

Assignment Project Exam Help
Data Abstractions

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Abelson & Sussman & S... ctions: 2.1
& (first part)2.2

Preview

- In the next few lectures we will examine various aspects of data abstraction including
 - Motivation for using/supporting data abstractions.
 - The use of abstraction barriers to represent different parts of a program.
 - How compound data is represented
 - How programs combine local and global procedures pasted together using compound data as an interface.
 - How symbolic data is represented
 - How generic procedures can be constructed in Scheme
 - The relationships between different types of abstraction.

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Data abstraction

- We are all familiar with the concept of data abstraction.
 - Concealing aspects of a data representation to make it more abstract.
- We are all familiar with the motivations for data abstraction
 - Making data simpler from the users' point of view.
 - Better matching abstractions to the needs of the users.
 - Allowing the underlying representation without affecting users programs.
 - Admitting the possibility of generic procedures, able to treat different abstractions with similar behaviour in the same way, at some level.
- Data abstraction is a tool for the programmer
 - reduces problems associated with making large or growing systems.

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Data Abstraction in Scheme

- Scheme provides no explicit mechanism for data-hiding
 - This is both a weakness and a strength
- It is a weakness because most abstractions can be broken by the programmer.
 - programmers need to know what they are doing
- From an expository length
 - There is no mandatory length
different ways of providing data abstractions
- In this part of the course we will use edu_assist_pro as a vehicle to explore
 - different ways data can be represented.
 - different ways of abstracting over data and
 - different ways abstractions interact.

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Data Abstraction example: rational numbers

- Rational numbers are numbers expressible using fractions:
 - e.g. $1/2$, $3/18$, $384/17$ and so on.
- We want to be able to treat rational numbers like ordinary numbers
 - we want to add, subtract, multiply, divide and test for equality.
- To do this we need ways of putting together and pulling apart
 - `make-rat` - to make a rational out of two integers.
 - `numer` - to return the numerator of a rational number.
 - `denom` - to return the denominator of a rational number.
- For now we will imagine that we have these operations and implement `add`, `subtract`, etc. in terms of them.
 - pretending operations exist is an important aspect of abstraction.

Rational numbers (2.1.1)

```
(define (add-rat x y)
  (make-rat (+ (* (numer x) (denom y))
                (* (numer y) (denom x)))
            (* (denom x) (denom y))))

(define (sub-rat x y)
  (make-rat (- (* (numer x) (denom y))
                (* (numer y) (denom x)))
            (* (denom x) (denom y))))
```

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- And so on for `mult-rat` and `div`
- Now, we need to create definitions for the auxiliary procedures
 - `numer`, `denom`, and `make-rat`

Representing Rational Numbers

- Rational numbers have two components
 - a numerator and denominator
- A mechanism is needed to glue these together
 - we use the Scheme primitives `cons`, `car` and `cdr`.

- `cons` glues together

`(cons 1 2)`

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- `car` accesses the first thing in a `cons`

`(car (cons 1 2)) => 1`

- `cdr` accesses the second thing in a `cons`

`(cdr (cons 1 2)) => 2`

Representing Rational numbers -cont'd

- Now we can define our representation in terms of `cons`, `car` and `cdr`:

```
(define (make-rat n d) (cons n d))
```

```
(define (numer x) (car x))
```

```
(define (denom x) (cdr x))
```

- We might want to print it in a pretty way:
 - the standard way is a bit ugly,

```
(define (print-rat x)
  (newline)
  (display (numer x))
  (display "/")
  (display (denom x)))
```

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Using rational numbers

```
(define one-third (make-rat 1 3))  
(print-rat (add-rat one-third one-third))  
=> 6/9
```

- This answer is un-normalised - we can fix this by modifying `make-rat`:

```
(define (make-rat  
  (let ((g https://eduassistpro.github.io/  
        (cons (/ n g) (/
```

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- Now...

```
(define one-third (make-rat 1 3))  
(print-rat (add-rat one-third one-third))  
=> 2/3
```

- That's better

Abstraction Barriers (2.1.2)

- Notice how we defined our `add-rat`, `sub-rat`, etc. procedures before we knew exactly how the underlying data was represented.
 - we made use of an abstraction barrier.
- There are several abstraction barriers in the rational number system...

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Abstraction Barriers

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- Note that we can change the representation at any level and, as long as the interface is the same, our program still works.

Back to data representations (2.1.3)

- We used the primitive functions `cons`, `car` and `cdr` to hold and access the numerator and denominator of the rational numbers.
 - Is there a level below these primitive functions?
 - Is there something more primitive than these primitives?
- It turns out that `c` represented in terms of other thi

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Representing cons, car, cdr

```
(define (cons x y)
  (lambda (m)
    (cond ((= m 0) x)
          ((= m 1) y)
          (else
           (error "Argument not 0 or 1 -- CONS" m)))))
```

```
(define (car z) (z 0))
```

```
(define (cdr z) (z
```

- Our new representation is interchangeable from the old:

```
(car (cdr (cons 1 (cons 3 2))))  
(cdr (cdr (cons 1 (cons 3 2)))) => 2
```

- Data can be represented purely as functions (as above)
 - The actual representation isn't important as long as the behaviour is what we expect.

Hierarchical data and lists 2.2

- Almost all compound data in Scheme programs uses pairs, formed from `cons`, in its underlying representation.
- Pairs can be used to form arbitrarily complex data structures.

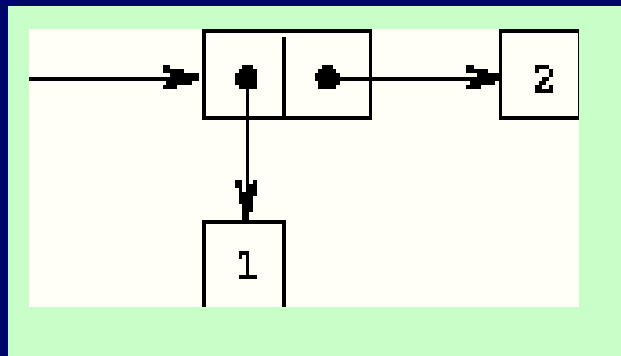
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- lists, trees and graphs can all be represented using pairs
- graphs are covered

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- Representing a single pair: `(cons 1 2)`



Other representations: trees

- Representing tree-like data

```
(cons (cons 1 2) (cons 3 4)):
```

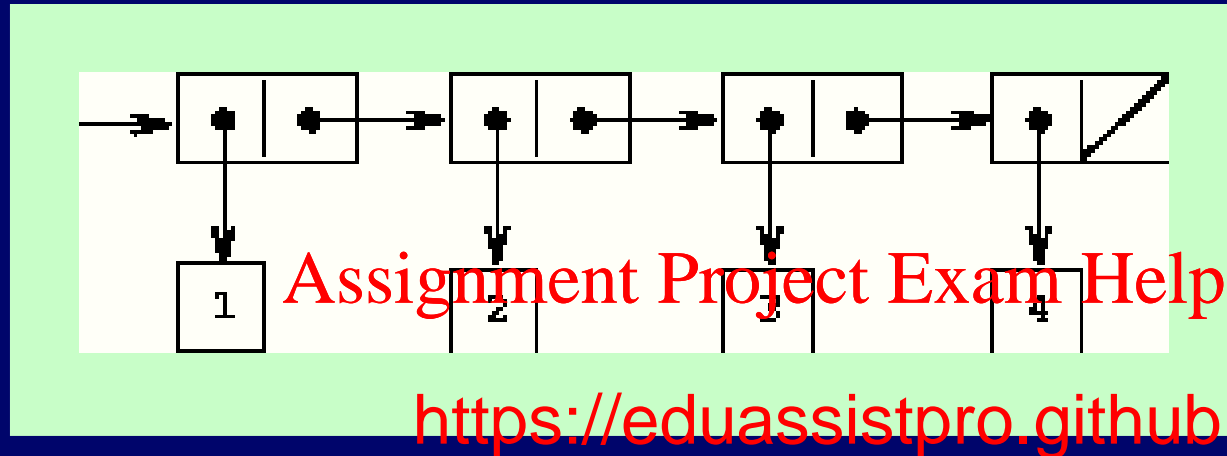
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Other representations: Lists

- Cons-lists: `(cons (1 (cons 2 (cons 3 (cons 4 ())))))`



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- `()` (nil) is a special value used to represent the end of a list.
- Lists are a very frequently used data structure in Scheme.
- There is even a special primitive used to construct lists, like the one above called `list`, e.g.

`(list 1 2 3 4)`

Other List operations

- `null?` - primitive procedure to determine if a list is `()`

`(null? (list 1 2)) => ()`

- `length` - primitive procedure returning the length of a list

`(length (list 1 2 3)) => 3`

- `append` - primitive

`(append (list 1 2 3) (list 4 5 6)) => (1 2 3 4 5 6)`

- `list-ref` - primitive procedure taking a list and an index

`(list-ref (list 1 2 3) 2) => 3`

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More list operations

- `map` - primitive to apply an operation to every element of a list.

```
(map sqr (list 1 2 3)) => (1 4 9)
```

- `filter` - a programmer-defined procedure to filter a list

```
(filter less-t (list 1 2 2)) => (1 2 2)
```

The definition is in the <https://eduassistpro.github.io/> repository. You can find your own version.

- `reduce` - a primitive to insert a binary operation between list elements

```
(reduce + 0 (list 1 2 3)) => 6
```

Review, Preview and Questions

- In this lecture we covered

- data abstractions in Scheme
- abstraction barriers
- cons, alternate representations for cons
- some basic procedures on cons-lists
- hierarchical data

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- *Exercises 2.3, 2.6, 2.17, 2.18, 2.20, 2.26*