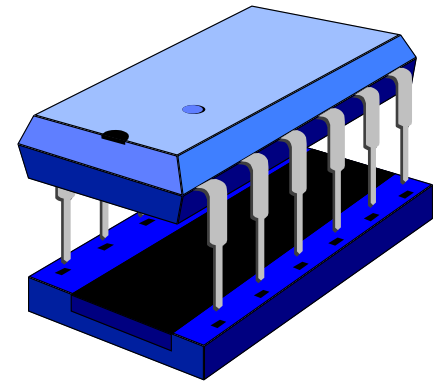


DATA

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Edwards)

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Why Binary Numbers?

- Computers process binary patterns

- Patterns of *0s* and *1s*

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- To represent data and to code it as a binary pattern

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- Most important to consider: bits and characters
 - Convert into binary

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Decimal to Binary

- Steps:

- Divide the number by 2 giving the quotient and the remainder
- Repeat previous until a zero quotient is obtained
- Answer is obtained by reading the remainder column **bottom to the top**

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Decimal to Binary (Example)

- What is 98_{10} in binary?

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	Quotient	Remainder
$24 \div 2$	12	
$12 \div 2$	6	
$6 \div 2$	3	0
$3 \div 2$	1	1
$1 \div 2$	0	1

1100010₂

$$\begin{aligned} 1100010_2 &= 1 * 2^6 + 1 * 2^5 + 0 * 2^4 + 0 * 2^3 + 0 * 2^2 + 1 * 2^1 + 0 * 2^0 \\ &= 64 + 32 + 0 + 0 + 0 + 2 + 0 = 98_{10} \end{aligned}$$

Octal (Base 8)

- Used in the past as a more convenient base for representing long binary values
- Converting to binary
 - Starting from the right end, each group of 3 bits (why? $8 = 2^3$) is converted to a single octal digit (called a triad)

- Example: What is 10101_2 in O

↓	↓
2	5

= 25_8

- Example: What is 357_8 in Binary?

3	5	7
↓	↓	↓
011	101	111

= 11101111_2

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Hexadecimal (Base 16)

- Used by programmers to represent long binary values
 - Preferred over Octal
- $16 = 2^4 \rightarrow$ 4 Binary digits represent one hexadecimal digit (bits) - starting from 0 each group of 4 bits represents a hexadecimal digit

- Example: What is 10010100_2 in hexadecimal?

1001	
↓	↓
9	4

$= 94_{16}$

- Example: What is 86_{16} in Binary?

8	6
↓	↓
1000	0110

$= 10000110_2$

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Binary vs. Hexadecimal

Hex	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
Decimal	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Binary	0	1	10	11	100	101	110	111	1000	1001	1010	1011	1100	1101	1110	1111

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- Generally:

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	1 byte =	8 binary digits =	2 hexadecimal digits
1 word =	2 bytes =	16 binary digits =	4 hexadecimal digits
1 long word =	4 bytes =	32 binary digits =	8 hexadecimal digits

Representing Data

- Data Types of interest

- Integers (Unsigned/Signed)

- Reals (Floating

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- Text

Signed and Unsigned Integers

- Natural numbers can be represented by their binary value within the computer

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- Representation are important

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- Several possibilities Add WeChat edu_assist_pro

- Sign & Magnitude
- One's Complement
- Two's Complement
- Excess-n (Bias-n)
- Binary-Coded Decimal (BCD)

Signed and Unsigned Integers

- In any representation, desirable properties are:
 - Only one bit pattern per value
 - Equal number of 0s and 1s
 - Maximum range of values
 - No gaps in the range
 - Fast, economic hardware implementation of integer arithmetic
 - Minimal number of transistors AND fast arithmetic, if possible

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Sign & Magnitude

- Leftmost (“most significant”) bit represents the **sign** of the integer
- Remaining bits to represent its magnitude
- For n-bits, $-(2^{n-1}) \leq +(2^{n-1}-1)$
- Simplest for human
- Two representations for zero
- Costly to implement (need to compare signs and implement subtractors)

Bit Pattern	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001	1010	1011	1100	1101	1110	1111
Unsigned	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Sign & Magnitude	+0	+1	+2	+3	+4	+5	+6	+7	-0	-1	-2	-3	-4	-5	-6	-7

One's Complement

- Negative numbers are the **complement** of the positive numbers
- $-(2^{n-1}-1) \leq \text{One's Complement} \leq +(2^{n-1}-1)$
 - Same as Sign & Magnitude
- Less intuitive (for <https://eduassistpro.github.io/>)
- Less costly to implement (Add WeChat edu_assist_pro)
- Bit fiddly

Bit Pattern	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001	1010	1011	1100	1101	1110	1111
Unsigned	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Sign & Magnitude	+0	+1	+2	+3	+4	+5	+6	+7	-0	-1	-2	-3	-4	-5	-6	-7
1s Complement	+0	+1	+2	+3	+4	+5	+6	+7	-7	-6	-5	-4	-3	-2	-1	-0

Two's Complement

- Negative of an integer is achieved by inverting each of the bits and adding 1 to it:
 - Two's complement of -3 (0011) \rightarrow 1100 (invert) + 1 \rightarrow 1101
- $-2^{n-1} \leq \text{Two's complement}$ <https://eduassistpro.github.io/>
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- Most useful property: $X - Y = X + (-Y)$
 - No need for a separate subtractor (Sign & Magnitude) or carry-out adjustments (One's Complement)

Two's Complement

- Only **one** bit pattern for zero 😊
 - Asymmetric - one *extra* negative value

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- Minor disadvantages

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Bit Pattern	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001	1010	1011	1100	1101	1110	1111
Unsigned	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Sign & Magnitude	+0	+1	+2	+3	+4	+5	+6	+7	-0	-1	-2	-3	-4	-5	-6	-7
1s Complement	+0	+1	+2	+3	+4	+5	+6	+7	-7	-6	-5	-4	-3	-2	-1	-0
2s Complement	+0	+1	+2	+3	+4	+5	+6	+7	-8	-7	-6	-5	-4	-3	-2	-1

Excess-n (Bias-n) - Motivation

- Sorting in Two's complement is not easy
 - Assuming you could compare numbers, it would always say negative numbers are greater !!!
- Suppose we want to keep the same ordering, but the smallest value and 111 represent the largest value in 3-bits?
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- This is the idea behind *excess representation* or *biased representation*
- bitstring with N 0's maps to the smallest value and the bitstring with N 1's maps to the largest value

Excess-n (Bias-n)

- Using 3-bits as example, 3-bits gives us: $2^3 = 8$ values in total
 - Assuming we start at -4 (1/2 of 8), we get: -4, -3, -2, -1, 0, 1, 2, 3
 - Smallest value =
 - Each value stored \rightarrow Excess-4 ☺

Stored value	
000	
001	-3
010	-2
011	-1
100	0
101	1
110	2
111	3

Excess-n (Bias-n)

Bit Pattern	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001	1010	1011	1100	1101	1110	1111
Unsigned	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Sign & Magnitude	+0	+1	+2	+3	+4	+5	+6	+7	-8	-7	-6	-5	-4	-3	-2	-1
1s Complement	+0	+1	+2	+3	+4	+5	+6	+7	-8	-7	-6	-5	-4	-3	-2	-1
2s Complement	+0	+1	+2	+3	+4	+5	+6	+7	-8	-7	-6	-5	-4	-3	-2	-1
Excess-8	-8	-7	-6	-5	-4	-3	-2	-1	0	1	2	3	4	5	6	7

Binary Coded Decimal (BCD)

- Each decimal digit is represented by a fixed number of bits, usually four or eight

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- Easy for human

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- Takes up much more space
- Assuming 4-bits, the number 9876510 can be encoded as:

9	8	7	6	5	1	0
1001	1000	0111	0110	0101	0001	0000

- Actual Binary: 100101101011010000011110 (24-bits)

Binary Coded Decimal (BCD)

Bit Pattern	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001	1010	1011	1100	1101	1110	1111
Unsigned	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Sign & Magnitude	+0	+1	+2	+3	+4	+5	+6	+7	+8	+9	-2	-3	-4	-5	-6	-7
1s Complement	+0	+1	+2	+3	+4	+5	+6	+7	+8	+9	-5	-4	-3	-2	-1	-0
2s Complement	+0	+1	+2	+3	+4	+5	+6	+7	-8	-7	-6	-5	-4	-3	-2	-1
Excess-8	-8	-7	-6	-5	-4	-3	-2	1	0	1	2	3	4	5	6	7
BCD	0	1	2	3	4	5	6	7	8	9	-	-	-	-	-	-

Characters

- Characters are mapped to bit patterns
- Common mappings are ASCII and Unicode

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- ASCII
 - Uses 7-bits (128 bit-patterns)
 - Most modern computer extend this to 8-bits yielding an extra 128 bit-patterns
 - 26 lowercase and uppercase letters, 10 digits, and 32 punctuation marks. Remaining 34 bit-patterns represent whitespace characters e.g. space (SP), tab (HT), return (CR), and special *control characters*

ASCII Character Set

Bit positions 654								Bit positions 3210
000	001	010	011	100	101	110	111	
NUL	DLE	SP	0	@	P	'	p	0000
SOH	DC1	!	1	A	Q	a	q	0001
STX	DC2	"	2	B	R	b	r	0010
ETX	DC3	#	3	C	S	c	s	0011
EOT	DC4	\$	4	D	T	d	t	0100
ENQ	NAK	%				e	u	0101
ACK	SYN	&				f	v	0110
BEL	ETB	'				g	w	0111
BS	CAN	(8	H		h	x	1000
HT	EM)	9	I		i	y	1001
LF	SUB	*	:	J		j	z	1010
VT	ESC	+	;	K	[k	{	1011
FF	FS	,	<	L	\	l		1100
CR	GS	-	=	M]	m	}	1101
SO	RS	.	>	N	^	n	~	1110
SI	US	/	?	O	_	o	DEL	1111

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Strings are represented as sequence of characters. E.g. **Fred** is encoded as follows:

English	F	r	e	d
ASCII (Binary)	0100 0110	0111 0010	0110 0101	0110 0100
ASCII (Hex)	46	72	65	64

Unicode

- Newer, more complex standard
- Attempting to provide a number for every character, no matter the language
- Over 120,000 characters already
- First 65,536 (16-bit) characters cover the major alphabets of the world – more and more programming languages support this
- First 127 characters correspond to ASCII characters

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