# Numerical Optimisation: Trust Region Methods Assignment Project Exam Help

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Assignment 3



#### 2D Subspace Method

Recall the constraint minimisation problem for the trust region

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$$\min m(p) = f(x_k) + g^T p + -p^T B p$$
 s.t.  $p \Delta$ 

Let until the strain of the st

We can take of out of this basis via: edu\_assist\_processination of this basis via:

$$p = Va$$



Now consider the minimisation problem in terms of this basis:

$$\min m_v(a) = f(x_k) + g_v^T a + \frac{1}{2} a^T B_v a \quad \text{ s.t. } ||a|| \leq \Delta,$$

Sweepen the fitting  $e \in I$ . As xrain his element full rank  $(g \text{ and } B^{-1}g \text{ are not collinear})$ , if  $B \text{ is s.p.d. so is } B_v$ . Note t

To sohttps://eduassistpro.github. of Theorem 4.1 Nocedal Wiright. From this theor have that a minimizes  $m_v$  s.t.  $||a|| \le \text{Add}$   $\text{VeChat}_{(B_v + \lambda I)} = -g$   $\lambda$  (1)  $(B_v + \lambda I)$  is s.p.d.

$$(B_{v} + \lambda I) a = -g \quad \lambda$$

$$\lambda(\Delta - ||a||) = 0,$$

$$(B_{v} + \lambda I) \text{ is s.p.d.}$$

$$(1)$$

#### This gives two cases:

•  $\lambda=0$  and  $||a||<\Delta$ . The unconstraint solution is inside the trust region. Then the first equation becomes:

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•  $\lambda$  0 and  $a = \Delta$ . The constraint is active. Then we can

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The additional equation is provided by the c

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To solve this system we make use of eigendecomposition of  $B_v$ :

$$B_{\nu} = Q^{T}DQ$$
 with  $Q$  orthonormal



Then we have:

$$Qa = -(D + \lambda I)^{-1}Qg_{\nu}$$

and realise that  $(Qa)^T(Qa) = a^TQ^TQa = a^Ta$ . We denote Assignment Project Exam Help

with https://eduassistpro.github.  $Q_a$  i || a|| a1 a2.

Add  $W^2$ Chatedu\_assist\_property

which we can transform to a 4th degree polynomial in  $\lambda$  assuming that  $d_i + \lambda > 0$ .

