



Minería de datos G.571

Feature selection: Correlation coefficient y Fisher's Score

Minería de Datos
Zavala Roman Irvin Eduardo 1270771

Correlation coefficient/Pearson's Correlation coefficient

$$r = \frac{n(\sum xy) - (\sum x)(\sum y)}{\sqrt{[n\sum x^2 - (\sum x)^2][n\sum y^2 - (\sum y)^2]}}$$

r = Pearson Coefficient

n = number of the pairs of the stock

$\sum xy$ = sum of products of the paired stocks

$\sum x$ = sum of the x scores

$\sum y$ = sum of the y scores

$\sum x^2$ = sum of the squared x scores

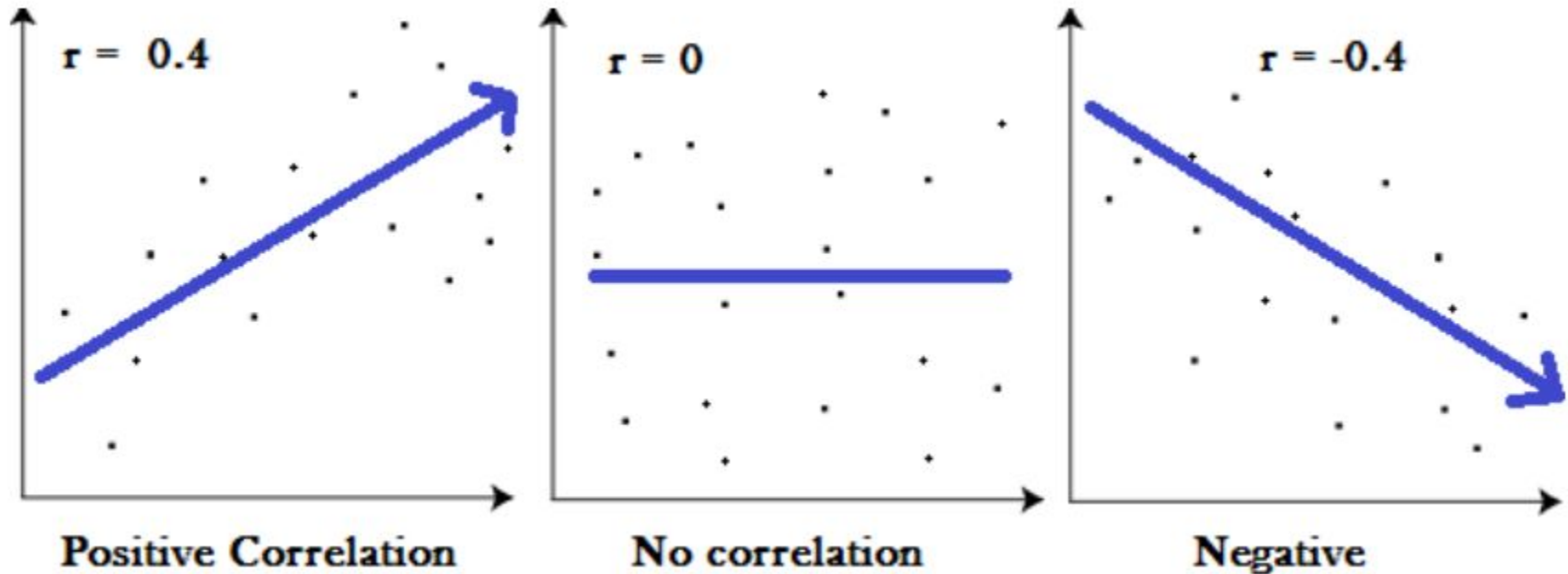
$\sum y^2$ = sum of the squared y scores

Correlation coefficient/Pearson's Correlation coefficient

	x	y	xy	x²	y²
	6	12	72	36	144
	8	10	80	64	100
	10	20	200	100	400
Σ	24	42	352	200	644

$$r = \frac{(3)(352) - (24)(42)}{\sqrt{(3 * 200 - (24)^2)(3 * 644 - (42)^2)}} = 0.7559$$

Correlation coefficient/Pearson's Correlation coefficient



Fuente:

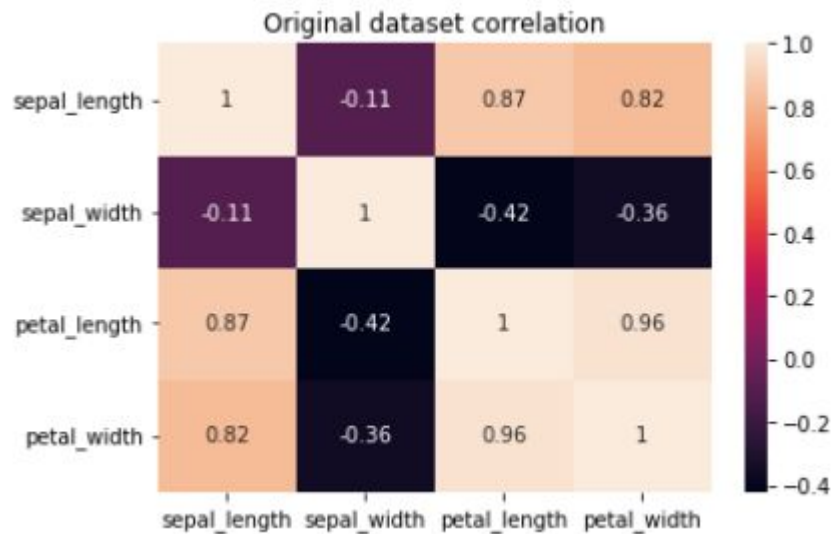
<https://www.statisticshowto.com/probability-and-statistics/correlation-coefficient-formula/>

Correlation coefficient/Pearson's Correlation coefficient

Entonces, ¿cuál es la idea?

Buscar atributos altamente correlacionados en el dataset y si esto sucede se puede eliminar uno o varios ya que los consideramos “redundantes”.

Prueba Iris



```
ax = plt.axes()
sns.heatmap(corr_matrix, annot = True)
ax.set_title('Original dataset correlation')
plt.show()
```

#Algoritmo corr coef para eliminar atributos redundantes

```
def corr_coef(dataset, threshold):  
    print(dataset)  
    col_corr = set()  
    corr_matrix = dataset.corr()  
    ax = plt.axes()  
    sn.heatmap(corr_matrix, annot = True)  
    ax.set_title('Original dataset correlation')  
    plt.show()  
    for i in range(len(corr_matrix.columns)):  
        for j in range(i):  
            if abs(corr_matrix.iloc[i, j]) > threshold:  
                colname = corr_matrix.columns[i]  
                col_corr.add(colname)  
    return col_corr
```

```
dataset = pd.read_csv('iris.csv')  
label = 'species'  
features = dataset.drop(label, axis = 1)  
target = dataset[[label]].apply(lambda x: pd.factorize(x)[0])  
corr_matrix = features.corr().abs()  
upper = corr_matrix.where(np.triu(np.ones(corr_matrix.shape), k=1).astype(bool))  
to_drop = [column for column in upper.columns if any(upper[column] > 0.85)]  
print(to_drop)
```

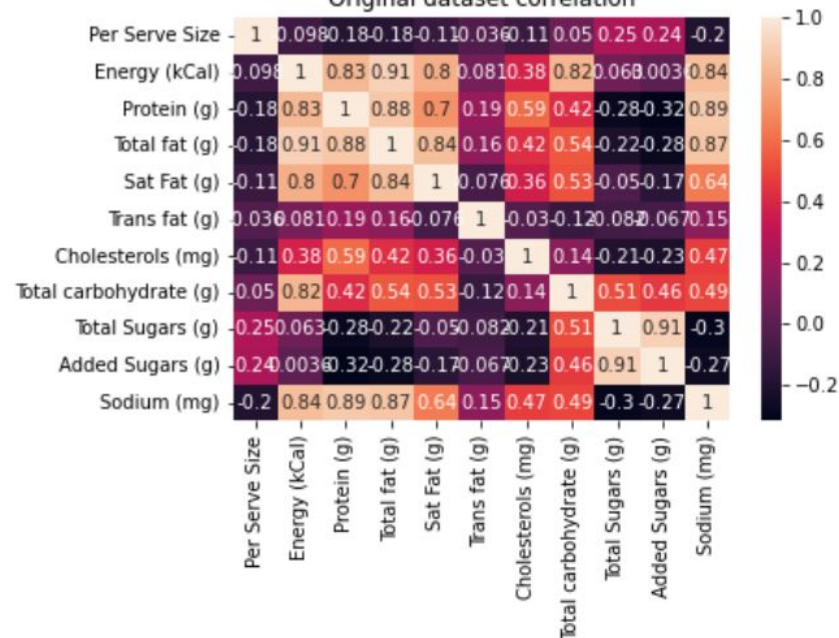
Resultado

```
      DATASET IRIS
Metodo 1 decide eliminar: {'petal_length', 'petal_width'}
Metodo 2 decide eliminar: ['petal_length', 'petal_width']
Final dataset:
      sepal_length  sepal_width
0              5.1           3.5
1              4.9           3.0
2              4.7           3.2
3              4.6           3.1
4              5.0           3.6
..            ...           ...
145            6.7           3.0
146            6.3           2.5
147            6.5           3.0
148            6.2           3.4
149            5.9           3.0

[150 rows x 2 columns]
```


Correlation coefficient con dataset Starbucks

Original dataset correlation



```

DATASET STARBUCKS
Metodo 1 decide eliminar: {'Added Sugars (g)', 'Sodium (mg)', 'Total fat (g)'}
Metodo 2 decide eliminar: ['Total fat (g)', 'Added Sugars (g)', 'Sodium (mg)']
Final dataset:
  Menu Items  ...  Total Sugars (g)
0    McVeggie™ Burger  ...      7.90
1    McAloo Tikki Burger®  ...      7.05
2    McSpicy™ Paneer Burger  ...      8.35
3    Spicy Paneer Wrap  ...      3.50
4    American Veg Burger  ...      7.85
..  ...  ...  ...
136  Tomato Ketchup Sachets  ...      2.33
137  Maple Syrup  ...     16.20
138  Cheese Slice  ...      0.54
139  Sweet Corn  ...      2.54
140  Mixed Fruit Beverage  ...     16.83

[141 rows x 9 columns]
    
```

Fisher's Score

Este método se basa en una función matemática que da como resultado un puntaje por atributo dando como resultado un ranking de todos los atributos.

$$F(\mathbf{x}^j) = \frac{\sum_{k=1}^c n_k (\mu_k^j - \mu^j)^2}{(\sigma^j)^2}$$

Esta no es la mejor versión de este método,
pero es de los más óptimos computacionalmente.

n_k Es el tamaño de la clase k-th

μ_k^j Media de la clase k-th respecto al feature j-th

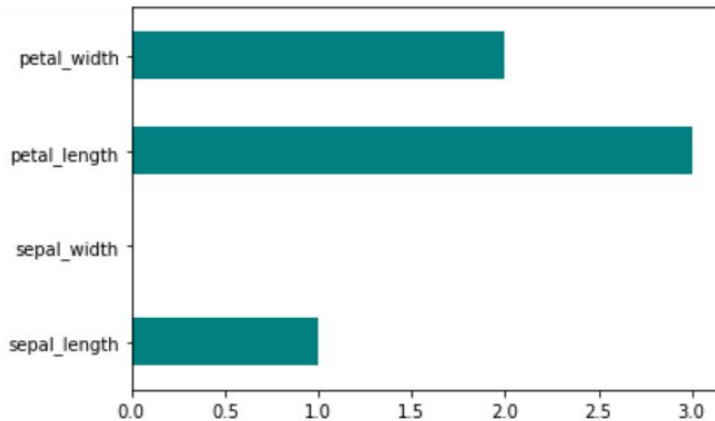
μ^j Media de la feature j-th

σ^j Desviación estándar de la feature j-th

Fisher's Score prueba Iris

```
from sklearn.feature.function.similarity_based import fisher_score
pd.options.mode.chained_assignment = None # default='warn'

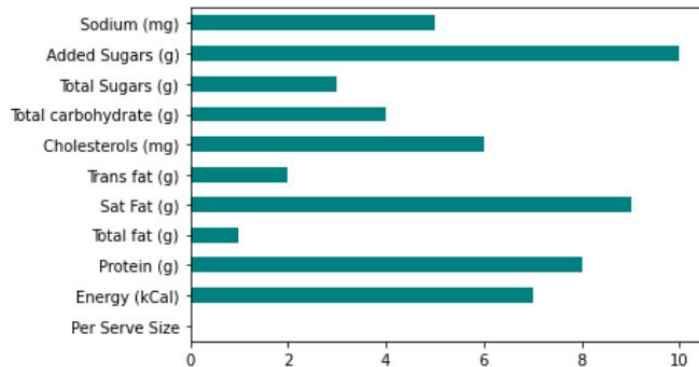
dataset = pd.read_csv('iris.csv')
array = dataset.values
X = array[:,0:4]
Y = array[:,4]
score = fisher_score.fisher_score(X,Y)
feat_importances = pd.Series(score, dataset.columns[0:len(dataset.columns)-1])
feat_importances.plot(kind = 'barh', color = 'teal')
plt.show()
```



Fisher's Score prueba Starbucks

```
from skfeature.function.similarity_based import fisher_score
pd.options.mode.chained_assignment = None # default='warn'

dataset = pd.read_csv('India Menu.csv')
dataset1 = dataset.replace('[^0-9]+', '', regex=True)
array = dataset.values
array1 = dataset1.values
X = array[:,2:len(dataset.columns)].astype(float)
Y = array[:,0]
score = fisher_score.fisher_score(X,Y)
feat_importances = pd.Series(score, dataset.columns[2:len(dataset.columns)])
feat_importances.plot(kind = 'barh', color = 'teal')
plt.show()
```



¿Cuáles seleccionar?

Aunque se deben escoger los valores más altos y quitar los más bajos, ninguna fuente dice hasta qué punto recortar o salvar atributos. Por lo que queda a criterio del analizador mantener los primeros m lugares del ranking. En este caso decidí agarrar el top 50%.

```
def fisher_score_selection(X, target, X_cols, dataset, porcentaje):
    score = fisher_score.fisher_score(X,Y)
    feat_importances = pd.Series(score, X_cols)

    feat_importances.plot(kind = 'barh', color = 'teal')
    plt.show()

    top = X.shape[1] * porcentaje//100
    feat_importances = feat_importances.sort_values(ascending=False)
    feat_importances.drop(feat_importances.tail(top).index,inplace=True)
    feat_importances = feat_importances.index.tolist()
    print("Selected: ", feat_importances)
    dataset = dataset[dataset.columns.intersection(feat_importances)]
    return dataset

dataset = pd.read_csv('iris.csv')
array = dataset.values
X = array[:,0:4]
X_cols = dataset.columns[0:4]
Y = array[:,4]
dataset = fisher_score_selection(X, Y, X_cols, dataset, 50)
print(dataset)
```

```
Selected: ['petal_length', 'petal_width']
   petal_length  petal_width
0           1.4           0.2
1           1.4           0.2
2           1.3           0.2
3           1.5           0.2
4           1.4           0.2
..          ...          ...
145          5.2           2.3
146          5.0           1.9
147          5.2           2.0
148          5.4           2.3
149          5.1           1.8
```

```

dataset = pd.read_csv('India_Menu.csv')
dataset1 = dataset.replace('[^0-9]+', '', regex=True)
array = dataset.values
array1 = dataset1.values
X = array[:,2:len(dataset.columns)].astype(float)
X_cols = dataset.columns[2:len(dataset.columns)]
Y = array[:,0]
dataset = fisher_score_selection(X, Y, X_cols, dataset, 50)
print(dataset)

```

```

Selected: ['Added Sugars (g)', 'Sat Fat (g)', 'Protein (g)', 'Energy (kCal)', 'Cholesterol (mg)', 'Sodium (mg)']
      Energy (kCal)  Protein (g)  ...  Added Sugars (g)  Sodium (mg)
0           402.05      10.24  ...           4.49      706.13
1           339.52       8.50  ...           4.07      545.34
2           652.76      20.29  ...           5.27     1074.58
3           674.68      20.96  ...           1.08     1087.46
4           512.17      15.30  ...           4.76     1051.24
..           ...           ...  ...           ...           ...
136          11.23       0.08  ...           1.64       71.05
137           86.40       0.00  ...           5.34       15.00
138           51.03       3.06  ...           0.00      178.95
139           45.08       1.47  ...           0.00        0.04
140           72.25       0.65  ...           0.00       10.80

[141 rows x 6 columns]

```

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