

NUMERICAL OPTIMISATION TUTORIAL 2

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EXERCISE 1

- (a) Code backtracking line search, steepest descent and Newton's algorithms. See Cody Courseworks for more guidance.

Submit your implementation via Cody Coursework.

[30pt]

- (b) Apply steepest descent and Newton's algorithms (with backtracking line search) to minimise the Rosenbrock function

$$f(x) = 100(y - x^2)^2 + (1 - x)^2.$$

Set the initial point $x_0 = (1.2, 1.2)^T$ and the initial step length $\alpha_0 = 1$. Plot the step sizes used by each method over the iterations as well as the trajectories traced by the iterates in \mathbb{R}^2 . Try explaining the trajectories.

Submit solution via Turnitin.

[40pt]

- (c) Redo the calculations in (b) with the more difficult starting point $x_1 = (-1.2, 0)^T$ and explain the trajectories.

Submit solution via

[10pt]

- (d) Repeat the calculation. This line search implementation provided in Moodle: `lineSearch.m`, `zoomInt.m`. Compare the new step lengths with those obtained with backtracking.

Submit solution via Turnitin.

[20pt]

Remark. The submission to Turnitin should not be longer than 4 pages. Avoid submitting more code than needed (if any) and focus on explaining your results.