## COMP3161/COMP9164 Supplementary Lecture Notes Type Safety and Exceptions

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When we define a static semanti properties about the dynamic. we can classify them, and integrations://eduassistpro.github.io/ systems. Lastly, we will extend MinHS with exceptions, an error-handling mechanism, which allows us to ensure the property of type safety in the presence of partial functions.

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that follows the execution of a program in small step semantics.

A behaviour is 1

with infinite sequence by repeating the first ps://eduassistpro.github.io/

set of behaviours. A With the definiti very simple property would be termination, expressed formally a F}, where  $b_i$  refers to the *i*th state in the behaviour thand refers to the se nat edu

### 1.1 Safety and Liveness

There are generally two ways to classify properties:

1. A safety property states that something **bad** does not happen. For example:

I will never run out of money.

Formally, these are those properties that may be violated by a finite prefix of a behaviour. For example, if I spend all my money at the pub and run out of money, then I have taken a finite sequence of steps that violates the property. Examples of safety properties we've seen before include hoare triples  $\{\varphi\}$  s $\{\psi\}$ , and many of the static semantics properties we've checked (e.g. that variables are initialised before they're used, and that all variables used are in scope).

2. A liveness property states that something **good** will happen. For example:

If I start drinking now, eventually I will be smashed.

These are properties that cannot be violated by a finite prefix of a behaviour — there is always some way to satisfy the property after any finite number of steps. For example, even if I drink 100 beers and am still not intoxicated, I could always get drunk on the 101st beer. So there is no telling that the property has been violated no matter how many steps I've already taken, as I could always satisfy the property later. Examples of liveness properties we've seen before include termination, and also the confluence of  $\beta$ -reduction.

A very powerful result from Alpern and Schneider<sup>1</sup> is that all properties are the intersection of some safety and some liveness property. For example, the property that "the program returns the number three" is the intersection of the liveness property that the program returns a value (as opposed to looping forever), and the safety property that says that any returned value of the program should be three.

### 1.2 Type Safety

A type system is a type of static semantics used for verifying programs and improving the reliability of software. It is, essentially, a means of annotating expressions and values in a program with a tag, called a type, which tells us something about the set of runtime data the expression can represent.

 $\frac{(x:\tau)}{\Gamma \vdash x}$  Adding types to  $\lambda$ -calculate to  $\lambda$ -calculate types types to  $\lambda$ -calculate types types

significantly, all terms will reduce to a normal form. Terms such as  $(\lambda x. x. x)(\lambda x. x. x)$ , which has no normal form, cannot be assigned a type under these rules (try it and see for yourself ©).

Furthermore, walso big that the normal file of eich term will have the same type is the original term. Assignment Project Exam Help

If we look at a language like MinHS however, we have built-in recursion in the form of the rectune of Scientific Control of the rectune of Scientific Control of the rectune of the rectune

(recfun f :: (Int Int) x = f x)3

will clearly loop forey

from adding types of the street of the stree

guarantee the safety part. This is a property called type safety.

Succinctly, it can be stated as:

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By "go wrong", we mean reaching a stuck state — that is, a non-final state with no outgoing transitions.

We can decompose type safety into two sub-lemmas:

A language with small-step states  $\Sigma$ , final states  $F \subseteq \Sigma$ , state transition relation  $\mapsto$ , and typing rules is type safe if it has two properties:

- Progress If a program can be typed, it is either a final state or can progress to another state. That is, if  $\vdash e : \tau$  then  $e \in F$  or  $\exists e'. e \mapsto e'$ .
- Preservation If a program has a type, evaluation will not change that type. That is, if  $\vdash e : \tau \text{ and } e \mapsto e' \text{ then } \vdash e' : \tau.$

It can be seen from the above definition that well typed programs will not reach a stuck state. If the program is a final state, then it is by definition not stuck. If not, we know from the progress property that the program must move to a new state. We know from preservation that this new state is also typed, which means (from progress) that it must either be a final state or progress to a new state. Similar reasoning applies until the program terminates (or loops).

$$e_1: \tau \xrightarrow{\text{progress}} e_2: \tau \xrightarrow{\text{progress}} e_3: \tau \xrightarrow{\text{preservation}} e_3$$

<sup>&</sup>lt;sup>1</sup>It's a readable paper if you're familiar with metric spaces. https://www.cs.cornell.edu/fbs/publications/ defliveness.pdf

It therefore follows that languages such as C, which are *unsafe*, could reach a stuck state. In such a situation, the program doesn't simply *halt* (or at least, it's not obliged to). What happens is left *undefined*. For example, there is no telling what this C program will do without referring to platform or compiler documentation:

```
int main() {
  return *((int*)(0x0));
}
```

Clearly, speaking of type safety is only applicable in the context of formal treatment of programming languages. Determining exactly what guarantees a type system gives you requires these techniques.

In general, the more expressive the type system is, the more information can be inferred by the compiler. Therefore, for pra

it was not, our compiler may not te type checking may not te hittps://eduassistpro.github.io/

2 Dealing with Partiality
Suppose we have a partial peration, such as division, typed as follows:

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We've assigned it a typ for any x will not re

- Change the sta tps://eduassistpro.githube.io/e are techniques to approximate this for turing-complete language cidable. For those that are interested, the proof is a corollary of
- Change the Arthur Gemantics Chis hatchedu\_assist\_pro

Seeing as MinHS is turing complete, we are unable to statically analyse if the program divides by zero. Hence, we shall extend the dynamic semantics of the language to handle the situation at runtime.

The simplest fix is to make partial functions yield some new state  $\mathtt{error} \in F$  for undefined cases:

Div 
$$v$$
 (Num  $0$ )  $\mapsto$  error

Furthermore, we would define error to interrupt any nested computation and produce error.

There are, of course, a very large number of additional error propagation rules. Here, our abstract machines actually buy us some brevity. We simply state that partial functions result in error, and completely annihilate the stack (e.g in the C Machine):

```
\mathtt{Div}\ v\ \Box \, \triangleright \, s \prec 0\ \mapsto\ \mathtt{error}
```

This guarantees *progress* - partial functions will evaluate to **error** where they are not defined, meaning that the evaluation will not hit a stuck state.

der

We have yet to ensure preservation, however. Preservation says that type is preserved across evaluation. Seeing as any partial function application (of any type) could evaluate to error, the only way to make error respect preservation is to make it a member of every type:

 $\Gamma \vdash \mathtt{error} : \tau$ 

### 2.1Exceptions

Adding a error state seems well and good for ensuring type safety, but many real-world languages have more robust, fine-grained error handling techniques, namely exceptions.

Exceptions are a means for a function to exit without returning. Instead, the function may raise an exception, which is caught by an exception handler somewhere further up the runtime stack. Most of you would have see

we will extend Minhs to 1 will evaluate  $e_1$ , and if R https://eduassistpro.githubingo/ $e_1$ , and start evaluating

These Try expressions can of course be nested, and exceptions can be re-Raised within an exception handler.

Exception rates Sicolar in the Hove example to the detail of the type of the is not relevant what type this is, it could be a special exception type, it could be an Interror

and raise expressions are of any type specified in the expression (for a similar reason to the typing of error):

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2.1.1 Dynamic Semantics for the C Machine
We introduce a new secution mode Cincidental to edu\_assist\_prediction is being raised, written  $\leq$ .

So, when we evaluate a try expression, we simply evaluate the first subexpression, and push the handler onto the stack:

$$s \succ \mathtt{Try}\ e_1\ x.e_2 \mapsto_c \mathtt{Try}\ \square\ x.e_2 \triangleright s \succ e_1$$

Then, if the evaluation returns, we simply discard the try stack frame:

$$\overline{\text{Try} \ \square \ x.e_2 \triangleright s \prec v \mapsto_c s \prec v}$$

If we encounter a raise expression, we first evaluate the exception value being raised:

$$s \succ \mathtt{Raise} \ \tau \ e \mapsto_c \mathtt{Raise} \ \tau \ \square \triangleright s \succ e$$

And, once it returns, we enter the new exception handling mode,  $\leq$ :

Raise 
$$\tau \square \triangleright s \prec v \mapsto_c s \preccurlyeq v$$

This mode continuously pops frames off the stack:

$$\overline{f \triangleright s \preccurlyeq v \mapsto_c s \preccurlyeq v}$$

Until at last we encounter a Try expression, where the handler is evaluated.

$$\overline{\text{Try } \square \ x.e_2 \triangleright s \preccurlyeq v \mapsto_c s \succ e_2[x:=v]}$$

## 2.1.2 Optimising Exceptions

The problem with this approach is one of performance. Raising an exception is O(n) in the size of the stack, which could be a serious performance hit if the stack is very large (for example, in a big recursive function).

Seeing as in our abstract machines we are concerned about performance, we will refine our machine definition to make exception handling fast.

We will define a new type of stack, a Handler stack. The empty handler stack is denoted by  $\star$ , and each handler frame consists of a runtime stack, and the handler expression:

$$\frac{s \; HStack \quad e \; Expr \quad r \; Stack}{ \langle r, x.e \rangle \rhd s \; HStack}$$

Our states will now resemble h, r = e, where h is the handler stack, r is the runtime stack. The "exception handling" mode

When we enter a Try https://eduassistpro.github.io/

We include the placehold of that if  $e_1 \times e_2 \mapsto (r, x.e_2) \triangleright h$ ,  $\operatorname{Try} \triangleright r \succeq e_1$  when the handler stack as it was not used:  $\begin{array}{c} \text{Assignment Project Exam Help} \\ \hline (r', x.e_2) \triangleright h, \operatorname{Try} \triangleright r \prec v \mapsto_c h, r \prec v \end{array}$ 

When we encounter a we immediately synttps://eduassistpro.github.io/ng us the trouble of manu

Note: It may seem inefficient to copy the runtime stack to the handle

Note however that, in the course of evaluating the try block, the machine will never pop off the Try placeholder. Therefore a pointer to the current runtime stack could be kept in the handler stack rather than a copy. Everything above that pointer is freed when an exception is raised.