### Two-Degrees-of-Freedom PID controllers

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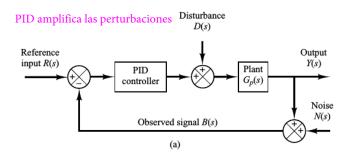
June 2020



## Modified PID Controls

#### Introduction

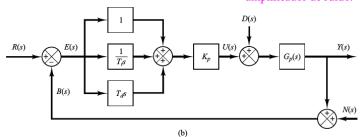
- In practical cases, there may be one requirement on the *response to disturbance input* and another requirement on the *response to reference input*.
- Often these two requirements conflict with each other and cannot be satisfied in the single-degree-of-freedom case.
- By increasing the degrees of freedom, we are able to satisfy both, response to disturbance and response to reference input.



# Modified PID Controls PI-D Control

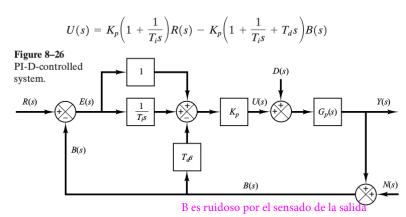
- If reference input is a step function, the derivative term in the control action will
  produce that u(t) will involve an impulse function.
- Such a phenomenon is called *set-point kick*.

Pasa también con el ruido. El bloque derivativo es un amplificador de ruido.



# Modified PID Controls PI-D Control, II

To avoid the set-point kick phenomenon (a pulse input), we may wish to operate the derivative action only in the feedback path so that differentiation occurs only on the feedback signal and not on the reference signal.



## Modified PID Controls PI-D Control, III

Notice that in the absence of the disturbances and noises, the closed-loop transfer function of the basic PID control system [shown in Figure 8–25(b)] and the PI-D control system (shown in Figure 8–26) are given, respectively, by

$$\frac{Y(s)}{R(s)} = \left(1 + \frac{1}{T_i s} + T_d s\right) \frac{K_p G_p(s)}{1 + \left(1 + \frac{1}{T_i s} + T_d s\right) K_p G_p(s)}$$

and

$$\frac{Y(s)}{R(s)} = \left(1 + \frac{1}{T_i s}\right) \frac{K_p G_p(s)}{1 + \left(1 + \frac{1}{T_i s} + T_d s\right) K_p G_p(s)}$$

It is important to point out that in the absence of the reference input and noises, the closed-loop transfer function between the disturbance D(s) and the output Y(s) in either case is the same and is given by

$$\frac{Y(s)}{D(s)} = \frac{G_p(s)}{1 + K_p G_p(s) \left(1 + \frac{1}{T_i s} + T_d s\right)}$$

Es el mismo para PID como para PI-D

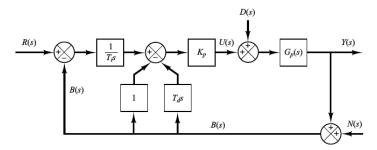
### Modified PID Controls

#### I-PD Control

- If reference input is a step function, both PID control and PI-D control involve a step function in the manipulated signal.
- The proportional action and derivative action are moved to the feedback path so that these actions affect the feedback signal only.

$$U(s) = K_p \frac{1}{T_i s} R(s) - K_p \left(1 + \frac{1}{T_i s} + T_d s\right) B(s)$$

I-PD



## Modified PID Controls I-PD Control

The closed-loop transfer function Y(s)/R(s) in the absence of the disturbance input and noise input is given by

$$\frac{Y(s)}{R(s)} = \left(\frac{1}{T_i s}\right) \frac{K_p G_p(s)}{1 + K_p G_p(s) \left(1 + \frac{1}{T_i s} + T_d s\right)}$$

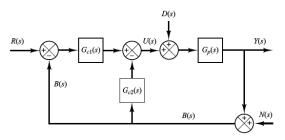
It is noted that in the absence of the reference input and noise signals, the closed-loop transfer function between the disturbance input and the output is given by

$$\frac{Y(s)}{D(s)} = \frac{G_p(s)}{1 + K_p G_p(s) \left(1 + \frac{1}{T_i s} + T_d s\right)}$$

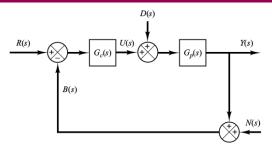
This expression is the same as that for PID control or PI-D control.

## Two-Degrees-of-Freedom Control Systems Introduction

- Instead of moving the entire derivative control action or proportional control action to the feedback path, it is possible to move only portions of these control actions to the feedback path.
- The characteristics of PI-PD control scheme lie between PID control and I-PD control.
- Similarly, PID-PD control can be considered.
- We will have one controller in the feedforward path and another controller in the feedback path. Such control schemes lead us to a two-degrees-of-freedom control scheme.



# Two-Degrees-of-Freedom Control Systems One-degree-of-freedom Control System



For this system, three closed-loop transfer functions  $Y(s)/R(s)=G_{yr}$ ,  $Y(s)/D(s)=G_{yd}$ , and  $Y(s)/N(s)=G_{yn}$  may be derived. They are

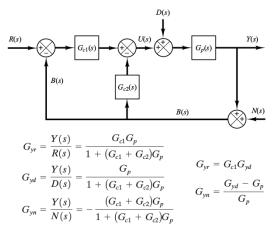
$$\begin{split} G_{yr} &= \frac{Y(s)}{R(s)} = \frac{G_c G_p}{1 + G_c G_p} \\ G_{yd} &= \frac{Y(s)}{D(s)} = \frac{G_p}{1 + G_c G_p} \\ G_{yn} &= \frac{Y(s)}{N(s)} = -\frac{G_c G_p}{1 + G_c G_p} \end{split}$$

$$G_{yr} = \frac{G_p - G_{yd}}{G_p}$$

$$G_{yn} = \frac{G_{yd} - G_p}{G_p}$$

How many of these closed-loop transfer functions are independent?

# Two-Degrees-of-Freedom Control Systems Two-degree-of-freedom Control System



How many of these closed-loop transfer functions are independent?

## Bibliography

 Ogata, Katsuhiko. Modern Control Engineering. Fifth Edition. Prentice Hall. 2009. Chapter 8.