


3D Hierarchical Modelling

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Intended Learning Outcomes

- Understand the need of hierarchical structuring for building articulated 3D objects
- Able to compute the relative coordinate transform between comp
- Able to represent object as a hierarchical structure using 

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Problem:

- Given a large number of graphics models which form parts of a whole object, it is cumbersome to animate each part by individual commands

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Example : Animate a car moving at a speed of 20 miles and in direction (2, 3, 4)

```
main ()
```

```
{
```

```
float s = 20.0; /* speed */
```

```
float d[3] = {2.0, 3.0, 4.0}; /* direction */
```

```
draw_chassis (s, d);
```

```
draw_right_front_wheel (s, d);
```

```
draw_left_front_wheel (s, d);
```

```
draw_right_rear_wheel (s, d);
```

```
draw_left_rear_wheel (s, d);
```

```
}
```

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Tree with directed edge

Bad Programming - Redundancy: the 4 draw wheel functions can be replaced by one function

Introduction of hierarchical structures

- Use *relative transformation* to link the movements of different parts
- Use a single function for a unique (single) part

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Directed Acyclic Graph (DAG)

- DAG is a graph with directed arc but no cycle
- It is a tree but additional allows more than one arc from a node

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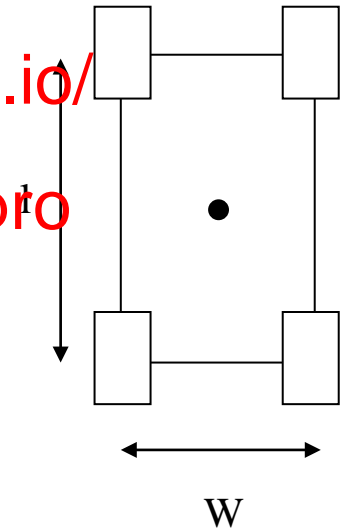
Revised program

```
main ()
{
    float s = 20.0;
    float d[3] = {2.0, 3.0, 4.0};
    float w = 2.0, l = 4.0; // width and length of the car

    draw_chass (s, d);

    glTranslatef ( w/2 , l/2, 0 );
    draw_wheel (s, d);
    glTranslatef ( -w, 0, 0 ); // position the left front
    draw_wheel (s, d);
    glTranslatef ( 0, -l, 0 ); // position the left rear wheel
    draw_wheel (s, d);
    glTranslatef ( w, 0, 0 ); // position the right rear wheel
    draw_wheel (s, d);
}
```

Let the initial coordinate system be the centroid of the car



We can make it more systematic by formally introducing coordinate system change, which we do below

Moving a Robot Arm – a 3 level hierarchy

Parts : **base B** (cylinder),

lower arm La (rectangular box)

upper arm Ua (rectangular box)

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Arm has 3 degree of fre

B rotate about Y by <https://eduassistpro.github.io/>

La rotate about Z by ϕ

Ua rotate about Z by ψ Add WeChat edu_assist_pro

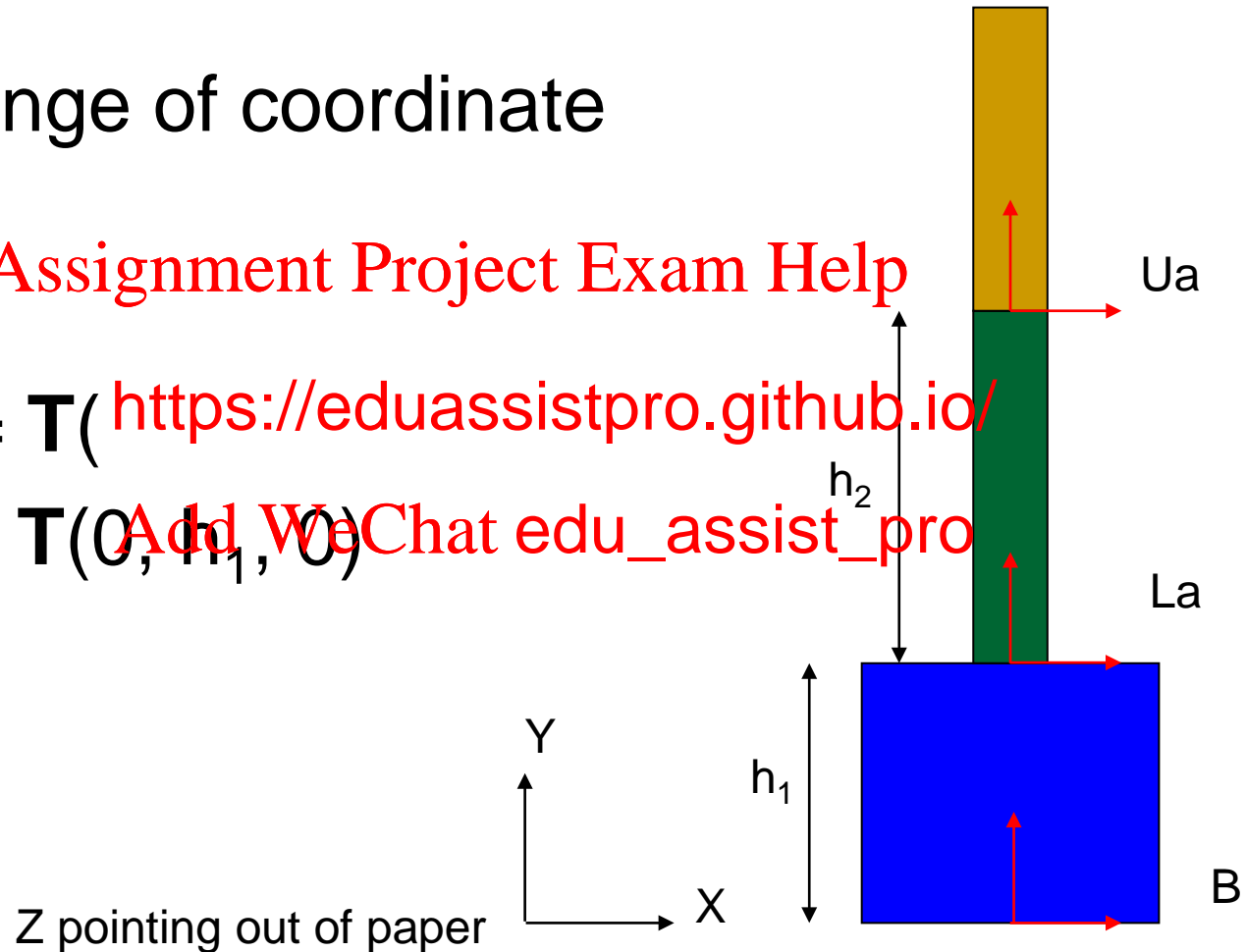
Relative Coordinate Transformations

- Use Change of coordinate system:

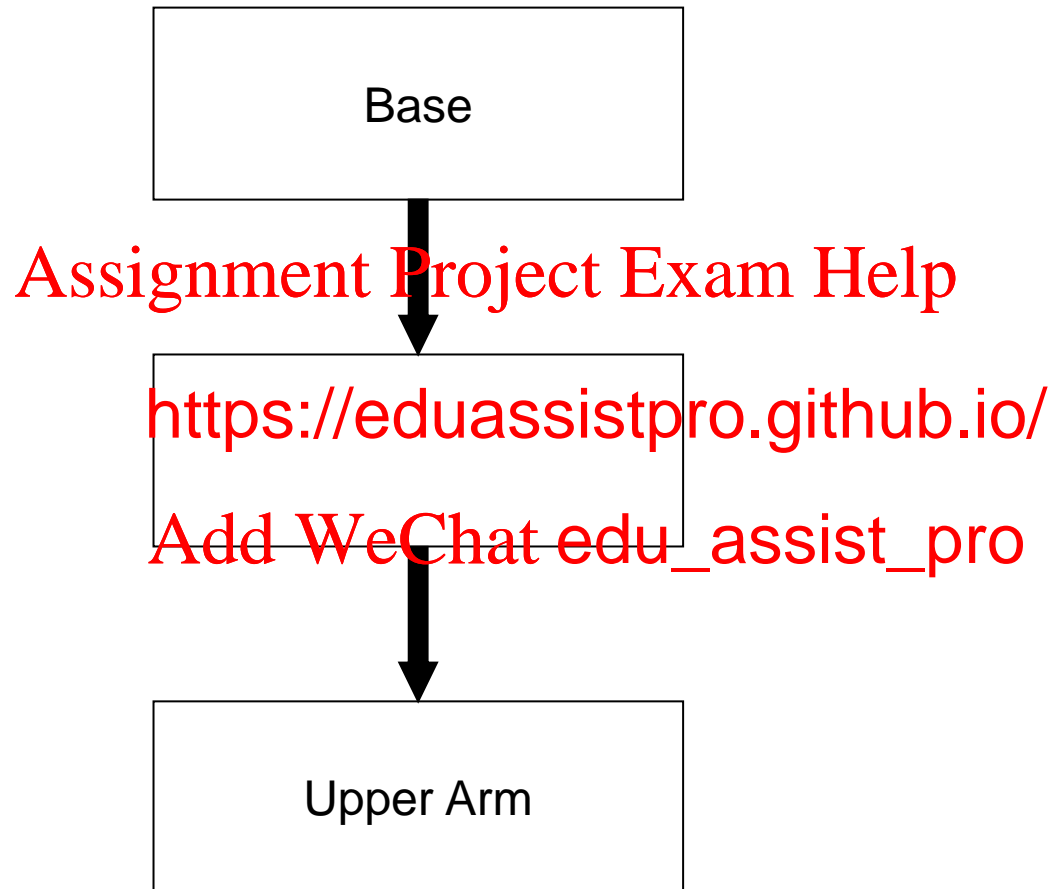
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- $\mathbf{M}_{La \leftarrow Ua} = \mathbf{T}(\text{https://eduassistpro.github.io/}$

- $\mathbf{M}_{B \leftarrow La} = \mathbf{T}(0, h_1, 0)$ Add WeChat edu_assist_pro



DAG



Write a program to ...

- Rotate the robot arm about its base by θ , then about its lower arm by ϕ , then about its upper arm by ψ

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- when rotating the lower arm, the upper arm should move; but when rotating the upper arm, only the upper arm should move.
- Solve this using a hierarchy concept

Program

```
robot_arm ()
{
    glRotatef (theta, 0.0, 1.0, 0.0); //  $\mathbf{R}_y(\theta)$  rotate the whole robot arm

    // each point of whole robot arm will be pre-multiplied by  $\mathbf{R}_y(\theta)$ 
    base ();

    glTranslatef (0.0, h1, 0.0); // coord. sy. to base coord. sy.
    glRotatef (phi, 0.0, 0.0, 1.0); //  $\mathbf{R}_z(\phi)$  in coord. sy.

    // each point of lower arm will be pre-multiplied by  $\mathbf{T}(0, h_1, 0)\mathbf{R}_z(\phi)$ 
    lower_arm ();

    glTranslatef (0.0, h2, 0.0); //  $\mathbf{M}_{La \leftarrow Ua}$  changes upper arm coord. sy. to lower arm coord. sy.
    glRotatef (psi, 0.0, 0.0, 1.0);

    // each point of upper arm will be pre-multiplied by  $\mathbf{R}_y(\theta)\mathbf{T}(0, h_1, 0)\mathbf{R}_z(\phi)\mathbf{T}(0, h_2, 0)\mathbf{R}_z(\psi)$ 
    upper_arm ();
}
```

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Moving a Robot

- Need to organize the hierarchy better
- Solution: use *glPushMatrix* and *glPopMatrix* to store and retrieve intermediate composite relative transformations

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Program

```
Robot ()
{
    glPushMatrix ();
    torso;

    glTranslate ...
    glRotate ...
    head ();

    glPopMatrix ();          /
    glPushMatrix ();

    glTranslate ...          /
    glRotate ...             // used in example 2
    left_upper_arm ();
    glTranslate ...
    glRotate ...
    left_lower_arm ();

    glPopMatrix ();          // go back to the node of the torso
    glPushMatrix ();

    glTranslate ...
    glRotate ...
    right_upper_arm ();

    :
}
```

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References

- Our exposition follows:

E. Angel, Interactive Computer Graphics: A Top-down Approach Using OpenGL, 5th Ed. (2009), Ch. 10.1-10.4

- Ch. 11 of text reference.

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