

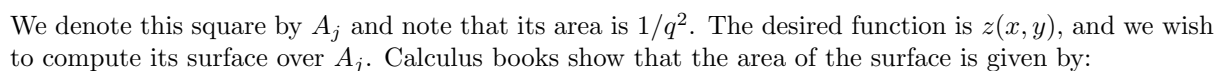
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[Adapted from Exercise 7.7 from Nocedal-Wright]

More specifically, we divide each edge of the square into  $q$  intervals of equal length, yielding  $(q+1)^2$  grid points. We label the grid points as:

so that each value of  $h$  generates a line. With each point, we associate a variable  $z_i$  that represents the height of the surface at this point. The values of the function are fixed by the boundary conditions at the  $4q$  grid points on the bo  $(q+1)^2 - 4q$  variables  $z_i$  so that the to

A typical subsquare in  $t$



Approximating the derivatives by finite differences,  $f_j$  has the form

The function  $F$  in `surfaceFunc_vector.m` implements the sum of all  $f_j$  over the unit square. The gradient and the Hessian of the cost function  $F$  are provided in `surfaceGrad.m` and `surfaceHess.m`, respectively.

## EXERCISE 1

Implement the Line Search Newton - Conjugate Gradient (LS-Newton-CG) algorithm (Algorithm 7.1 from Nocedal-Wright). More help is provided in *Cody Coursework*.

*Submit your implementation via Cody Coursework.*

[30pt]

## EXERCISE 2

You are given an adaptation of the trust region SR-1 function in `trustRegionLS.m` and the 2D subspace in `solverCM2dSubspaceExtLS.m`. Point out and explain the relevant modifications in the solver `solverCM2dSubspaceExtLS.m`.

*Submit your solution via Turnitin.*

[20pt]

## EXERCISE 3

Compute and plot a minimal area surface function with given the boundary conditions:

- ★ Bottom edge:  $B_B(t) = \sin(\pi t), t \in [0, 1]$ .
- ★ Left edge:  $B_L(t) = \sin(\pi t + \pi), t \in [0, 1]$ .
- ★ Top edge:  $B_T(t) = \sin(3\pi t), t \in [0, 1]$ .
- ★ Right edge:  $B_R(t) = \sin(3\pi t + \pi), t \in [0, 1]$ .

(a) using the LS-Newton-CG algorithm,

(b) using the BFGS algorithm (provided),

(c) using the Trust Region

Discretization with  $q$  that you consider relevant in the minimisation.

*Submit your solution via Turnitin.*

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[50pt]

**Remark.** The submission to Turnitin should not exceed 6 explicitly asked for and focus on explaining your results.

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