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Regression III: Kernels

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Outline

- ► Dual form of ridge regression

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Linear algebraic identity

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$$x$$
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Linear algebraic identity: for any A $\mathbb{R}^{n \times d}$ and $b = \frac{1}{\sqrt{n}} \begin{bmatrix} y_1 \\ \vdots \\ R^n \times d \end{bmatrix}$ $Help$

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► Check: multiply both sides by

Alternative (dual) form for ridge regression (1)

► Implications for ridge regression

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- PAdiction with entire transfer assist_property $x^{\mathsf{T}}\hat{w} = \sum_{i=1}^{n} \hat{\alpha}_i \cdot x^{\mathsf{T}}x_i$

Alternative (dual) form for ridge regression (2)

▶ Therefore, can "represent" predictor via data points x_1, \ldots, x_n and $\hat{\alpha}$.

Assigning englest reproposation, except agoing the lp to get α : solve linear system involving K (and not A directly)

- lacktriangle To make prediction on x: iterate through the x_i to compute
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Quadratic expansion

► Suppose we want to do feature expansion to get all quadratic terms in $\varphi(x)$

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$$\varphi(x)^{\mathsf{T}}\varphi(x') = (1 + x^{\mathsf{T}}x')^2.$$

Similar trick for cubic expansion, quartic expansion, etc.

cross terms

Gaussian kernel

For any $\sigma > 0$, there is an infinite-dimensional feature

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ightharpoonup Feature expansion for d=1 and

$$\varphi(x) = e^{-x^2/2} \left(1, x, \frac{x^2}{\sqrt{2!}}, \frac{x^3}{\sqrt{3!}}, \dots \right).$$

Kernels

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A Hred H so special hind of inner product assist. pr

 \blacktriangleright Algorithmically, we don't have to worry about what φ is. Instead, just use k.

Kernel ridge regression (1)

- ▶ Training data $(x_1, y_1), \dots, (x_n, y_n) \in \mathcal{X} \times \mathbb{R}$
- Assignment, Project Exam Help $(\varphi(x_i)^{\mathsf{T}}w y_i)^2 + \lambda \|w\|_2^2$
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 - Lating = Wie winat edu_assist_pregression objective is equivalent to

$$\frac{1}{n}\|K\alpha - y\|_2^2 + \lambda \alpha^\mathsf{T} K\alpha$$

where $y = (y_1, \dots, y_n) \in \mathbb{R}^n$.

Kernel ridge regression (2)

Minimizer wrt α is solution $\hat{\alpha}$ to linear system of equations

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▶ Return predictor that is represented by $\hat{\alpha}$ \mathbb{R}^n and x_1, \ldots, x_n

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i=1

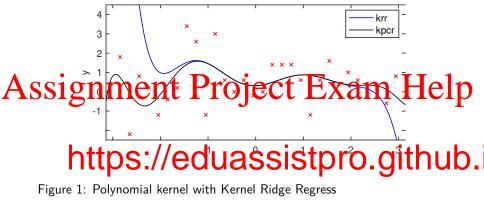
In Auction Pia We Chat edu_assist_property $|\hat{w}^{\mathsf{T}}\varphi(x) - \hat{w}^{\mathsf{T}}\varphi(x')| \leq ||\hat{w}|| = \sqrt{\hat{\alpha}^{\mathsf{T}}K\hat{\alpha}} \cdot ||\varphi(x) - \varphi(x')||_2$

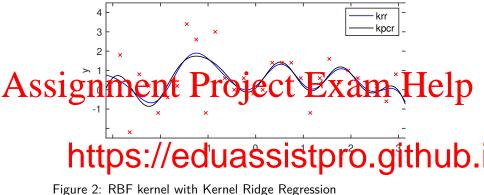
Kernel methods

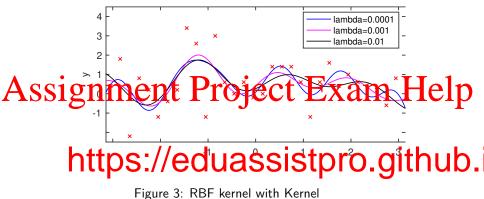
► Many methods / algorithms can be "kernelized" into kernel methods

Assignment teigher of every diex can Help spectral regularization" with kernels: solve $g(K/n)\alpha = y/n$

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New kernels from old kernels

- ightharpoonup Suppose k_1 and k_2 are positive definite kernel functions.
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Postscript

- ▶ Problem with kernel methods when n is large
- Assigning crediction of the property of the pr

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