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# COMP3161/COMP9164 Supplementary Lecture Notes Overloading

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So far, all the operations we hav type, as for example additionally such and type at all, such a hit ps://eduassistpro.giththey.worko/

In practice, this is not sufficient for a general purpose language. If we add, for example, floating point numbers to MinHS, we want at least all the operations we have on integers to be available on floats as well so we need (+xxxx): Eleat + Float + Float + However, this would make the language pretty amoving yours, and get even werse ignored language with a more realistic set of types, including integers and floats of different size.

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### 1 Type Classes in Haskellhat edu\_assist\_pro

The idea behind type classes is to group a set of types together if they hav similar operations in common. For example, in Haskell, the type class within which the *methods* addition, multiplication, subtraction and such are defined is called Num, and contains the types Int, Integer (not fixed length), Float and Double.

For example, the type of addition is:

```
(+) \ : \forall \ a. \ \mathtt{Num} \ a \ \Rightarrow \ a \ \rightarrow \ a \rightarrow \ a
```

which reads as: for all types a in type class Num, (+) has the type  $a \Rightarrow a \rightarrow a \rightarrow a$ . The constraint Num restricts the types which addition can be applied to.

The Eq type class in Haskell contains all types whose elements can be tested for pairwise equality. When you type :info Eq into GHCi, the interpreter lists all its methods:

```
 (==) \ :: \ \mathsf{Eq} \ a \ \Rightarrow \ a \ \rightarrow \ a \ \rightarrow \ \mathsf{Bool}   (/=) \ :: \ \mathsf{Eq} \ a \ \Rightarrow \ a \ \rightarrow \ a \ \rightarrow \ \mathsf{Bool}
```

Also listed are the types which are in this type class. Basic integral types are included:

instance Eq Int instance Eq Float instance Eq Double instance Eq Char instance Eq Bool

Also, generative rules that specify instances that themselves depend on another instance:

instance Eq 
$$a \Rightarrow$$
 Eq  $[a]$   
instance Eq  $a \Rightarrow$  Eq (Maybe  $a$ )  
instance (Eq  $a$ , Eq  $b$ )  $\Rightarrow$  Eq  $(a, b)$ 

These are rules about type class membership: if a type a is in Eq, then lists of a are also in Eq, as well as Maybe a. If two types a and b are both in Eq, so are pairs of a and b. Operations on these compound types are implemented in terms of the operations of the argument types. So, two pairs of values are considered to be equal if both of their components are equal:

$$\begin{array}{l} \textbf{instance} \; (\texttt{Eq} \; a, \texttt{Eq} \; b) \; \Rightarrow \; \texttt{Eq} \; (a,b) \; \textbf{where} \\ (==) \; (a_1,b_1) \; (a_2,b_2) = (a_1 == a_2) \; \&\& \; (b_1 == b_2) \end{array}$$

And equality of lists can be defined, for example, as follows:

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Other examples of predefined type classes are Show and Read. A user can extend these type classes and define new Assestgnment Project Exam Help

#### 2 SAssignment Project Exam Help

We write:

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Extending implicitly typed MinHS with type classes, we all type variables:  $A dd W e C h at edu\_assist\_pro$ 

Predicates  $P ::= C \tau$ Polytypes  $\pi ::= \tau \mid \forall a. \ \pi \mid P \Rightarrow \pi$ Monotypes  $\tau ::= \text{Int} \mid \text{Bool} \mid \tau + \tau \mid \cdots$ Class names C

Our typing judgement  $\Gamma \vdash e : \pi$  now includes a set of type class axiom schema A:

$$\mathcal{A} \mid \Gamma \vdash e : \pi$$

This set contains predicates for all type class instances known to the compiler, including generative instances, which take the form of implications like Eq  $a \Rightarrow$  Eq [a].

To add typing rules for this, we leave the existing rules unchanged, save that they thread our axiom set  $\mathcal{A}$  through.

In order to use an overloaded type, one must first show that the predicate is *satisfied* by the known axioms, written  $\mathcal{A} \Vdash P$ :

$$\frac{\mathcal{A} \mid \Gamma \vdash e : P \Rightarrow \pi \quad \mathcal{A} \ \Vdash P}{e : \pi} \text{Inst}$$

If, adding a predicate to the known axioms, we can conclude a typing judgement, then we can overload the expression with that predicate:

$$\frac{P, \mathcal{A} \mid \Gamma \vdash e : \pi}{\mathcal{A} \mid \Gamma \vdash e : P \Rightarrow \pi} GEN$$

Putting these rules to use, we could show that 3.2 + 4.4, which uses the overloaded operator (+), is of type Float:

- 1. We know that  $(+) :: \forall a. (Num \ a) \Rightarrow a \rightarrow a \rightarrow a \in \Gamma.$
- 2. We know that Num Float  $\in A$ .
- 3. Instantiating the type variable a, we can conclude that (+) :: (Num Float)  $\Rightarrow$  Float  $\rightarrow$  Float.
- 4. Using the Inst rule above and (3), we can conclude (+) :: Float  $\rightarrow$  Float
- 5. By the function application rule, we can conclude 3.2 + 4.4:: Float as required.

#### 3 Overloading Resolved

Up to this point, we only discusse about the dynamic semantics the correct concrete oper that ps://eduassistpro.github.io/best way.

In object oriented language, objects typically know what to do—that is, an object is associated with a so-called virtual method or dispatch table, which contains all the methods of the object's class. This approach is it appropriate a language file MaHS, where averaging of emoter of education aren't objects and can be of basic type, but we can use a similar idea: we pass the table of all the methods of a class to an overloaded function, and replace the overloaded function with one that simply highest appropriate method type the table. We call this table \*Calcionary\*, and in MinHS, we represent a table with n functions as n-tuple.

Type classes are c

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Instances become *values* of the dictionary type:

instance Eq Bool where

True == True = True

False == False = True

== = = False

a /= b = not 
$$(a == b)$$

becomes

True == $_{Bool}$  True = True

False == $_{Bool}$  False = True

== $_{Bool}$  = not  $(a ==_{Bool} b)$ 
 $eqBoolDict = ((== $_{Bool}), (/=_{Bool}))$$ 

Programs that rely on overloading now take dictionaries as parameters:

$$same :: \forall a. \ (\text{Eq } a) \Rightarrow [a] \rightarrow \text{Bool}$$
  $same \ [] = \text{True}$   $same \ (x : []) = \text{True}$   $same \ (x : y : xs) = x == y \wedge same \ (y : xs)$ 

Becomes:

```
same:: \forall a. \ (\texttt{EqDict}\ a) \rightarrow [a] \rightarrow \texttt{Bool} same\ eq\ [] = \texttt{True} same\ eq\ (x:[]) = \texttt{True} same\ eq\ (x:y:xs) = (\mathsf{fst}\ eq)\ x\ y \wedge same\ eq\ (y:xs)
```

In some cases, we can make instances also predicated on some constraints:

```
\begin{array}{lll} \mathbf{instance} \ (\mathbf{Eq} \ a) \Rightarrow (\mathbf{Eq} \ [a]) \ \mathbf{where} \\ & [] & == \ [] & = \ \mathbf{True} \\ & (x:xs) \ == \ (y:ys) \ = \ x == y \wedge (xs == ys) \\ & \_ & == \ \_ & = \ \mathbf{False} \\ & a \ /= \ b \ = \ \mathbf{not} \ (a == b) \end{array}
```

Such instances are transform

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