

We denote this square by A_j and note that its area is $1/q^2$. The desired function is $z(x, y)$, and we wish to compute its surface over A_j . Calculus books show that the area of the surface is given by:

EXERCISE 1

Implement the Line Search Newton - Conjugate Gradient (LS-Newton-CG) algorithm (Algorithm 7.1 from Nocedal-Wright). More help is provided in *Cody Coursework*.

Submit your implementation via Cody Coursework.

[30pt]

EXERCISE 2

You are given an adaptation of the trust region SR-1 function in `trustRegionLS.m` and the 2D subspace in `solverCM2dSubspaceExtLS.m`. Point out and explain the relevant modifications in the solver `solverCM2dSubspaceExtLS.m`.

Submit your solution via Turnitin.

[20pt]

EXERCISE 3

Compute and plot a minimal area surface function with given the boundary conditions:

- ★ Bottom edge: $B_B(t) = \sin(\pi t), t \in [0, 1]$.
- ★ Left edge: $B_L(t) = \sin(\pi t + \pi), t \in [0, 1]$.
- ★ Top edge: $B_T(t) = \sin(3\pi t), t \in [0, 1]$.
- ★ Right edge: $B_R(t) = \sin(3\pi t + \pi), t \in [0, 1]$.

(a) using the LS-Newton-CG algorithm,

(b) using the BFGS algorithm (provided),

(c) using the Trust Region

Discretization with q that you consider relevant in the minimisation.

Submit your solution via Turnitin.

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[50pt]

Remark. The submission to Turnitin should not exceed 6 explicitly asked for and focus on explaining your results.

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