### Assignment Project Exam Help

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- Minimum spanning trees
- 2 Prim MST

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- Sync MST Level 1 Components edu\_assist\_pr
- Sync MST Level 2 Components
- Memento

#### Spanning trees (ST)

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- (1): min-height ST
  here also BFS ST (cf. sync Echo)
   (2): shortest paths ST (cf. sync Async Bellm assist property of the sync async Bellm as a sync async Bellm assist property of the sync async Bellm as a sync async Bellm async Bellm as a sync async Bellm as a sync async B
  - (3): minimum ST (cf. sync/async GHS) here also DFS ST (cf. sync/async Cidon)
  - (1,2,3,...) : arbitrary ST (cf. async Echo)

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#### Minimum spanning tree (MST) algorithms

• If edges have different weights, then there is a unique MST

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- faster algorithms almost linear: Chazelle randonication witeer weights: ... ecu\_assist\_pr
- Distributed MST (sync,async): GHS Gallager, Humblet and Spira (1983):  $O(N \log N)$ ; improvements linear O(N); or even sub-linear

<sup>&</sup>lt;sup>1</sup> "Because Sollin was the only computer scientist in this list living in an English speaking country, this algorithm is frequently called Sollin's algorithm" (Wiki)

Side-bar: Minimum spanning networks in biology

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Borůvka – red: Common MWOE (min-weight out edge)

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Borůvka – red: Common MWOE (min-weight out edge)

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Borůvka – red: Common MWOE (min-weight out edge)

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#### Prim and Kruskal as particular cases of Boruvka

Kruskal is a restricted Boruvka, where we only use the overall ASS i layest cost MWGE (Dathesessarily configor) of thus at all yell per step, we only merge 2 trees (one single 2-way merge)

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- Boruvka deals with all MWOEs at the same "
  "Avel" in the distributed has a the same "
  munti-way merges simultaneously the day as a same as a sam
- Quotation marks indicate that many things may happen at the same "step" or "level" ...
- The distributed MST versions exploit this ability of Boruvka

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#### All unrooted trees (edge shapes) with 4 & 5 nodes

Looking for MWEs (minimal working examples) where Kruskal

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- Here the selected roots have minimum eccentricities
- WLG (without loss of generality), are these all that need consideration?

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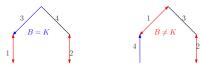
#### Five nodes – Kruskal essentially different from Boruvka?

• B step 1: collects all red (Common MWOE) and blue (one

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#### Four nodes

## Assignment Project Exam Help on 4 nodes, Kruskal is NOT essentially different from Boruvka

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#### Further discussions

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- In any multi-way merge there is always one Common MWOE
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  - · Add We Chatsed assist\_pr
  - Level k trees, for any  $k \ge 0$

#### Distributed MST (Sync)

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  - could be obtained by a preliminary phase
- Factore Weekstate eassist\_produced
  - e..g, by lexicographical comparisons, where each edge  $\{i,j\}$  is represented by an ordered triple (w,v,v'),v< v', where w= edge weight, v,v'= ID's of i,j

#### Sync MST - Comparing weights with equal weights

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$$\{1,2\} = (10,1,2) < \{1,3\} = (10,1,3) < \{4,3\} = (10,3,4)$$

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#### Distributed MST (Sync)

• Time complexity:  $O(N \log N)$ 

## Assignment Project Exam Help evels: O(log N); each level defines a spanning forest

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- Each component has a distinguished lead identifies the component
- For connected graphs, the algorithm ends with a MST (unique, if edges have different weights)

#### Distributed MST (Sync)

• Details may vary, with slightly different performance...

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report

## Add We Charled edu\_assist\_pre-root to ensure correct component identificat

- To ensure correct component identificat 1 takes a predefined number of steps, O(N) nodes may need to stay idle until this count is completed
  - depending on the actual algorithm details, this may happen in different ways

#### Sync MST - Level 0 Components

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#### Sync MST - Level 0 Components

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connect!

#### Sync MST - Level 1 Components

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#### Sync MST - Level 1 Components

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initiate

#### Sync MST - Level 1 Components

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#### Sync MST - Level 2 Components

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#### Sync MST - Level 2 Components

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#### Sync MST - Memento

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- At each given step: Kruskal merges exactly t

  merges of tree-virguland (2000 assist\_pr
- The steps of sequential Borůvka correspond to more complex levels (phases) in distributed Sync MST

#### Sync MST - Memento

- The MST is unique, if weights are pairwise distinct (but this Assignative arrange to be be be be be being the comparison of the position of the core, in all tree

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- the core, i.e. of the single common MWOE (t that the chot was seed that edule assist\_pr
- A level k union tree has size  $> 2^k$ exponentially and there are at most  $\log N$  phases
- To ensure required synchronicity, each level requires O(N) steps (this is ok, as there are only few levels)

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#### Sync MST - Memento

The accept and reject messages are not really needed; i.e. the Assignmental harmonic birth for this decision Help

• The report messages are evaluated on-the fly, at each node,

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- the best MWOE of that subtree
- The chart Messechatte Gelle assist prom the leader to the node holding the overal
- The connect messages reshape the tree, by transporting the leadership, i.e. resetting parent and child pointers along their path

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#### Async MST – GHS and variants

Specific difficulties of the async version - not present in the sync version:

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they have not learned this yet (logical error)

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- More generally, component trees may be a (logical and complexity issues) Add We Chat edu\_assist\_prediction of the complexity issues) Read more in Lynch's textbook:
  - §4.4 : sync GHS
  - §15.5 : async GHS, plus summary revision of sync GHS
  - §15.3 : async STtoLeader (on unrooted STs)