Parallel Computing with GPUs: Parallel

Dr Paul Ric

http://paulrichmond.shef.ac

COM4521/

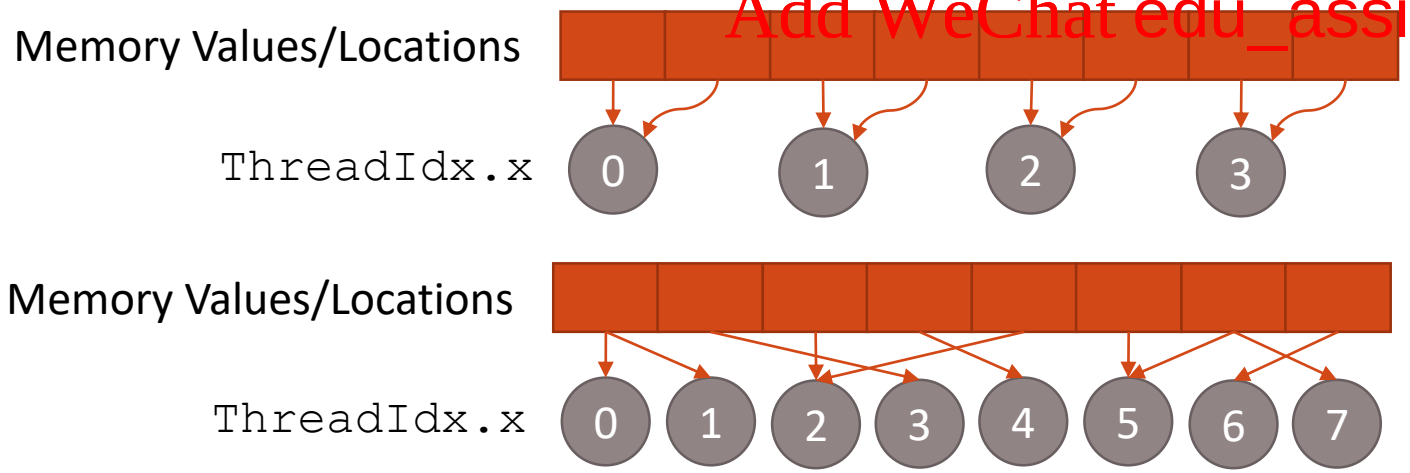
- Parallel Patterns Overview
- Reduction
- Scan

What are parallel Patterns

- Parallel patterns are high level building blocks that can be used to create algorithms
- Implementation is abstracted to give a higher level view
- Patterns describe techniques suited to parallelism
  - Allows algorithms to b om ground up
  - Top down approach ally…
- Consider a the simplest parallel pat
  - Takes the input list *i*
  - Applies a function *f*
  - Writes the result list *o* by applying *f* to all members of *i*
  - Equivalent to a CUDA kernel where *i* and *o* are memory locations determined by `threadIdx` etc.

Gather

- Multiple inputs and single coalesced output
- Might have sequential loading or random access
  - Affect memory performance
- Differs to map due to multiple inputs

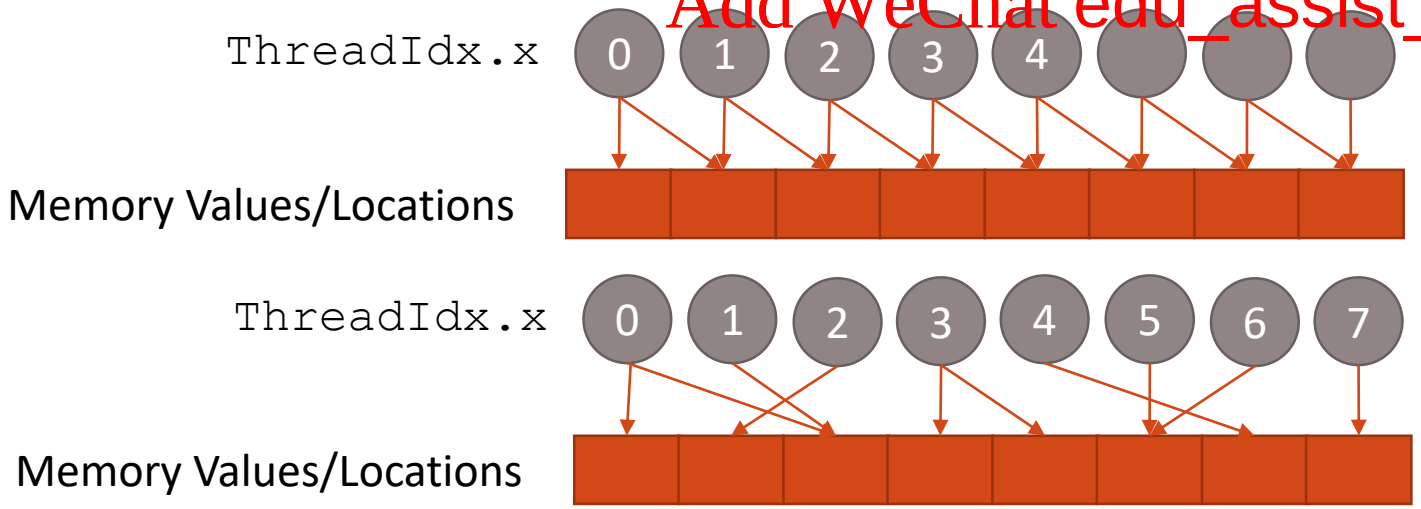


Gather operation
- Read from a number of locations

Gather operation
- Read from a number of locations
- Random access load

Scatter

- Reads from a single input and writes to one or many
- Can be implemented in CUDA using atomics
- Write pattern will determine performance

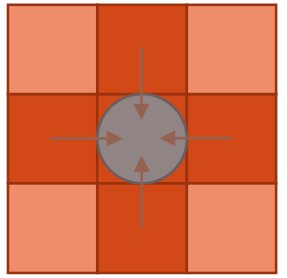


Scatter operation
- Write to a number of locations
- Collision on write

Scatter operation
- Write to a number of locations
- Random access write?

Other Parallel Patterns

- Stencil
  - Gather a fixed pattern, usually based on locality
  - See 2D shared memory examples
- **Reduce (this lecture)**
  - Reduce value to a sing e pairs
  - Combined with Map t with intermediate shuffle or sort)
- **Scan (this lecture)**
  - Compute the sum of previous value in a set
- Sort (*later*)
  - Sort values or <value, key> pairs



Stencil Gather

- ❑Parallel Patterns Overview
- ❑Reduction
- ❑Scan

Reduction

- A reduction is where **all** elements of a set have a common *binary associative operator* ($\oplus$) applied to them to "reduce" the set to a single value
  - Binary associative = order in which operations is performed on set does not matter
    - E.g. `(1 + 2) + 3 + 4 == 1 + (2 + 3) + 4 == 10`
- Example operators
  - Most obvious example is a
  - Other examples, Maximum
- Serial example is trivial but how does this allel?


```
int data[N];
int i, r;
for (int i = 0; i < N; i++){
  r = reduce(r, data[i]);
}
```

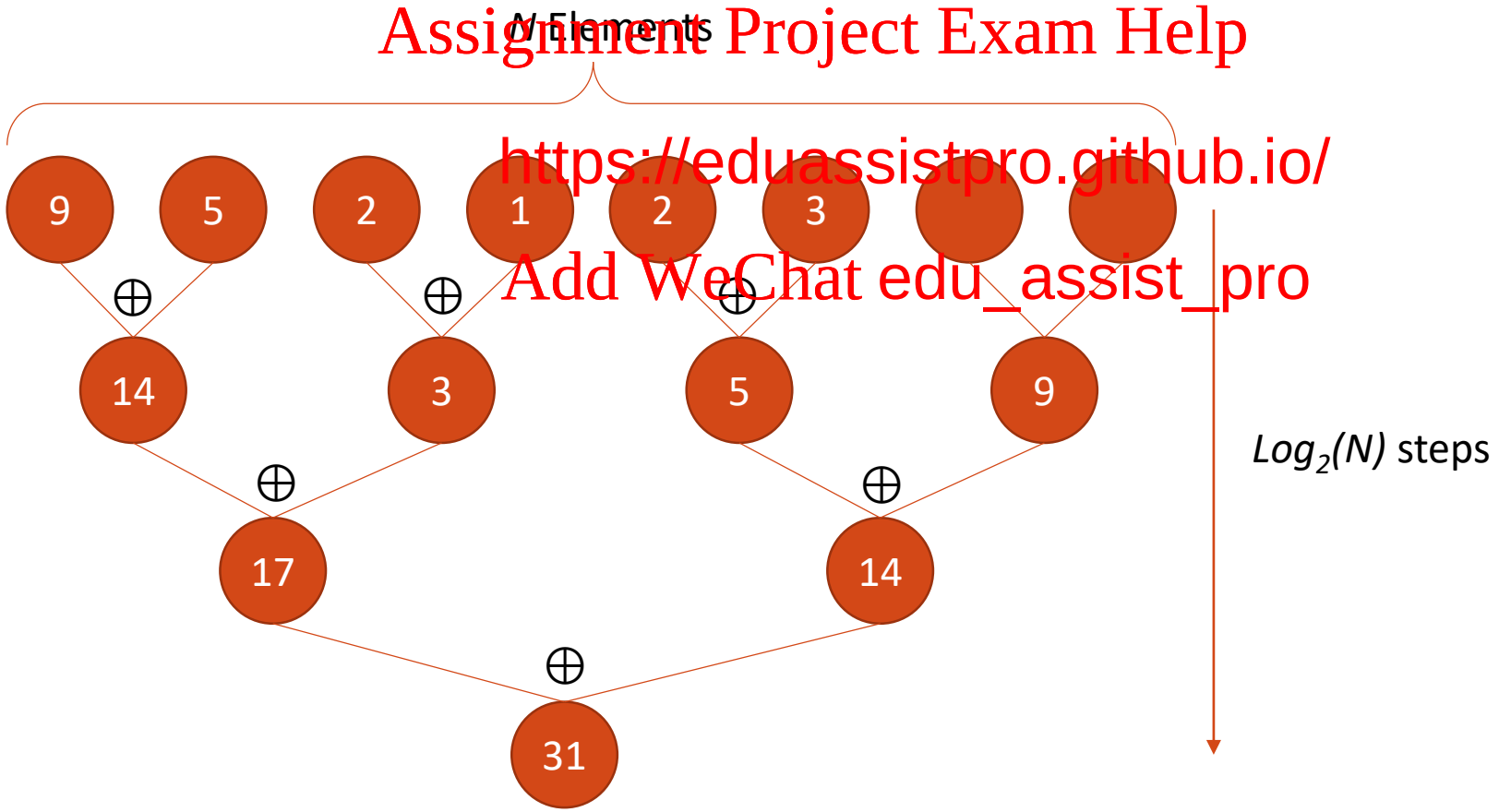
OR

```
int data[N];
int i, r;
for (int i = N-1; i >= 0; i--){
  r = reduce(r, data[i]);
}
```

```
int reduce(int r, int i){
  return r + i;
}
```

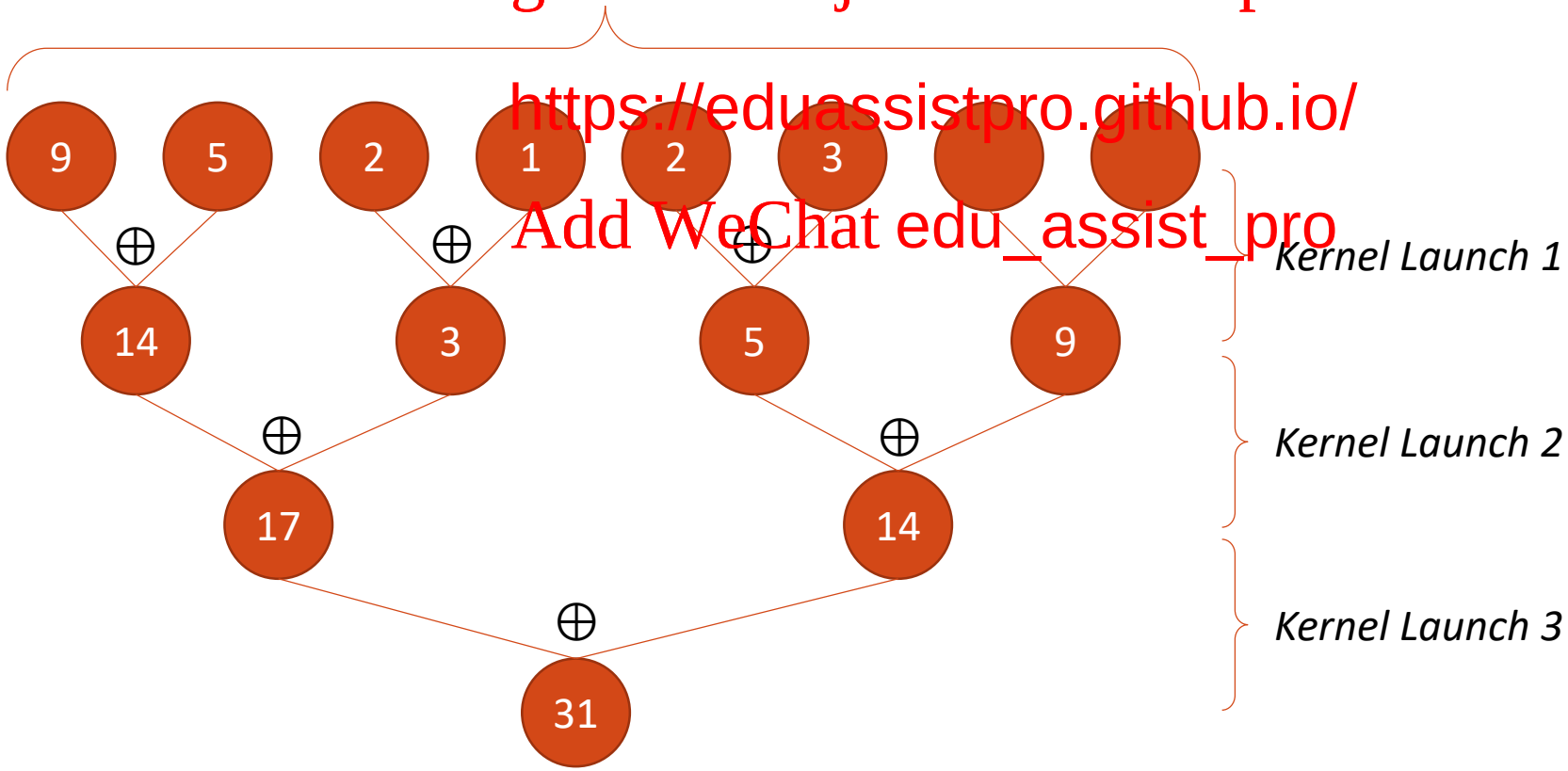
Parallel Reduction

- Order of operations does not matter so we don't have to think serially.
- A tree based approach can be used
  - At each step data is reduced by a factor of 2



Parallel Reduction in CUDA

- No global synchronisation so how do multiple blocks perform reduction?
- Split the execution into multiple stages
  - Recursive method



Recursive Reduction Problems

- What might be some problems with the following?

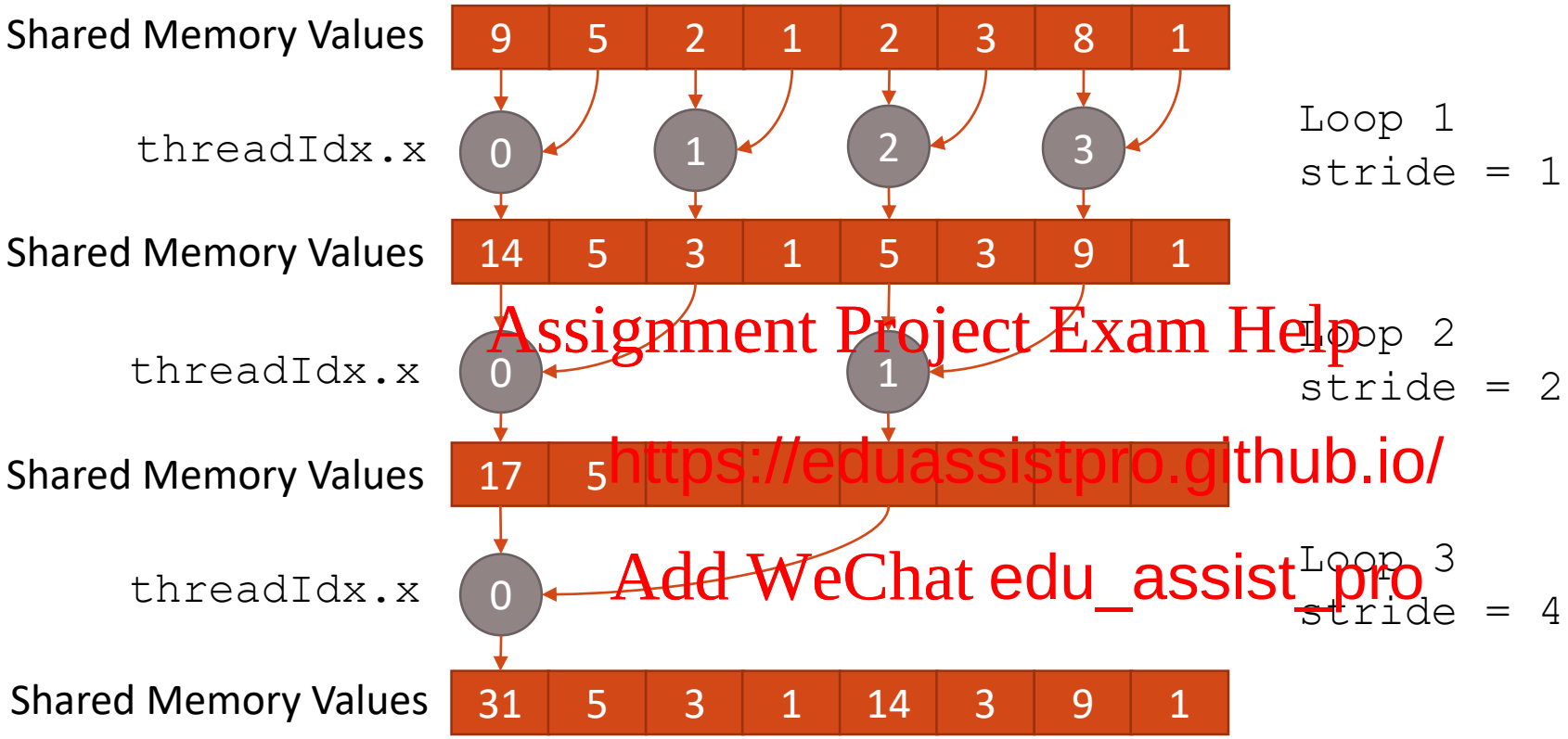

```
__global__ void sum_reductio                                    lts){

  extern __shared__ int sdata[];
  unsigned int i = blockIdx.x*blockDim.x + threadIdx.x;

  sdata[threadIdx.x] = input[i];
  __syncthreads();

  if (i % 2 == 0){
    results[i / 2] = sdata[threadIdx.x] + sdata[threadIdx.x+1]
  }

}
```

Block Level Reduction

- Lower launch overhead (reduction within block)
- Much better use of shared memory

```
__global__ void sum_reduction(float *input, float *block_results){
  extern __shared__ int sdata[];

  unsigned int i = blockIdx.                          ;
  sdata[threadIdx.x] = input
  __syncthreads();

  for (unsigned int stride = 1; stride < blo          de*=2){
    unsigned int strided_i = threadIdx.x * 2
    if (strided_i < blockDim.x){
      sdata[strided_i] += sdata[strided_i + stride]
    }
    __syncthreads();
  }

  if (threadIdx.x == 0)
    block_results[blockIdx.x] = sdata[0];
}
```

Block Level Recursive Reduction



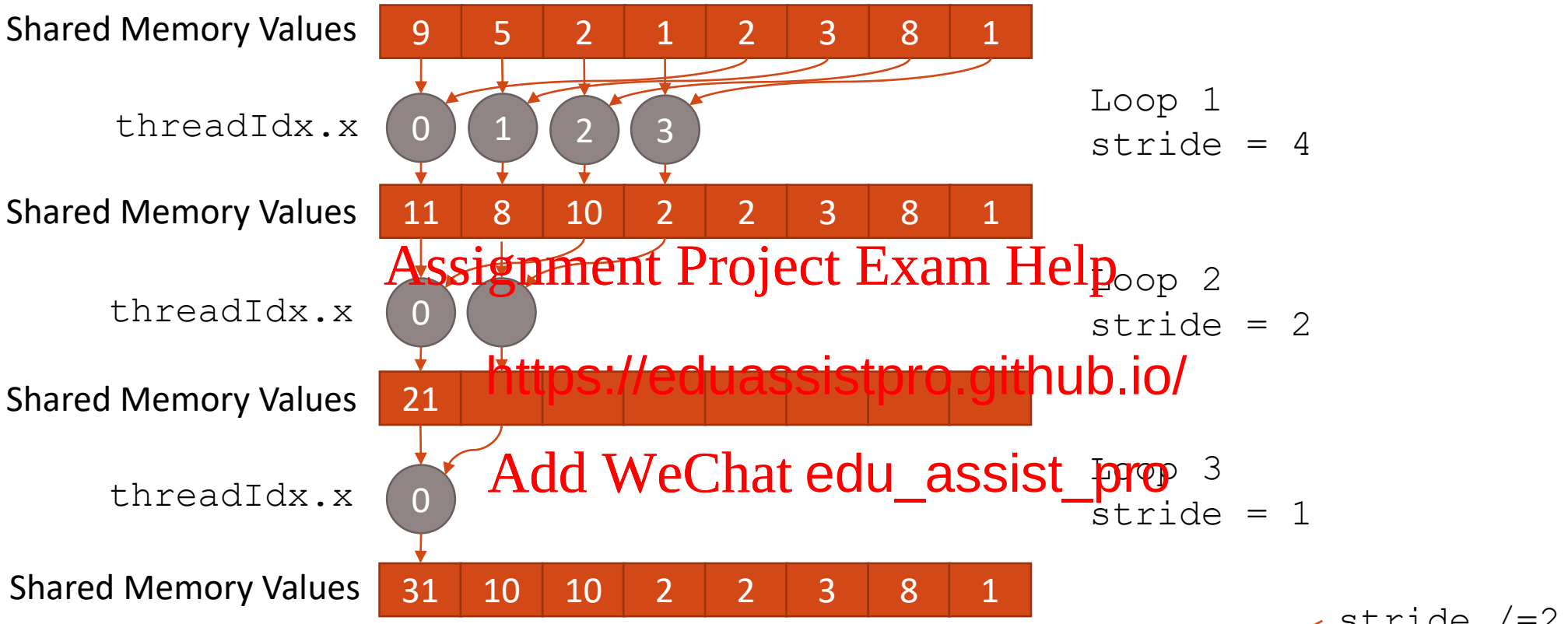

```
for (unsigned int stride = 1; stride < blockDim.x; stride*=2){
  unsigned int strided_i = threadIdx.x * 2 * stride;
  if (strided_i < blockDim.x){
    sdata[strided_i] += sdata[strided_i + stride]
  }
  __syncthreads();
}
```

Block Level Reduction

- Is this shared memory access pattern bank conflict free?


```
for (unsigned int stride = 1; stride < blockDim.x; stride*=2){
  unsigned int stri                                    de;
  if (strided_i < b
    sdata[strided_i
  }
  __syncthreads();
}
```

Block Level Reduction (Sequential Addressing)




```
for (unsigned int stride = blockDim.x/2; stride > 0; stride>>=1){
  if (threadIdx.x < stride){
    sdata[threadIdx.x] += sdata[threadIdx.x + stride]
  }
  __syncthreads();
}
```

stride /=2

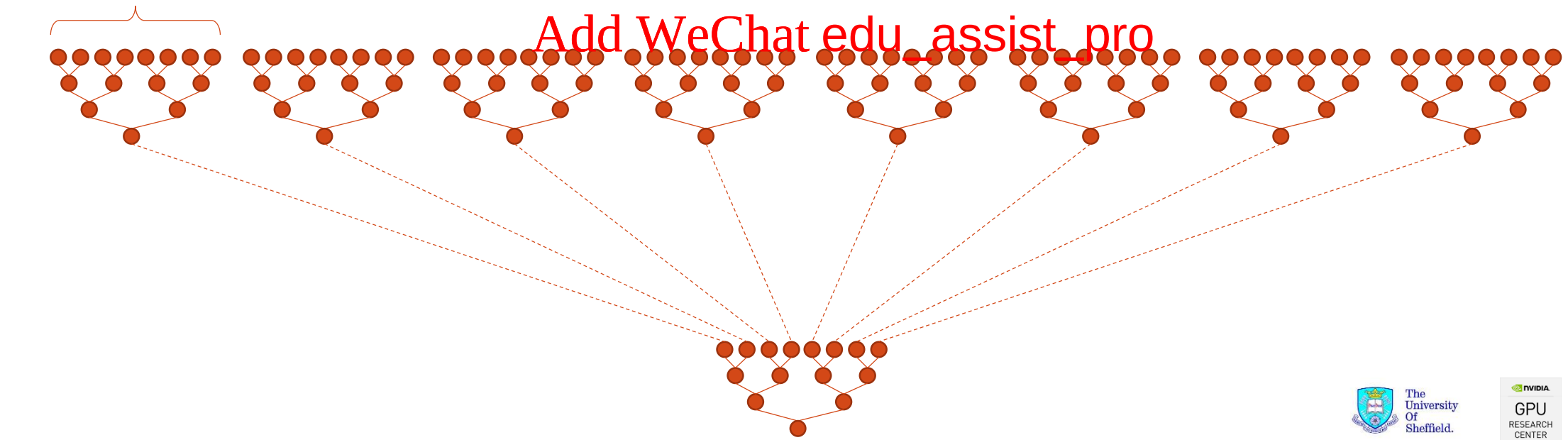
sm_stride	1			
loop stride	1			
threadIdx.x			index	bank
0			1	1
1			2	2
2			3	3
3			4	4
4			5	5
5			6	6
6			7	7
7			8	8
8			9	9
9			10	10
10			11	11
11			12	12
12			13	13
13			14	14
14			15	15
15			16	16
16			17	17
17			18	18
18			19	19
19			20	20
20			21	21
21			22	22
22			23	23
23			24	24
24			25	25
25			26	26
26			27	27
27			28	28
28			29	29
29			30	30
30			31	31
31			32	0
			Banks Used	32
			Max Conflicts	1

- Now conflict free regardless of the reduction loop stride
- The stride between shared memory variable accesses for threads is *always* sequential

- Caref pes of stride discussed
  1. Loop stride (of algorithm)
  2. SM *variable* stride (in 4 bytes)

Global Reduction Approach

- Use the recursive method
  - Our block level reduction can be applied to the result
  - At some stage it may be more effective to simply sum the final block on the CPU
- Or use atomics on blo



Global Reduction Atomics

```
__global__ void sum_reduction(float *input, float *result){
  extern __shared__ int sdata[];

  unsigned int i = blockIdx.x*blockDim.x + threadIdx.x;
  sdata[threadIdx.x] = input[i];
  __syncthreads();

  for (unsigned int stride =                    stride>>=2){
    if (threadIdx.x < stride
      sdata[threadIdx.x] += sdata[threadIdx.
    }
    __syncthreads();
  }

  if (threadIdx.x == 0)
    atomicAdd(result, sdata[0]);
}
```

Further Optimisation?

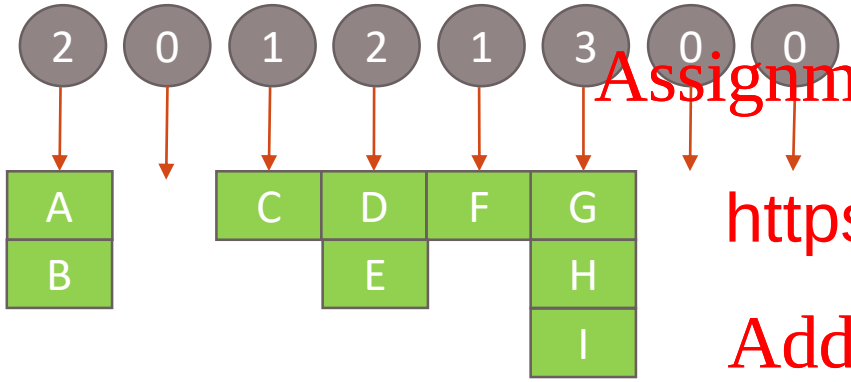
- Can we improve our technique further?

```
__global__ void sum_reduction(float *input, float *result){
  extern __shared__ int sdata[];

  unsigned int i = blockIdx.x*blockDim.x + threadIdx.x;
  sdata[threadIdx.x] = in
  __syncthreads();

  for (unsigned int stride = blockDim.x/2             ; stride>>=2){
    if (threadIdx.x < stride){
      sdata[threadIdx.x] += sdata[threadI              e]
    }
    __syncthreads();
  }

  if (threadIdx.x == 0)
    atomicAdd(result, sdata[0]);
}
```

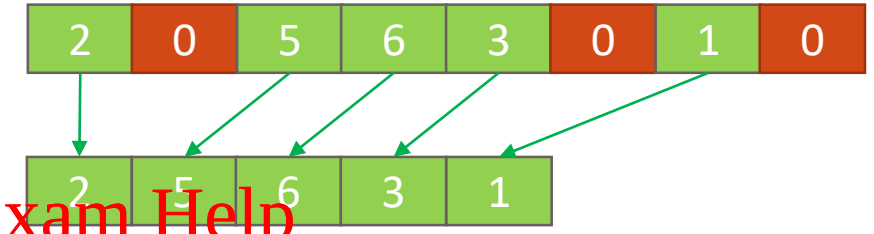
- ❑Parallel Patterns Overview
- ❑Reduction
- ❑Scan

What is scan?

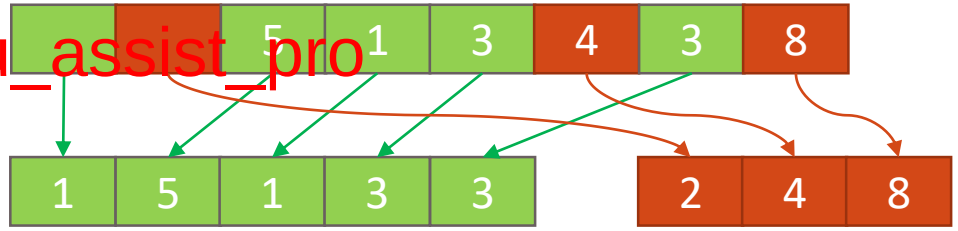
❑Consider the following …



Output variable numbers of values per thread



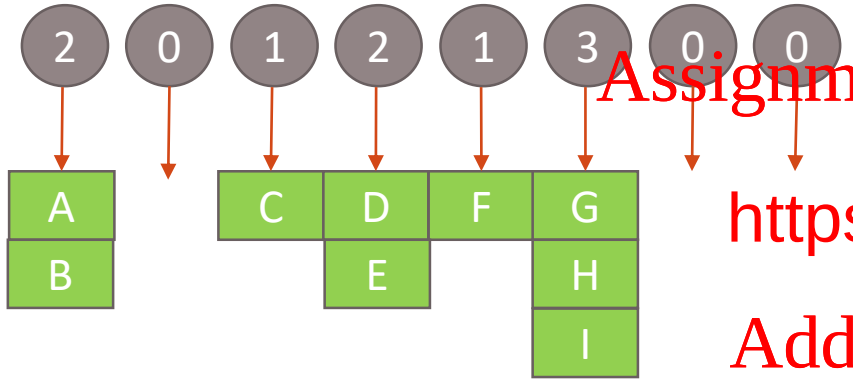
ve empty elements from array (compact)



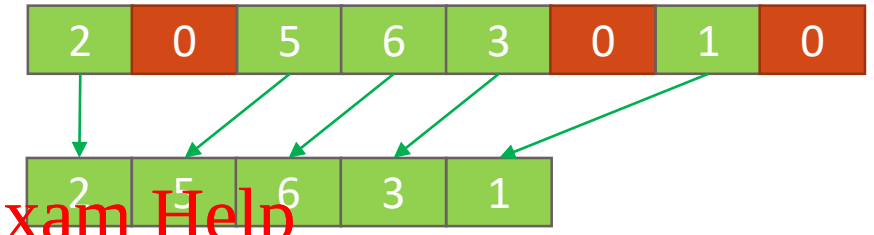
Split elements from array based on condition (split)

What is scan?

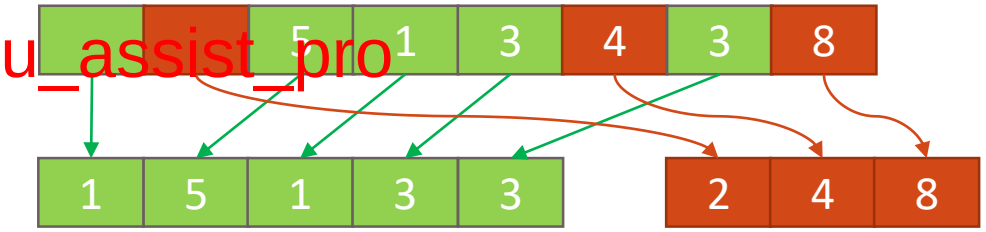
- Consider the following …



Output variable numbers of values per thread



ve empty elements from array (compact)

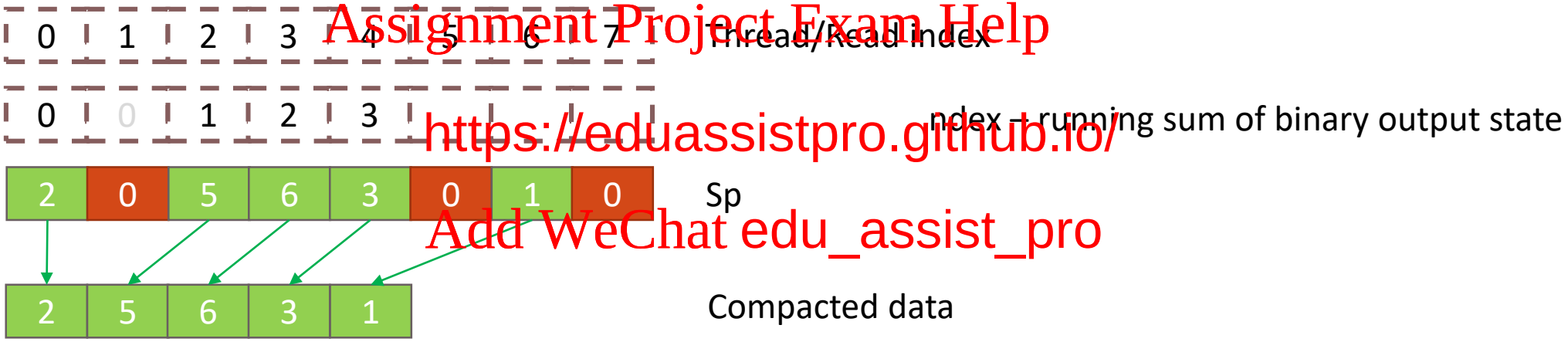


Split elements from array based on condition (split)

- Each has the same problem
  - Not even considered for sequential programs!
- Where to write output in parallel?

Parallel Prefix Sum (scan)

- Where to write output in parallel?
  - Each threads needs to know the output location(s) it can write to avoid conflicts.



- The solution is a parallel prefix sum (or scan)
  - Given the inputs $A = [a_0, a_1, \ldots, a_{n-1}]$ and binary associate operator $\oplus$
  - $Scan(A) = [0, a0, (a_0 \oplus a_1), \ldots, (a_0 \oplus a_1 \oplus \ldots \oplus a_{n-1})]$

Serial Parallel Prefix Sum Example

- E.g. Given the input and the addition operator
  - A= [2, 6, 2 ,4, 7, 2 ,1, 5]
  - Scan(A) = [0, 2, 2+6, 2+6+2, 2+6+2+4, …]
  - Scan(A) = [0, 2, 8, 10, 14, 21, 23, 24]
- More generally a seri n additive scan using a running sum looks like


```
int A[8] = { 2, 6, 2, 4,          ;
int scan_A[8];
int running_sum = 0;
for (int i = 0; i < 8; ++i)
{
  scan_A[i] = running_sum;
  running_sum += A[i];
}
```

Serial Scan for Compaction

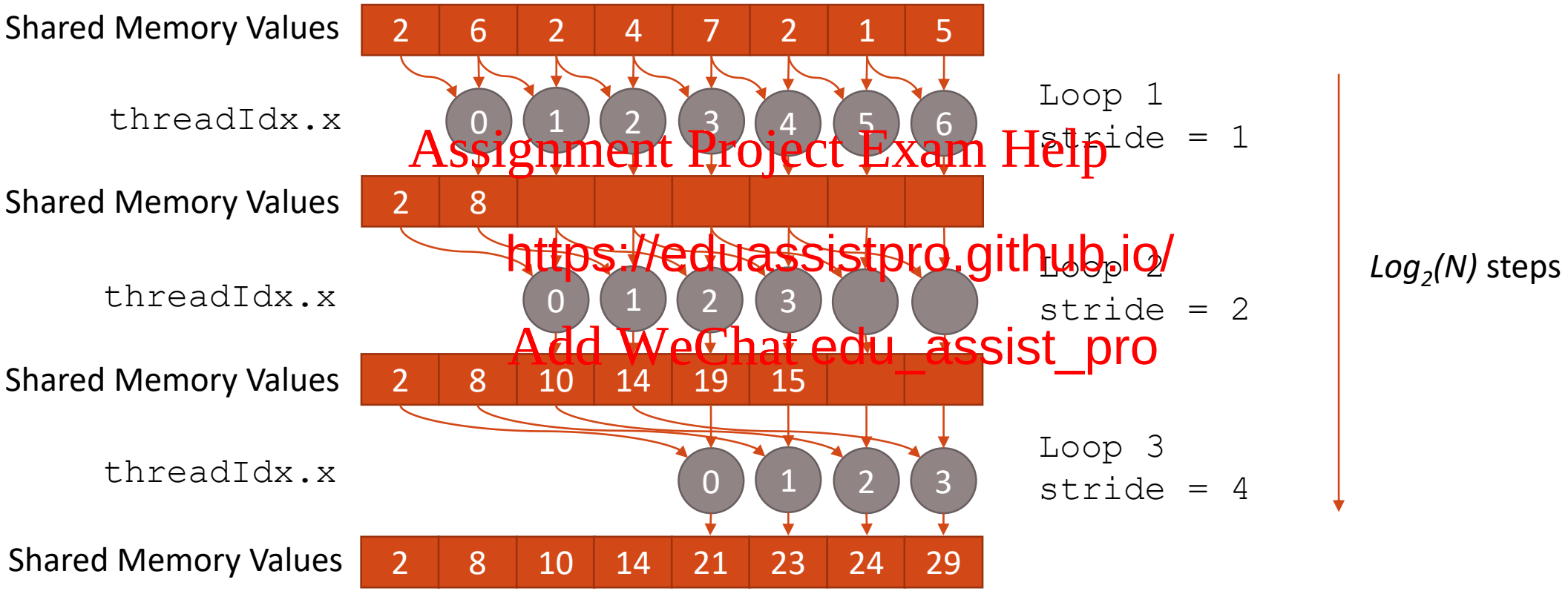
```
int Input[8] = { 2, 0, 5, 6, 3, 0, 1, 0 };
int A[8] =     { 2, 0, 5, 6, 3, 0, 1, 0 };
int scan_A[8];
int output[5]
int running_sum = 0;

for (int i = 0; i < 8; ++i){
  A[i] = Input>0;
}

for (int i = 0; i < 8; ++i){
  scan_A[i] = running_sum;
  running_sum += A[i];
}

for (int i = 0; i < 8; ++i){
  int input = Input[i];
  if (input > 0){
    int idx = scan[i];
    output[idx] = input;
  }
}
```



```
// generate scan input
// A = {1, 0, 1, 1, 1, 0, 1, 0}

                    = {0, 1, 1, 2, 3, 4, 4, 5}

// scattered write
// output = {2, 5, 6, 3, 1}
```

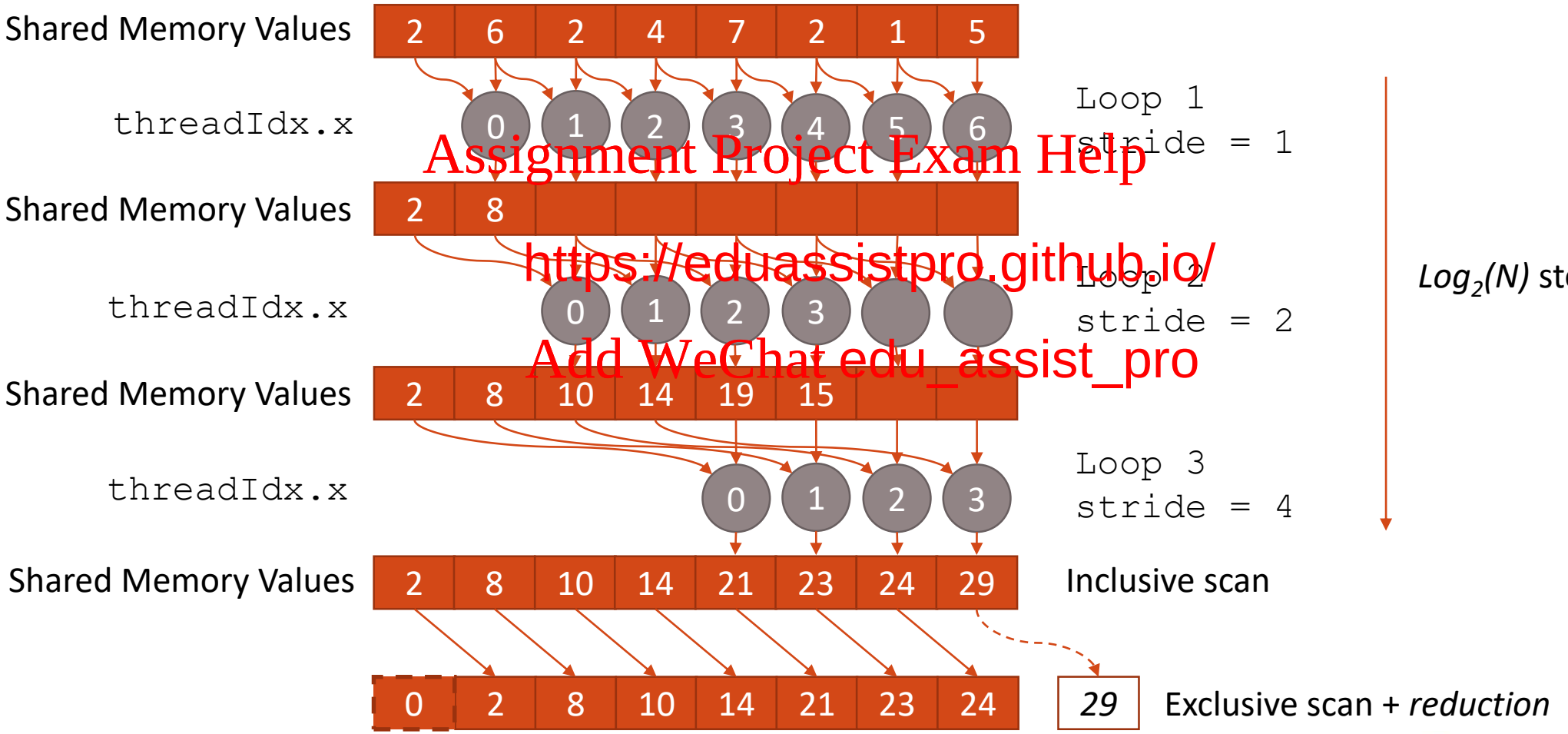
Parallel Local (Shared Memory) Scan

After Log(*N*) loops each sum has local plus preceding 2^n-1 values



Inclusive Scan

Parallel Local Scan



Implementing Local Scan with Shared Memory

```
__global__ void scan(float *input) {
  extern __shared__ float s_data[];
  s_data[threadIdx.x] = input[threadIdx.x + blockIdx.x*blockDim.x];

  for (int stride = 1; stride<blockDim.x; stride<<=1) {
    __syncthreads();
    float s_value = (threadIdx.x >= stride) ? s_data[threadIdx.x - stride] : 0;
    __syncthreads();
    s_data[threadIdx.x] += s_va
  }

  //something with global results?
}
```

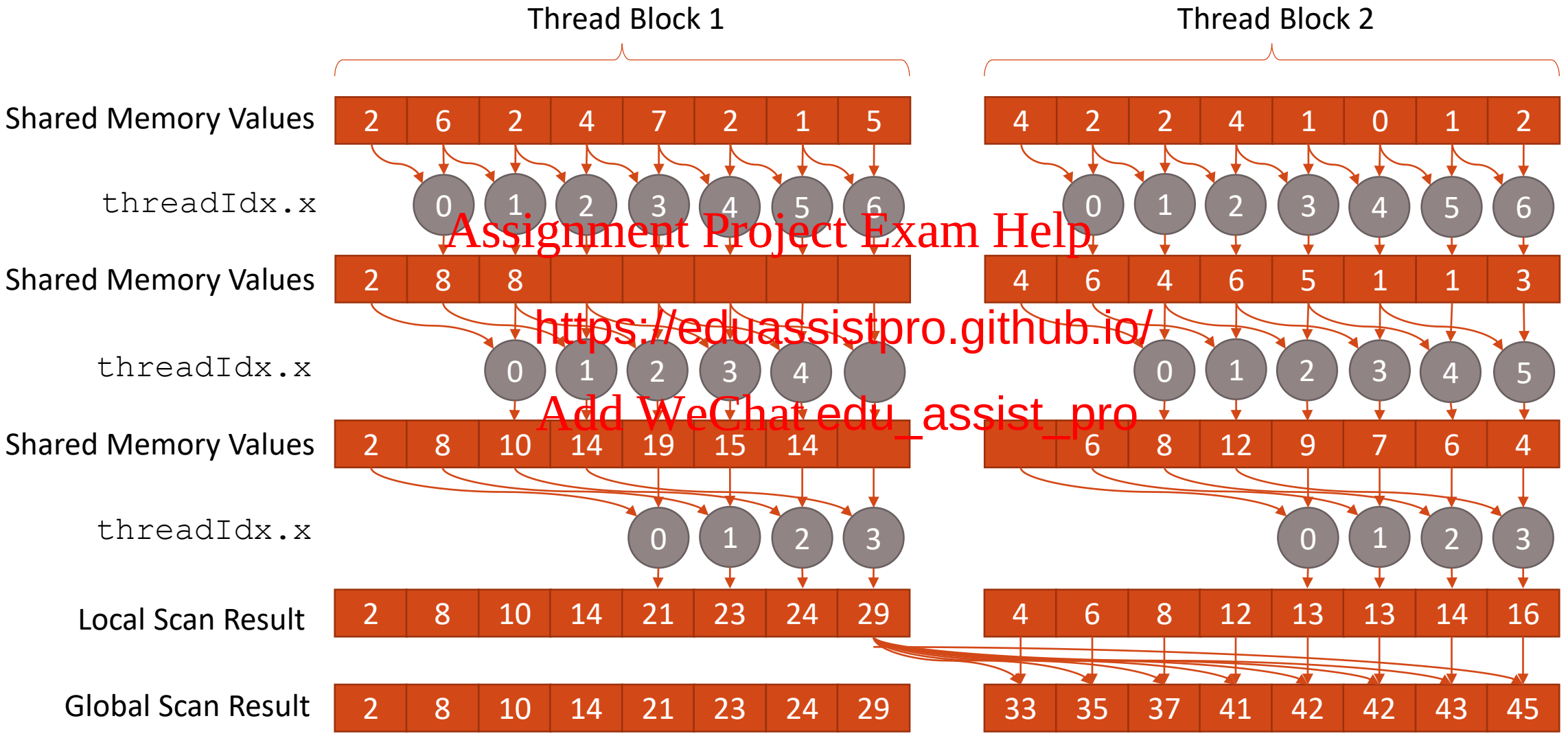

- No bank conflicts (stride of 1 between threads)
- Synchronisation required between read and write

Implementing Local Scan (at warp level)

```
__global__ void scan(float *input) {
  __shared__ float s_data[32];
  float val1, val2;

  val1 = input[threadIdx.x + blockIdx.x*blockDim.x];

  for (int s = 1; s < 32; s <<= 1) {
    val2 = __shfl_up(val1, s);
    if (threadIdx.x % 32 >= s)
      val1 += val2;
  }

  //store warp level results}
```


- Exactly the same as the block level technique but at warp level
- Warp prefix sum is in `threadIdx.x%32==31`
- Either use shared memory to reduce between warps
  - Or consider the following global scan approaches.

Implementing scan at Grid Level



Implementing scan at Grid Level

- Same problem as reduction when scaling to grid level
  - Each block is required to add the reduction value from proceeding blocks

- Global scan therefore requires either;
  1. Recursive scan kern
     - Additional kernel to
  2. **Atomic Increments (next slides)**
     - **Increment a counter for block level results**
     - **Additional kernel to add sums of proceeding blocks to each value**

Global Level Scan (Atomics Part 1)

```
__device__ block_sums[BLOCK_DIM];

__global__ void scan(float *input, float *local_result) {
  extern __shared__ float s_data[];
  s_data[threadIdx.x] = input[threadIdx.x + blockIdx.x*blockDim.x];

  for (int stride = 1; stride<blockDim.x; stride<<=1) {
    __syncthreads();
    float s_value = (thread                              threadIdx.x - stride] : 0;
    __syncthreads();
    s_data[threadIdx.x] += s_value;
  }

  //store local scan result to each thread
  local_result[threadIdx.x + blockIdx.x*blockDim.x] = s_data[threadIdx.x];

  //atomic store to all proceeding block totals
  if (threadIdx.x == 0){
    for (int i=0; i<blockIdx.x; i++)
      atomicAdd(&block_sums[i], s_data[blockDim.x-1]);
  }
}
```

Global Level Scan (Atomics Part 2)

- After completion of the first kernel, block sums are all synchronised
- Use first thread in block to load block total into shared memory
- Increment local result


```
__device__ block_sums[BLOCK_DIM];

__global__ void scan_update(int *local_result, int *global_result) {
  extern __shared__ float block_total;
  int idx = threadIdx.x + blockIdx.x*block

  if (threadIdx.x == 0)
    block_total = block_sums[blockIdx.x];

  __syncthreads();

  global_result[idx] = local_result[idx]+block_total;
}
```

Summary

- Parallel Patterns create a bottom up model for constructing algorithms from parallel building blocks
- Reduction can be implemented recursively however re-use of data avoid costly memory movement operations
- Scan is a building bloc ems
  - Can be used for comp
- Parallel patterns can be optimised read block and grid levels.
- Atomics can be used in the reduction or scan value summation between blocks or warps
- Lots of potential techniques to implement and evaluate
  - Fortunately in many cases libraries and examples already exist

Acknowledgements and Further Reading

- https://devblogs.nvidia.com/parallelforall/faster-parallel-reductions-kepler/
  - All about application of warp shuffles to reduction
- https://stanford-cs193g-sp2010.googlecode.com/lecture_6/parallel_patterns_1.ppt
  - Scan material based loosely on this le
- http://docs.nvidia.com/cuda/samples/6_Advanced/reduction/doc/reduction.pdf
  - Reduction material is based on this fantastic lecture by Mark Harris (NVIDIA)