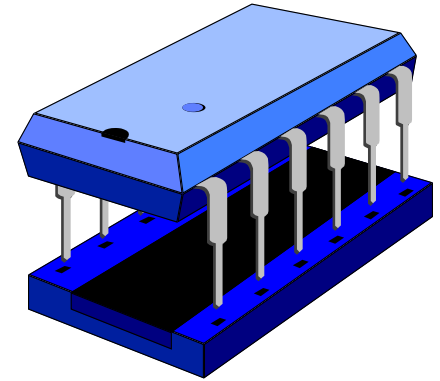


# BASIC CIRCUITS AND MEMORY



Assignment Project Exam Help

---

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

**Bernhard Kainz** (with thanks to  
**Edwards)**

**N. Dulay** and **E.**

[b.kainz@imperial.ac.uk](mailto:b.kainz@imperial.ac.uk)

# Digital Circuits

- Basic Circuits

- Half Adder **Assignment Project Exam Help**

- Full Adder **<https://eduassistpro.github.io/>**

- Latches **Add WeChat edu\_assist\_pro**

# Adders

- A digital circuit that performs **addition** of numbers
- Not only used in arithmetic logic unit(s), but also in other parts of the processor used to calculate addresses, table lookups, etc.  
<https://eduassistpro.github.io/>  
Add WeChat edu\_assist\_pro
- Most common adders operate on 2 numbers

# Half Adder

- Consider adding two 1-bit binary numbers together:

	0	0	1	1
+				1
				??

Add WeChat edu\_assist\_pro

- Input – 2 separate lines

# Half Adder

- Consider adding two 1-bit binary numbers together:

	0	0	1	1
+				1
				10

- Input – 2 separate lines
- Output – two bits – how do we represent this?
  - Use two separate lines (Sum and Carry)

# Half Adder

- Can we now draw the circuit?

- What do we need? – Truth Tables

- One each for sum <https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

# Half Adder

- Recall

	0	0	1	1
	0	1	0	1
				10

Assignment Project Exam Help

<https://eduassistpro.github.io/>

- Truth Table

A	B	A + B		Carry
0	0	0	0	0
0	1	1	1	0
1	0	1	1	0
1	1	2	0	1

Add WeChat edu\_assist\_pro

# Half Adder

- Selecting Gates

Sum	Carry	XOR	And
0	0	0	0
1	0	1	0
1	0	1	0
0	1	0	1

- Hence, we can build the expressions as:

- $\text{Sum} = A \oplus B$
- $\text{Carry} = A \cdot B$



# Half Adder

- Circuit

A      Assignment Project Exam Help  
Sum

B      <https://eduassistpro.github.io/>  
Add WeChat edu\_assist\_pro

A      Carry

B

Is this Correct?

# Half Adder

- A more concise and better version 😊

A Assignment Project Exam Help  
B <https://eduassistpro.github.io/>  
Add WeChat edu\_assist\_pro

Sum  
Carry

# Full Adder

- Half-adders have a major limitation
  - Cannot accept a carry bit from a previous stage → they cannot be chained together to add multi-bit numbers
- Full-adders can <https://eduassistpro.github.io/>
  - Third bit is the carry-in bit
- Can be cascaded to produce adders of any number of bits by daisy-chaining the carry of one output to the input of the next

Assignment Project Exam Help

Add WeChat edu\_assist\_pro

# Full Adder

Assignment Project Exam Help

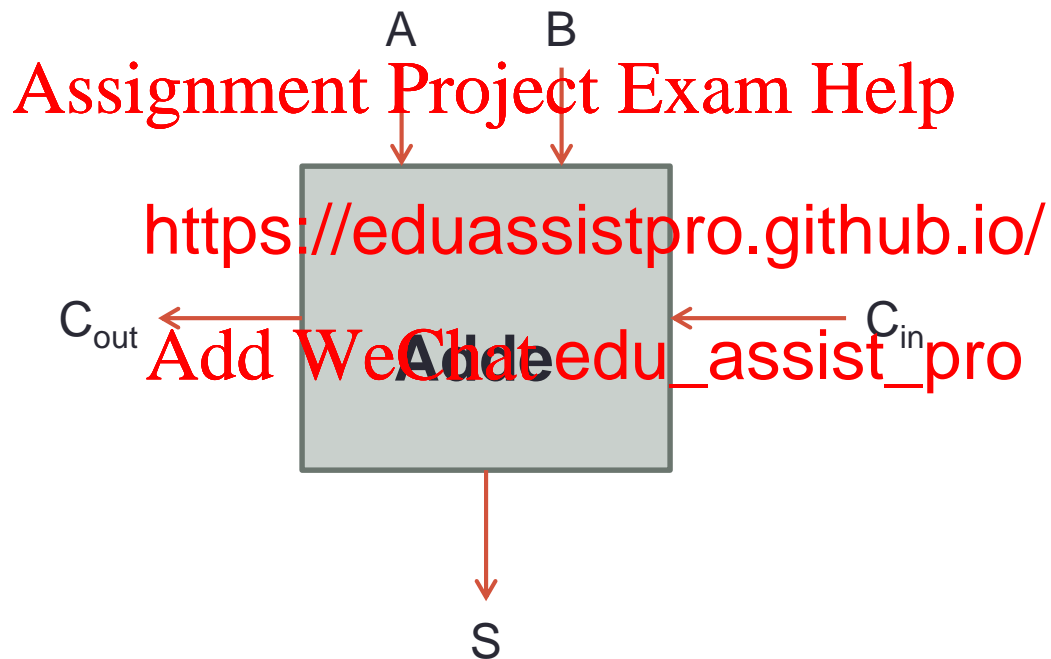
<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

$$\begin{aligned} S &= A \oplus B \oplus C_{in} \\ C_{out} &= (A \cdot B) + C_{in} \cdot (A \oplus B) \end{aligned}$$

# Full Adder

- Conceptually



# Ripple-Carry Adder

- Consists of several full adders connected in a series so that the carry must propagate through every full adder before the addition is complete
- Require the least number of full adders, but they are the slowest
- Carry-Lookahead Adder (homework)

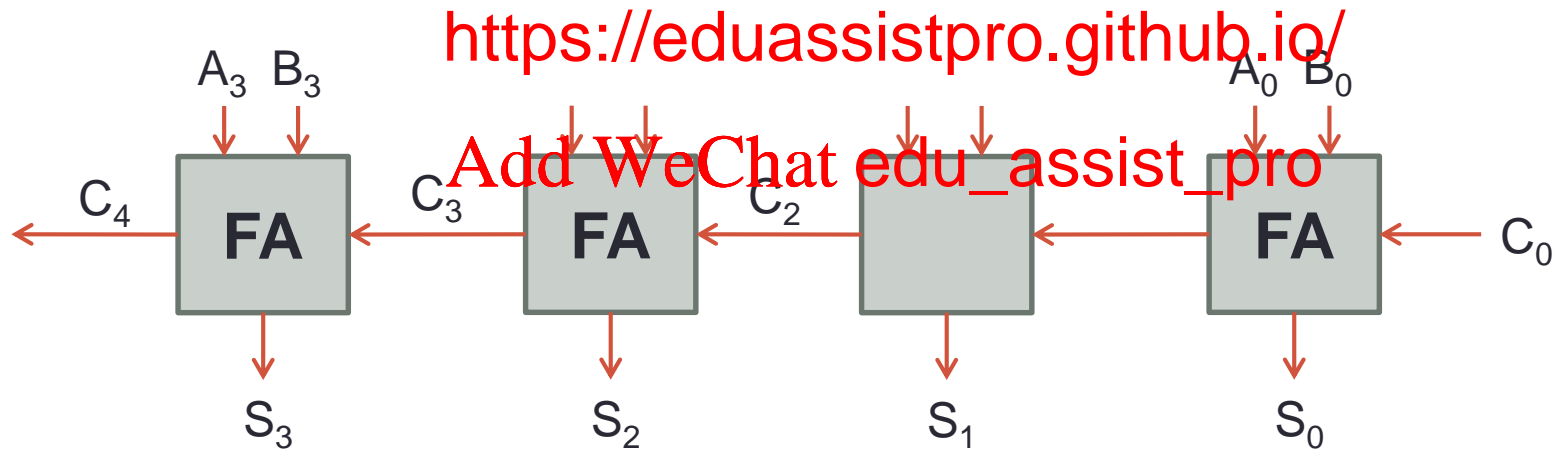
Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

# Ripple-Carry Adder

- The following diagram shows a four-bit adder, which adds the numbers A and B, as well as a carry input, together to produce S and the carry output.



# Gates

- Building blocks for combinatorial circuits
  - Output depends only on current input
- All gates can be constructed using NAND gates
- What if we would like to store
  - Use a *feedback* mechanism where the output values depend indirectly, on themselves



# Latches

- Building blocks to sequential circuits

- Can be built from gates

Assignment Project Exam Help

- Able to rememb

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

- Useful web-page

- <http://www.play-hookey.com/digital/sequential/>

# Latches

- SR-latch
  - S = Set
  - R = Reset

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

# Latches

- $S = 0, R = 0$

<sup>0</sup>  
Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

0

- Value of Q does not change → value is 'remembered'
  - Sometimes called the *latch* state

# Latches

- $S = 1, R = 0$

<sup>0</sup>  
Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

1

- Set the value of Q

# Latches

- $S = 0, R = 0$

<sup>0</sup>  
Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

0

- Value of Q stays the same – it ‘remembers’ 😊

# Latches

- $S = 0, R = 1$

<sup>1</sup>  
Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

0

- Reset the value of Q to 0
- $S = 1, R = 1$  leads to undefined state

# Latches

- SR-Latch: Truth table

S	R	Q	Q'
0			
0			1
1	0		
1	1	U	

# Flip-Flops

- Latches are *asynchronous* → output changes very soon after the input changes

## Assignment Project Exam Help

- Most computers
  - Outputs of all th <https://eduassistpro.github.io/> simultaneously to the rhythm of a global *clock signal*
- A *flip-flop* is a synchronous version of the latch

Add WeChat edu\_assist\_pro



# Memory

- Useful variation on the SR latch circuit is the Data latch, or D latch
- Constructed by using the inverted S input as the R input signal
  - Allows for a single input as input is inverted

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

# Memory

- Two basic types of memory
- Static RAM (SRAM)
  - Bit-cell is a latch
  - Fast, not very dense (more transistors to implement)
  - Primarily used in cache
  - Consumes less power
- Dynamic RAM (DRAM)
  - Bit-cell is a transistor and capacitor (which leaks information)
    - Storage has to be periodically refreshed
  - Primarily used in main memory
  - Cheaper than SRAM

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

# Memory

- Memories hold binary values
  - Data (e.g. Integers, Reals, Characters)
  - CPU Instructions
  - Memory Addresses (Pointers to instructions)
- Contents remain unchanged unless overwritten with a new binary value
  - Some of them lose the content when power is turned off (volatile memory)

# Memory – Examples

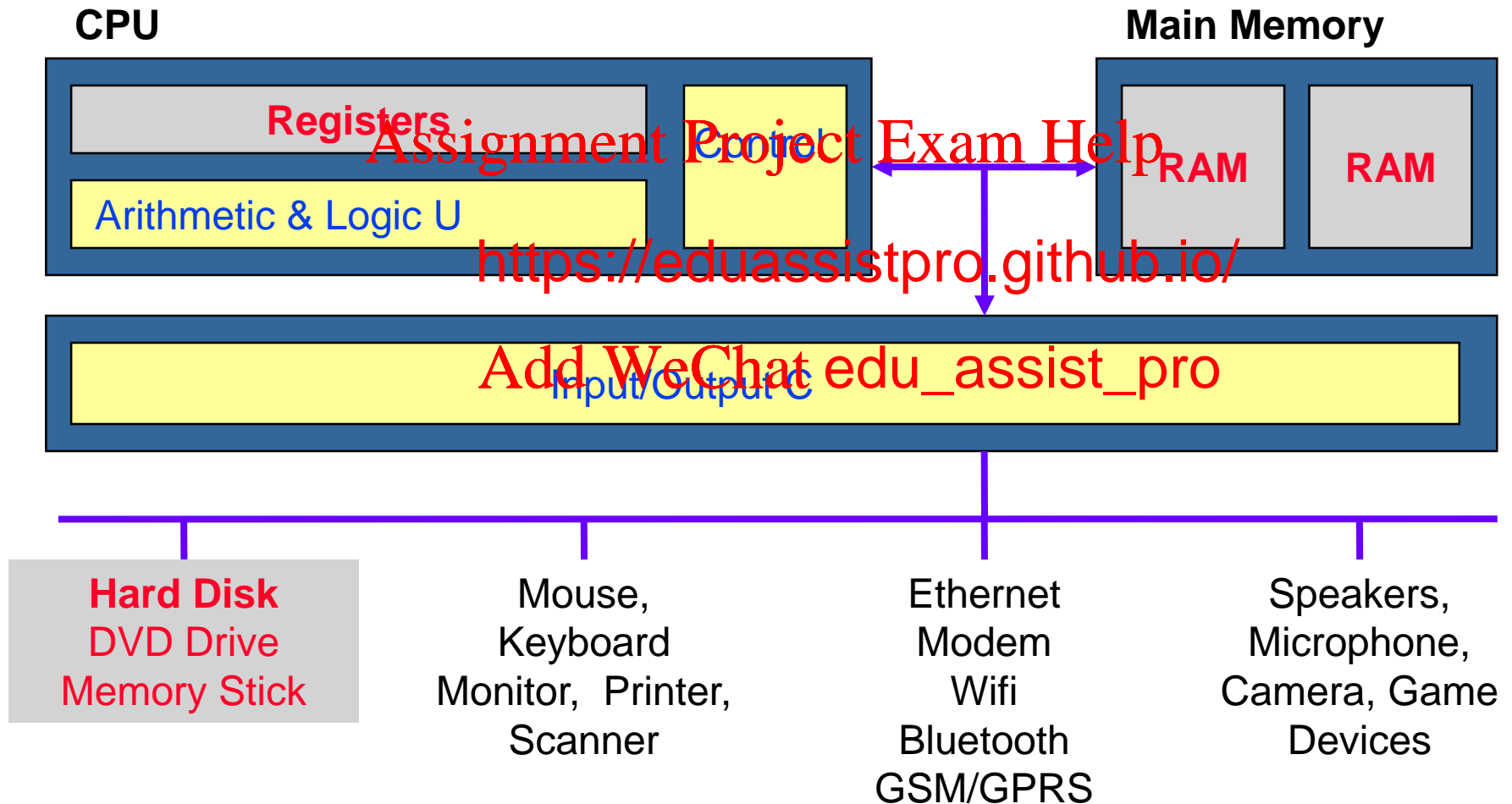
- CPU, Registers, Caches – L1, L2 [L3]
- Mainboard
  - RAM (Random
  - Caches
  - I/O Registers & Buffers
  - Video-card Memory
- Storage Devices
  - Hard Disks, CDs, DVDs, Tapes, Memory Sticks, Flashcards

Assignment Project Exam Help

<https://eduassistpro.github.io/>

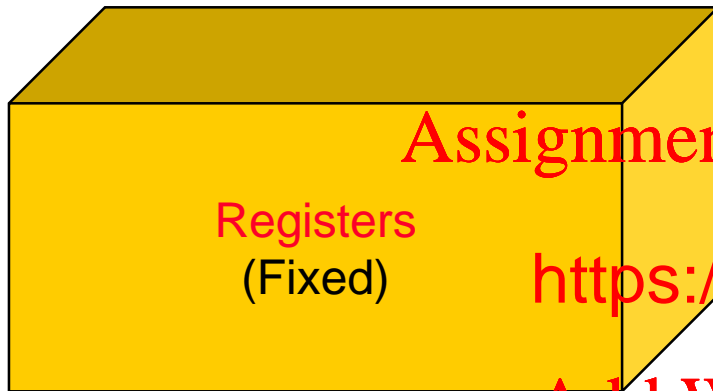
Add WeChat edu\_assist\_pro

# Computer Architecture

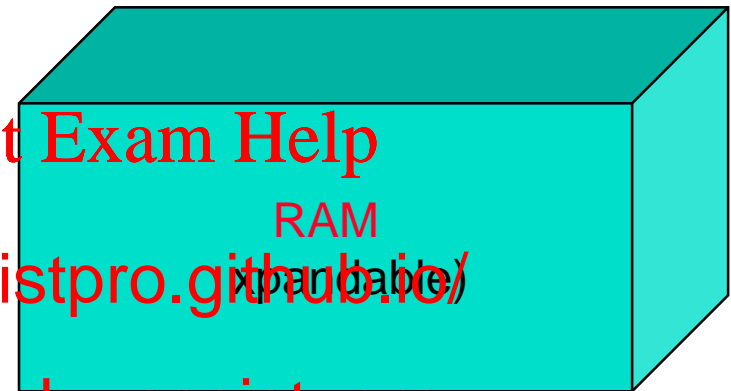


# 3 Types of Memory

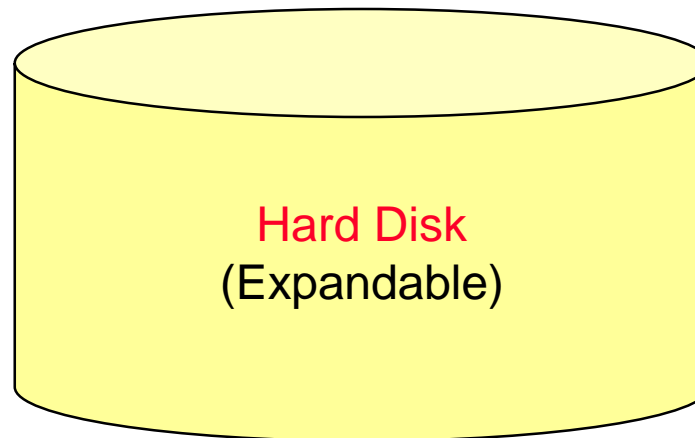
CPU



Main Memory



Storage  
Device



Assignment Project Exam Help

<https://eduassistpro.github.io/>

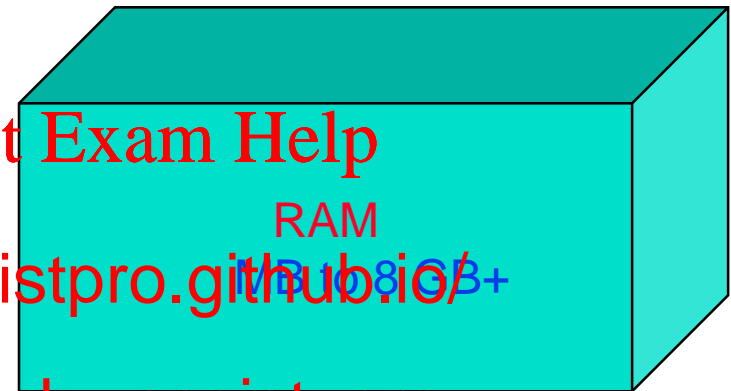
Add WeChat edu\_assist\_pro

# Capacity

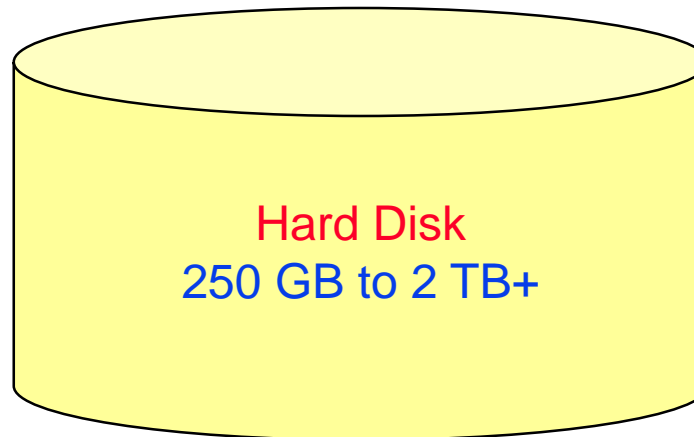
CPU



Main Memory



Storage  
Device



1 KB =  $2^{10}$  bytes

1 MB =  $2^{20}$  bytes

1 GB =  $2^{30}$  bytes

1TB =  $2^{40}$  bytes

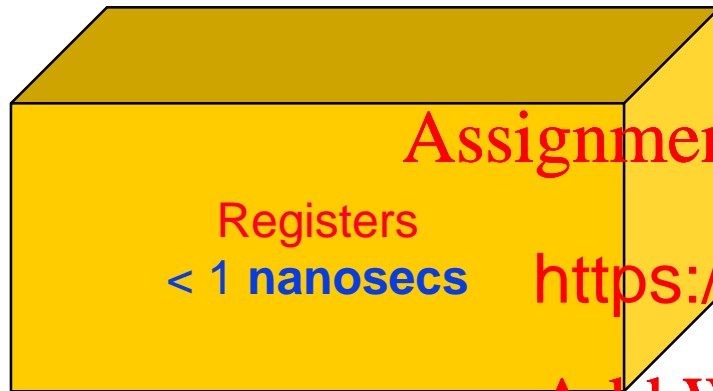
Assignment Project Exam Help

<https://eduassistpro.github.io/>

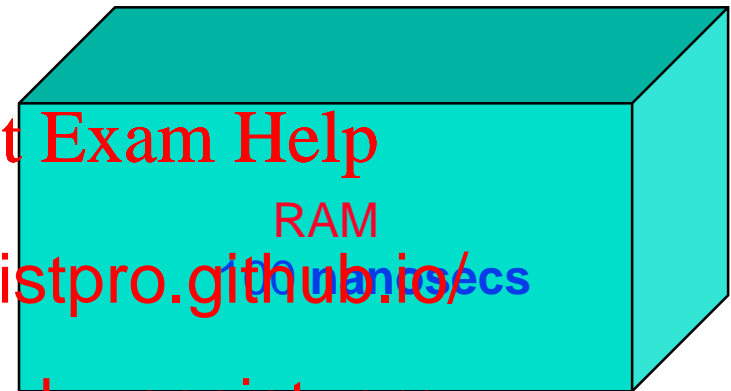
Add WeChat edu\_assist\_pro

# Speed (Access Time)

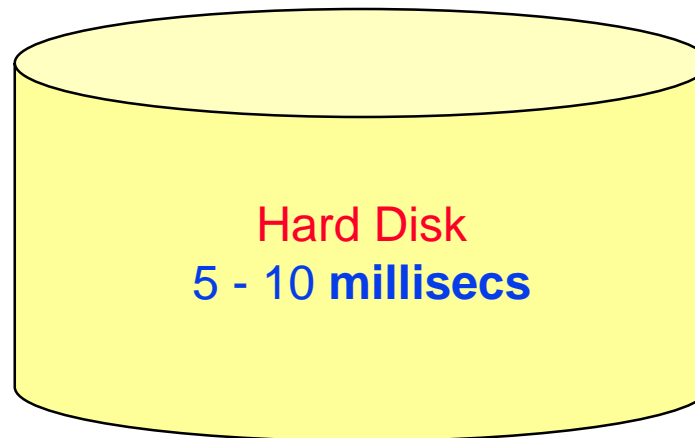
CPU



Main Memory



Storage  
Device



milli =  $10^{-3}$   
micro =  $10^{-6}$   
nano =  $10^{-9}$

Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro



# Volatility

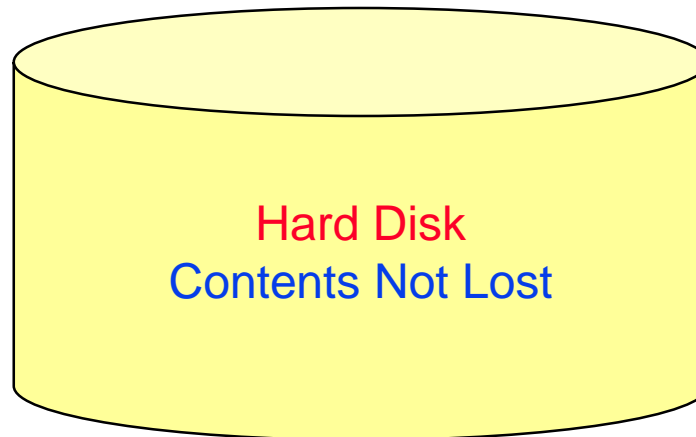
CPU



Main Memory



Storage  
Device



Assignment Project Exam Help

<https://eduassistpro.github.io/>

Add WeChat edu\_assist\_pro

# Summary

