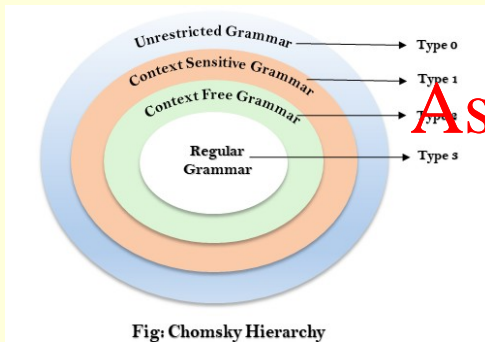


# COSC1107 Computing Theory

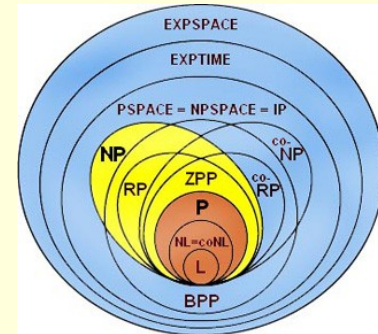
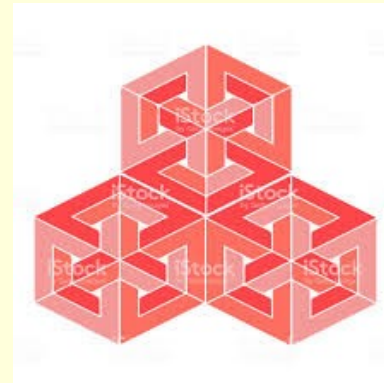
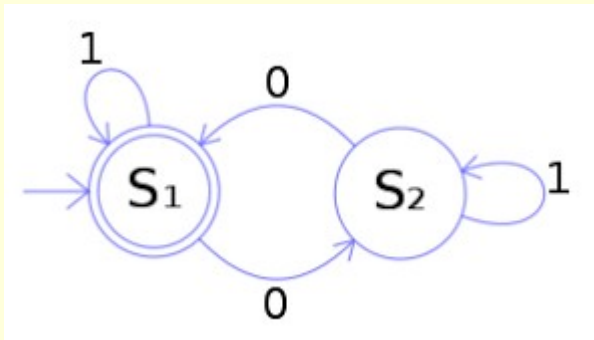
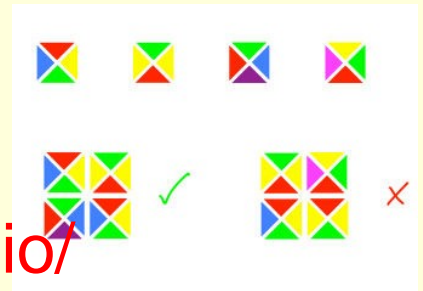
(We will commence soon. We are just allowing a few minutes for people to join and set up. *Please mute your microphone unless you are speaking.* You can raise your hand or use the chat at any time.)

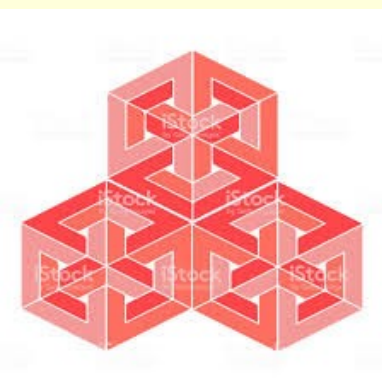
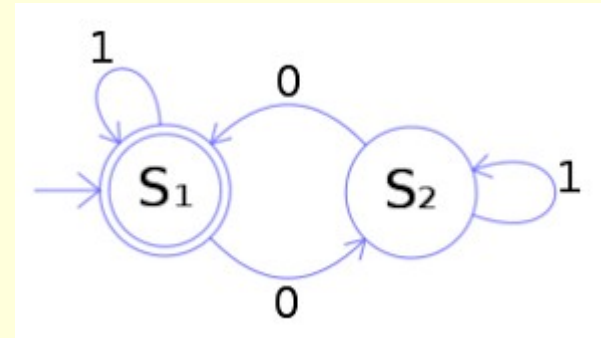
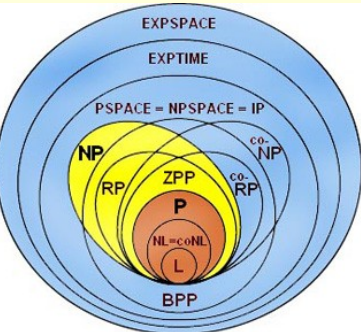


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# COSC1107

## Assignment Project Exam Help

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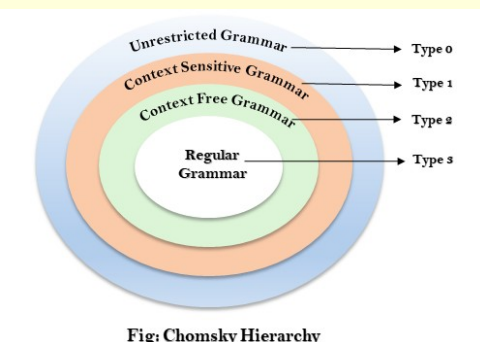
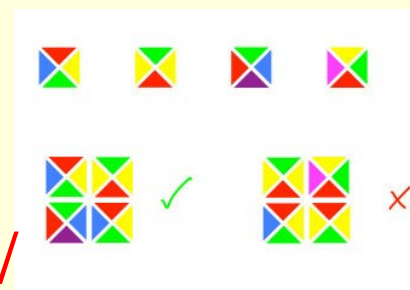


Fig: Chomsky Hierarchy

James Harland

[james.harland@rmit.edu.au](mailto:james.harland@rmit.edu.au)

\* With thanks to Sebastian Sardina

*Intro music 'Far Over' playing now ...*



Week 12

Computing Theory

# Acknowledgement



RMIT University acknowledges the people of the Woiwurrung and Boon wurrung language groups of the eastern Kulin Nations on whose unceded lands we conduct the business of RMIT University respectfully acknowledge Elders, past and present.

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RMIT also acknowledges the Traditional Custodians and their Ancestors of the lands and waters across Australia where we conduct our business.

(add your name [here](#) to volunteer for this or email me)

(my personal Acknowledgement of Country is [here](#))

# Acknowledgement



As we gather virtually, from all areas around South Central Victoria, we acknowledge the people of the Eastern and Western Kulin Nations.

## Assignment Project Exam Help

In this time when our Wilam (camp or meeting place) is dispersed across many separate groups, all feel a strong sense of Noogal (belonging) to our land, our people, our families, and our community. We are using alternative and accessible methods.

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We acknowledge that the lands we are conducting our business today remains unceded. We respectfully acknowledge the first nations people of the five Kulin Nations, their Ancestors and Elders, past, present and emerging. (thanks to Nick Balkin for this acknowledgement)

# Weekly Schedule



	Lectorial	Tutorial	Assessment
12	Research and requests	Sample exercise	Assignment 2
14-16	--	--	Final exercise

Assignment Project Exam Help

- ~~Quiz 10 deadline is 11:59pm Monday 11<sup>th</sup> October~~
- Assignment 2 de <https://eduassistpro.github.io/> esday 19<sup>th</sup> October
- Questions 4b, 4e of Assignmen Add WeChat edu\_assist\_pro submitted via a special quiz on Canvas (not as part of the PDF report)
- Other questions & csv files to be submitted as files
- Do not use zip files!



# Weekly Schedule



	Lectorial	Tutorial	Assessment
12	Research and requests	Sample exercise	Assignment 2
14-16	--	--	Final exercise

**Final exercise** Assignment Project Exam Help

- Released at 9.0
- Due by 9.00am on Friday 5th
- Time is Melbourne time (UTC)
- Expected time spent on the task is 4-6 hours
- Sample exercise will covered in tutorials in Week 12
- An additional practice exercise will be released soon

<https://eduassistpro.github.io/>

Add Chat at edu\_assist\_pro  
[re](#)

# Questions?

Questions?



## Assignment Project Exam Help

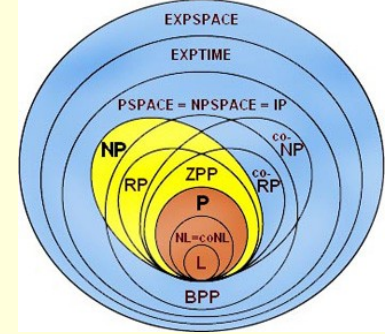
<https://eduassistpro.github.io/>

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Questions?



# Requests



Requests for Week 12 class received by Friday 8<sup>th</sup> October:

Zip!

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Nada!

Nothi

Request? What  
request? I thought  
you were making the  
request?



# CES Survey

We want to hear your feedback!

This is your opportunity to tell us about your experiences related to:

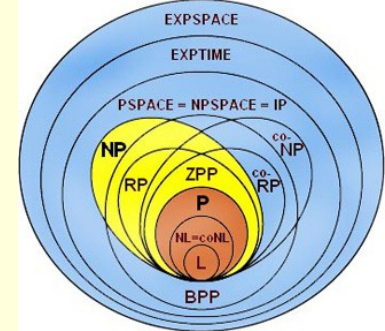
- Assessments
- Methods of teaching
- Technology use
- Learning materials

Head to [rmit.edu.au/surveys](https://rmit.edu.au/surveys) to see what student feedback have helped change in the past

Deadline is **Sunday 24<sup>th</sup> October**

Week 12

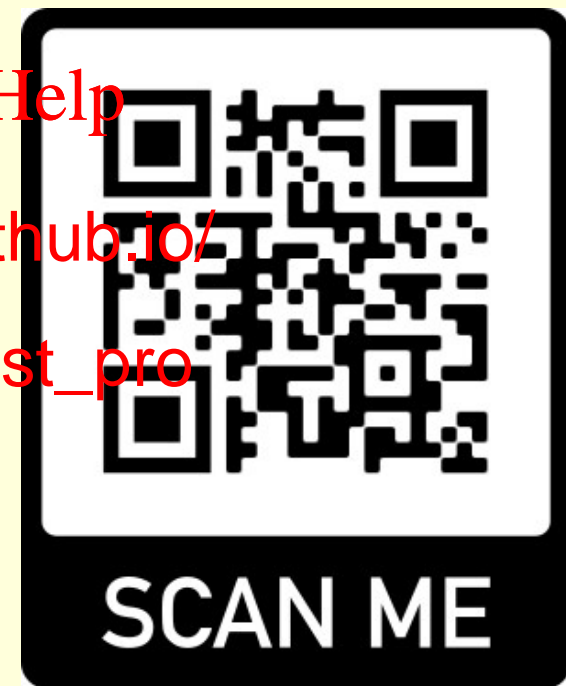
Computing Theory



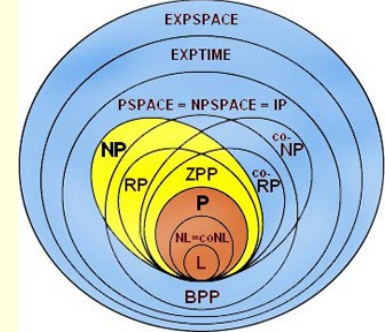
Assignment Project Exam Help

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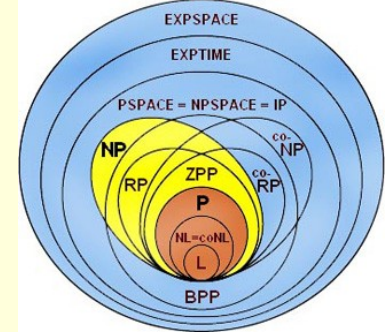
# CES Survey



- Your feedback is important!
- CES scores are used for evaluation of courses and staff
- Developments in **Assignment Project Exam Help** feedback
- <https://eduassistpro.github.io/>
- Weekly Quizzes
- Less assessment tasks
- Design of exercise
- All of these were new for 2021

PLEASE FILL IN YOUR SURVEY!

# 'Far Over'



Lilypond (from <http://lilypond.org/>)

- Free "music engraving tool"
- "Programmer's" way to write sheet music  
("more similar to a programming language than a graphical score editing program")
- Arrangement of ~~tune~~
- Generated score
- Generated MIDI + <https://eduassistpro.github.io/>

Assignment Project Exam Help

\header{title = "Far Over ..."}  
}

global = {  
  \key d \minor  
  \time 4/4  
  \dynamicUp  
}

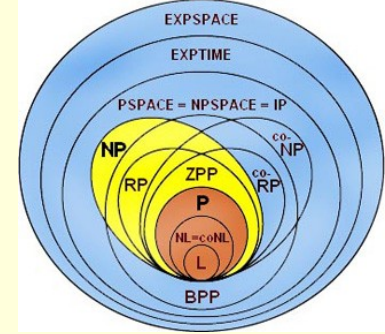
Tenornotes = \transpose d d \relative c' {  
  d,1~d4 r4 a4 c4 d2. f4 g4 a8 (g8) f4 e4 d1~d4  
  a4 d4 e4 e1~e4 f4 g4 f8 (e8) d1~d4  
  f4 g4. e8 a1~a4 f4 g4. d8 e1~e4  
  a,4 c4 e4 f1~f4 g8 (f8) e4 c4 d1

... Week 12

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Computing Theory

# 'Far Over'



Audacity (from <https://www.audacityteam.org/>)

- Free multi-track audio editor and recorder
- Play 'click track' (MIDI version from Lilypond) in headphones
- Sing each individual part in time with the click track.
- Mix tracks together
- Repeat previous two
- Export project as MP3 (because that's easy to play)
- Export project as MP3 (because that's easy to play)

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"Entire choir"



# Questions?

Questions?



## Assignment Project Exam Help

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Questions?





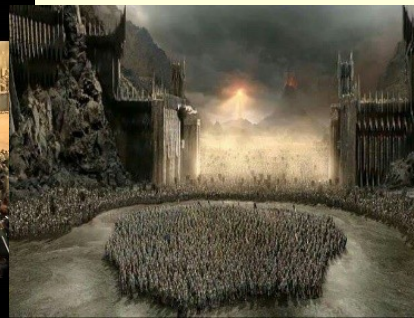
# Think music! (This will take 1 minute!)



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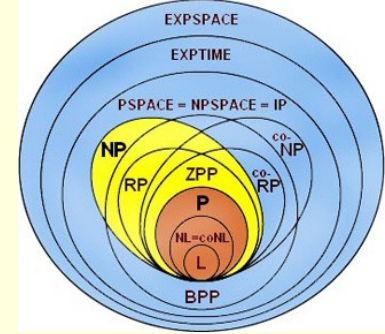
# Research

- Busy beaver
- Placid Platypus
- Universal TMs
- Platypus Game

Assignment Project Exam Help

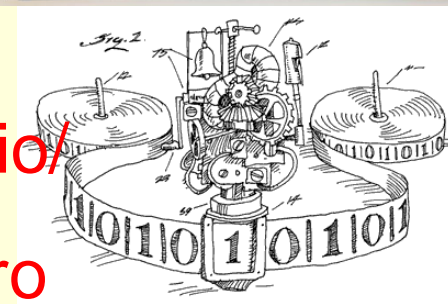
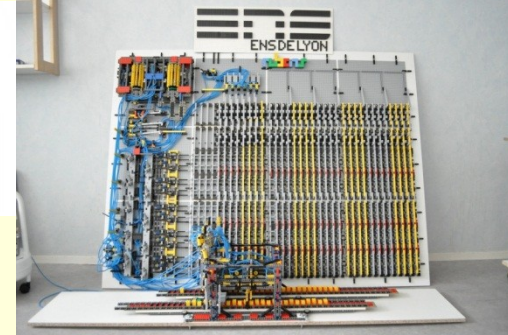
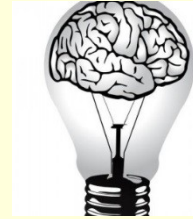
<https://eduassistpro.github.io/>

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# GET READY!

# Computable Functions



Some functions are not computable!

Turing Machines of a particular type:

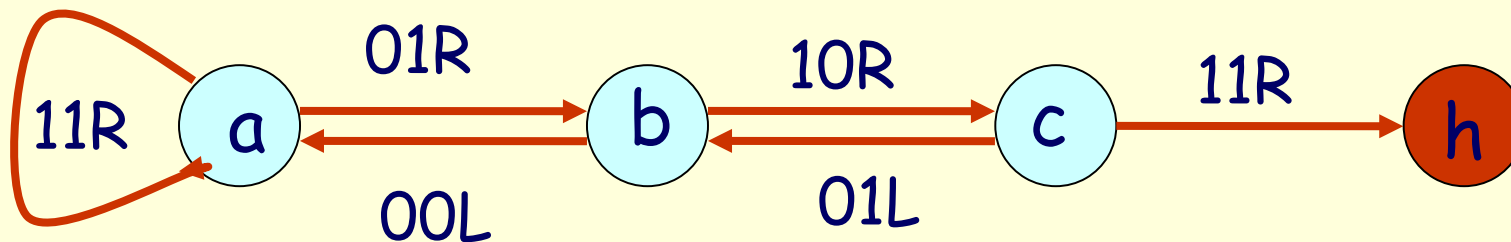
- Deterministic
- Symbols are 0 and 1
- Only consider blank input
- n states plus a halt state

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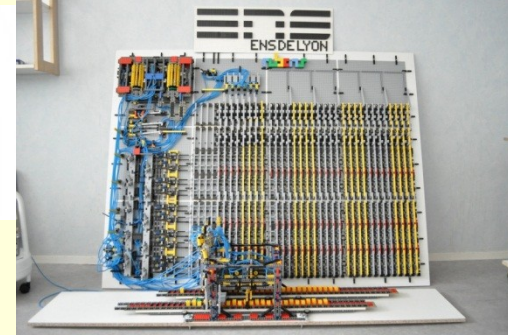
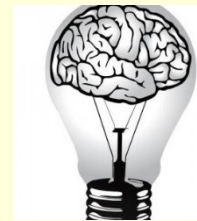
<https://eduassistpro.github.io/>

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n



# Busy Beaver

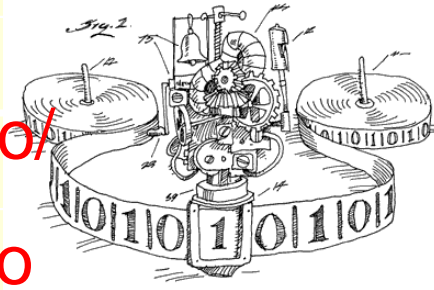


What is the largest number of 1's that can be printed by a terminating  $n$ -state machine?

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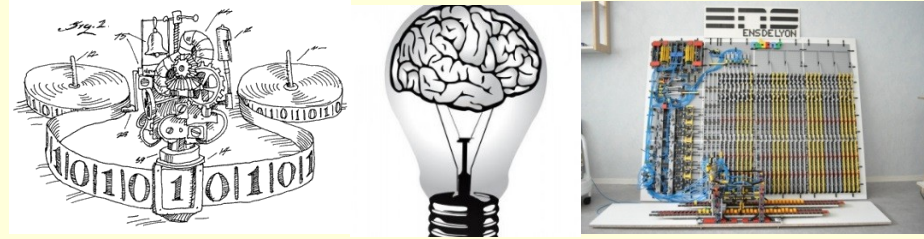
<https://eduassistpro.github.io/>

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$n$	#1's (produced)	
1	1	
2	4	
3	6	21
4	13	107
5	$\geq 4098$	$\geq 47,176,870$ (??)
6	$\geq 3.51 \times 10^{18,276}$	$\geq 7.41 \times 10^{36,534}$ (!!)

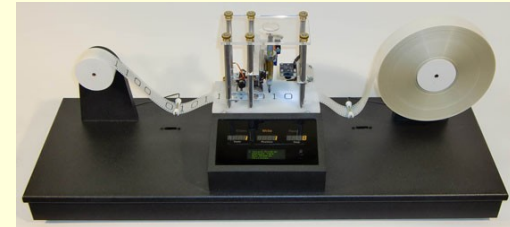
# Busy Beaver



- Busy Beaver function is **non-computable**; it grows **faster than any computable function (!!)**
- Various mathematical bounds known  
Assignment Project Exam Help
- All surpassed in <https://eduassistpro.github.io/>
- Seems hopeless for  $n \geq 7$   
Add WeChat edu\_assist\_pro
- Values for  $n \leq 5$  seem settled (but as yet unproven)



Week 12



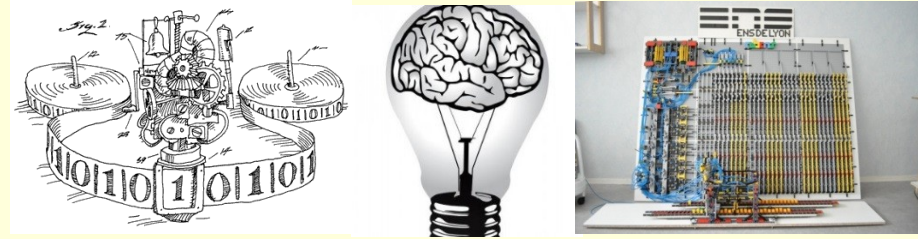
Computing Theory

<https://eduassistpro.github.io/>

## Week 12

# Computing Theory

# Busy Beavers



- $n = 1, 2, 3$  solved by Lin and Rado in 1960's
- $n = 4$  solved by Brady in 1970's
  - "proof" unsatisfactory; 200+ cases "checked by hand"
- $n = 5, 6$ 
  - monster m <https://eduassistpro.github.io/> and 2000's,
  - proof still not complete
  - Bigger monsters could be!
- Much evidence missing and is being re-created

See Heiner Marxen's web page for more



# Questions?

Questions?



## Assignment Project Exam Help

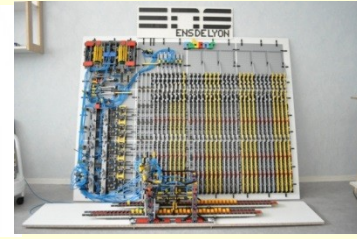
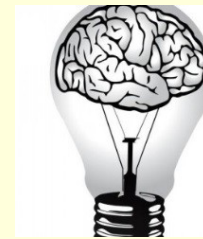
<https://eduassistpro.github.io/>

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Questions?



# Busy Beaver Grows FAST!



The busy beaver function is non-computable, because it grows faster than any computable function!

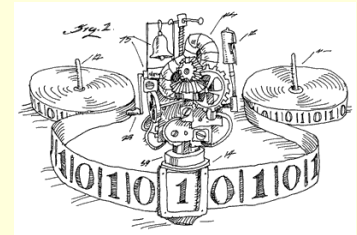
**Proof:** Let  $f$  be any computable function.

As  $f$  computable,

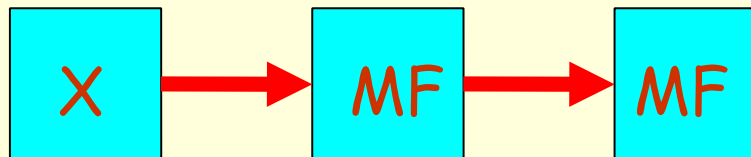
$$F(x) = \sum_{0 \leq i \leq x} f(i)$$

So there is a  $k$ -state machine  $M$  such that  $M$  halts on  $x$  1's

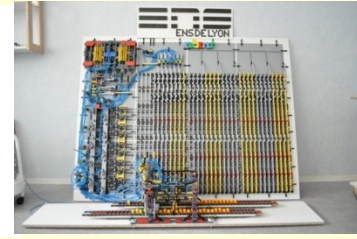
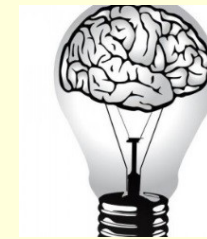
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Consider  $M$ :  $X$  then  $MF$  then  $MF$  where  $X$ : blank  $\rightarrow x$  1's.  
Note  $X$  has  $x$  states.

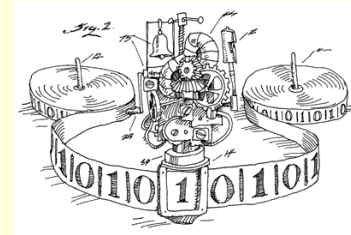


# Busy Beaver Grows FAST!



$M$  behaves as follows:

- $M$  first writes  $x$  1's
- $M$  mimics  $MF$  writing  $F(x)$  1's on the tape
- $M$  mimics  $MF$   $F(F(x))$  1's on the tape



<https://eduassistpro.github.io/>

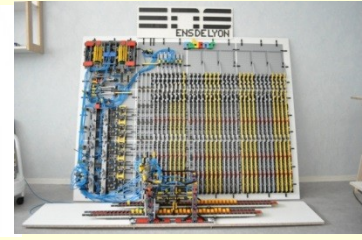
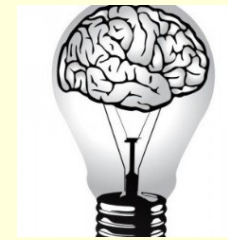
$M$  has  $x + 2k$  stat

$bb(n+2k) \geq 1$ 's output by  $M = x + F(x) + F(F(x)) > F(F(x)) > F(x+2k) > f(x+2k)$

Now  $F(x) \geq x^2 > x + 2k$  for  $x > m$ , and  $F(x) > F(y)$  when  $x > y$ , and so  $F(F(x)) > F(x+2k) > f(x+2k)$

So  $bb(x+2k) \geq x + F(x) + F(F(x)) > F(F(x)) > F(x+2k) > f(x+2k)$

# Busy Beaver Grows FAST!



This means that  $bb(n)$  grows faster than any computable function (!)

Hence  $bb(n)$  is not computable

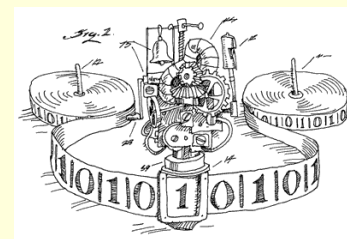
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$n^{n!} + 12$  is computable <https://eduassistpro.github.io/>

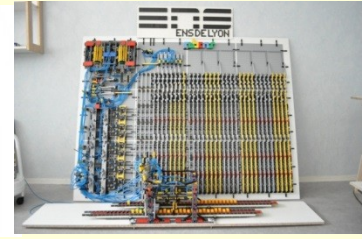
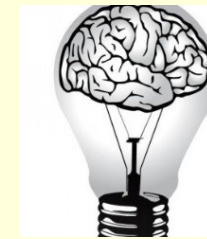
(insert your "worst nightmare" function here)

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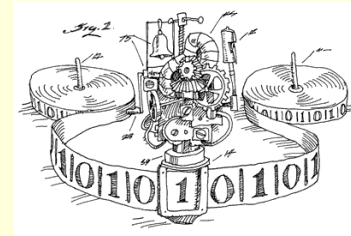
# I WIN! I ALWAYS WIN!



# Finding Busy Beavers



- Generate all machines of a given size
- Remove those which do not terminate
- Take maximum of the rest



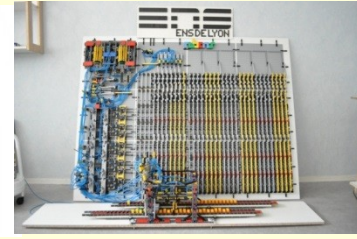
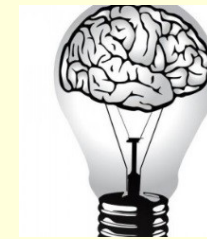
Assignment Project Exam Help

Problem 1: There are machines with  $n$  states  
( $n=5$  gives 'only' 2 <https://eduassistpro.github.io/> ones (!) ☺)

Problem 2: How can we write a program to classify machines  
into terminating and non-terminating?

No **general** method, but ...

# Monsters are rare ...



prod	5	6	7	8	9	10	11	12	13
number	73,61				79	13	6	5	2

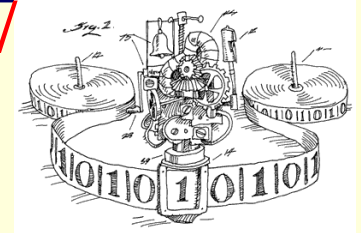
Assignment Project Exam Help

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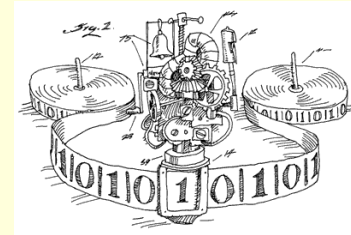
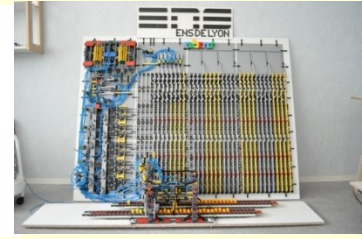
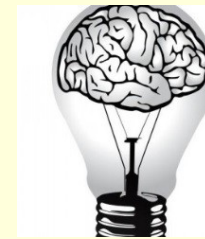
Of 117,440,512 4-state machi

- 89,207 irredundant and terminate with  $\text{prod} \geq 5$
- only 2,561 machines with  $\text{prod} > \text{bb}(3)$
- loops abound!





# 5-state monsters ...



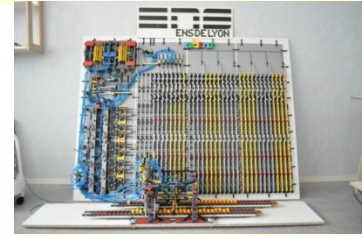
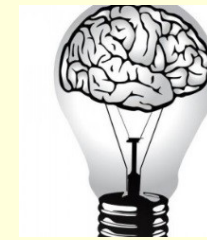
prod	max	transitions
4098	12,288	47,176,870
4098	6,144	11,798,826
4097	764	764
4097	6,143	6,143
4096	6,143	11,804,910
4096	6,143	11,804,896
1471	1,474	2,358,064

Assignment Project Exam Help

<https://eduassistpro.github.io/>

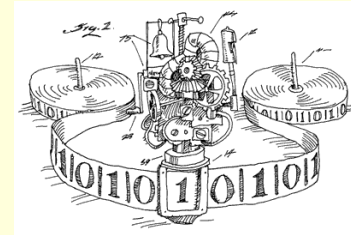
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# Platypus Machines



An  $n$ -state machine of productivity  $m$  shows

- $bb(n) \geq m$
- at most  $n$  states are needed to print  $m$  1's



Question: what is the minimum number of states needed to print

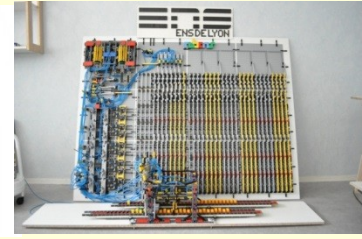
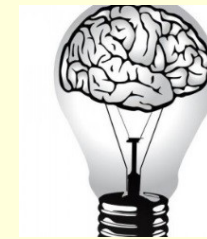
<https://eduassistpro.github.io/>

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We call this the placid platypus



# Known Platypus values



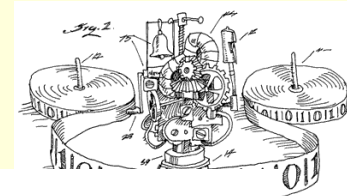
- 1-83 except 46, 48, 50, 74, 75, 77, 80, 82
- 87, 88, 89, 91, 99, 112, ...
- ..., 1471, (...?), 4096, 4097, 4098

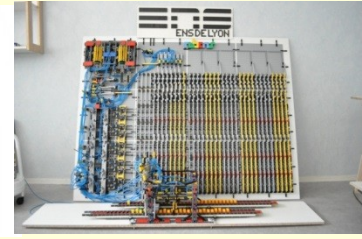
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Question: Is it true that there is a machine which prints  $m$  1's for each  $bb(m)$ ?

This is certainly false for  $bb(5)$  to  $bb(6)$ .





- 

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A cartoon illustration of a platypus, a small brown marsupial with a long, flat, white bill and a small eye. It is shown in a crawling or swimming posture on a green patch of grass.

# Questions?

Questions?



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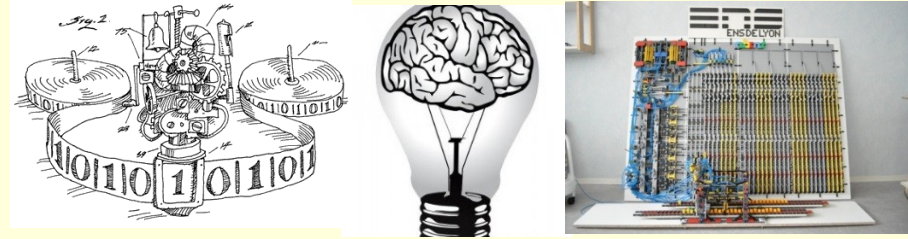
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Questions?



# Universal TMs



- Quest for the smallest universal TM goes on ...
- Involves searching similar (but larger) spaces

Alain Colmerauer (KR'08 talk)

- $U$  on  $\text{code}(M)c$
- Let  $M = U$
- $U$  on  $\text{code}(U)c$

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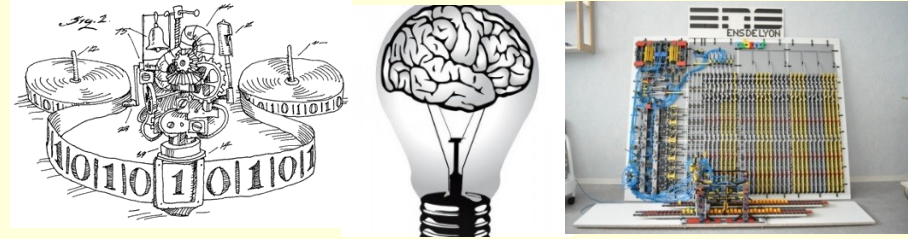
- Let  $w = \text{blank}$  (and assume  $c$  blank)
- $U$  on  $\text{code}(U)$  simulates  $U$  on blank

Hence pseudo-universality test:  $M$  is pseudo-universal if  $M$  on  $\text{code}(M)$  simulates  $M$  on blank





# Universal TMs



- What exactly is the definition of a universal Turing machine?
- How can such definitions be used to identify universal machines "in the wild"?
- What constrain <https://eduassistpro.github.io/> ing function?
- Does a UTM have to terminat
- Must a UTM terminate on  $\text{code}(M)\text{code}(w)$  exactly when  $M$  terminates on  $w$ ?
- What is an appropriate "architecture" for a UTM?  
( $\text{code}(M)\text{code}(w)$  vs  $\text{code}(w)\text{code}(M)$  )

# Questions?

Questions?



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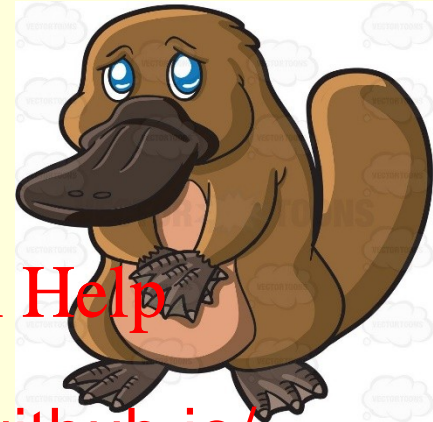
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Questions?



# The Platypus Game



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# The Platypus Game

This is a research project!

- You have done a lot of initial experimentation
- Rules and scoring much improved
- Still need to find champion machines
- 2-animal and 3-animal cases?
- Eliminate unfair
- Exercise in Tur
- Exercise in dealing with Chat
- More work to be done!

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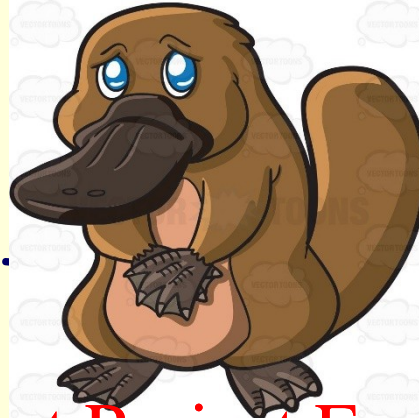
35,456



# That's it!



am ou



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# That's it!



I am out of here!

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The lecture

ed.



**Break time!** (We resume when all the pictures are gone! This will take 3 minutes!)



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