
COMPGV19: Tutorial 2

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Marta Betcke and Kiko Rul#lan

Exercise 1

Program the steepest descent and Newton algorithms using the backtracking line search, Algorithm 3.1. Use them to minimise the Rosenbrock function (2.20). Set the initial step length $\alpha_0 = 1$ and print the step length used by each method at each iteration. First try the initial point $\mathbf{x}_0 = (1.2, 1.2)^T$ and then use \mathbf{t}

```
clear all
```

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Rosenbrock function

For computation define as function of 1 vector varia

```
F.f = @(x) 100.*(x(2) - x(1)^2).^2 + (1 - x(1)).^2; % function handler, 2-dim vector
F.df = @(x) [-400*(x(2) - x(1)^2)*x(1) - 2*(1 - x(1));
            200*(x(2) - x(1)^2)]; % gradient handler, 2-dim vector
F.d2f = @(x) [-400*(x(2) - 3*x(1)^2) + 2, -400*x(1); -400*x(1),
            200]; % hessian handler, 2-dim vector
% For visualisation proposes define as function of 2 variables
rosenbrock = @(x,y) 100.*(y - x.^2).^2 + (1 - x).^2;
```

Backtracking line search

```
% Initialisation
alpha0 = 1;
c1 = 1e-4;
tol = 1e-6;
maxIter = 300;

%=====
% Point x0 = [1.2; 1.2]
%=====
```

```
x0 = [1.2; 1.2];

% Steepest descent backtracking line search
lsOptsSteep.rho = 0.1;
lsOptsSteep.c1 = c1;
lsFun = @(x_k, p_k, alpha0) backtracking(F, x_k, p_k, alpha0,
    lsOptsSteep);
[xSteep, fSteep, nIterSteep, infoSteep] =
    descentLineSearch(F, 'steepest', lsFun, alpha0, x0, tol, maxIter);

% Newton backtracking line search
lsOptsNewton.rho = 0.9;
lsOptsNewton.c1 = c1;
lsFun = @(x_k, p_k, alpha0) backtracking(F, x_k, p_k, alpha0,
    lsOptsNewton);
[xNewton, fNewton, nIterNewton, infoNewton] =
    descentLineSearch(F, 'newton', lsFun, alpha0, x0, tol, maxIter);

% Define grid for visualisation
n = 300;
x = linspace(0.7,1.5,n+1);
Y = x;
[x,y] = meshgrid(x,y);

% Iterate
figure;
hold on;
plot(infoSteep, 'LineWidth', 2, 'MarkerSize', 3); % only first
plot(infoNewton.xs(1,:), infoNewton, 'LineWidth', 2, 'MarkerSize', 3); % only first
contour(X, Y, log(max(rosenbrock(X,
title('x_k: descent with line search')
legend('Steepest descent', 'Newton');
```

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```
% Step 1e
figure;
semilogy(infoSteepest.alphas(1:30), '-', 'MarkerSize', 2); hold on;
semilogy(infoNewton.alphas(1:end), '-', 'MarkerSize', 2);
grid on;
title('alpha_k: backtracking');
legend('Steepest Descent', 'Newton');
```

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```
% Plot ei
eigSteep = [];
eigNewton = [];
for i = 1:size(infoSteep.xs, 2)
    eigSteep = [eigSteep eig(F.d2f(infoSteep.xs(:, i)))];
end
for i = 1:size(infoNewton.xs, 2)
    eigNewton = [eigNewton eig(F.d2f(infoNewton.xs(:, i)))];
end
figure;
plot(eigSteep(1, 1:30), 'Color', [1 0.2 0.8], 'LineWidth', 2);
hold on;
plot(eigSteep(2, 1:30), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(eigNewton(1, :), 'Color', [0.2 1 0.8], 'LineWidth', 2);
plot(eigNewton(2, :), 'Color', [0.2 1 0.5], 'LineWidth', 2);
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig 2');
title('Eigenvalues of the Hessian');
grid on;
xlabel('iteration');

figure;
plot(sign(eigSteep(1, 1:30)), 'Color', [1 0.2 0.8], 'LineWidth', 2);
hold on;
plot(sign(eigSteep(2, 1:30)), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(sign(eigNewton(1, :)), 'Color', [0.2 1 0.8], 'LineWidth', 2);
plot(sign(eigNewton(2, :)), 'Color', [0.2 1 0.5], 'LineWidth', 2);
```

```
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig  
2');  
title('Sign of eigenvalues of the Hessian');  
grid on;  
xlabel('iteration');
```

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```
%=====
% Point x
%=====
x0 = [-1.2; 1]

% Steepest descent backtracking lin
lsOptsSteep.rho = 0.1;
lsOptsSteep.c1 = c1;
lsFun = @(x_k, p_k, alpha0) backtracking(F, x_k, p_k, alpha0,
    lsOptsSteep);
[xSteep, fSteep, nIterSteep, infoSteep] =
    descentLineSearch(F, 'steepest', lsFun, alpha0, x0, tol, maxIter);

% Newton backtracking line search
lsOptsNewton.rho = 0.9;
lsOptsNewton.c1 = c1;
lsFun = @(x_k, p_k, alpha0) backtracking(F, x_k, p_k, alpha0,
    lsOptsNewton);
[xNewton, fNewton, nIterNewton, infoNewton] =
    descentLineSearch(F, 'newton', lsFun, alpha0, x0, tol, maxIter);

% Define grid for visualisation
n = 300;
x = linspace(-1.5, 1.5, n+1);
y = linspace(-0.5, 2.5, n+1);
[X, Y] = meshgrid(x, y);

% Iterate plot
```

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```
figure;
hold on;
plot(infoSteepest.xs(1, :), infoSteepest.xs(2, :), '-or', 'LineWidth',
     2, 'MarkerSize', 3); % only first 10 iterations
plot(infoNewton.xs(1, :), infoNewton.xs(2, :), '-*g', 'LineWidth',
     2, 'MarkerSize', 3); % only first 10 iterations
contour(X, Y, log(max(rosenbrock(X,Y), 1e-3)), 20);
title('x_k: descent with line search')
legend('Steepest descent', 'Newton');
```

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```
% Step length plot
figure;
semilogy(infoSteepest.alphas(1:30), '-or', 'LineWidth', 2, 'MarkerSize',
         2); hold on;
semilogy(infoNewton.alphas(1:end), '-*g', 'LineWidth',
         2, 'MarkerSize', 2);
grid on;
title('alpha_k: backtracking');
legend('Steepest Descent', 'Newton');
```

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```
% Plot eigenvalues
eigSteep = [];
eigNewton = [];
for i = 1:size(infoSteep.xs, 2)
    eigSteep = [eigSteep eig(F.d2f(
end
for i = 1:size(infoNewton.xs, 2)
    eigNewton = [eigNewton eig(F.d2f(infoNewton.xs(:, i)))];
end
figure;
plot(eigSteep(1, 1:30), 'Color', [1 0.2 0.8], 'LineWidth', 2);
hold on;
plot(eigSteep(2, 1:30), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(eigNewton(1, :), 'Color', [0.2 1 0.8], 'LineWidth', 2);
plot(eigNewton(2, :), 'Color', [0.2 1 0.5], 'LineWidth', 2);
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig
2');
title('Eigenvalues of the Hessian');
grid on;
xlabel('iteration');

figure;
plot(sign(eigSteep(1, 1:30)), 'Color', [1 0.2 0.8], 'LineWidth', 2);
hold on;
plot(sign(eigSteep(2, 1:30)), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(sign(eigNewton(1, :)), 'Color', [0.2 1 0.8], 'LineWidth', 2);
```



```
plot(sign(eigNewton(2, :)), 'Color', [0.2 1 0.5], 'LineWidth', 2);  
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig  
2');  
title('Sign of eigenvalues of the Hessian');  
grid on;  
xlabel('iteration');
```

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Line search <https://eduassistpro.github.io/> **conditions**

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```
% Initialisation
alpha_max = alpha0;
c1 = 1e-4; %0.01;
%c2 = 0.9; % choose 0.1 for steepest descent, 0.9 for Newton
tol = 1e-6;

%=====
% Point x0 = [1.2; 1.2]
%=====
x0 = [1.2; 1.2];

% Steepest descent line search strong WC
lsOptsSteep.c1 = c1;
lsOptsSteep.c2 = 0.1;
lsFun = @(x_k, p_k, alpha0) lineSearch(F, x_k, p_k, alpha_max,
    lsOptsSteep);
[xSteep, fSteep, nIterSteep, infoSteep] =
    descentLineSearch(F, 'steepest', lsFun, alpha0, x0, tol, maxIter);

% Newton line search strong WC
lsOptsNewton.c1 = c1;
lsOptsNewton.c2 = 0.9;
lsFun = @(x_k, p_k, alpha0) lineSearch(F, x_k, p_k, alpha_max,
    lsOptsNewton);
```

```
[xNewton, fNewton, nIterNewton, infoNewton] =  
    descentLineSearch(F, 'newton', lsFun, alpha0, x0, tol, maxIter);  
  
% Define grid for visualisation  
n = 300;  
x = linspace(0.7,1.5,n+1);  
y = linspace(0.7,1.8,n+1);  
[X,Y] = meshgrid(x,y);  
  
% Iterate plot  
figure;  
hold on;  
plot(infoSteep.xs(1, :), infoSteep.xs(2, :), '-or', 'LineWidth',  
     2, 'MarkerSize', 3); % only first 10 iterations  
plot(infoNewton.xs(1, :), infoNewton.xs(2, :), '-*g', 'LineWidth',  
     2, 'MarkerSize', 3); % only first 10 iterations  
contour(X, Y, log(max(rosenbrock(X,Y), 1e-3)), 20);  
title('x_k: descent with line search')  
legend('Steepest descent', 'Newton');
```

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```
% Step length plot  
figure;  
semilogy(infoSteep.alphas(1:30), '-or', 'LineWidth', 2, 'MarkerSize',  
         2); hold on;  
semilogy(infoNewton.alphas(1:end), '-*g', 'LineWidth',  
         2, 'MarkerSize', 2);  
grid on;
```

```
title('alpha_k: line search WC');  
legend('Steepest Descent', 'Newton');
```

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```
% Plot eigenvalues  
eigSteep = [];  
eigNewton = [];  
for i = 1:size(infoSteep.xs, 2)  
    eigSteep = [eigSteep eig(F.d2f(infoSteep.xs(:, i)))];  
end  
for i = 1:size(infoNewton.xs, 2)  
    eigNewton = [eigNewton eig(F.d2f(infoNewton.xs(:, i)))];  
end  
figure;  
plot(eigSteep(1, 1:30), 'Color', [1 0.2 0.8], 'LineWidth', 2);  
hold on;  
plot(eigSteep(2, 1:30), 'Color', [1 0.2 0.5], 'LineWidth', 2);  
plot(eigNewton(1, :), 'Color', [0.2 1 0.8], 'LineWidth', 2);  
plot(eigNewton(2, :), 'Color', [0.2 1 0.5], 'LineWidth', 2);  
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig  
2');  
title('Eigenvalues of the Hessian');  
grid on;  
xlabel('iteration');  
  
figure;  
plot(sign(eigSteep(1, 1:30)), 'Color', [1 0.2 0.8], 'LineWidth', 2);  
hold on;
```

```
plot(sign(eigSteep(2, 1:30)), 'Color', [1 0.2 0.5], 'LineWidth', 2);  
plot(sign(eigNewton(1, :)), 'Color', [0.2 1 0.8], 'LineWidth', 2);  
plot(sign(eigNewton(2, :)), 'Color', [0.2 1 0.5], 'LineWidth', 2);  
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig  
2');  
title('Sign of eigenvalues of the Hessian');  
grid on;  
xlabel('iteration');
```

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```
%=====
% Point x
%=====
x0 = [-1.2; 1]

% Steepest descent line search stro
lsOptsSteep.c1 = c1;
lsOptsSteep.c2 = 0.1;
lsFun = @(x_k, p_k, alpha0) lineSearch(F, x_k, p_k, alpha_max,
    lsOptsSteep);
[xSteep, fSteep, nIterSteep, infoSteep] =
    descentLineSearch(F, 'steepest', lsFun, alpha0, x0, tol, maxIter);

% Newton g line search strong WC
lsOptsNewton.c1 = c1;
lsOptsNewton.c2 = 0.9;
lsFun = @(x_k, p_k, alpha0) lineSearch(F, x_k, p_k, alpha_max,
    lsOptsNewton);
[xNewton, fNewton, nIterNewton, infoNewton] =
    descentLineSearch(F, 'newton', lsFun, alpha0, x0, tol, maxIter);

% Define grid for visualisation
n = 300;
x = linspace(-1.5, 1.5, n+1);
y = linspace(-0.5, 2.5, n+1);
[X, Y] = meshgrid(x, y);
```

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```
% Iterate plot
figure;
hold on;
plot(infoSteep.xs(1, :), infoSteep.xs(2, :), '-or', 'LineWidth',
     2, 'MarkerSize', 3); % only first 10 iterations
plot(infoNewton.xs(1, :), infoNewton.xs(2, :), '-*g', 'LineWidth',
     2, 'MarkerSize', 3); % only first 10 iterations
contour(X, Y, log(max(rosenbrock(X,Y), 1e-3)), 20);
title('x_k: descent with line search')
legend('Steepest descent', 'Newton');
```

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```
% Step length plot
figure;
semilogy(infoSteep.alphas(1:30), '-or', 'LineWidth', 2, 'MarkerSize',
         2); hold on;
semilogy(infoNewton.alphas(1:end), '-*g', 'LineWidth',
         2, 'MarkerSize', 2);
grid on;
title('alpha_k: line search WC');
legend('Steepest Descent', 'Newton');
```

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```
% Plot eigenvalues
eigSteep = [];
eigNewton = [];
for i = 1:size(infoSteep.xs, 2)
    eigSteep = [eigSteep eig(F.d2f(
end
for i = 1:size(infoNewton.xs, 2)
    eigNewton = [eigNewton eig(F.d2f(infoNewton.xs(:, i)))];
end
figure;
plot(eigSteep(1, 1:30), 'Color', [1 0.2 0.8], 'LineWidth', 2);
hold on;
plot(eigSteep(2, 1:30), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(eigNewton(1, :), 'Color', [0.2 1 0.8], 'LineWidth', 2);
plot(eigNewton(2, :), 'Color', [0.2 1 0.5], 'LineWidth', 2);
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig
2');
title('Eigenvalues of the Hessian');
grid on;
xlabel('iteration');

figure;
plot(sign(eigSteep(1, 1:30)), 'Color', [1 0.2 0.8], 'LineWidth', 2);
hold on;
plot(sign(eigSteep(2, 1:30)), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(sign(eigNewton(1, :)), 'Color', [0.2 1 0.8], 'LineWidth', 2);
```



```
plot(sign(eigNewton(2, :)), 'Color', [0.2 1 0.5], 'LineWidth', 2);  
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig  
2');  
title('Sign of eigenvalues of the Hessian');  
grid on;  
xlabel('iteration');
```

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descentLineSearch.m

Wrapper function executing iteration with descent d

od

```
function [xMin, fMin, nIter, info] = descentLineSearch(F, descent, ls,
    alpha0, x0, tol, maxIter)
% DESCENTLINESEARCH Wrapper function executing descent with line
% search
% [xMin, fMin, nIter, info] = descentLineSearch(F, descent, ls,
% alpha0, x0, tol, maxIter)
%
% INPUTS
% F: structure with fields
%   - f: function handler
%   - df: gradient handler
%   - f2f: Hessian handler
% descent: specifies descent direction {'steepese', 'newton'}
% ls: function handle for computing the step length
% alpha0: initial step length
% rho: in (0,1) backtraking step length reduction factor
% c1: constant in sufficient decrease condition  $f(\mathbf{x}_k + \alpha_k \mathbf{p}_k) >$ 
%      $f_k + c1 \cdot \alpha_k \cdot (\mathbf{df}_k)' \cdot \mathbf{p}_k$ 
%     Typically chosen small, (default 1e-4).
% x0: initial iterate
```

```
% tol: stopping condition on minimal allowed step
%     norm(x_k - x_k_1)/norm(x_k) < tol;
% maxIter: maximum number of iterations
%
% OUTPUTS
% xMin, fMin: minimum and value of f at the minimum
% nIter: number of iterations
% info: structure with information about the iteration
%   - xs: iterate history
%   - alphas: step lengths history
%
% Copyright (C) 2017  Marta M. Betcke, Kiko Rullan

% Parameters
% Stopping condition {'step', 'grad'}
stopType = 'grad';

% Initialization
nIter = 0;
x_k = x0;
info.xs = x0;
info.alphas = alpha0;
stopCond = false;

% Loop until stopping condition is reached
while (~stopCond)
    % Increment iteration counter
    nIter = nIter + 1;

    % Compute descent direction
    switch lower(descent)
        case 'steepest'
            p_k = -F.df(x_k); % steepest descent direction
        case 'newton'
            p_k = -F.d2f(x_k)\F.df(x_k); % Newton direction
    end

    % Call line search given by handle ls for computing step length
    alpha_k = ls(x_k, p_k, alpha0);

    % Update x_k and f_k
    x_k_1 = x_k;
    x_k = x_k + alpha_k*p_k;

    % Store iteration info
    info.xs = [info.xs x_k];
    info.alphas = [info.alphas alpha_k];

    switch stopType
        case 'step'
            % Compute relative step length
            normStep = norm(x_k - x_k_1)/norm(x_k_1);
            stopCond = (normStep < tol);
```

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```
        case 'grad'
            stopCond = (norm(F.df(x_k), 'inf') < tol*(1 +
tol*abs(F.f(x_k)))));
        end

end

% Assign output values
xMin = x_k;
fMin = F.f(x_k);
```

backtracking.m

Backtracking line search

```
function [alpha, info] = backtracking(F, x_k, p, alpha0, opts)
% BACKTRACKING Backtracking line search to satisfy sufficient decrease
condition
% [alpha, info] = backtracking(F, x_k, p, alpha0, opts);
%
% INPUTS
% F: struct
%   - f: function handle
%   - df: gradient function handle
% x_k: current iterate
% p: descent direction
% alpha0: initial step length
% opts: backtracking specific options
%   - rho: in (0,1) backtracking step length reduction factor
%   - c1: constant in sufficient decrease condition f(x_k + alpha_k*p)
%         > f(x_k) + c1*alpha_k*(df_k'*p)
%         Typically chosen small, (default 1e-4).
%
% OUTPUTS
% alpha: step length
% nIter: number of iterations
% info: structure with information about the backtracking iteration
%   - alphas: step lengths history
%
% Copyright (C) 2017 Marta M. Betcke, Kiko Rullan

% Default values
if nargin < 5 || ~isfield(opts, 'c1')
    opts.c1 = 1e-4;
end
% Choose
% rho = 0.1 for steepest descent, conjugate gradients
% rho = 0.9 for Newton, Quasi-Newton
if nargin < 5 || ~isfield(opts, 'rho')
```

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```

    opts.rho = 0.9; % Newton
end
if nargin < 4
    alpha0 = 1; % Newton
end

% Initialize info structure
info.alphas = alpha0;
info.rho = opts.rho;
info.c1 = opts.c1;

% Initial step length
alpha = alpha0;

% Compute f, grad f at x_k
f_k = F.f(x_k);
df_k = F.df(x_k);

% Backtracking linesearch for computing step length
while F.f(x_k + alpha*p) > f_k + opts.c1*alpha*(df_k'*p)
    alpha = opts.rho*alpha;
    info.alphas = [info.alphas alpha];
end

```

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lineSearch

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Line search algorithm find steps satisfying strong W

cedal Algorithm 3.5)

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```

function [alpha_s, info] = lineSearch(alpha_max, opts)
% LINESEARCH Line Search algorithm satisfying strong Wolfe conditions
% alpha_s = lineSearch(F, x_k, p_k, alpha_max, opts)
%
% INPUTS
% F: structure with fields
%   - f: function handler
%   - df: gradient handler
% x_k: current iterate
% p_k: descent direction
% alpha_max: maximum step length
% opts: line search specific option structure with fields
%   - c1: constant in sufficient decrease condition
%          $f(x_k + \alpha_k p_k) > f(x_k) + c1 \alpha_k (df_k' p_k)$ 
%         Typically chosen small, (default 1e-4)
%   - c2: constant in strong curvature condition
%          $|df(x_k + \alpha_k p_k)' p_k| \leq c2 |df(x_k)' p_k|$ 
%
% OUTPUT
% alpha_s: step length
% info: structure containing alpha_j history
%
% Reference: Algorithm 3.5 from Nocedal, Numerical Optimization

```

```

%
% It generates a monotonically increasing sequence of step lengths
alpha_j.
% Uses the fact that interval (alpha_j_1, alpha_j) contains step
lengths satisfying strong Wolfe conditions
% if one of the conditions below is satisfied:
% (C1) alpha_j violates the sufficient decrease condition
% (C2) phi(alpha_j) >= phi(alpha_j_1)
% (C3) dphi(alpha_j) >= 0
%
% Copyright (C) 2017 Kiko Rullan, Marta M. Betcke

% Paramters
% Multiple of alpha_j used to generate alpha_{j+1}
FACT = 10;

% Calculate handle to function phi(alpha) = f(x_k + alpha*p_k)
% Phi: function structure with fields
% - phi: function handler
% - dphi: derivative handler
Phi.phi = @(alpha) F.f(x_k + alpha*p_k);
Phi.dphi = @(alpha) (F.df(x_k + alpha*p_k))*p_k;
% Initialization
alpha(1)
phi_i(1)
dphi_i(1)
alpha(2)
alpha_s = 0;
n = 2;
maxIter = 10;
stop = false;

while (n < maxIter && stop == false)
    phi_i(n) = Phi.phi(alpha(n));
    dphi_i(n) = Phi.dphi(alpha(n));
    if(phi_i(n) > phi_i(1) + opts.c1*alpha(n)*dphi_i(1) || (phi_i(n)
    >= phi_i(n-1) && n > 2))
        alpha_s = zoomInt(Phi, alpha(n-1), alpha(n), opts.c1,
        opts.c2);
        stop = true;
    elseif(abs(dphi_i(n)) <= -opts.c2*dphi_i(1))
        alpha_s = alpha(n);
        stop = true;
    elseif(dphi_i(n) >= 0)
        alpha_s = zoomInt(Phi, alpha(n), alpha(n-1), opts.c1,
        opts.c2);
        stop = true;
    end;
    %alpha(n+1) = 0.5*(alpha(n)+alpha_max);
    alpha(n+1) = max(FACT*alpha(n), alpha_max);
    n = n + 1;
end

```

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```
info.alphas = alpha;
```

Zoom function used by the line search above (Wright, Nocedal Algorithm 3.6)

```
function [alpha, info] = zoomInt(Phi, alpha_l, alpha_h, c1, c2)
% ZOOMINT Zoom algorithm for line search with strong Wolfe conditions
% alpha = zoomInt(Phi, alpha_l, alpha_h, c1, c2)
%
% INPUTS
% Phi: structure for function of step length phi(alpha) = f(x_k +
%     alpha*p_k) with fields
%   - phi: function handler
%   - dphi: derivative handler
% alpha_l: lower boundary of the trial interval
% alpha_h: upper boundary of the trial interval
% c1 & c2: constants for Wolfe conditions (see lineSearch.m)
%
% OUTPUT
% alpha: step length
% info: structures containing iteration history
% Reference: Algorithm 3.5 from Nocedal, Numerical Optimization
%
% Property
% (P1) In the set of step lengths satisfying
%     strong W
% (P2) Among the step lengths generating the
%     sufficient decrease condition
%     alpha_l is the one with smallest
% (P3) alpha_h is chosen such that d
%     _h - alpha_l) <
%     0
%
% Copyright (C) 2017 Kiko Rullan, Marta M. Betcke

% Parameters
% Trial step in {'bisection', 'interp2'}
TRIALSTEP = 'bisection';
tol = eps;

% Structure containing information about the iteration
info.alpha_ls = [];
info.alpha_hs = [];
info.alpha_js = [];
info.phi_js = [];
info.dphi_js = [];

n = 1;
stop = false;
maxIter = 100;
while (n < maxIter && stop == false)
    % Find trial step length alpha_j in [alpha_l, alpha_h]
    switch TRIALSTEP
```

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```

        case 'bisection'
            alpha_j = 0.5*(alpha_h + alpha_l);
        case 'interp2'
        end
    end
    phi_j = Phi.phi(alpha_j);

    % Update info
    info.alpha_ls = [info.alpha_ls alpha_l];
    info.alpha_hs = [info.alpha_hs alpha_h];
    info.alpha_js = [info.alpha_js alpha_j];
    info.phi_js = [info.phi_js phi_j];

    if abs(alpha_h - alpha_l) < tol
        alpha = alpha_j;
        stop = true;
        warning('Line search stopped because the interval became too small. Return centre of the interval.')
    end

    if (phi_j > Phi.phi(0) + c1*alpha_j*Phi.dphi(0) ||
        Phi.phi(alpha_j) >= Phi.phi(alpha_l))
        % alpha_j does not satisfy sufficient decrease condition -> look for alpha < alpha_j
        % or phi(alpha_j) >= phi(alpha_l)
        % -
        alp
        % U
        info.dphi_js = [info.dphi_js
    else
        % alpha_j satisfies sufficient decrease condition
        dphi_j = Phi.dphi(alpha_j);

        % Update info
        info.dphi_js = [info.dphi_js dphi_j];

        if (abs(dphi_j) <= -c2*Phi.dphi(0))
            % alpha_j satisfies strong curvature condition
            alpha = alpha_j;
            stop = true;
        elseif (dphi_j*(alpha_h - alpha_l) >= 0)
            % alpha_h : dphi(alpha_l)*(alpha_h - alpha_l) < 0
            % alpha_j violates this condition but swapping alpha_l <->
            alpha_h will reestablish it
            % -> [alpha_j, alpha_l]
            alpha_h = alpha_l;
        end
        alpha_l = alpha_j;
    end
end
end

```

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