COMPGV19: Tutorial 2

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Marta Betcke and Kiko Rul#lan

Exercise 1

Program the steepest descent and Newton algorithms using the backtracking line search, Algorithm 3.1. Use the steep in the line of the local process of the line of the local process. Let the initial point $x_0 = 1$ and print the step length used by each method at each iteration. First try the initial point $x_0 = (1.2, 1.2)^T$ and then use t

clear all https://eduassistpro.github.io/

Rosenbrock function

For computation define as function of Pvector varia edu_assist_pro

```
 \begin{split} F.f &= @(x) \ 100.*(x(2) - x(1)^2).^2 + (1 - x(1)).^2; \ \$ \ function \\ handler, \ 2-dim \ vector \\ F.df &= @(x) \ [-400*(x(2) - x(1)^2)*x(1) - 2*(1 - x(1)); \\ &\qquad \qquad 200*(x(2) - x(1)^2)]; \ \$ \ gradient \ handler, \ 2-dim \ vector \\ F.d2f &= @(x) \ [-400*(x(2) - 3*x(1)^2) + 2, \ -400*x(1); \ -400*x(1), \\ 200]; \ \$ \ hessian \ handler, \ 2-dim \ vector \\ \$ \ For \ visualisation \ proposes \ define \ as \ function \ of \ 2 \ variables \\ rosenbrock &= @(x,y) \ 100.*(y - x.^2).^2 + (1 - x).^2; \end{split}
```

Backtracking line search

```
x0 = [1.2; 1.2];
% Steepest descent backtracking line search
lsOptsSteep.rho = 0.1;
lsOptsSteep.c1 = c1;
lsFun = @(x_k, p_k, alpha0) backtracking(F, x_k, p_k, alpha0,
 lsOptsSteep);
[xSteep, fSteep, nIterSteep, infoSteep] =
 descentLineSearch(F, 'steepest', lsFun, alpha0, x0, tol, maxIter);
% Newton backtracking line search
lsOptsNewton.rho = 0.9;
lsOptsNewton.c1 = c1;
lsFun = @(x_k, p_k, alpha0) backtracking(F, x_k, p_k, alpha0,
[xNewton, fNewton, nIterNewton, infoNewton] =
 descentLineSearch(F, 'newton', lsFun, alpha0, x0, tol, maxIter);
% Define grid for visualisation
n = 300;
x = linspace(0.7, 1.5, n+1);
         gnment Project Exam Help
% Iterate
figure;
         https://eduassistpro.github.jo/
hold on;
plot(info
 2, 'MarkerSize', 3); % only first
plot(infoNewton.xs(1,:), infoNewto
2, 'MarkeAid of 3 We ly hist edu_assist_pro
contour(x, y, log(max(rosenbrock(x,
title('x_k: descent with line search')
legend('Steepest descent', 'Newton');
```

```
https://eduassistpro.github.io/
figure;
semilogy(infoSteep.alphas(1:30), '-
2); hold A:dd WeChat edu_assist_pro
semilogy(infoNewton.alphas(1:end), edu_assist_pro
2, 'MarkerSize', 2);
grid on;
title('alpha_k: backtracking');
legend('Steepest Descent', 'Newton');
```

```
* Plot ei https://eduassistpro.github.io/
eigSteep = [];
eigNewton = [];
for i = 1: Azelo for eigsteep eig (F. azr edu_assist_pro
for i = 1:size(infoNewton.xs, 2)
    eigNewton = [eigNewton eig(F.d2f(infoNewton.xs(:, i)))];
end
figure;
plot(eigSteep(1, 1:30), 'Color', [1 0.2 0.8], 'LineWidth', 2);
hold on;
plot(eigSteep(2, 1:30), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(eigNewton(1, :), 'Color', [0.2 1 0.8], 'LineWidth', 2);
plot(eigNewton(2, :), 'Color', [0.2 1 0.5], 'LineWidth', 2);
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig
2');
title('Eigenvalues of the Hessian');
grid on;
xlabel('iteration');
figure;
plot(sign(eigSteep(1, 1:30)), 'Color', [1 0.2 0.8], 'LineWidth', 2);
hold on;
plot(sign(eigSteep(2, 1:30)), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(sign(eigNewton(1, :)), 'Color', [0.2 1 0.8], 'LineWidth', 2);
plot(sign(eigNewton(2, :)), 'Color', [0.2 1 0.5], 'LineWidth', 2);
```

```
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig
2');
title('Sign of eigenvalues of the Hessian');
grid on;
xlabel('iteration');
```

https://eduassistpro.github.io/

```
x0 = [-1.2Add WeChat edu_assist_pro % Steepest descent backtracking lin
```

```
% Steepest descent backtracking lin
lsOptsSteep.rho = 0.1;
lsOptsSteep.c1 = c1;
lsFun = @(x_k, p_k, alpha0) backtracking(F, x_k, p_k, alpha0,
 lsOptsSteep);
[xSteep, fSteep, nIterSteep, infoSteep] =
 descentLineSearch(F, 'steepest', lsFun, alpha0, x0, tol, maxIter);
% Newton backtracking line search
lsOptsNewton.rho = 0.9;
lsOptsNewton.c1 = c1;
lsFun = @(x_k, p_k, alpha0) backtracking(F, x_k, p_k, alpha0,
 lsOptsNewton);
[xNewton, fNewton, nIterNewton, infoNewton] =
 descentLineSearch(F, 'newton', lsFun, alpha0, x0, tol, maxIter);
% Define grid for visualisation
n = 300;
x = linspace(-1.5, 1.5, n+1);
y = linspace(-0.5, 2.5, n+1);
[X,Y] = meshgrid(x,y);
% Iterate plot
```

```
figure;
hold on;
plot(infoSteep.xs(1, :), infoSteep.xs(2, :), '-or', 'LineWidth',
   2, 'MarkerSize', 3); % only first 10 iterations
plot(infoNewton.xs(1, :), infoNewton.xs(2, :), '-*g', 'LineWidth',
   2, 'MarkerSize', 3); % only first 10 iterations
contour(X, Y, log(max(rosenbrock(X,Y), le-3)), 20);
title('x_k: descent with line search')
legend('Steepest descent', 'Newton');
```

```
% Step length plot
figure;
semilogy(infoSteep.alphas(1:30), '-or', 'LineWidth', 2, 'MarkerSize',
   2); hold on;
semilogy(infoNewton.alphas(1:end), '-*g', 'LineWidth',
   2, 'MarkerSize', 2);
grid on;
title('alpha_k: backtracking');
legend('Steepest Descent', 'Newton');
```

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```
% Plot eigenvalues
eigSteep = [];
                            hat edu_assist_pro
eigNewton ★[}
    eigSteep = [eigSteep eig(F.d2f(
end
for i = 1:size(infoNewton.xs, 2)
    eigNewton = [eigNewton eig(F.d2f(infoNewton.xs(:, i)))];
end
figure;
plot(eigSteep(1, 1:30), 'Color', [1 0.2 0.8], 'LineWidth', 2);
plot(eigSteep(2, 1:30), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(eigNewton(1, :), 'Color', [0.2 1 0.8], 'LineWidth', 2);
plot(eigNewton(2, :), 'Color', [0.2 1 0.5], 'LineWidth', 2);
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig
2');
title('Eigenvalues of the Hessian');
grid on;
xlabel('iteration');
figure;
plot(sign(eigSteep(1, 1:30)), 'Color', [1 0.2 0.8], 'LineWidth', 2);
hold on;
plot(sign(eigSteep(2, 1:30)), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(sign(eigNewton(1, :)), 'Color', [0.2 1 0.8], 'LineWidth', 2);
```

```
plot(sign(eigNewton(2, :)), 'Color', [0.2 1 0.5], 'LineWidth', 2);
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig
2');
title('Sign of eigenvalues of the Hessian');
grid on;
xlabel('iteration');
```

Line searc https://eduassistpro.github.io/conditions

```
% Initialia told ; WeChat edu_assist_pro
c1 = 1e-4; %0.01;
%c2 = 0.9; % choose 0.1 for steepest descent, 0.9 for Newton
tol = 1e-6;
%==========
% Point x0 = [1.2; 1.2]
x0 = [1.2; 1.2];
% Steepest descent line search strong WC
lsOptsSteep.c1 = c1;
lsOptsSteep.c2 = 0.1;
lsFun = @(x_k, p_k, alpha0) lineSearch(F, x_k, p_k, alpha_max,
 lsOptsSteep);
[xSteep, fSteep, nIterSteep, infoSteep] =
 descentLineSearch(F, 'steepest', lsFun, alpha0, x0, tol, maxIter);
% Newton line search strong WC
lsOptsNewton.c1 = c1;
lsOptsNewton.c2 = 0.9;
lsFun = @(x_k, p_k, alpha0) lineSearch(F, x_k, p_k, alpha_max,
 lsOptsNewton);
```

```
[xNewton, fNewton, nIterNewton, infoNewton] =
 descentLineSearch(F, 'newton', lsFun, alpha0, x0, tol, maxIter);
% Define grid for visualisation
n = 300;
x = linspace(0.7, 1.5, n+1);
y = linspace(0.7, 1.8, n+1);
[X,Y] = meshgrid(x,y);
% Iterate plot
figure;
hold on;
plot(infoSteep.xs(1, :), infoSteep.xs(2, :), '-or', 'LineWidth',
 2, 'MarkerSize', 3); % only first 10 iterations
plot(infoNewton.xs(1, :), infoNewton.xs(2, :), '-*g', 'LineWidth',
 2, 'MarkerSize', 3); % only first 10 iterations
contour(X, Y, log(max(rosenbrock(X,Y), 1e-3)), 20);
title('x k: descent with line search')
legend('Steepest descent', 'Newton');
```

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Add WeChat edu_assist_pro

```
% Step length plot
figure;
semilogy(infoSteep.alphas(1:30), '-or', 'LineWidth', 2, 'MarkerSize',
   2); hold on;
semilogy(infoNewton.alphas(1:end), '-*g', 'LineWidth',
   2, 'MarkerSize', 2);
grid on;
```

```
title('alpha_k: line search WC');
legend('Steepest Descent', 'Newton');
```

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```
* Plot eightelep Avelds WeChat edu_assist_pro
eigNewton = [];
for i = 1:size(infoSteep.xs, 2)
    eigSteep = [eigSteep eig(F.d2f(infoSteep.xs(:, i)))];
end
for i = 1:size(infoNewton.xs, 2)
    eigNewton = [eigNewton eig(F.d2f(infoNewton.xs(:, i)))];
end
figure;
plot(eigSteep(1, 1:30), 'Color', [1 0.2 0.8], 'LineWidth', 2);
plot(eigSteep(2, 1:30), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(eigNewton(1, :), 'Color', [0.2 1 0.8], 'LineWidth', 2);
plot(eigNewton(2, :), 'Color', [0.2 1 0.5], 'LineWidth', 2);
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig
title('Eigenvalues of the Hessian');
grid on;
xlabel('iteration');
figure;
plot(sign(eigSteep(1, 1:30)), 'Color', [1 0.2 0.8], 'LineWidth', 2);
hold on;
```

```
plot(sign(eigSteep(2, 1:30)), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(sign(eigNewton(1,:)), 'Color', [0.2 1 0.8], 'LineWidth', 2);
plot(sign(eigNewton(2,:)), 'Color', [0.2 1 0.5], 'LineWidth', 2);
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig 2');
title('Sign of eigenvalues of the Hessian');
grid on;
xlabel('iteration');
```

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```
VeChat edu_assist_pro
x0 = [-1.2 \land 1]
% Steepest descent line search stro
lsOptsSteep.c1 = c1;
lsOptsSteep.c2 = 0.1;
lsFun = @(x_k, p_k, alpha0) lineSearch(F, x_k, p_k, alpha_max,
 lsOptsSteep);
[xSteep, fSteep, nIterSteep, infoSteep] =
 descentLineSearch(F, 'steepest', lsFun, alpha0, x0, tol, maxIter);
% Newton g line search strong WC
lsOptsNewton.c1 = c1;
lsOptsNewton.c2 = 0.9;
lsFun = @(x_k, p_k, alpha0) lineSearch(F, x_k, p_k, alpha_max,
 lsOptsNewton);
[xNewton, fNewton, nIterNewton, infoNewton] =
 descentLineSearch(F, 'newton', lsFun, alpha0, x0, tol, maxIter);
% Define grid for visualisation
n = 300;
x = linspace(-1.5, 1.5, n+1);
y = linspace(-0.5, 2.5, n+1);
[X,Y] = meshgrid(x,y);
```

```
% Iterate plot
figure;
hold on;
plot(infoSteep.xs(1, :), infoSteep.xs(2, :), '-or', 'LineWidth',
    2, 'MarkerSize', 3); % only first 10 iterations
plot(infoNewton.xs(1, :), infoNewton.xs(2, :), '-*g', 'LineWidth',
    2, 'MarkerSize', 3); % only first 10 iterations
contour(X, Y, log(max(rosenbrock(X,Y), le-3)), 20);
title('x_k: descent with line search')
legend('Steepest descent', 'Newton');
```

```
% Step length plot
figure;
semilogy(infoSteep.alphas(1:30), '-or', 'LineWidth', 2, 'MarkerSize',
   2); hold on;
semilogy(infoNewton.alphas(1:end), '-*g', 'LineWidth',
   2, 'MarkerSize', 2);
grid on;
title('alpha_k: line search WC');
legend('Steepest Descent', 'Newton');
```

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```
% Plot eigenvalues
eigSteep = [];
                            hat edu_assist_pro
eigNewton ★[}
    eigSteep = [eigSteep eig(F.d2f(
end
for i = 1:size(infoNewton.xs, 2)
    eigNewton = [eigNewton eig(F.d2f(infoNewton.xs(:, i)))];
end
figure;
plot(eigSteep(1, 1:30), 'Color', [1 0.2 0.8], 'LineWidth', 2);
plot(eigSteep(2, 1:30), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(eigNewton(1, :), 'Color', [0.2 1 0.8], 'LineWidth', 2);
plot(eigNewton(2, :), 'Color', [0.2 1 0.5], 'LineWidth', 2);
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig
2');
title('Eigenvalues of the Hessian');
grid on;
xlabel('iteration');
figure;
plot(sign(eigSteep(1, 1:30)), 'Color', [1 0.2 0.8], 'LineWidth', 2);
hold on;
plot(sign(eigSteep(2, 1:30)), 'Color', [1 0.2 0.5], 'LineWidth', 2);
plot(sign(eigNewton(1, :)), 'Color', [0.2 1 0.8], 'LineWidth', 2);
```

```
plot(sign(eigNewton(2, :)), 'Color', [0.2 1 0.5], 'LineWidth', 2);
legend('Steepest Eig 1', 'Steepest Eig 2', 'Newton Eig 1', 'Newton Eig
2');
title('Sign of eigenvalues of the Hessian');
grid on;
xlabel('iteration');
```

https://eduassistpro.github.io/

descentLineSearch.m Add WeChat edu_assist_pro

Wrapper function executing iteration with descent d

```
function [xMin, fMin, nIter, info] = descentLineSearch(F, descent, ls,
alpha0, x0, tol, maxIter)
% DESCENTLINESEARCH Wrapper function executing descent with line
% [xMin, fMin, nIter, info] = descentLineSearch(F, descent, ls,
alpha0, x0, tol, maxIter)
% INPUTS
% F: structure with fields
% - f: function handler
   - df: gradient handler
   - f2f: Hessian handler
% descent: specifies descent direction {'steepese', 'newton'}
% ls: function handle for computing the step length
% alpha0: initial step length
% rho: in (0,1) backtraking step length reduction factor
% c1: constant in sufficient decrease condition f(x_k + alpha_k*p_k) >
f k + c1*alpha k*(df k')*p k
     Typically chosen small, (default 1e-4).
% x0: initial iterate
```

```
% tol: stopping condition on minimal allowed step
      norm(x k - x k 1)/norm(x k) < tol;
% maxIter: maximum number of iterations
% OUTPUTS
% xMin, fMin: minimum and value of f at the minimum
% nIter: number of iterations
% info: structure with information about the iteration
  - xs: iterate history
   - alphas: step lengths history
% Copyright (C) 2017 Marta M. Betcke, Kiko Rullan
% Parameters
% Stopping condition {'step', 'grad'}
stopType = 'grad';
% Initialization
nIter = 0;
x k = x0;
info.xs = x0;
sing alphas in alpha Project Exam Help
% Loop un
                                                ations
while (~s
         https://eduassistpro.github.io/
   nIter = nIter + 1;
   * CompAeddeWeChat edu_assist_pro
   switch lower (descent)
      case 'steepest'
       p_k = -F.df(x_k); % steepest descent direction
     case 'newton'
       p_k = -F.d2f(x_k)\F.df(x_k); % Newton direction
    end
    % Call line search given by handle ls for computing step length
   alpha_k = ls(x_k, p_k, alpha0);
    % Update x k and f k
   x_k_1 = x_k;
   x_k = x_k + alpha_k*p_k;
   % Store iteration info
   info.xs = [info.xs x k];
    info.alphas = [info.alphas alpha k];
   switch stopType
     case 'step'
       % Compute relative step length
       normStep = norm(x_k - x_k_1)/norm(x_k_1);
       stopCond = (normStep < tol);</pre>
```

backtracking.m

Backtracking line search

```
function [alpha, info] = backtracking(F, x_k, p, alpha0, opts)
% BACKTRACKING Backtracking line search to satisfy sufficient decrease
Assignment Project Exam Help
% INPUTS
         https://eduassistpro.github.io/
    - df:
% x_k: current iterate
% p: descent direction.
% alpha0: Aidd swegthat edu_assist_pro % opts: backtracking specific optio
% - rho: in (0,1) backtraking step length reduction factor
% - c1: constant in sufficient decrease condition f(x_k + alpha_k*p)
> f(x k) + c1*alpha k*(df k'*p)
         Typically chosen small, (default 1e-4).
응
% OUTPUTS
% alpha: step length
% nIter: number of iterations
% info: structure with information about the backtracking iteration
  - alphas: step lengths history
% Copyright (C) 2017 Marta M. Betcke, Kiko Rullan
% Default values
if nargin < 5 | ~isfield(opts, 'c1')</pre>
 opts.c1 = 1e-4;
end
% Choose
% rho = 0.1 for steepest descent, conjugate gradients
% rho = 0.9 for Newton, Quasi-Newton
if nargin < 5 || ~isfield(opts, 'rho')</pre>
```

```
opts.rho = 0.9; % Newton
end
if nargin < 4</pre>
 alpha0 = 1; % Newton
end
% Initialize info structure
info.alphas = alpha0;
info.rho = opts.rho;
info.cl = opts.cl;
% Initial step length
alpha = alpha0;
% Compute f, grad f at x k
f_k = F.f(x_k);
df k = F.df(x k);
% Backtracking linesearch for computing step length
while F.f(x_k + alpha*p) > f_k + opts.c1*alpha*(df_k')*p
  alpha = opts.rho*alpha;
Arssignment Project Exam Help
```

lineSearchhttps://eduassistpro.github.io/

Line search algorithm find steps satisfying strong W

cedal Algorithm 3.5)

```
function [alpha_s, info] = lineSear
% LINESEARCH Line Search algorithm satisfying strong Wolfe conditions
% alpha_s = lineSearch(F, x_k, p_k, alpha_max, opts)
% INPUTS
% F: structure with fields
% - f: function handler
   - df: gradient handler
% x_k: current iterate
% p k: descent direction
% alpha max: maximum step length
% opts: line search specific option structure with fields
% - c1: constant in sufficient decrease condition
         f(x_k + alpha_k*p_k) > f(x_k) + c1*alpha_k*(df_k'*p_k)
         Typically chosen small, (default 1e-4)
   - c2: constant in strong curvature condition
         |df(x_k + alpha_k*p_k)'*p_k| <= c2*|df(x_k)'*p_k|
% OUTPUT
% alpha_s: step length
% info: structure containing alpha j history
% Reference: Algorithm 3.5 from Nocedal, Numerical Optimization
```

```
응
% It generates a monotonically increasing sequence of step lenghts
alpha j.
% Uses the fact that interval (alpha j 1, alpha j) contains step
lengths satisfying strong Wolfe conditions
% if one of the conditions below is satisfied:
% (C1) alpha_j violates the sufficient decrease condition
% (C2) phi(alpha j) >= phi(alpha j 1)
% (C3) dphi(alpha j) >= 0
% Copyright (C) 2017 Kiko Rullan, Marta M. Betcke
% Paramters
% Multiple of alpha j used to generate alpha {j+1}
% Calculate handle to function phi(alpha) = f(x k + alpha*p k)
% Phi: function structure with fields
% - phi: function handler
% - dphi: derivative handler
Phi.phi = @(alpha) F.f(x_k + alpha*p_k);
Assignment Project Exam Help
% Initialization
alpha(1)
phi i(1)
dphi_i(1) https://eduassistpro.github.io/
alpha(2)
alpha_s = 0;
n = 2;
maxIter = A:dd WeChat edu_assist_pro
while (n < maxIter && stop == false)</pre>
   phi i(n) = Phi.phi(alpha(n));
   dphi_i(n) = Phi.dphi(alpha(n));
    if(phi i(n) > phi i(1) + opts.cl*alpha(n)*dphi i(1) | | (phi i(n))
 >= phi_i(n-1) && n > 2))
       alpha_s = zoomInt(Phi, alpha(n-1), alpha(n), opts.c1,
 opts.c2);
       stop = true;
    elseif(abs(dphi_i(n)) <= -opts.c2*dphi_i(1))</pre>
       alpha_s = alpha(n);
       stop = true;
    elseif(dphi_i(n) >= 0)
       alpha s = zoomInt(Phi, alpha(n), alpha(n-1), opts.c1,
 opts.c2);
       stop = true;
    end;
    alpha(n+1) = 0.5*(alpha(n)+alpha max);
    alpha(n+1) = max(FACT*alpha(n), alpha_max);
   n = n + 1;
end
```

```
info.alphas = alpha;
```

Zoom function used by the line search above (Wright, Nocedal Algorithm 3.6)

```
function [alpha, info] = zoomInt(Phi, alpha_1, alpha_h, c1, c2)
% ZOOMINT Zoom algorithm for line search with strong Wolfe conditions
% alpha = zoomInt(Phi, alpha l, alpha h, c1, c2)
% INPUTS
% Phi: structure for function of step length phi(alpha) = f(x_k + y_k)
alpha*p k) with fields
% - phi: function handler
% - dphi: derivative handler
% alpha_1: lower boundary of the trial interval
% alpha_h: upper boundary of the trial interval
% c1 & c2: constants for Wolfe conditions (see lineSearch.m)
% OUTPUT
% alpha: step length
* Assignment Project Exam Help  
* Reference: Algorithm 3.5 from Nocedal, Numerical Optimization
응
% Propert
* (P1) In https://eduassistpro.github:io//g
strong W
% (P2) Among the step lengths gener
 sufficient decrease condition
alpace two ewith at ledu (P3) alpha h is chose such that d
 0
응
% Copyright (C) 2017 Kiko Rullan, Marta M. Betcke
% Parameters
% Trial step in {'bisection', 'interp2'}
TRIALSTEP = 'bisection';
tol = eps;
% Structure containing information about the iteration
info.alpha ls = [];
info.alpha_hs = [];
info.alpha_js = [];
info.phi js = [];
info.dphi_js = [];
n = 1;
stop = false;
maxIter = 100;
while (n < maxIter && stop == false)</pre>
    % Find trial step length alpha_j in [alpha_l, aplha_h]
    switch TRIALSTEP
```

```
case 'bisection'
       alpha j = 0.5*(alpha h + alpha l);
     case 'interp2'
    end
   phi_j = Phi.phi(alpha_j);
    % Update info
   info.alpha ls = [info.alpha ls alpha l];
    info.alpha_hs = [info.alpha_hs alpha_h];
    info.alpha_js = [info.alpha_js alpha_j];
    info.phi_js = [info.phi_js phi_j];
   if abs(alpha h - alpha l) < tol</pre>
     alpha = alpha_j;
     stop = true;
     warning('Line search stopped because the interval became to
 small. Return centre of the interval.')
    end
    if (phi_j > Phi.phi(0) + c1*alpha_j*Phi.dphi(0) ||
Phi.phi(alpha_j) >= Phi.phi(alpha_l))
    * alpha j does not Project Exam Help

* or phi(alpha_j) >= phi(alpha_l)
     % -
         https://eduassistpro.github.io/
      info.dphi_js = [info.dphi_js
                   WeChat edu_assist_pro
       dphi_j = Phi.dphi(alpha_j);
        % Update info
       info.dphi_js = [info.dphi_js dphi_j];
       if (abs(dphi_j) <= -c2*Phi.dphi(0))</pre>
          % alpha_j satisfies strong curvature condition
           alpha = alpha_j;
           stop = true;
       elseif (dphi_j*(alpha_h - alpha_l) >= 0)
         % alpha_h : dphi(alpha_l)*(alpha_h - alpha_l) < 0</pre>
         % alpha_j violates this condition but swapping alpha_l <->
 alpha_h will reestablish it
         % -> [alpha j, alpha l]
           alpha_h = alpha_l;
       alpha_l = alpha_j;
    end
end
```

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