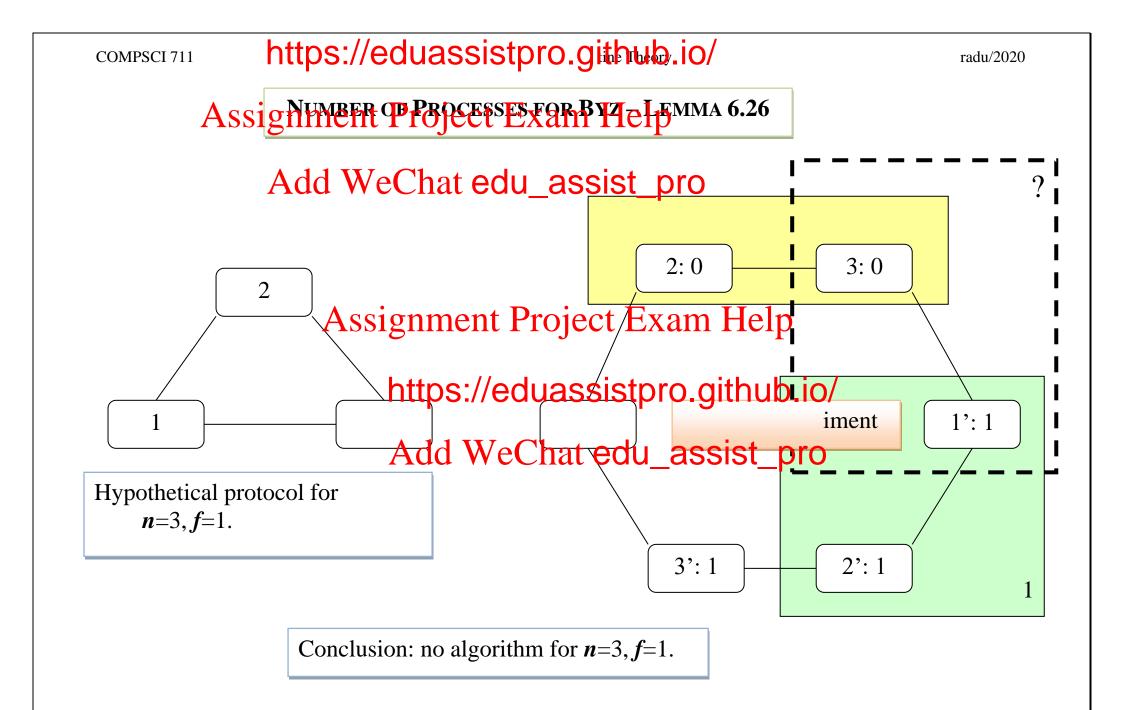
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BYZANTINE AGREEMENT PASTEW THE ORETI CALLETS ULTS.

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THEOREM 6.27 Project Exam Helpfor $3 \le n \le 3f$ No solution for $2 \le n \le 3f$ Project Exam Helpfor $3 \le n \le 3f$ $0 \le 3$ "subnets" with at most f processes in each

o contradiction (with lemma 6.26)

Add WeChat edu_assisterpison algorithm that can solve the or such an n, and we construct an algorithm that can solve the problem for 3 processes,

n=2

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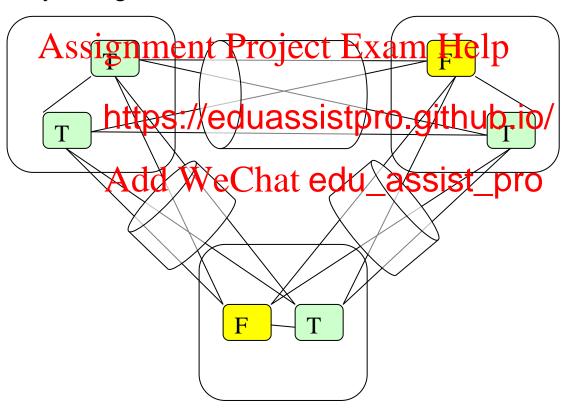
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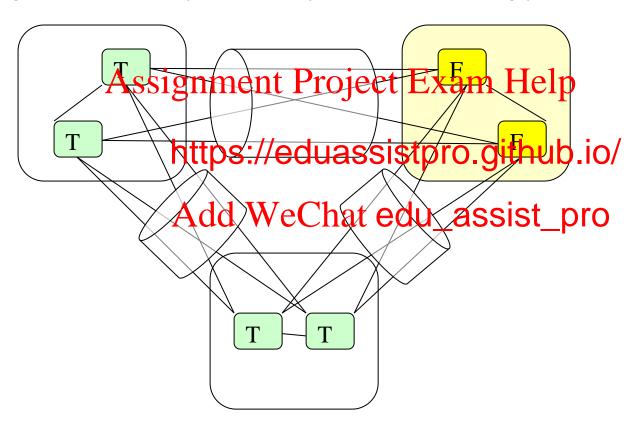
F

Assignment Project Exam Help Proof by contradiction

- We assume that the ny small property problem, if at most f are faulty regardless how these f faulty node
- o These "small" processes are totally unaware that they are now clustered into 3 "large" nodes, connected by 3 "large" channels



- o Replacing an arbitrary one "large e" Byzantine node is tantamount to replacing its content by the shift edu_assist fully nodes (w/ their channels)
- o Not doing this will be easily detected, by the others, as wrongly formatted messages



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AN EIG TREE WITH N=4 (# OF PROCESSES) AND L=2 (LEVELS)

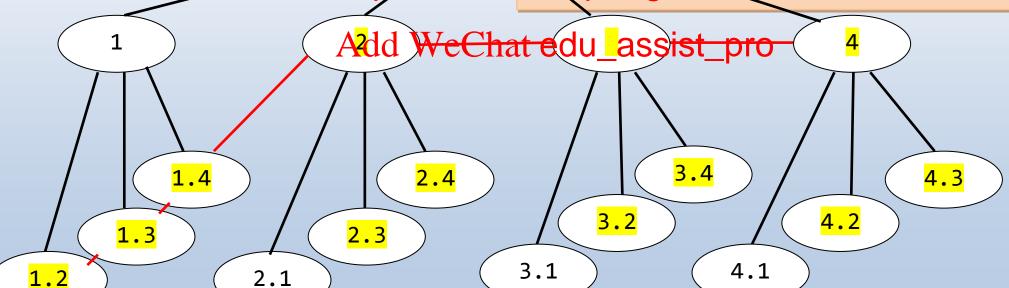
• Assignment Project Exam Help
• Level #1: 1 group with N=4 siblings

- onsider that process #1 is "faulty" o Level #2 : 4 groups xith N-Werth edu_assist_par €2, #3, #4 are "non-faulty"
 - Level #L : each group has N-L+1 si
- o For Byz agreement, L=F+1, here F=1, L=2
- o Observe the node labelling scheme

- o Observe the distribution of labels ending in one of 2, 3, 4
 - o a majority at leaves, if L≤F+1
- o The nodes will be filled le systement Project Examt Hady each path, if L≥F+1
 - o First, top-down, by L mess

erefore at least 1 "cut" across

o Then, bottom-up, after the https://eduassistpro.gitaubiliq/ay a role in the proof



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Tree nodes with labels ending in the number of a non-faulty process play a critical role!

o Examples (prav. slide): 22 edu_assist_pro

The number of levels, L, is a well-chosen critical number!

- If L ≥ F+1, then each root-to-leaves branch contains at least one such tree node
 Except λ, there are Fe htree node labels cannot contain duplicates)
- o If L≤F+1, then each sib https://eduassistpro.githubai@/ct majority of such tree nodes

The smallest sibling group (at the leaves 1 edu_assist_pro 1 tree nodes, thus

 $N-L+1 = N-(F+1)+1 = N-F \ge 3F+1-F = 2F+1$ tree nodes at least, out of which at most F can end in numbers of faulty processes

 \circ The algorithm chooses L = F+1!

CONSIDER (PHOSPECON VEHICANA) COMPANDON DECISION IS TAKEN)

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A tree node with label x is $\frac{common}{}$ if it has the same $\frac{newval}{}$ () across all non-faulty processes, i.e.,

 $\frac{\mathbf{newval}(x)_i = \mathbf{newval}(x)_j}{\mathbf{Assignment Project Exam Help}}$

Note: $val(x)_i$ and $val(x)_i$ m

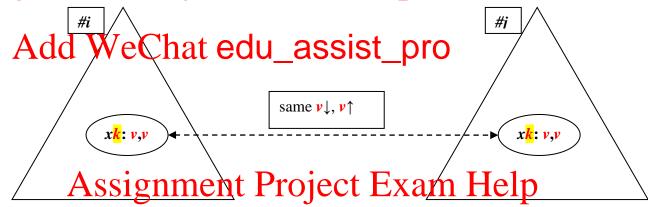
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- A set of tree nodes which contains at least tracedu_assistooptroleaves) path is called a path covering.
- o The red "cut" across the previous sample EIG tree is a *path covering*.
- A **common path covering** is a **path covering** where all tree nodes are **common**.
- As we will see, the red "cut" across the previous sample EIG tree is also a *common path covering*.

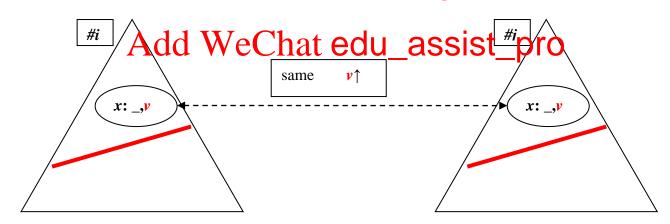
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- All nodes above a common, because all their children are common although these may have different newval()'s.
- Thus the $\frac{root}{\lambda}$ is also $\frac{common}{\lambda}$.

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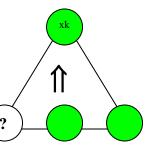


o all nodes and common hat edu_assist_pro

All xk nodes are common because they have a strict majority of xkl xkl'
... common children sharing the same val() and newval()

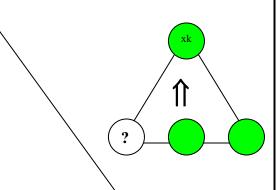
xk common path covering

- o *xk* ... **common** nodes
- o other common nodes
- o non-common nodes



xk common path covering

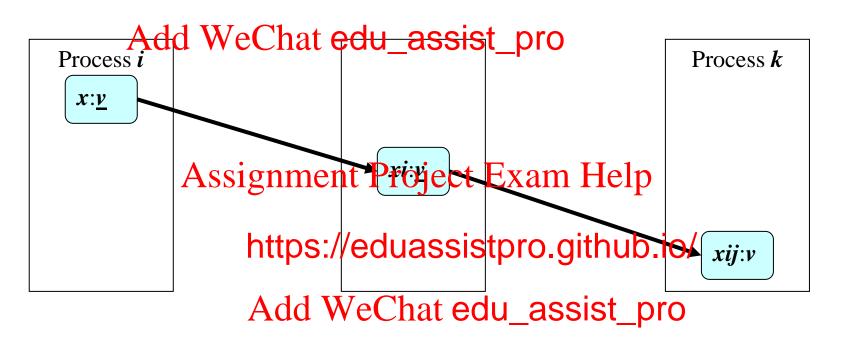
λ



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Assignment Messaging in the Figure Total (recall)



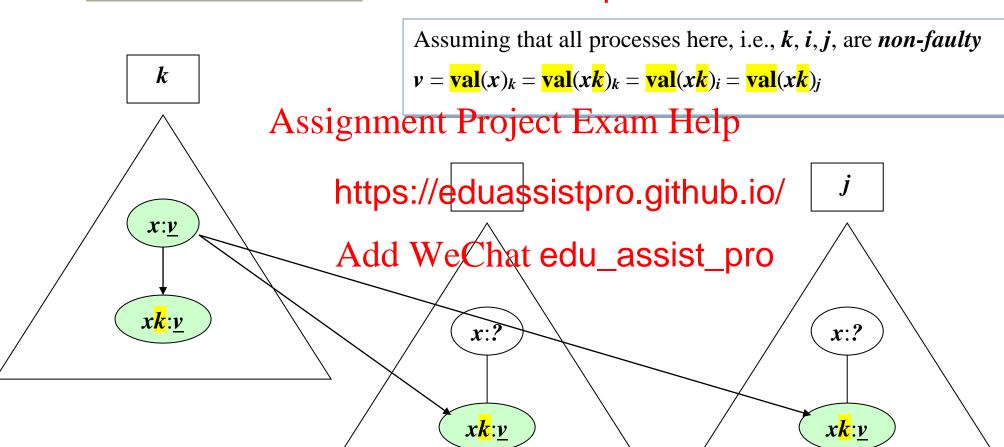
assume that x does not contain i, j

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LEMMA de WeChat edu_assist_pro



All nodes with labels Active What edu_assist a process, have the same val() and newval() across all non-faulty proce

 $\frac{\mathbf{newval}(\mathbf{x}_{k}^{\mathbf{k}})_{i} = \mathbf{val}(\mathbf{x}_{k}^{\mathbf{k}})_{i} = \mathbf{val}(\mathbf{x}_{k}^{\mathbf{k}})_{j} = \mathbf{newval}(\mathbf{x}_{k}^{\mathbf{k}})_{j} \text{ for all } i, j \text{ that are } \mathbf{non-faulty} \text{ processes}$

As a corollary, all such no essergument Project Exam Help

In fact, they are "more than

are also equal, to the same value

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The proof follows on next slides

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As we will further see:

- \circ The condition of lemma 6.16 is **not** necessary, i.e., there could also be other **common** nodes with labels of the form xk', where k' is a faulty process.
- \circ All first level nodes are common! This result ensures a common decision at the root λ .

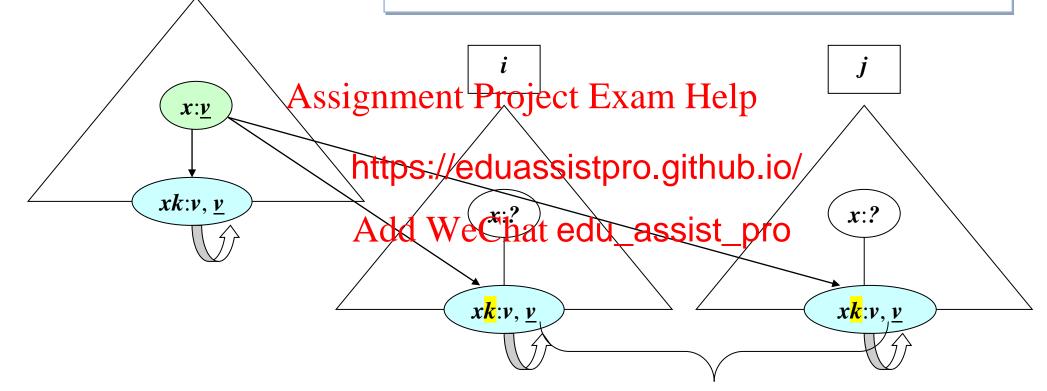
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LEMMA 6.16 FOR LEAVES OF Assuming that all processes here, i.e., k, i, j, are non-faulty of the second substituting $v = val(x)_k = val(xk)_k = val(xk)_i = val(xk)_j = val(xk)_i =$

Add WeChat edu_assist_prod($x_k^{\mathbf{k}}$)_i = $\frac{\mathbf{newval}(x_k^{\mathbf{k}})_i}{\mathbf{newval}(x_k^{\mathbf{k}})_i}$

n for leaves: **newval**() = **val**()



Add WeChatedu_assist_pro_height of node $x_k^{\mathbf{k}}$, and the def of newval()

for nodes when there is a *majority* voting for the same v

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 $xk:v, \underline{v}$

x:v

 $xkl:v, \underline{v}$

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dd WeChat edu assist pro *x*:?

 \circ A majority of the children of xkhave the form xkl where l is a number of a *non-faulty* process: same $val(xkl) = val(xk) = val(x)_k$.

 The induction hypothesis holds for these nodes (less height):

same newval(xkl)

 $xk:v, \underline{v}$

 $x^{\underline{k}}:v,\underline{v}$

xkl:v, \underline{v}

 $x^{\underline{k}}:v,\underline{v}$

x:?

 $xklv, \underline{v}$

 $xkl:v, \underline{v}$

Add WeChat edu_assist_prop path covering the whole EIG tree!

• How to build such a common path covering?

Top down on each branch, until we find a tree node Project ends with the later of a non-faulty process

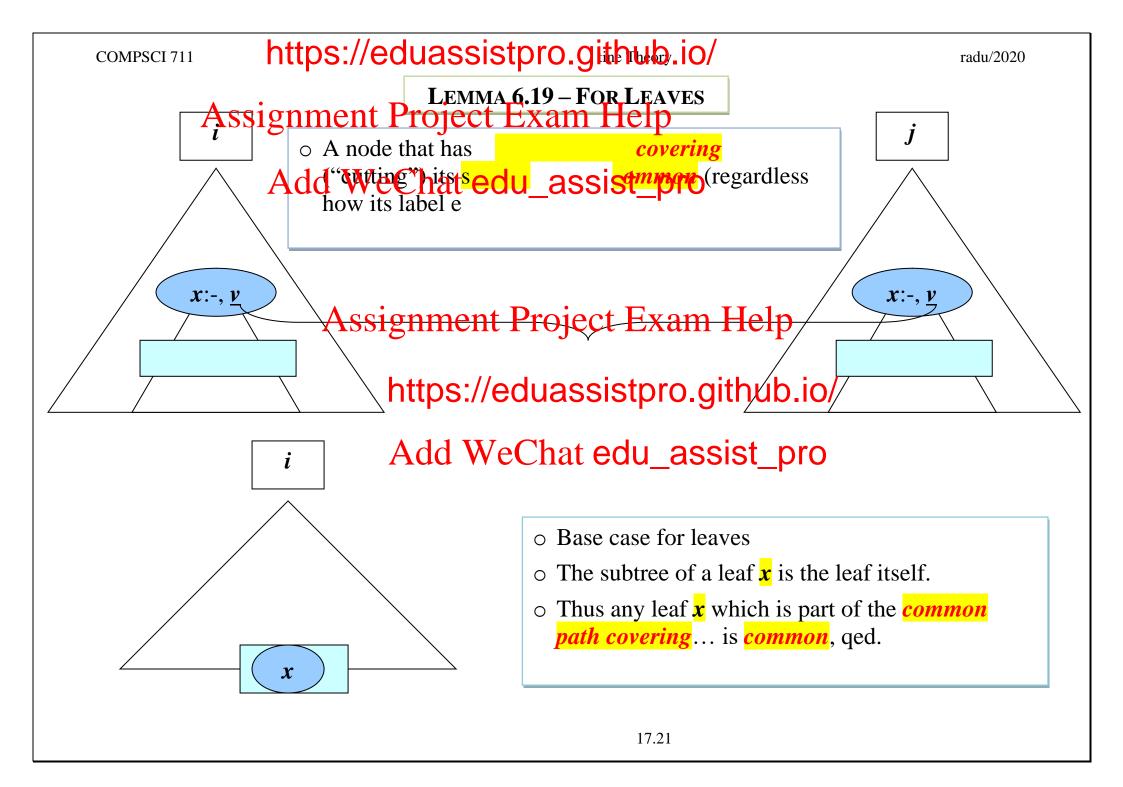
t end with k, where k is a **non-**

https://eduassistpro.githubertos/such a label on each

 x^{k}

Add We Chatwedu_assistucpfice nodes have common

• Thus, this is *common path covering* of the EIG tree!



Assignment Preyed 19x For Non-beaves

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i

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xl

If x is itself part of the common path covering, then, well, it is common, qed.

X

- Otherwise, all its children such as xl (no matter if l is or not faulty) will be common by induction (height-1)
- \circ And then x will be **common** by the definition of **newval**()

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Assignment Project Exam Helpaulty processes

o All nodes above a common path covering the tree are also *common*, including the root λ .

o Thus, they have the same **newval**() across all non-

o Agreement!

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- We almost proved that the EIG algorithm solves the Byz agreement problem.
- We have now the **agreement**
- What is still missing?

o Termination Aick that what edu_assist a per F+1 messaging rounds

o What else? Assignment Project Exam Help

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LEMMA 6.17 Add Validation at edu_assist_pro

Assume that all esses start with the same initial value v

```
Proof - using Lemma 6.16

newval(xk)_i = val(xk)_i = val(xk)_j = newval(xk)_j, for all non-faulty k, i, j

In particular

newval(k)_i = val(k)_i

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on-faulty k, i, j

Thus, all first level nodes carrespowding to non-edu_assist share the same newval(k)_i = val(k)_i

And they form a strict majority, so the root deci

validity!
```

THEOREM 6.21

The EIG algorithm solves the Byz agreement problem!