- Chapter 2 of Szeliski

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- Chapter 2 of Shapiro and Stockman

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Acknowledgements

- Several slides from Derek Hoiem, Alexei Efros, Steve Seitz, David Forsyth and Erik Meijering
- Images <https://eduassistpro.github.io/>
- Some material, including tables, were drawn from the textbooks Add WeChat edu_assist_pro and associated online resources