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Question 1 (3 marks)

You are choosing a main course at a restaurant, from a menu containing three items: bibim-bap, haggis and manakish.

Suppose we have propositions B, H and M, with the following meanings.

- B: You choose bibimbap.
- H: You choose haggis.
- M: You choose manakish.

Use B, H and M to write a proposition, in Conjunctive Normal Form, that is True precisely when you choose either the bibimbap or both the other items.

Question 2 (5 marks)

Suppose you have predicates belongs to P and belongs to NP with the following meanings, where variable Streeth Can tray in the Ct Exam Help

 $belongsToP(X): \quad the language \ X \ belongs \ to \ the \ class \ P. \\ belongsToNP($

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(a) In the space below, write a statement in predicate logic with the me

 $\underset{P \text{ is a proper subset of NP (i.e., }P \subseteq NP}{\textbf{Add WeChat edu_assist_pro}}$

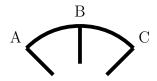
To do this, you may only use: the above two predicates; quantifiers; logical connectives; equality. (In particular, you may not use \subseteq or \subset or \neq , etc, and in fact they would not help.)

- (b) For the statement "P is a proper subset of NP", which one of the following holds? Circle (A), (B), (C) or (D) to indicate your answer.
 - (A) The statement is True.
 - (B) The statement is False.
 - (C) It is not known whether it's True or False, but it's generally believed to be True.
 - (D) It is not known whether it's True or False, but it's generally believed to be False.

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Question 3 (7 marks)

A knob is used to select one of three positions A, B, C, as shown in the following diagram.



The position of the knob is recorded every second for some nonzero period of time.

The knob can never be turned from A to C, or from C to A, without spending at least one second in position B. The initial position of the knob can be any of A, B, C.

Consider the language of all possible strings of knob positions recorded in this way.

(a) Give a regular expression for this language.

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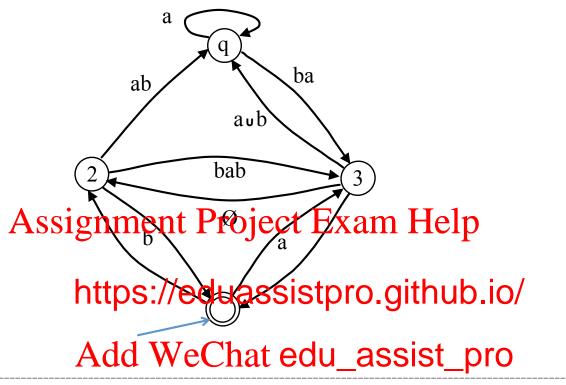
(b) Give a Finite Automaton for this language.

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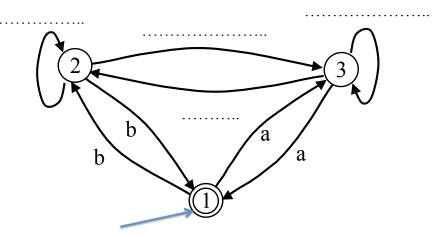
Question 4 (5 marks)

Consider the following Generalised Nondeterministic Finite Automaton (GNFA). Construct an equivalent GNFA with the top state, q, removed.

Show your answer by writing in the four missing transition labels, on the dotted lines, in the second diagram below.



YOUR ANSWER:



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Question 5
Consider the following Finite Automaton.

(6 marks)

(a) Which is a graph meant ship is country to the present ones that are accepted.

b

- ab https://edwassistpro.github.io/
- (b) Consider the string label flow in that teleprine three string xy^iz is also accepted by the FA.

Do this by drawing vertical lines between the parts of the string given on the next line:

aabab

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Question 6 (4 marks)

The following table describes part of a Finite Automaton with three states. The second row, for state 2, has not been filled in.

What could the state-2 row be, if you are given that the number of states of this FA is **not minimum**?

Write all possible state-2 rows in the second table below. Use as many rows as you need, one for each possible state-2 row. You may not need all the rows available.

state	a	Ъ
Start 1	2	3
2		
Final 3	1	2

YOUR ANSWER:

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Question 7 (6 marks)

This question uses the following **Definitions** and **Facts**.

Definitions:

- If L is any language, the reversal of L is the set of all reversals of strings in L. In other words, you obtain the reversal of L by taking every string in L and writing it backwards. So, for example, the string abb becomes bba.
- If L is any language over the alphabet $\{a,b\}$, then the interchange of a and b forms a new language as follows: take every string in L, and replace every a by b and every b by a, simultaneously. So, for example, the string abb becomes baa.

Facts:

- The class of regular languages is closed under reversal.
- The class of regular languages is closed under interchange of a and b.
- The language AB := { $a^n b^n : n \in \mathbb{N}$ } is not regular.

Your task: Assignment Project Exam Help Using these facts, and any other closure properties of regular languages you like, prove by contradiction tha

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is not regular.

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Question 8

(3 marks)

Explain how to derive, for an

recognised by the FAhttps://eduassistpro.github.io/

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Question 9 (12 marks)

Consider the following Context-Free Grammar:

$$S \rightarrow X$$
 (1)

$$X \rightarrow sXh$$
 (2)

$$X \rightarrow \varepsilon$$
 (3)

(a) Give a derivation for the string ssshhh.

Each step in your derivation must be labelled, on its right, by the number of the rule used.

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(b) Give a parse tree for the sam

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(c) Prove by induction on n, that for all $n \ge 0$, the string $\mathbf{s}^n \mathbf{h}^n$ has a derivation in this grammar of n+2 steps.

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Question 10 (6 marks)

This question uses the same Context-Free Grammar as the previous question. Here it is again for convenience:

$$S \rightarrow X$$
 (1)

$$X \rightarrow sXh$$
 (2)

$$X \to \varepsilon$$
 (3)

Complete the following diagram to give a Pushdown Automaton for the language generated by this grammar.

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Question 11 (5 marks) State (without proof) the Pumping Lemma for Context-Free Languages, and briefly describe

State (without proof) the Pumping Lemma for Context-Free Languages, and briefly describe its main purpose.

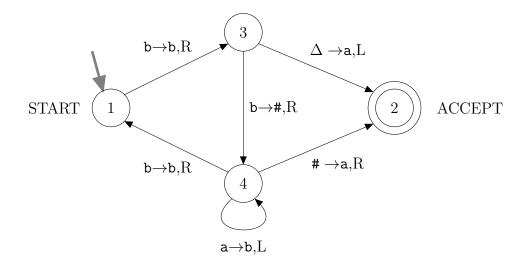
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Question 12 (6 marks)

Consider the following Turing machine.



Trace the solution in the page. Trace the solution of the next page.

The lines show the co each line, fill in the state S://eduassistpro.github.io/currently-scanned ch aracter as Δ (but there is no need to show subsequent blank characters).

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To get you started, the first line has been filled in already.

At start of step	1:	State:	1	Tape:	<u>b</u>	b	a	Δ		
At start of step	2:	State:		Tape:						
At start of step	3:	State:		Tape:						
At start of step	4:	State:		Tape:						
At start of step	5:	State:		Tape:						
At start of step	6:. S12	State:	ent	Projec	t E	xa	m i	He	lp	
At start of step	7:	State:								
At start of step	8:	State:		duass Tape:	•					
At start of step			We —	Chat e	du	<u>_</u> a	ISS	ist_	_pı	0
At start of step	10:	State:		Tape:						
At start of step	11:	State:		Tape:						
At start of step	12:	State:		Tape:						

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Question 13 (4 marks)

For each of the following decision problems, indicate whether or not it is decidable.

You may assume that, when Turing machines are encoded as strings, this is done using the Code-Word Language (CWL).

Decision Problem	your answer			
	(tick one box	x in each row)		
Input: a Turing machine M . Question: Does there exist a string w that is accepted by M in at most 7 steps?	Decidable	Undecidable		
Input: a Turing machine M . Question: Does there exist a string w that is accepted by M ?	Decidable	Undecidable		
Input: a string w . Question: Does there exist a Turing machine that accepts w ? Assignment Project Exam Input: a Turing machine M , and a string w . Question: Is w the e https://eduassistpro.g	Decidable	Undecidable Undecidable		
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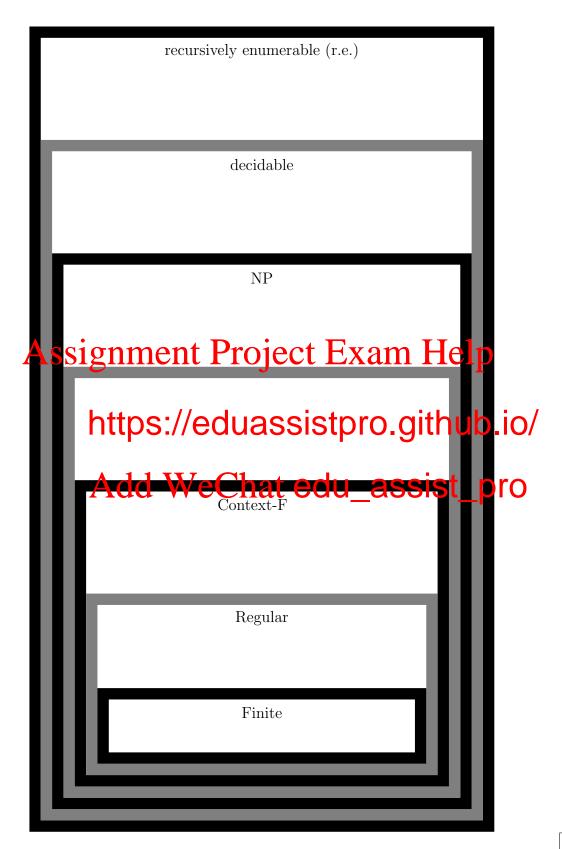
Question 14 (10 marks)

The Venn diagram on the right shows several classes of languages. For each language (a)–(j) in the list below, indicate which classes it belongs to, and which it doesn't belong to, by placing its corresponding letter in the correct region of the diagram.

If a language does not belong to any of these classes, then place its letter above the top of the diagram.

You may assume that, when Turing machines are encoded as strings, this is done using the Code-Word Language (CWL), with input alphabet $\{a,b\}$ and tape alphabet $\{a,b,\#,\Delta\}$.

- (a) The set of all palindromes of even length.
- (b) The set of all positive integers, in binary, whose number of bits is odd.
- (c) The set of all strings of correctly matched parentheses.
- (d) The set of all encodings of Turing machines that have at least three states.
- (e) The set of all encodings of Turing machines that have at most three states.
- (f) The set of all encodings of Turing machines that halt for some input.
- (g) The set of all goodings of ruring macrines that loop forever for all imputs.
- (h) The set of all satisfiable Bo
- (i) The set of all https://eduassistpro.github.io/every variable appears a
- (j) The set of all nondecreasing strings of digits, i.e that no digit is ever followed by Work digitate Casts okassis of the property of the control of the



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Question 15 (6 marks)

If L is a language and s is a string, then $L\Delta s$ denotes the language formed by removing s from L if it is there already, and adding s to L otherwise. In other words,

$$L\Delta s := \left\{ \begin{array}{l} L \setminus \{s\}, & \text{if } s \in L, \\ L \cup \{s\}, & \text{if } s \notin L. \end{array} \right.$$

Prove that L is decidable if and only if $L\Delta s$ is decidable.

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Question 16 (5 marks)

Below is a proof that the Halting Problem is undecidable. But some parts are missing; these are shown as blank spaces, underlined.

Your task is to fill in the underlined spaces to complete the proof. In some cases, options are given in square brackets.

Proof. Assume that the Halting Problem is actually decidable.

Then the Halting Problem has a decider D.

Using D, we can construct a Turing machine E that does the following:

- 1. Input: encoding of a Turing machine M.
- 2. Run decider D to determine whether or not M halts when given itself as input.
- 3. **IF** the answer from D is **Yes**, then

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4. **IF** the answe

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Now consider what happens if E is given, as input, an encoding of <i>itself</i> .	
If E halts on input E , then running D in line 2 gives the answer [Yes/No].	
So, using statement $___$ [3 or 4], we see that D actually $___$	·
On the other hand,	
if E does not halt on input E , then running D in line 2 gives the answer [Yes/No].	
So, using statement \dots [3 or 4], we see that D actually \dots	·
This is a contradiction.	
So the Halting Problem must be undecidable.	Official use only

Question 17 (6 marks)

Suppose you have an enumerator M_1 for a language L and another enumerator M_2 for its complement \overline{L} .

(a) Explain how to construct a decider for L that uses the enumerators M_1 and M_2 .

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(b) What does this tell you about recursively enumerable (r.e.) languages whose complements are also recursively enumerable? (Only one short sentence is required here.)

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Question 18 (13 marks)

A **perfect matching** in a graph G is a subset X of the edge set of G that meets each vertex exactly once. In other words, no two edges in X share a vertex, and each vertex of G is incident with exactly one edge in X.

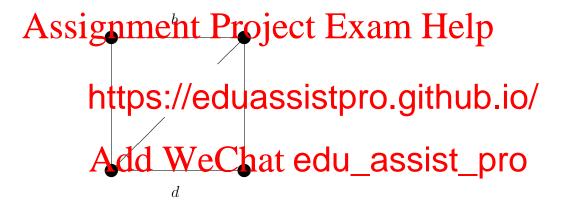
The PERFECT MATCHING decision problem is as follows.

PERFECT MATCHING

Input: Graph G.

Question: Does G have a perfect matching?

For example, in the following graph, the edge set $\{a, e\}$ is a perfect matching. But $\{a, b, e\}$ is not a perfect matching (since, for example, a and b share a vertex), and $\{a\}$ is not a perfect matching (since some vertices are not incident with the edge in this set).



Let W be the above graph.

(a) Construct a Boolean expression E_W in Conjunctive Normal Form such that the satisfying truth assignments for E_W correspond to perfect matchings in the above graph W.

(h)	Give a	nolynomial-time	reduction from	PERFECT MATCHING to SATISFIABILITY.
(1)	i Give a	. рогупоннал-инне	геансыон пош	EPDPPOLIMATOBLINGTOBALISPIADIDLIT.

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Question 19 (8 marks)

Prove that the GRAPH 4-COLOURABILITY problem is NP-complete, by reduction from GRAPH 3-COLOURABILITY. You may assume that GRAPH 3-COLOURABILITY is NP-complete.

Definitions:

For any positive integer k, a k-colouring in a graph G is an assignment of "colours" from the set $\{1, 2, ..., k\}$ to the vertices of G such that (a) each vertex gets exactly one colour from the set, and (b) adjacent vertices get different colours.

GRAPH 3-COLOURABILITY

Input: Graph G.

Question: Does G have a 3-colouring?

GRAPH 4-2018 RABILITY Project Exam Help

Question: Does G h

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END OF EXAMINATION