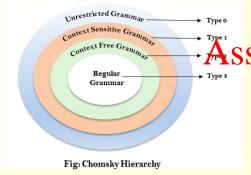
COSC1107 Computing Theory

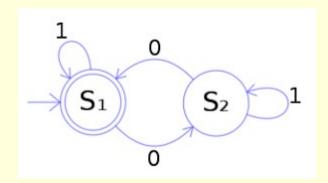
(We will commence soon. We are just allowing a few minutes for people to join and set up. Please mute your microphone unless you are speaking. You can raise your hand or use the chat at any time.)



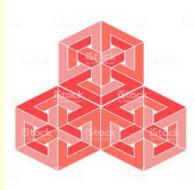
Assignment Project Exam Help

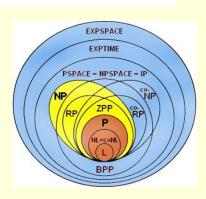


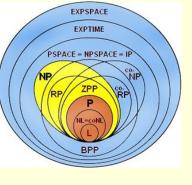
Add WeChat edu_assist_pro



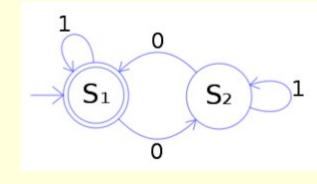


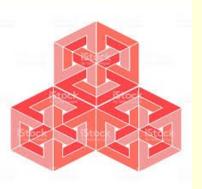








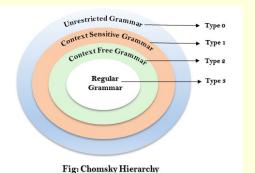




COSC1107 Assignment Project Exam Help

https://eduassistpro.github.io/

Add We Chat edu_assist_pro



James Harland

james.harland@rmit.edu.au

* With thanks to Sebastian Sardina

Intro music 'Far Over' playing now ...



Week 6

Acknowledgement



RMIT University acknowledges the people of the Woi
wurrung and Boon wurrung language groups of the
eastern Kukin Nations op whose funceded lands we conduct
the business o University
respectfully achttps://eduassistpro.githubsi@nd Elders,
past and presentdd WeChat edu_assist_pro

RMIT also acknowledges the Traditional Custodians and their Ancestors of the lands and waters across Australia where we conduct our business.

(add your name <u>here</u> to volunteer for this or email me)

Week 6

Computing Theory

Overview

- Questions?
- Converting NFAs to DFAs
- Questions? Assignment Project Exam What can be done
- Pumping Lemm be done https://eduassistpro.github.io/
- Questions?
- Platypus Game Add WeChat edu_assist_pro
- Questions?



Weekly Schedule

| | | Lecture/Lectorial | Tutorial | Assessment | |
|---|--------|---|--|-----------------|--|
| | 1 | Formal languages, grammars | Motivations & Mathematical preliminaries | | |
| | 2 | Finite State Machines | Grammars Foundations | Quiz 1 | |
| | 3 | Pushdown Automata, nondeterminism Assignment Pr | NFAs and DFAs oject Exam Help | Quiz 2 | |
| | 4 | Turing machines | Peshdown automata * | Quiz 3 | |
| | 5 | Computability, universali | elationships | Quiz 4 | |
| < | | Computability, universali https://edu | iassistpro.gitnub.io/ 🕛 | Assisumes | |
| | 6 | Pumping Lemma, NFA->DFA conversion | Comp ality | Assignment 1, | |
| | | Add WeC | hat edu assist pro | Quiz 5 | |
| | 7 | Chomsky Hierarchy | hat edu_assist_pro Nond ing Lemma | Quiz 6 | |
| | 8 | Unrestricted grammars | | Quiz 7 | |
| | 9 | Complexity and intractability | Unrestricted grammars | Quiz 8 | |
| | 10 | Zero-knowledge proofs | Complexity and intractab Ainalysis | Quiz 9 | |
| | 11 | Closure properties, problem reduction | Zero-knowledge proofs | Quiz 10 | |
| | 12 | | Closure properties, problem | | |
| | | Research and requests | reduction Assessment | Assignment 2 | |
| | 14-1AA | cek 6 | Computing The | orinal exercise | |

Mid-semester break



- No classes 28 1 brandous trope 2 1 Exseptember
- No deadlines i https://eduassistpro.github.io/

- Add WeChat edu_assist_pro
 RMIT encourages all to 'T ak' this week!
- Be kind to yourself and turn off for the week if you can

Week 7



"We want you in NZ for one day"

"Which day?"
Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu_assist_pro
Professor Sardina

Monday 5th September only



Questions?



Questions?

Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu_assist_pro

Questions?







Fig: Chomsky Hierarchy

Chomsky Hierarchy

| Automata | Languages Week 8 | Grammars |
|--|---|--|
| | Undecidable languages | |
| Turing Machines | Recursively enumerable languages imment Project Exa | |
| Linear Bounded Automata | tns://eduassistoro | → Context-sensitive |
| (Nondeterministic) Pushdown Automata | Context-free I dd WeChat edu_a | ntext-free grammars SSIST_PrO |
| Deterministic Pushdown Automata | ?? (Deterministic CF?) Week 7 | 333 |
| Nondeterministic Finite Automata & Deterministic Finite Automata | Regular languages Week 6 | Regular grammars & regular expressions |

Week 9

DFAs



Algorithm to



Fig: Chomsky Hierarch

What can DFAs do?

- Everything that NFAs can
- For every NFA there is an equivalent DFA
- DFA may be exponentially larger ...
- There is an Agental Project Exam Heppivert an NFA For any regular a to DFA
- For any regular q

- For any regular ehttps://eduassistpro.github.io/

Add WeChat edu_assist_pro

What can't DFAs do?

- Recognise context-free languages
- Recognise context-sensitive languages
- Recognise recursive languages

Property of DFAs (Pumping Lemma) used to derive a contradiction







Fig: Chomsky Hierarchy

DFAs

- Simpler to implement
- Harder to combine
- Simpler to show properties
- Simpler to showing an area Resoluted Exam Help
- More 'machine-f

Define exact

https://eduassistpro.github.io/ ges (!!)
Add WeChat edu_assist_pro

- Simpler to specify
- Trivial to combine
- Harder to analyse
- Simpler to show 'negative' results
- More 'human-friendly'

Quiz time!

Go to Canvas and find the guiz Lectorial 6 Question set

- Not worth any marks
- You can consult other students if you wish Assignment Project Exam Help Time limit will be 10 minutes

https://eduassistpro.github.io/

Add WeChat edu_assist_pro

Week 5

Go!

The pictures will take 10 minutes to disappear!

Thomas music means 1 minute left!



ssignment Project Exam Help

https://eduassistpro.github





Questions?



Questions?

Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu_assist_pro

Questions?







Two key issues

- May contain transitions
- May contain more than one transition for a given state and input

Two solutions ssignment Project Exam Help

- Compute the -cl
 - Consider an ihttps://eduassistpro.github.io/
- Compute the pos

- e NFA
- These will be A heads that the du_assist_pro

States of the DFA are the sets of possible states in the NFA





How did you go?

Question 1 Consider the NFA M below. Construct a DFA which accepts the same language as M.

Assignment Project Exam Help

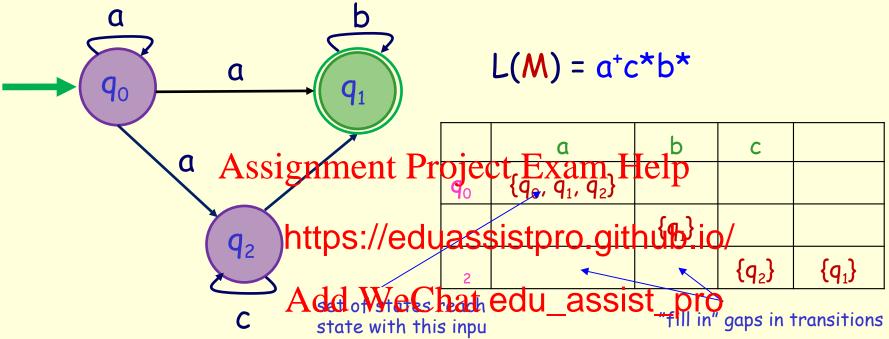
https://eduassistpro.github.io/

Add WeChat edu_assist_pro





Fig: Chomsky Hierarchy



DFA construction uses this table



| | a | Ь | С |
|-----------------------|---------------------|-------------------|-----------------------------------|
| q ₀ | $\{q_0, q_1, q_2\}$ | | |
| q_1 | | {q ₁ } | |
| q ₂ | | | {q ₁ ,q ₂ } |



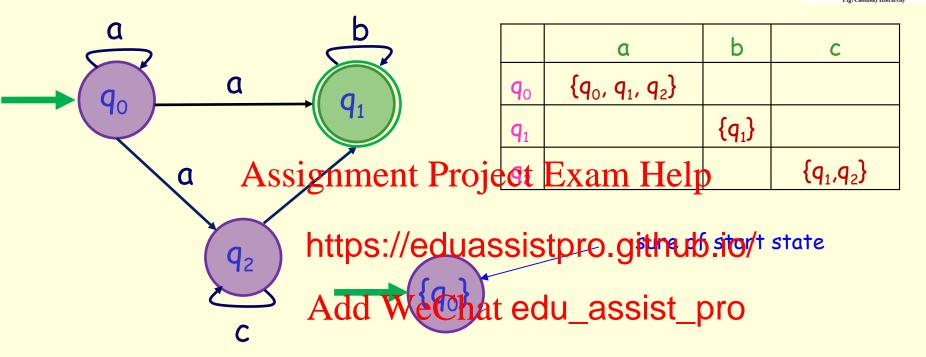






Fig: Chomsky Hierarchy

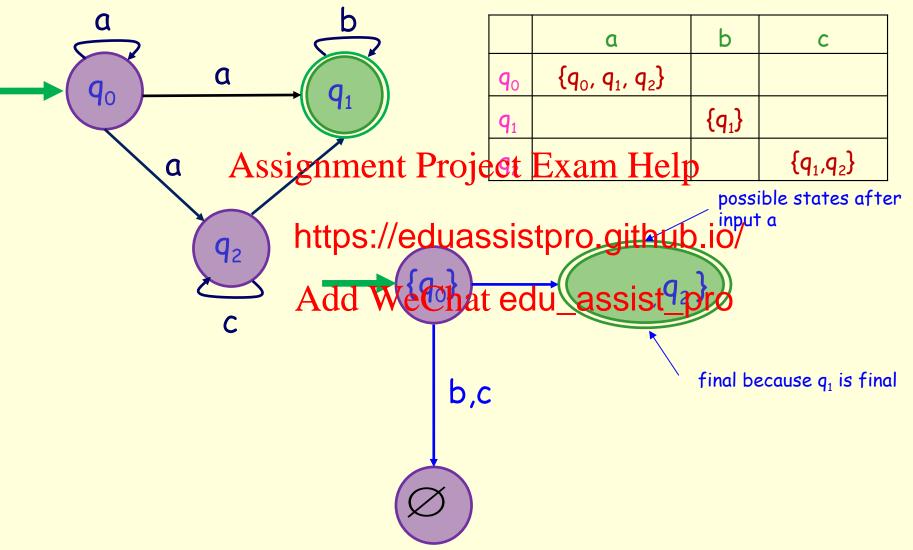
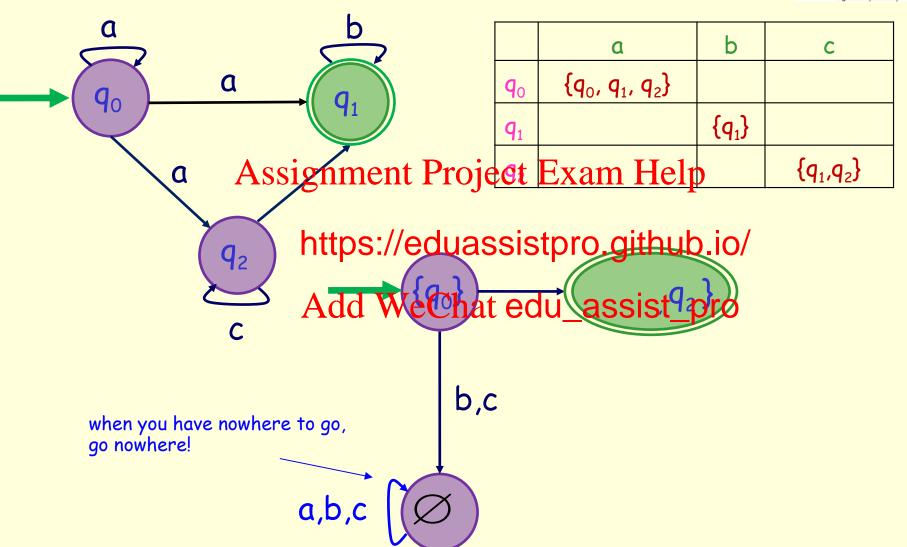
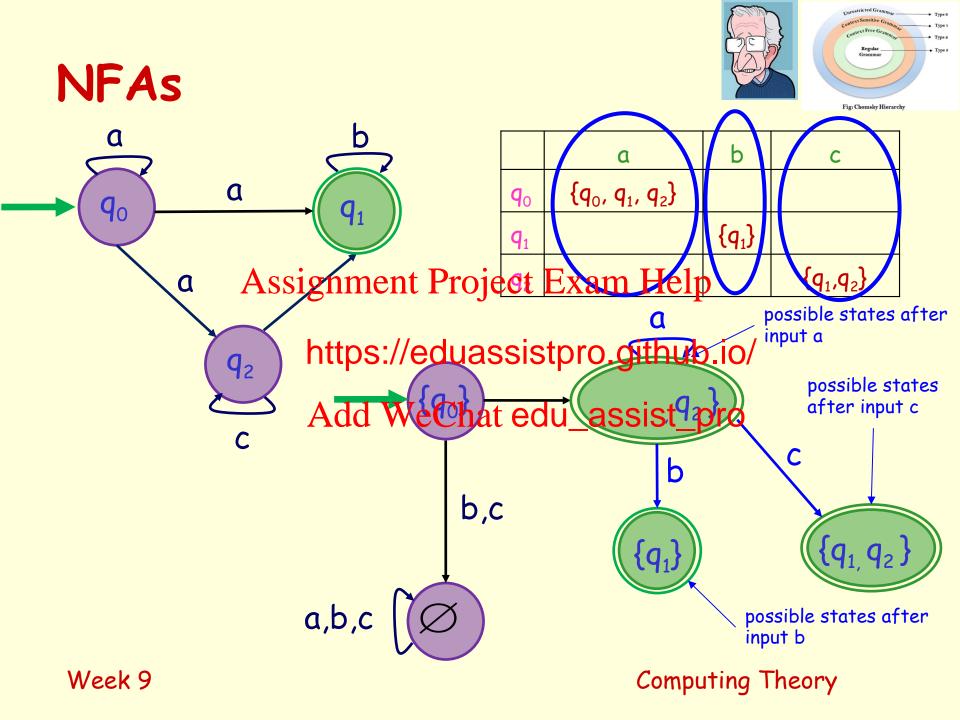




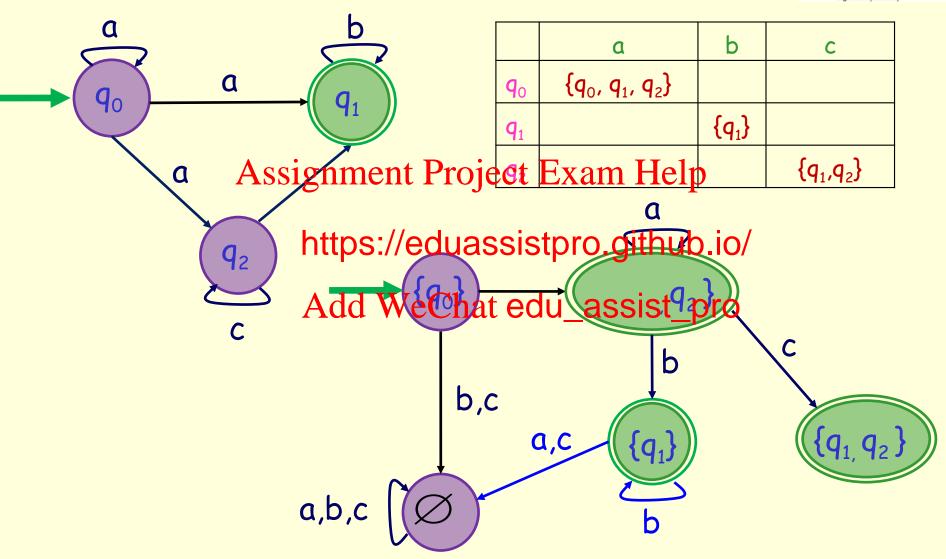
Fig: Chomsky Hierarchy







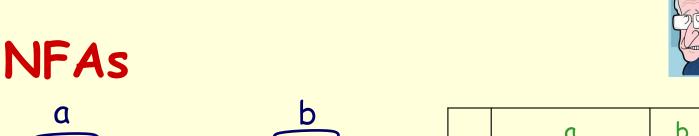
NFAs

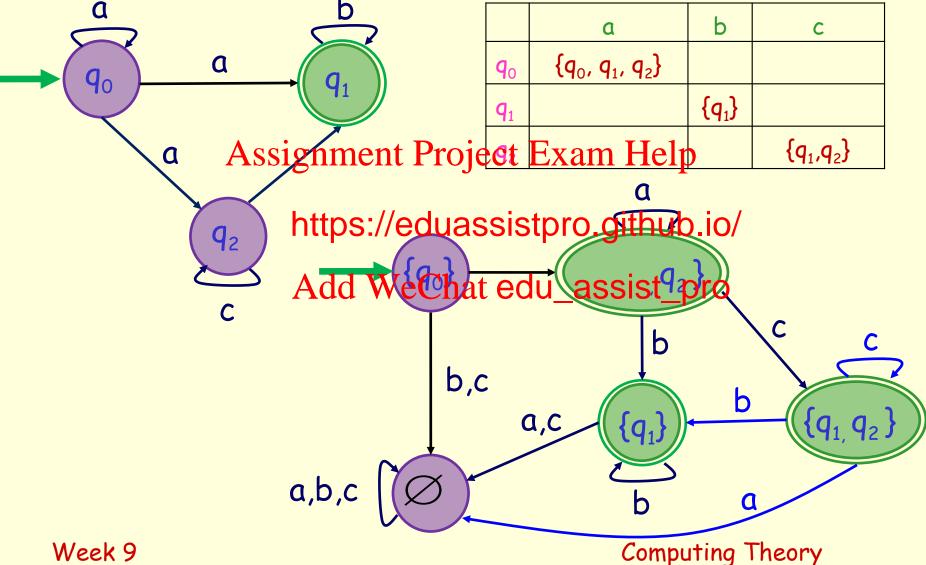


Week 9



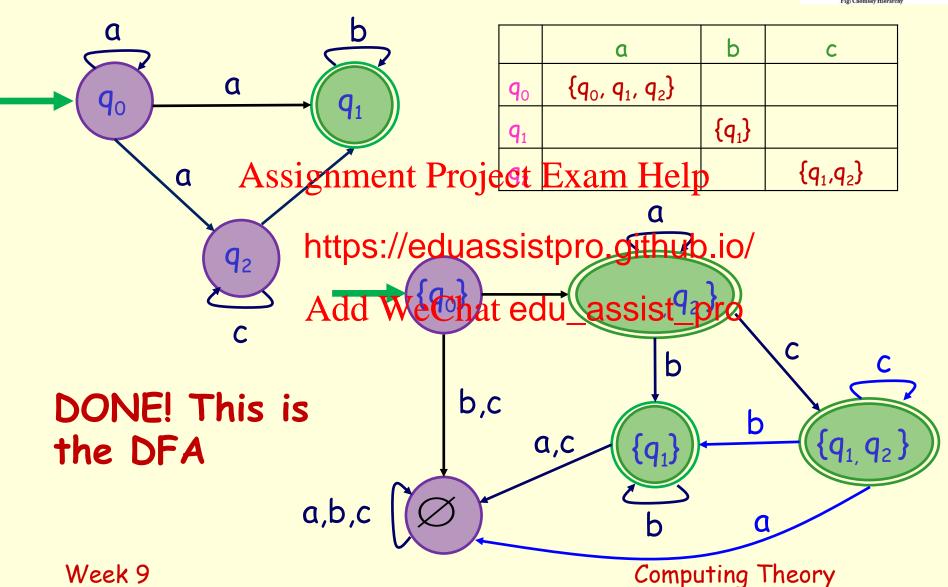
Fig: Chomsky Hierarchy







NFAs



Questions?

Questions?

Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu_assist_pro

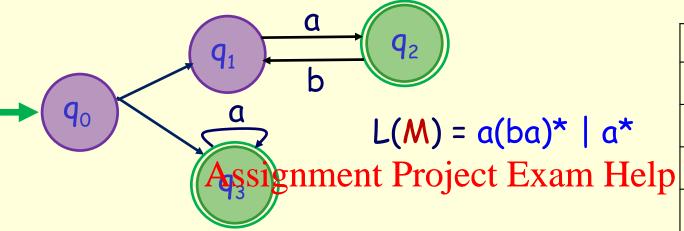
Questions?







Fig: Chomsky Hierarchy



| | a | Ь |
|-----------------------|-------------------|---|
| q ₀ | ${q_2, q_3}$ | |
| q_1 | $\{q_2\}$ | |
| q ₂ | | |
| q ₃ | {q ₃ } | |

https://eduassistpro.github.io/

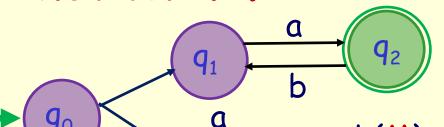


Add WeChat edu_assist_pro





Fig: Chomsky Hierarchy



L(M) = a(ba)* | a*

Assignment Project Exam Help

| | a | Ь |
|-----------------------|-------------------|---|
| q ₀ | ${q_2, q_3}$ | |
| q_1 | {q ₂ } | |
| q ₂ | | |
| q ₃ | {q ₃ } | |

https://eduassistpro.github.io/

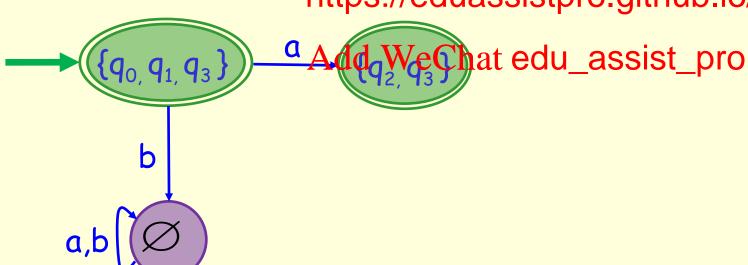
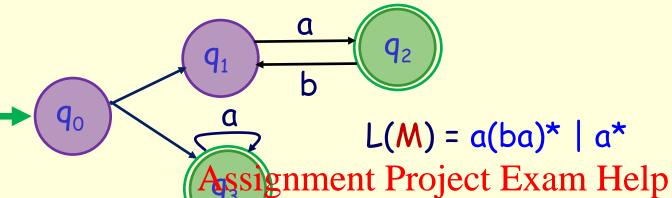






Fig: Chomsky Hierarchy



| | α | Ь |
|-----------------------|-------------------|---|
| q ₀ | $\{q_2, q_3\}$ | |
| q_1 | {q ₂ } | |
| q ₂ | | |
| q ₃ | {q ₃ } | |

https://eduassistpro.github.io/

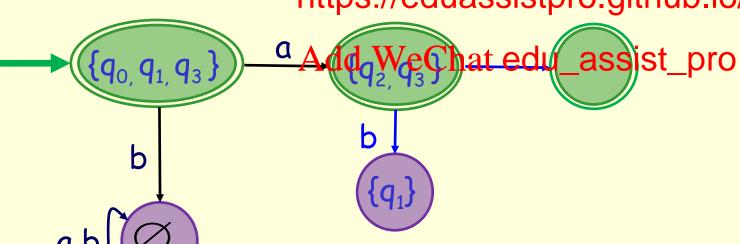
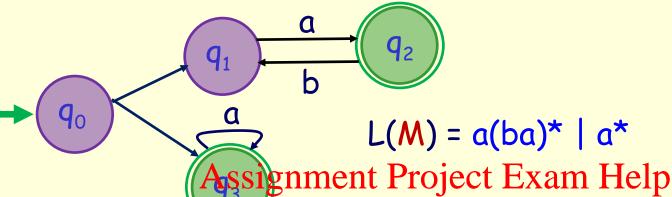




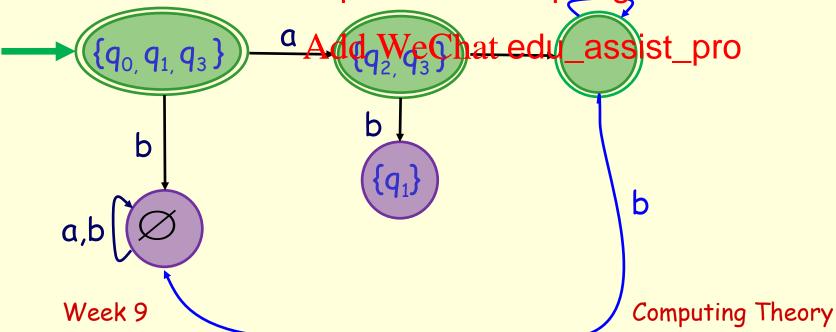


Fig: Chomsky Hierarchy



| | a | b |
|-----------------------|-------------------|---|
| q ₀ | $\{q_2, q_3\}$ | |
| q_1 | {q ₂ } | |
| q_2 | | |
| q ₃ | {q ₃ } | |

https://eduassistpro.github.io/





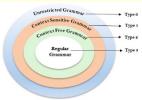
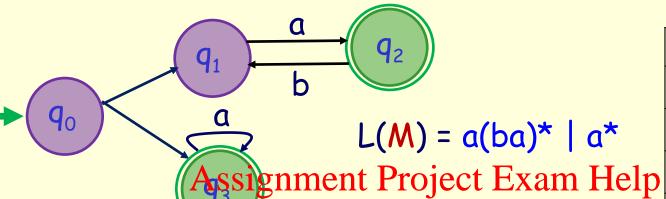


Fig: Chomsky Hierarchy



| | а | Ь |
|-----------------------|-------------------|---|
| q ₀ | ${q_2, q_3}$ | |
| q_1 | {q ₂ } | |
| q_2 | | |
| q ₃ | {q ₃ } | |

https://eduassistpro.github.io/

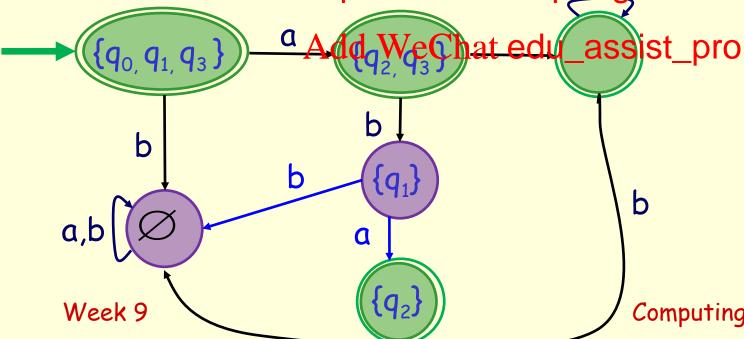
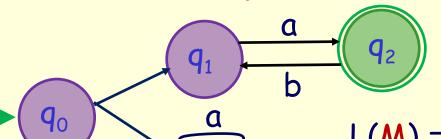






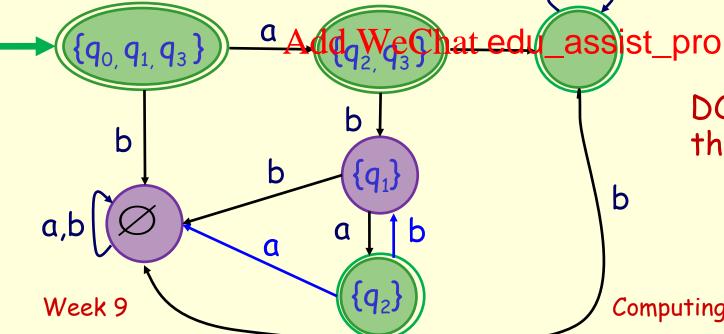
Fig: Chomsky Hierarchy



 $L(M) = a(ba)^* \mid a^*$ Assignment Project Exam Help

| | а | Ь |
|-----------------------|-------------------|---|
| q ₀ | ${q_2, q_3}$ | |
| q_1 | {q ₂ } | |
| q ₂ | | |
| q ₃ | {q ₃ } | |

https://eduassistpro.github.io/



DONE! This is the DFA

NFA to DFA

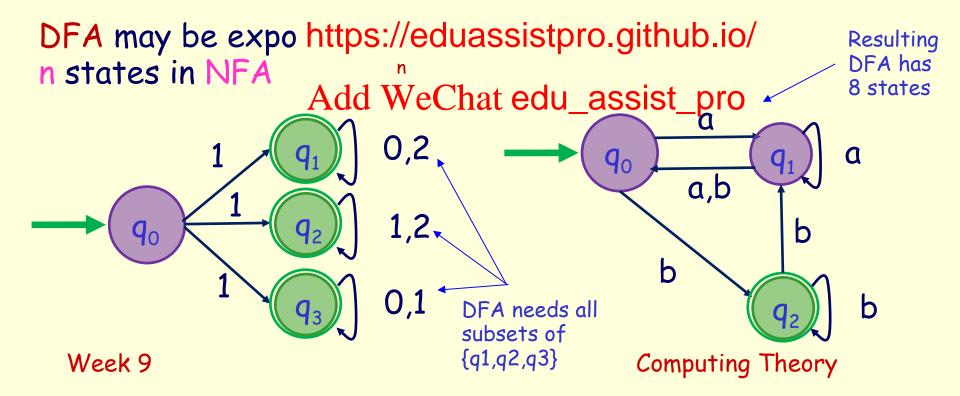




Fig: Chomsky Hierarchy

- 1. Start with -closure for each state
- 2. Generate t table
- 3. Initial state of DFA is -closure of initial state in NFA
- 4. Construct DFA
 Ssignment Project Exam Help

 Keep adding states until all transitions are to existing states



Questions?

Questions?

Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu_assist_pro

Questions?



DFAs



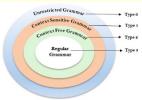


Fig: Chomsky Hierarchy

What can DFAs do?

- Everything that NFAs can
- For every NFA there is an equivalent DFA
- DFA may be exponentially larger ...
 There is an Againmenta Project Exam Help
- For any regular g
- For any regular ehttps://eduassistpro.github.io/

Add WeChat edu_assist_pro

What can't DFAs do?

- Recognise context-free languages
- Recognise context-sensitive languages
- Recognise recursive languages

Property of DFAs (Pumping Lemma) used to derive a contradiction

Limitation of DFAs





Fig: Chomsky Hierarchy

| Memory Size | Memory access |
|---------------------|----------------------|
| Bounded* | Defined by machine |
| Unbounded | Top of stack only |
| ment Project Exam F | Telp (see Week 8) |
| | • |

* bounded means th

Turing Machines

https://eduassistpro.gith@b.10/(ie unlimited)
n in advance

Add WeChat edu_assist_pro en a DFA pro tring longer

I can't count that high.

What happens when a DFA pro

than the number of states?

"Now you are getting some



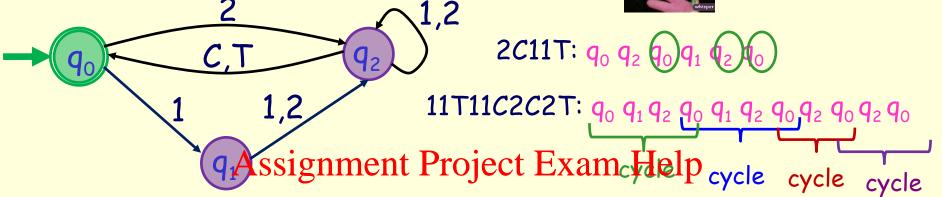




Limitation of DFAs









0100110: $q_0 q_0 q_1 q_0 q_0 q_1 q_2 q_0$

0000010: $q_0 q_0 q_0 q_0 q_0 q_0 q_1 q_0$

For any string w L(M) with $|w| \ge \#$ states in M, there is a cycle

Week 6

Limitation of DFAs



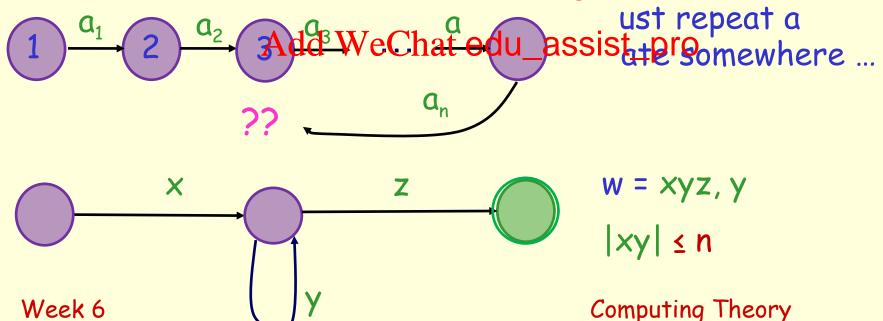


Let L be any regular language Then there is a DFA M such that L = L(M)

Let the number of states in M be n Assignment Project Exam Help

Consider w L(M) wit

https://eduassistpro.github.io/



Questions?



Questions?

Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu_assist_pro

Questions?





For any regular language L, there is $n \ge 1$ such that for any $w \perp w \mid w \mid \ge n$, there exist x, y, z such that w = xyz and

- 1. |xy| ≤ n Assignment Project Exam Help
- 2. y
- 3. x y z L for ahttps://eduassistpro.github.io/

Add WeChat edu_assist_pro So for any L, for some n find $w = h |w| \ge n$

- If L is regular, then xz, xyz, xyyz, xyyyz, xyyyz, ... are all in L
- If $xy^{j}z$ L for some $j \ge 0$, then L is not regular



Usual use is to show languages not regular by contradiction

- Assume L is regular Project Exam Help
 Apply Pumping
- Choose string whttps://eduassistpro.github.io/
 Use |xy| ≤ n to
- 5. Choose i such thadd We Chatedu_assist works)
- 6. Contradiction!

Conclude that L is not regular

All such proofs the same except steps 3 & 5







The language $L = \{a^ib^i \mid i \ge 0\}$ is not regular

Proof: Assume L is regular. Then the Pumping Lemma applies are there is an $n \ge 1$ such that for all $w \ge s$ such that $|w| \ge 1$, |w| = xyz

- 1. |xy| ≤ n
- https://eduassistpro.github.io/ 2. y
 3. x yⁱ z L for all i ≥ 0

Add WeChat edu_assist_pro

Choose $w = a^n b^n$ and so $w \mid L$ and $\mid w \mid \geq n$. mping Lemma, $w = xyz = a^nb^n$ and $|xy| \le n$. So $y = a^j$ for some $1 \le j \le n$.

First n characters of xy are a's

Choose i = 2 and consider xyyz = $a^{n+j}b^n$ By the Pumping Lemma, ant bn L (!!)

Hence L is not regular.



The language $L = \{ xx^R \mid x \{a,b\}^* \}$ is not regular

Proof: Assume L is regular. Then the Pumping Lemma applies and there is an $n \ge 1$ such that for all $w \ge s$ such that $|w| \ge 1$, |w| = xyz

- 1. |xy| ≤ n
- https://eduassistpro.github.io/ y
 x yⁱ z L for all i ≥ 0

Add WeChat edu_assist_pro

Choose w = anbban and so w L and |w| > Pumping Lemma, $w = xyz = a^nbba^n$ and $|xy| \le n$. So $y = a^j$ for some $1 \le j \le n$.

First n characters of xy are a's

Choose i = 2 and consider xyyz = an+j bban By the Pumping Lemma, anti bban L (!!)

Hence L is not regular.



The language $L = \{a^i \mid i \text{ is prime}\}\$ is not regular

Proof: Assume L is regular. Then the Pumping Lemma applies are there is an $n \ge 1$ such that for all $w \ge s$ such that $|w| \ge 1$, |w| = xyz

- 1. |xy| <u>≤</u> n
- https://eduassistpro.github.io/ y
 x yⁱ z L for all i ≥ 0

Add WeChat edu_assist_pro

Choose w = am where m is prime and m > nd $|w| \ge n$. So by the Pumping Lemma, $w = xyz = a^m$ and $|xy| \le n$.

This means |xyz| = m

Choose i = m+1 and consider $|xy^{m+1}z| = |xyz| + m|y| = m + m|y| = m(|y|+1)$ By the Pumping Lemma, $a^{m(|y|+1)}$ L but m(|y|+1) is not prime (!!)

Hence L is not regular.

Week 6

Computing Theory



The language L = { ??? } is not regular

Proof: Assume L is regular. Then the Pumping Lemma applies are there is an $n \ge 1$ such that for all $w \ge s$ such that $|w| \ge 1$, |w| = xyz

- 1. |xy| ≤ n
- https://eduassistpro.github.io/ y
 x yⁱ z L for all i ≥ 0

Add WeChat edu_assist_pro

```
Choose w = ??? and so w \perp and |w| \geq n.
                                                         mping Lemma, w =
xyz = ???? and |xy| \le n. So y = ????
```

Choose i = ??? (try 2 first) and consider xy'z = ???? By the Pumping Lemma, ??????? L (!!)

Hence L is not regular.

Regular languages



Regular languages

- Generated by regular grammars
- Specified by regular expressions
 Accepted by Rigament Project Exam Help
- Accepted by D
- Pumping Lemmahttps://eduassistpro.github.io/
- Pumping Lemma used by cont edu_assist_pro languages not regular
- Any NFA can be converted into an equivalent DFA
- DFA can be exponentially larger than the NFA

(there is also a Pumping Lemma for context-free languages)

Questions?



Questions?

Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu_assist_pro

Questions?



The Platypus Game



Assignment Project Exam H

https://eduassistpro.github.io/



Add WeChat edu_assist_pro

The Platypus Game

Assignment 2

- Round-robin + knockout tournament
- 2,500 machine Assignment Project Exam Help
- 3,126,250 matches https://eduassistpro.github.io/
- 0.59 seconds per 1,000 matches Add WeChat edu_assist_pro
- About 30 minutes
- I will take your top 10 for the knock-out phase
- Will post more about this on Ed soon





That's it!



I am out of here!

Assignment Project Exam Help



https://eduassistpro.github.io/

Add WeChat edu_assist_pro



That's it!



I am out of here!

Assignment Project Exam Help

https://eduassistpro.github.io/

Thed We Chat edu_assistepro

Break time! (We resume when all the pictures are gone! This will take 3 minutes!)





Assignment Project Exam Help

https://eduassistpro.github.io/

Add WeChat edu_assist_pro



Marking

S_1 S_2 S_1 S_2 S_2

Why did I lose marks for ...??



AWhenmeid Project Exanthemp

Ar https://eduassistpro.github.io/

Perhaps Washat edu_assistmproat night ...

Never feed them after midnight!

. . .

Alternative Scheme?



Poor Acceptable Exceeds Expectations Outstanding Troll Dreadful

Outstanding - CONGRATULATIONS! Your exemplary powers of deduction and a formidable knowledge of the inner workings of the magical world reveal you to be a witch or wizard of genuine skill and learning.

Assignment Project Exam Help

Exceeds Expectations -

rformance!

Acceptable - demonstrat https://eduassistpro.github.io/

Poor - Alas - we regret to into hay Wife Chathedu_assisted Pros may have been due to factors outside your control (eg: polterge , examination nerves or a malfunctioning quill.) Please do not disconsolate.

Dreadful - We are sorry to inform you that you have failed.

Troll - You would appear either to have abandoned the test due to factors outside your control (eg, earthquake, poltergeist attack), or else you are a troll, in which case you are to be congratulated on being able to use a computer and have achieved the grade of O.F.T. (Outstanding for Trolls).

Marking

Computing Theory

Alternative Scheme?



Poor Acceptable Exceeds Expectations Outstanding Troll Dreadful

Outstanding - CONGRATULATIONS! Your exemplary powers of deduction and a formidable knowledge of the inner workings of the magical world reveal you to be a witch or wizard of genuine skill and learning.

Assignment Project Exam Help

Exceeds Expectations -

rformance!

Acceptable - demonstrat https://eduassistpro.github.io/

Poor - Alas - we regret to into hay Wife Chathedu_assisted Pros may have been due to factors outside your control (eg: polterge , examination nerves or a malfunctioning quill.) Please do not disconsolate.

Dreadful - We are sorry to inform you that you have failed.

Troll - You would appear either to have abandoned the test due to factors outside your control (eg, earthquake, poltergeist attack), or else you are a troll, in which case you are to be congratulated on being able to use a computer and have achieved the grade of O.F.T. (Outstanding for Trolls).

Marking

Computing Theory