

CDMA with Noise Solution

In the class, we have considered CDMA in an ideal system. However, in reality, we have much more complicated scenario: Users will experience noise.

Consider the scenario with one sender and one receiver. The chipping sequence is $(-1 -1 -1 +1 -1 +1 +1 +1)$. Suppose the sender sends bit “1”, then the signal sent will be $(-1 -1 -1 +1 -1 +1 +1 +1)$. In the channel, noise is added to the signal so that the received signal will be $(-1+n_1 -1+n_2 -1+n_3 +1+n_4 -1+n_5 +1+n_6 +1+n_7 +1+n_8)$, where n_1, \dots, n_8 are noise terms. They are independently normally distributed with zero mean and σ^2 variance, in this question, $\sigma^2 = 1$. Formally, $n_i \sim N(0, 1)$. You should know the normal distribution in a prerequisite course.

After the computing the inner product at the receiver, what “value” does the receiver derive? If the value is smaller than 0, it is decoded as -1, otherwise, it is decoded as 1. Use the provided table to find the probability that it is wrongly decoded as -1.

The tail probability (Q function) of a standard normal distribution is given in the attached `q_function.pdf`.

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(1) Inner product/M: $R=1+(-n_1-n_2-n_3-n_4+n_5+n_6+n_7+n_8)/8$

$n_i \sim N(0, 1)$.

$-n_i \sim N(0, 1)$.

$n_i/8 \sim N(0, 1/64)$.

$$-n_i/8 \sim N(0, 1/64).$$

This is because if n is a Gaussian random variable with variance σ^2 , $a*n$ is a Gaussian random variable with variance $a^2\sigma^2$

$$R \sim N(1, 1/8) = (\mu_0, \sigma_0^2)$$

This is because the sum of two independent Gaussian random variables is still a Gaussian random variable. See

https://en.wikipedia.org/wiki/Sum_of_normally_distributed_random_variables

$$X \sim N(\mu_X, \sigma_X^2)$$

$$Y \sim N(\mu_Y, \sigma_Y^2)$$

$$Z = X + Y,$$

then

$$Z \sim N(\mu_X + \mu_Y, \sigma_X^2 + \sigma_Y^2).$$

$$P(R < 0) = Q\left(\frac{|0 - \mu_0|}{\sigma_0}\right) = Q(2.82) \approx 2.4012 \times 10^{-3}$$

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It follows the definition of Q function, see <https://en.wikipedia.org/wiki/Q-function>

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