

<p style="text-align: center;">COMPSCI 753: Algorithms for Massive Data Assignment 1: Locality-sensitive Hashing (Worth 5 Pts in Total) Due date: 23:59 14 August 2022</p>

Learning Objectives: The goal of this assignment is to investigate Locality-sensitive Hashing (LSH) framework for near neighbor search on real-world datasets. We have learned how to construct hash tables using multiple hash functions in LSH family for near neighbor retrieval in sublinear time during weeks 2-3. By accomplishing this assignment, you will be familiar with the following concepts:

- Hash Table Construction
- Hash Table Lookup
- Search Quality Evaluation

General Instruction:

This core component in this assignment is to construct a document retrieval system upon the LSH framework. This assignment consists of three parts. Please write a **python program** to complete the following components:

- Part I: Construct LSH Hash Tables for All News Articles
- Part II: Perform
- Part III: Invest

Datasets:

Let's consider two classes of BBC news articles: `bitvector_all.csv` and `bitvector_query.csv`. `bitvector_all.csv` is a tab-separated line with three columns: `<news_id\tword_features\tnews class>`, where `news_id` is a unique string ID, `word_features` is a sequence of tab-separated binary values. Each entry in the `word_features` refers to the occurrence of a token. You can find their original new articles in `text_all.csv` and `text_query.csv`, accordingly in `bbc.zip` on Canvas.

Submission:

Please submit a single **report** (.pdf) and the **source code with detailed comments** (.py or .ipynb or .html) on Canvas by **23:59, Sunday 14 August 2022**. The answer file must contain your studentID, UPI and name.

Penalty Dates:

The assignment will not be accepted after the last penalty date unless there are special circumstances (e.g., sickness with medical certificate, family/personal emergencies). Penalties will be calculated as follows as a percentage of the mark for the assignment.

- By 23:59, Sunday 14 August 2022 (No penalty)
- By 23:59, Monday 15 August 2022 (25% penalty)
- By 23:59, Tuesday 16 August 2022 (50% penalty)

Part I: Construct LSH Hash Tables for All News Articles [40 pts]

(a) Load `bitvector_all.csv` and `bitvector_query.csv`. Construct a feature vector for each news article in the dataset. Please report the number of articles, and the number of features (n) for these two sets of data. [5 pts]

(b) Construct a family of MinHash functions in the LSH family by taking a prime $p \geq n$ and for $0 < a < p$, $0 \leq b < p$ with the number of tables ($l=10$) and a tunable choice of hash size (k). Please report the family of MinHash functions you have generated with $l=10$ and $k=2$. [15 pts]

(c) Construct LSH hash tables using your hash functions with the number of tables ($l=10$) and bucket size of your choice (m). Please report the collision distribution of the l hash tables with all documents hashed into m buckets using heatmap plot, where x-axis is m , y-axis is $l=10$, and the values at (m, l) refers to the number of colliding articles). [20 pts]

Part II: Nearest Neighbor Search [35 pts]

(a) Query the LSH tables and return the top-10 articles that have the highest Jaccard similarities as the answer. For each query document \mathbf{q} in our queries dataset Q , firstly, find the set of articles D_q that collide with \mathbf{q} in at least one hash table. Compute Jaccard similarity between \mathbf{q} and each article in D_q . Please report the list of top-10 articles with highest Jaccard similarity in descending order for each query \mathbf{q} (i.e., four lists in total). The article with the highest Jaccard similarity is ranked

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(b) Compute Jaccard similarity between \mathbf{q} and each article in D_q . Please report the list of top-10 articles with highest Jaccard similarity in descending order for each query \mathbf{q} (i.e., four lists in total). [10 pts]

(c) Compare the query time in Part II(a) and Part II(b). Please report the query times and comment on their differences if any. [5 pts]

Part III: Search Quality Evaluation [25 pts]

(a) Investigate the impact of the hash size (k). Given $l=10$, for each value of hash size k compute the F1-score for each query \mathbf{q} ($F1_q$) using the reported result from query \mathbf{q} in Part II(a) as search results and Part II(b) as ground-truth. Take the average of F1-score across all queries at k . Please report:

- the F1-score plot with a varying $k=[2,4,8]$. (Note: $F1 = \frac{1}{|Q|} \sum_{q \in Q} F1_q$,

$F1_q = \frac{TP}{TP + 1/2 (FP + FN)}$, where TP (FP/FN) refers to the number of true positives (false positives / false negatives) of the top- K similar articles in the ground-truth for the query \mathbf{q} (K is capped at 10)

- the average query time in milliseconds with a varying $k=[2,4,8]$. [20 pts]

(b) Explain what you have observed from Part III(a) and suggest how you would tune the number of hash size (k) in terms of higher F1-score and lesser query time, respectively? [5 pts]