Market Metrics

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Contents

Executive summary
Introduction
Geting Data
Overview of data
Portfolio Analysis
KeyMetrics x Porfolio Mitigation
Conclusion

Executive summary

This capstone program is based on evaluating how financial metrics relates to each sector and how to explore which components tends to deliver the best overall risk mitigation portfolio decision and how to create a portfolio.

The data used for this project is on companies that are in the SP500 index. First there is an exploratory analysis of the data and how it relates to the metrics from industries and sector segments as well as its price and risk.

Sectors are then evaluated by daily prices in order to determine the best set of clusters that represents the groups of sectors presented in the SP500.

The first portfolio is created per sector to understand which sectors to chose in order to mitigate risks per ROI (Return on investment), then a second porfolio is created in each sector to evaluate the best and worst companies to mitigate risk.

All 57 metrics are then evaluated per sector and the best and worst companies of portfolio in order to understand how they relate with sectors and risk mitigation.

Lastly the price of the chosen companies of portfolio are predicted and the portfolio is rebalanced per period in order to evaluate how prices prediction changes the behavior of risk mitigation.

Introduction

This project aims to understand how financial metrics relates to each sector and how to explore which components tends to deliver the best overall risk mitigation portfolio decision and how to create a porftolio.

This is a personal attempt to merge a brief study on machine learning techniques and financial analysis from courses from michigan coursera and harvardx. From my perspectiva, most of the financial analysis is usually based on the ratio of risk versus return of an investment.

The issue is that studies teach us how to evaluate companies based on a set of benchmarked metrics and to evaluate data manually, my intent is to organize it in a broader perspective and gather as much data as

possible in order to evaluate critically how financial metrics work per companies segments and how to use this information to evaluate risk and return of a portfolio investment.

This is a broad area of study and many metrics and analysis are beyond my understanding. This means that conceptual mistakes can happen, but I'm willing to evaluate this in order to achieve a better understanding of the market.

Geting Data

Libraries

Load the packages needed for this project:

- Handle API: library(httr) and library(jsonlite)
- Tidy metrics: library(tidyverse)
- List manipulation: library(purrr)
- Data preparation: library(recipes) and library(janitor)
- Data exploration visual: library(patchwork) and library(ggstatsplot)
- Machine learning models: library(h2o)
- Time based preparation: library(anytime), library(timetk) and library(tibbletime)
- Markdown tables: library(knitr) and library(kableExtra)
- Portfolio Analytics: library(PortfloioAnalytics)

```
require(httr) #Working with url
library(jsonlite) #Working with json data for API
library(tidyverse) #Tidy dataframe packages
library(purrr) #list manipulation
library(janitor) # Data cleansing and pivot
library(patchwork) #Easy grid arrange of ggplots
library(tidyquant) #Set of finance packages
library(anytime) #read any type of date format
library(readxl) #read/write excel data
library(stringr) #string manipulation
library(timetk) #tibble format for time based dataframe
library(tibbletime) #tibble format for time based dataframe
library(PortfolioAnalytics) #Porfolio analysis
library(ROI) #Optimization package
library(ROI.plugin.glpk) #Plugins needed
library(ROI.plugin.quadprog) #Plugins needed
library(knitr) #Tables in rmd
library(kableExtra) #Graphics for knitr tables
library(cowplot) #Grid plot for list plots
library(ggstatsplot) #Statistical testing in plot
library(h2o) #Machine learning models
library(lime) #Allow for black box models to be easily evaluated
library(lubridate) #Allow for changes in date format
library(gridExtra)
library(ggdendro)
library(zoo)
library(tsibble)
library(broom)
```

Table 1: API Structure

~	- A	1
Category	Informaton	url
Company Valuation	Symbols List	https://financialmodelingprep.com/api/v3/company/stock/list
Company Valuation	Company Profile	https://financialmodelingprep.com/api/v3/company/profile/
Company Valuation	Income Statement	https://financialmodelingprep.com/api/v3/financials/income-statemer
Company Valuation	Balance Sheet Statement	https://financialmodelingprep.com/api/v3/financials/balance-sheet-st
Company Valuation	Cash Flow Statement	https://financialmodelingprep.com/api/v3/financials/cash-flow-statem
Company Valuation	Company Financial Ratios	https://financialmodelingprep.com/api/v3/financial-ratios/
Company Valuation	Company Enterprise Value	https://financialmodelingprep.com/api/v3/enterprise-value/
Company Valuation	Company Key Metrics	https://financialmodelingprep.com/api/v3/company-key-metrics/
Company Valuation	Company Rating	https://financialmodelingprep.com/api/v3/company/rating/
Stock Price	Stock Real-time Price	https://financialmodelingprep.com/api/v3/stock/real-time-price/
Stock Price	Historical Daily Price	https://financialmodelingprep.com/api/v3/historical-price-full/

```
options(scipen=999)
```

Data

The data obtained is from an API from financial modeling prep.com which consists of:

```
API_Structure <- tribble(
     ~Category, ~Informaton, ~url, ~Options, ~TimeUpdate,
     "Company Valuation", "Symbols List", "https://financialmodelingprep.com/api/v3/company/stock/list", NU
     "Company Valuation", "Company Profile", "https://financialmodelingprep.com/api/v3/company/profile/", "c
     "Company Valuation", "Income Statement", "https://financialmodelingprep.com/api/v3/financials/income-s
     "Company Valuation", "Balance Sheet Statement", "https://financialmodelingprep.com/api/v3/financials/
     "Company Valuation", "Cash Flow Statement", "https://financialmodelingprep.com/api/v3/financials/cash
     "Company Valuation", "Company Financial Ratios", "https://financialmodelingprep.com/api/v3/financial-company Valuation", "Company Enterprise Value", "https://financialmodelingprep.com/api/v3/enterprise Value Val
     "Company Valuation", "Company Key Metrics", "https://financialmodelingprep.com/api/v3/company-key-met
     "Company Valuation", "Company Rating", "https://financialmodelingprep.com/api/v3/company/rating/", "C
     "Stock Price", "Stock Real-time Price", "https://financialmodelingprep.com/api/v3/stock/real-time-pri
     "Stock Price", "Historical Daily Price", "https://financialmodelingprep.com/api/v3/historical-price-f
) %>%
     mutate(id = row number()) %>%
     select(id, everything())
kable(API_Structure[,-1], caption = "API Structure") %>%
     kable_styling(full_width = F)
```

Brief overview of stock lists

In order to use the API structure two functions are created to help getting the data

```
#Company informations
GetCompanyProfile <- function(url, company = NULL){
headers = c(</pre>
```

```
`Upgrade-Insecure-Requests`= '1'
params = list(
  `datatype` = 'json'
res <- httr::GET(url = pasteO(url, "/", company),
                  httr::add_headers(.headers=headers), query = params)
data <- content(res, as = "text")</pre>
data <- from JSON (data, flatten = T) %>%
 flatten_dfr()
return(data)
}
#Get data from API structure
GetData <- function(url, company = NULL, Period = NULL){</pre>
headers = c(
  `Upgrade-Insecure-Requests`= '1'
params = list(
  `datatype` = 'json'
if (is.null(company) & is.null(Period)) {
  res <- httr::GET(url = url,</pre>
                    httr::add_headers(.headers=headers), query = params)
} else if (is.null(Period)) {
 res <- httr::GET(url = paste0(url, "/", company),</pre>
                    httr::add_headers(.headers=headers), query = params)
} else {
  res <- httr::GET(url = pasteO(url,"/",company, "?period=",Period),</pre>
                    httr::add_headers(.headers=headers), query = params)
}
data <- content(res, as = "text")</pre>
data <- from JSON (data, flatten = T) %>%
        detect(is.data.frame) %>%
        as_tibble()
return(data)
```

```
Let's get all company symbols from the API
Stock_Lists <- GetData(url = "https://financialmodelingprep.com/api/v3/company/stock/list")
glimpse(Stock_Lists)
## Observations: 13,854
## Variables: 4
## $ symbol <chr> "SPY", "CMCSA", "KMI", "INTC", "MU", "GDX", "GE", "BAC", "...
              <chr> "SPDR S&P 500", "Comcast Corporation Class A Common Stock"...
## $ name
              <dbl> 254.19, 38.22, 12.64, 50.08, 37.38, 25.50, 7.08, 21.98, 33...
## $ price
## $ exchange <chr> "NYSE Arca", "Nasdaq Global Select", "New York Stock Excha...
There is 13584 symbols, in order to explore the data we must choose a sample set from this dataset. In order
to understand each sector, SP500 companies are a good choice since it is usually used to define how the US
market is and represents a great variety of sectors and industries segments.
#SP500 Indexes
SP500 <- tq_index("SP500")</pre>
## Getting holdings for SP500
Stock_Lists <- GetData(url = "https://financialmodelingprep.com/api/v3/company/stock/list") %>%
               filter(symbol %in% SP500$symbol) %>% #Symbols of SP500
               filter(!symbol %in% c("J", "AMCR")) #Companies that doesn't have data from API and causes
glimpse(Stock_Lists)
## Observations: 502
## Variables: 4
              <chr> "CMCSA", "KMI", "INTC", "MU", "GE", "BAC", "AAPL", "MSFT",...
## $ symbol
              <chr> "Comcast Corporation Class A Common Stock", "Kinder Morgan...
```

Project Data

\$ name

\$ price

From the API structure the data required for this project is: 1. Segments: Data with information of sectors and industries segments of stocks 2. PriceSectors: Price of companies grouped by industries and sectors segments 3. KeyMetrics: Key financial metrics of stock market and companies 4. Historical prices: Stock market prices of companies

\$ exchange <chr> "Nasdaq Global Select", "New York Stock Exchange", "Nasdaq...

<dbl> 38.22, 12.64, 50.08, 37.38, 7.08, 21.98, 252.86, 146.57, 1...

After exhaustive analysis, the capacity of memory for this project is at 400 stock market symbols and because of that the 502 stocks will be reduced to 400 on each data

• Segments:

```
segments <- Stock_Lists[1:400, ] %>% #Filter data for memory capacity
            mutate(Company_Profile = map(symbol, ~GetCompanyProfile(API_Structure[2,4], company = ..1))
            select(Company_Profile) %>% #Select nested list
            unnest() %>% # Unnest it
            mutate(industry = case_when(industry == "" ~ "Funds", TRUE ~ industry), #Set sectors and in
                   sector = case_when(sector == "" ~ "Funds", TRUE ~ sector)) %>%
            select(symbol, companyName, industry, sector) #Select the data required for this dataframe
```

```
glimpse(segments)
## Observations: 400
## Variables: 4
                 <chr> "CMCSA", "KMI", "INTC", "MU", "GE", "BAC", "AAPL", "MSF...
## $ symbol
## $ companyName <chr> "Comcast Corporation Class A Common Stock", "Kinder Mor...
                 <chr> "Entertainment", "Oil & Gas - Midstream", "Semiconducto...
## $ industry
                 <chr> "Consumer Cyclical", "Energy", "Technology", "Technolog...
## $ sector
  • PriceSectors:
PriceSectors <- Stock_Lists[1:400, ] %% #Filter data for memory capacity
                mutate(Company_Profile = map(symbol, ~GetCompanyProfile(API_Structure[2,4],
                                                                         company = ..1))) %>% #Get Data
                select(Company_Profile) %>% #Select nested list
                unnest() %>% # unnest it
                mutate(industry = case_when(industry == "" ~ "Funds", TRUE ~ industry), #Set sectors a
                       sector = case_when(sector == "" ~ "Funds", TRUE ~ sector))
glimpse(PriceSectors)
## Observations: 400
## Variables: 17
                       <chr> "CMCSA", "KMI", "INTC", "MU", "GE", "BAC", "AAPL"...
## $ symbol
## $ price
                       <dbl> 38.22, 12.64, 50.08, 37.38, 7.08, 21.98, 252.86, ...
                       <chr> "1.061551", "0.75548", "0.90978", "1.951096", "1....
## $ beta
                      <chr> "25631996", "16375424", "27534578", "27161027", "...
## $ volAvg
                       <chr> "1.74016823E11", "2.86303601E10", "2.14192161E11"...
## $ mktCap
                     <chr> "0.84", "0.8", "1.26", "0", "0.04", "0.6", "2.92"...
## $ lastDiv
                       <chr> "34.44-47.74", "12.32-22.58", "42.86-69.29", "32....
## $ range
## $ changes
                       <dbl> 2.18, -0.09, 5.47, 2.91, 0.42, 1.54, 10.65, 11.15...
## $ changesPercentage <chr> "(+6.05%)", "(-0.71%)", "(+12.26%)", "(+8.44%)", ...
## $ companyName
                       <chr> "Comcast Corporation Class A Common Stock", "Kind...
                       <chr> "Nasdaq Global Select", "New York Stock Exchange"...
## $ exchange
                       <chr> "Entertainment", "Oil & Gas - Midstream", "Semico...
## $ industry
## $ website
                       <chr> "https://corporate.comcast.com", "http://www.kind...
                       <chr> "Comcast Corp is a media and technology company. ...
## $ description
                       <chr> "Brian L. Roberts", "Steven J. Kean", "Brian M. K...
## $ ceo
                       <chr> "Consumer Cyclical", "Energy", "Technology", "Tec...
## $ sector
## $ image
                       <chr> "https://financialmodelingprep.com/images-New-jpg...
  • KeyMetrics:
Since there are 57 metrics in the API dataset, a description of each metric and measure formula was created
#metrics
path <- "Market KeyMetrics.xlsx"</pre>
Metrics_Info <- path %>%
                excel_sheets() %>%
                set_names() %>%
                map(read_excel, path = path)
kable(head(Metrics_Info$KeyMetrics), caption = "10 Metrics info") %>%
```

kable_styling(full_width = F)

Table 2: 10 Metrics info

Segment	Metric	Explanation	
Fundamental	Revenue per Share	Ratio that computes the total revenue earned per share over a desi	
Income Statement	Net Income per Share	How much of a firm's net income was to each share of common sto	
Fundamental	Operating Cash Flow per Share	Company's ability to generate cash	
Fundamental	Free Cash Flow per Share	How much cash a business generates after accounting for capital ex	
Fundamental	Cash per Share	Available cash to a business divided by the number of equity share	
Fundamental	Book Value per Share	Value of allshares divided by the number of shares issued.	

```
KeyMetrics <- Stock_Lists[1:400, ] %>% #Filter data for memory capacity
              mutate(Company_Key_Metrics = map(symbol, ~GetData(API_Structure[8,4], company = ..1))) %>
              select(symbol, name, Company_Key_Metrics) %>% #Select data and nested API data
              unnest(Company_Key_Metrics) %>% # Unnest it
              gather(key = "metric", value = "value", -symbol, -date, -name) %% # Pivot the metrics pe
              inner_join(segments, by = "symbol") %>% #Get segments data to enrich the dataset
              inner_join(Metrics_Info$KeyMetrics, by = c("metric"="Metric")) %>% #Get the description a
              select(-companyName) %>% # Remove duplicate columns
              mutate(value = as.double(value), date = anydate(date)) %% # Fix data structure
              group_by(metric, Explanation, Formula) %>% # Nest data per metric
              nest()
glimpse(KeyMetrics)
## Observations: 57
## Variables: 4
## Groups: metric, Explanation, Formula [57]
                <chr> "Revenue per Share", "Net Income per Share", "Operating...
## $ Explanation <chr> "Ratio that computes the total revenue earned per share...
## $ Formula
               <chr> "Total revenue / shares", "Net income / average outstan...
## $ data
                 <list<df[,7]>> CMCSA
  • Historical prices:
Historical Prices <- Stock_Lists[1:400, ] %>% #Filter data for memory capacity
                    #Get Data per symbo
                    mutate(Historical_Daily_Price = map(symbol, ~GetData(API_Structure[11,4],
                                                                         company = ..1) %>%
                                                                 mutate(date = anytime(date)))) %>%
                    #Adjust monthly price
                    mutate(Monthly_AdjPrice = map(Historical_Daily_Price, ~..1 %>%
                                                    tq transmute(select = close,
                                                                 mutate_fun = to.monthly,
                                                                 indexAt = "lastof"))) %>%
                    select(-price) %>% # Remove duplicated column
                    inner_join(segments, by = "symbol") %>% #Enrich dataframe with segments data
                    select(symbol:exchange, industry:sector, everything(), -companyName) #Select and or
glimpse(HistoricalPrices)
```

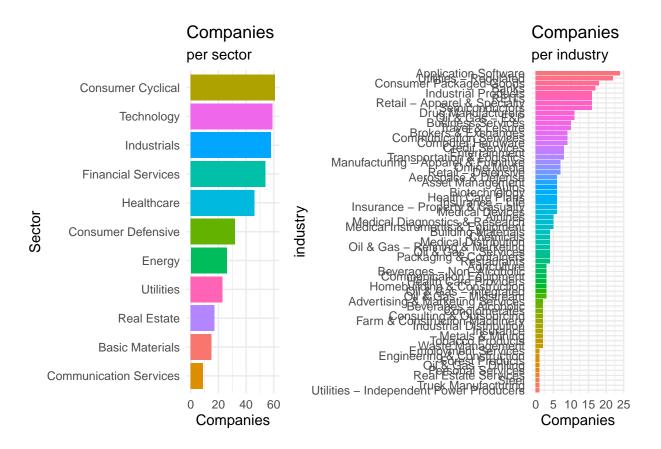
Observations: 400
Variables: 7

Overview of data

Industry & Sector

Let's check the amount of companies per sector and industry segments

```
p1 <- segments %>%
      mutate(industry = fct_rev(fct_infreq(sector))) %>%
      ggplot() +
      aes(x = industry, fill = sector) +
      geom_bar() +
      coord_flip() +
      scale_fill_hue() +
      guides(fill = "none") +
      theme_minimal()+
      labs(title = "Companies", subtitle = "per sector", y = "Companies", x = "Sector")
p2 <- segments %>%
      mutate(industry = fct_rev(fct_infreq(industry))) %>%
      ggplot() +
      aes(x = industry, fill = industry) +
      geom_bar() +
      coord_flip() +
      scale_fill_hue() +
      guides(fill = "none") +
      theme_minimal() +
      labs(title = "Companies", subtitle = "per industry", y = "Companies")
p1 | p2
```



Some discoveries on SP500 companies segments:

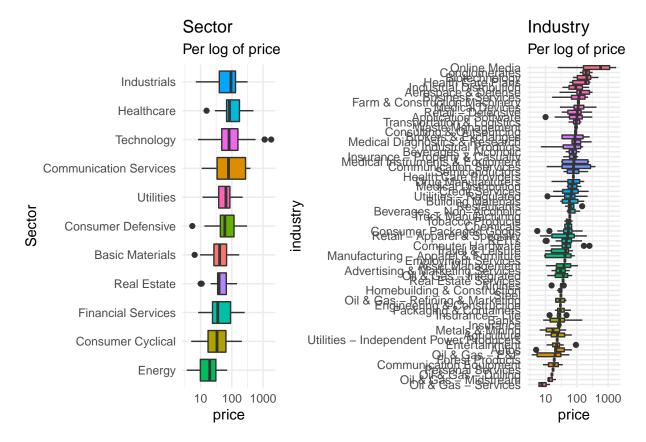
- 1. The maximum amount of companies per sector is around 60 and it seems to be centered around 6 sectors and skewed to the right which could relate to some sectors having more companies in average or being more advantageous to the portfolio.
- 2. Industries segments shows that 6 sectors are mixed in the amount of companies, having software, consumer packaged goods and banks as top amount of companies in SP500

Now let's see how does price is distributed per segments:

```
p1 <- PriceSectors %>%
    mutate(industry = fct_reorder(sector, price)) %>%
    ggplot() +
    aes(x = industry, y = price, fill = sector) +
    geom_boxplot() +
    scale_y_log10() +
    coord_flip() +
    scale_fill_hue() +
    guides(fill = "none") +
    theme_minimal() +
    labs(title = "Sector", subtitle = "Per log of price", x = "Sector")

p2 <- PriceSectors %>%
    mutate(industry = fct_reorder(industry, price)) %>%
    ggplot() +
    aes(x = industry, y = price, fill = industry) +
    geom_boxplot() +
```

```
scale_y_log10() +
coord_flip() +
scale_fill_hue() +
guides(fill = "none") +
theme_minimal()+
labs(title = "Industry", subtitle = "Per log of price")
p1 | p2
```

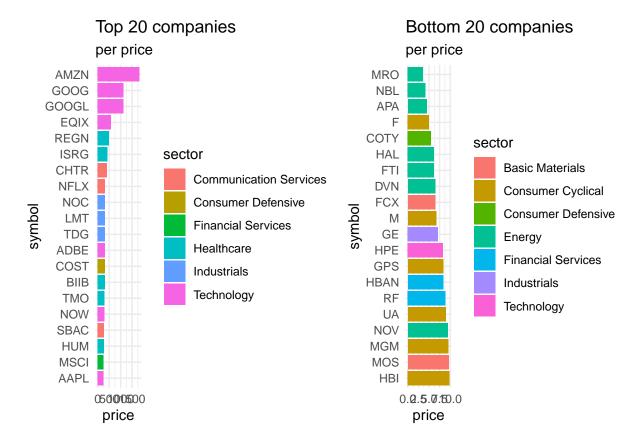


It seems that price per sector is usually around at the same mean with some variability, this variability is explained by the huge aount of difference on industry segment. This means that industry segment is a better metric to evaluate the dispersion of price rather than sectors.

Let's check the top/bottom 20 companies prices

```
p1 <- PriceSectors %>%
    mutate(price = as.double(price)) %>%
    arrange(-price) %>%
    head(20) %>%
    mutate(symbol = fct_reorder(symbol, price)) %>%
    ggplot() +
    aes(x = symbol, y = price, fill = sector) +
    geom_col() +
    coord_flip() +
    scale_fill_hue() +
    theme_minimal() +
    labs(title = "Top 20 companies", subtitle = "per price")
```

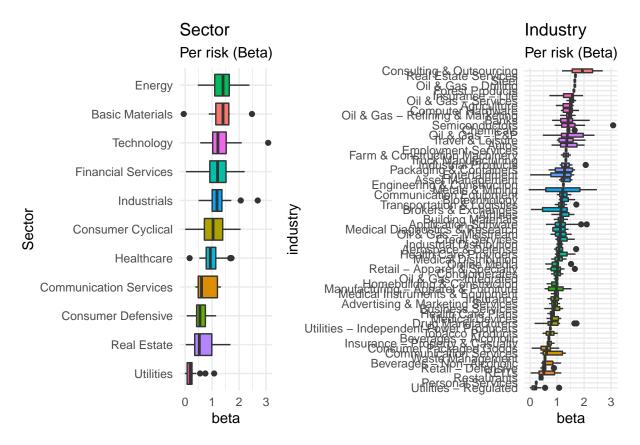
```
p2 <- PriceSectors %>%
    mutate(price = as.double(price)) %>%
    filter(price > 0) %>%
        arrange(price) %>%
        head(20) %>%
        mutate(symbol = fct_rev(fct_reorder(symbol, price))) %>%
        ggplot() +
        aes(x = symbol, y = price, fill = sector) +
        geom_col() +
        coord_flip() +
        scale_fill_hue() +
        theme_minimal() +
        labs(title = "Bottom 20 companies", subtitle = "per price")
p1 | p2
```



It does seem that those 6 sectors variability grants them in general the top 20 and bottom companies price Now let's see how does risk is distributed per segments:

```
p1 <- PriceSectors %>%
    mutate(beta = as.double(beta)) %>%
    mutate(industry = fct_reorder(sector, beta)) %>%
    ggplot() +
    aes(x = industry, y = beta, fill = sector) +
    geom_boxplot() +
```

```
coord_flip() +
      scale_fill_hue() +
      guides(fill = "none") +
      theme_minimal() +
      labs(title = "Sector", subtitle = "Per risk (Beta)", x = "Sector")
p2 <- PriceSectors %>%
      mutate(beta = as.double(beta)) %>%
      mutate(industry = fct_reorder(industry, beta)) %>%
      ggplot() +
      aes(x = industry, y = beta, fill = industry) +
      geom_boxplot() +
      coord flip() +
      scale_fill_hue() +
      guides(fill = "none") +
      theme_minimal() +
      labs(title = "Industry", subtitle = "Per risk (Beta)")
p1 | p2
```



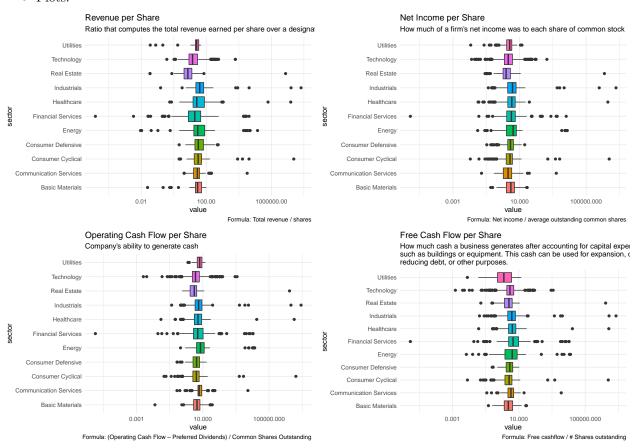
It seems that risk per sector changes slightly and it's quite impressive to see that energy and basic materials are on the top risk sector. On industry side, it seems some oindustries have a lot of variability on risk and consulting & outsourcing industry is on the top, it seems counterintuitive, I was expected to see financial services and technology being riskier.

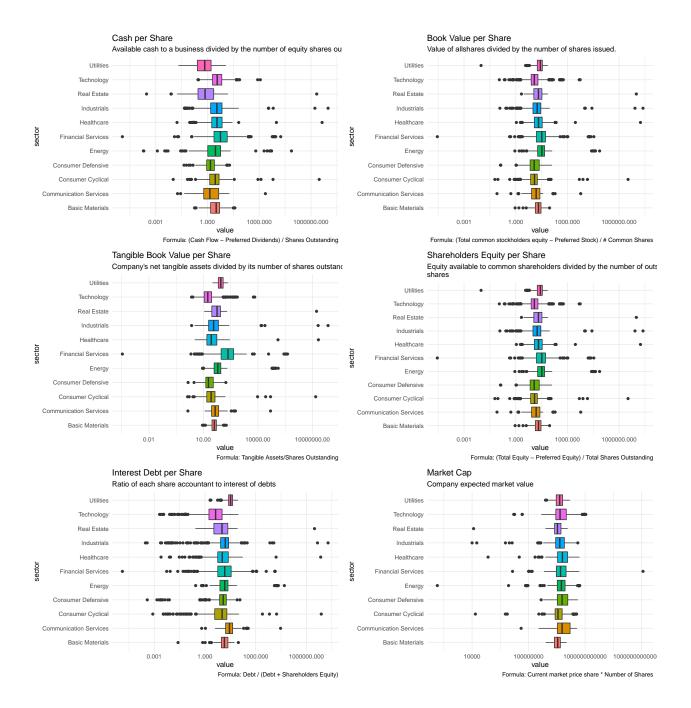
KeyMetrics

Since there are 57 metrics, it's important to create a ggplot function and use it in each sector, this function will include in the labs of plot the brief explanation and the formula in order to help understand each metric

```
plots <- function(data, metric, Explanation, Formula){
    ggplot(data) +
        aes(x = sector, y = value, fill = sector) +
        geom_boxplot() +
        scale_fill_hue() +
        scale_y_continuous(trans = "log10") +
        theme_minimal() +
        coord_flip() +
        guides(fill = "none") +
        labs(title = metric, subtitle = Explanation, caption = paste0("Formula: ",Formula))
}</pre>
```

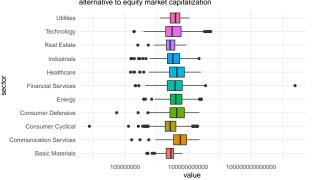
• Plots:





Enterprise Value

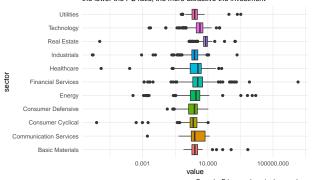
Measure of a company's total value, often used as a more comprehens alternative to equity market capitalization



Formula: Market capitalization + Debt + Minority Shareholders + Preference Shares - Cash & Cash equivalents

Price to Sales Ratio

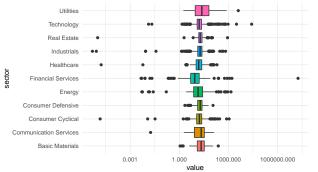
Company's market capitalization divided by the revenue of the past 12 r the lower the PS ratio, the more attractive the investment



Formula: Price per share / sales per share

PFCF ratio

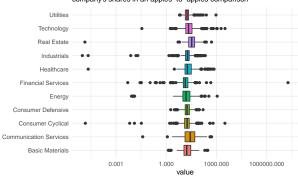
Price to free cash flow ratio is a valuation method used to compare a cocurrent share price to its per-share free cash flow



Formula: Price per share / (Cash flow / Shares outstanding)

PE ratio

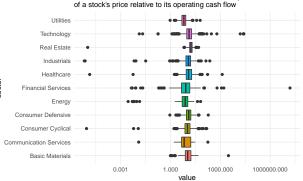
Price to earnings ratio is a measure to determine the relative value of a company's shares in an apples-to-apples comparison



Formula: Earnings per Share / Price per Share

POCF ratio

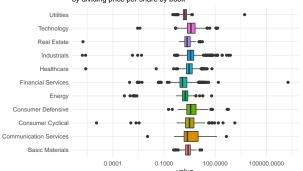
Price to cash flow stock valuation indicator or multiple that measures th



Formula: Share price / Operating Cash Flow per Share

PB ratio

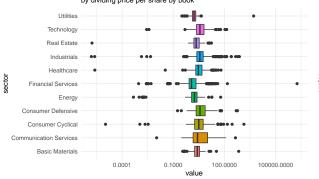
Price to book ratio is to compare a firm's market to book value and is do by dividing price per share by book



Formula: Market price per share / Book value per share

PTB ratio

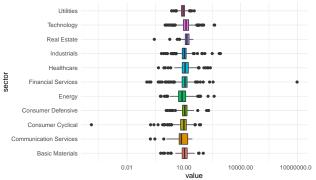
Price to book ratio is to compare a firm's market to book value and is deby dividing price per share by book



Formula: (total assets - total liabilities) / number of shares

Enterprise Value over EBITDA

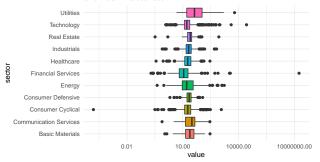
Good measure to estimate the cash flow of a company



Formula: (Market Capitalization + Preferred Shares + Minority Interest + Debt - Total Cash) / EBITDA

EV to Free cash flow

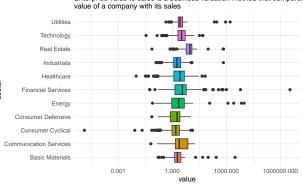
Compares the total valuation of the company with its ability to generate cashflow, he lower the ratio of enterprise value to the free cash flow figure the faster a company can pay back the cost of its acquisition or generat to reinvest in its business



Formula: Free Cash Flow / Enterprise Value

EV to Sales

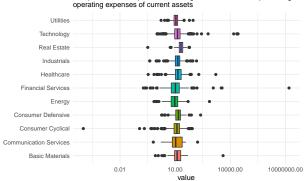
Enterprise value to sales is a business valuation method that compares



Formula: (Market Capitalizato + Debt - Cash Cash) / Annual Sales

EV to Operating cash flow

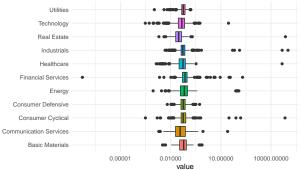
Enteprise value to op cash flow is a good to measure the percentage al



Formula: (Market Capitalization + Total Debt - Cash)/Cash from Operations

Earnings Yield

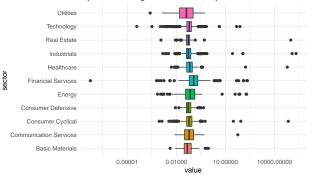
Earnings per share for the most recent 12–month period divided by the market price per share.



Formula: Earnings per Share / Price per Share

Free Cash Flow Yield

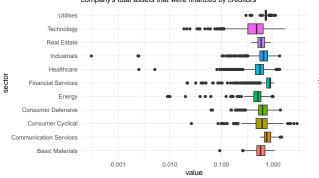
Financial solvency ratio that compares the free cash flow per share a α expected to earn against its market value per share



Formula: Free Cash Flow / Market Capitalization

Debt to Assets

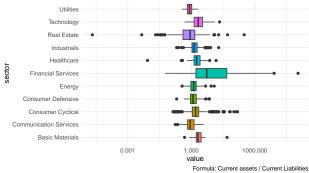
Indicator of a company's financial leverage. It tells you the percentage c company's total assets that were financed by creditors



Formula: Total debts / total assets

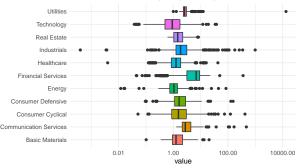
Current ratio

Liquidity ratio that measures whether a firm has enough resources to m short-term obligations. It compares a firm's current assets to its current liabilities



Debt to Equity

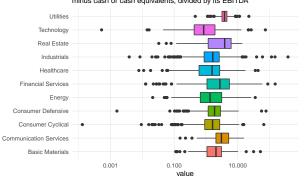
Financial ratio indicating the relative proportion of shareholders' equity debt used to finance a company's assets. Closely related to leveraging, ratio is also known as risk, gearing or leverage



Formula: Total liabilites / total equity

Net Debt to EBITDA

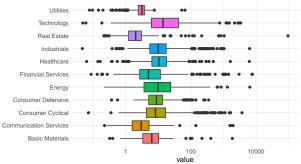
Measurement of leverage, calculated as a company's interest–bearing I minus cash or cash equivalents, divided by its EBITDA



Formula: (Total Debt-Cash&Equivalents) / EBITDA

Interest Coverage

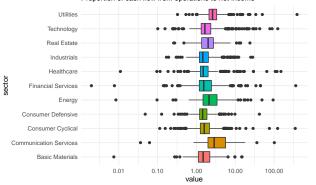
Measure of a company's ability to meet its interest payments. Interest c ratio is equal to earnings before interest and taxes (EBIT) for a time per often one year, divided by interestexpenses for the same time period



Formula: EBIT / Interest Expense

Income Quality

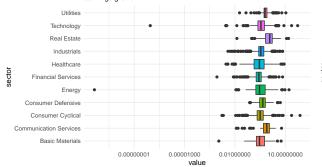
Proportion of cash flow from operations to net income



Formula: Net cash from operating activities / Net income

Payout Ratio

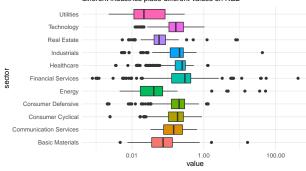
Fraction of net income a firm pays to its stockholders in dividends: The of earnings not paid to investors is left for investment to provide for futule arnings growth



Formula: Total dividend Payments / (Net income + Noncash expenses - Noncash sales)

R&D to Revenue

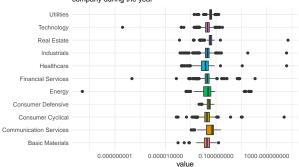
Measures the percentage of sales that is allocated to R&D expenditure: is not as effective when looking at companies in different industries bec different industries place different values on R&D



Formula: Total R&D / Total sales revenue

Dividend Yield

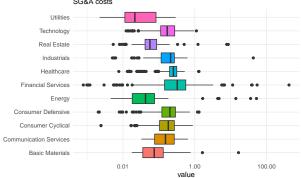
Dividend yield is used to calculate the earning on investment (shares) considering only the returns in the form of total dividends declared by the company during the year



Formula: Annual dividend / Current Stock Pricec

SG&A to Revenue

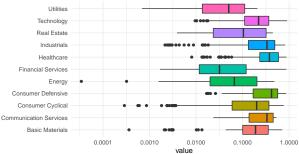
It tells you what percent of every dollar your company earned gets suck SG&A costs



Formula: Total SG&A / Total sales revenue

Intangibles to Total Assets

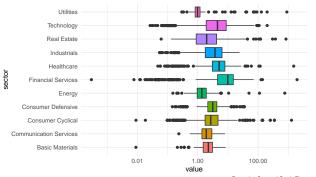
The goodwill to assets ratio is a financial measurement that compares t intangible assets like a brand name, customer list, or unique position in industry to the total assets of the company in an effect to see if goodwil being recorded properly



Formula: Intangibles / Total Assets

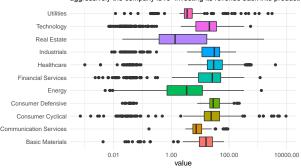
Capex to Operating Cash Flow

Assesses how much of a company's cash flow from operations is being capital expenditure



Formula: Capex / Cash Flow

The Capex to Revenue ratio measures a company's investments in projection and other capital assets to its total sales. The ratio shows he aggressively the company is re–investing its revenue back into producti

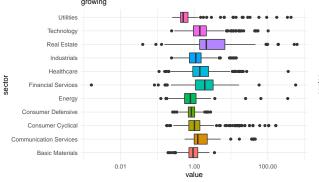


Capex to Revenue

Formula: Capex / Revenue

Capex to Depreciation

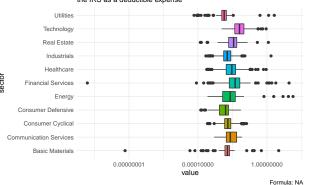
If a company regularly has more CapEx than depreciation, its asset bas



Formula: Capex / Depreciation

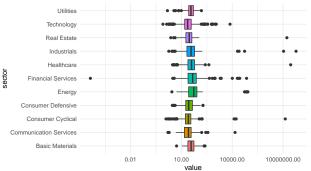
Stock-based compensation to Revenue

Represents a noncash expense that reduces book income, which isn't the IRS as a deductible expense



Graham Number

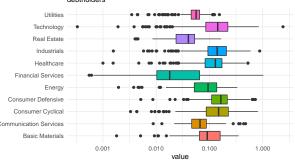
The Graham number is a figure that measures a stock's fundamental $\nu_{\!R}$ taking into account the company's earnings per share and book value p



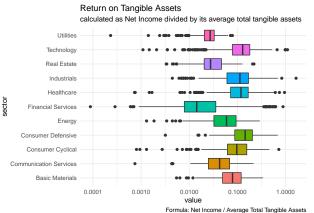
Formula: sqrt(22.5 * earnings per share * book value)

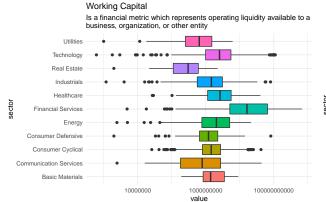
ROIC

Return on invested capital, is a ratio used in finance, valuation and accounting, as a measure of the profitability and value-creating potenti companies relative to the amount of capital invested by shareholders are debtholders.

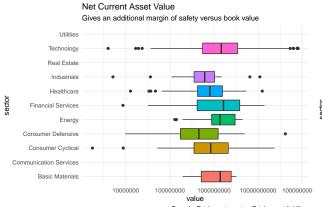


Formula: NA





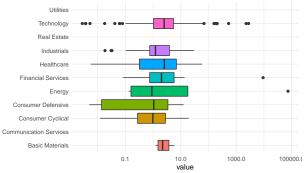
Formula: Accounts receivable + Inventory - Accounts payable



Formula: Total curret assets - Total current liabilites

Graham Net-Net

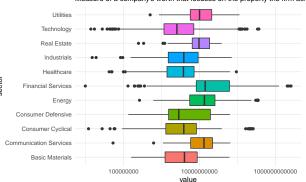
Net-net is a value investing technique in which a company is valued ba on its net current assets



Formula: (Current Assets - Total Liabilities + Preferred Stock / Shares Outstanding

Tangible Asset Value

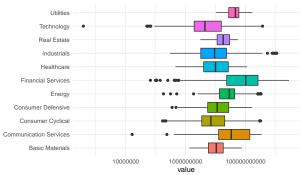
Measure of a company's worth that focuses on the property the firm act



Formula: Total assets - Intangible assets - Total liabilities

Invested Capital

Total amount of money raised by a company by issuing securities to eq shareholders and debt to bondholders



Formula: (Net income – dividend) / (debt + equity)

Average Receivables Total amount of money owed to your business by your customers from account divided by AR periods Utilities Technology Real Estate Industrials Healthcare Financial Services Energy Communication Services Basic Materials 1000000000 100000000000 10000000 Formula: Average of Receivables

Days Sales Outstanding

Utilities Technology

Real Estate

Industrials

Healthcare

Consumer Defensive

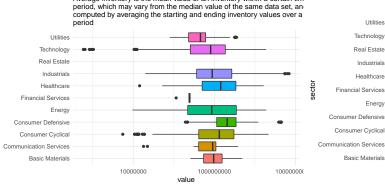
Consumer Cyclical

Basic Materials

Measure of the average number of days that it takes a company to colle after a sale has been made



Average Payables



Average inventory is the mean value of an inventory within a certain tim

Formula: Average of inventory

Days of Inventory on Hand

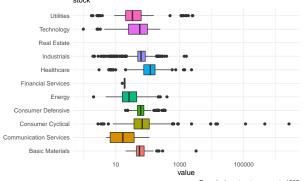
Measure of how quickly a business uses up the average inventory it ker stock

value

100

Formula: accounts receivable / Total Credits sales * Nperiods

10000

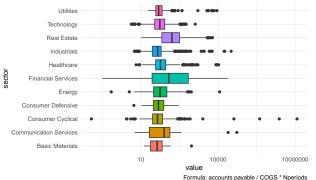


Formula: inventory turnover rate / 365

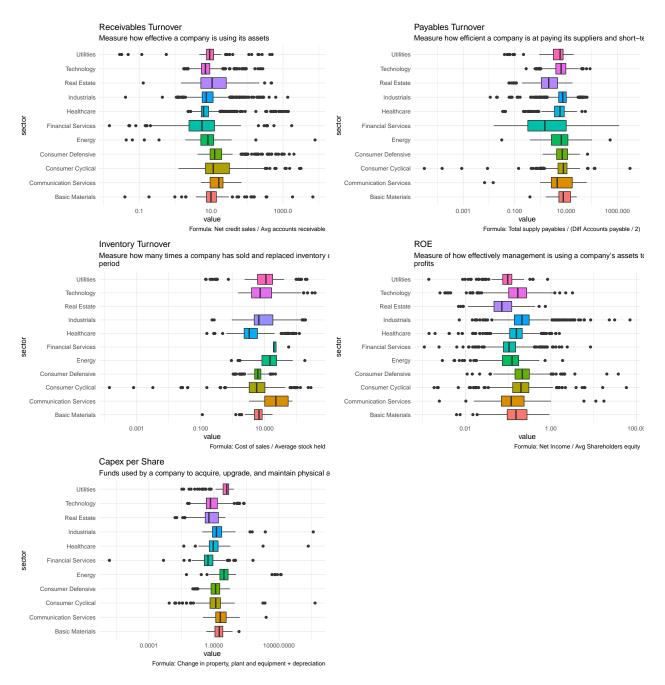
Days Payables Outstanding

Average Inventory

Financial ratio that indicates the average time (in days) that a company to pay its bills and invoices to its trade creditors



Formula: accounts payable / COGS * Nperiods



It seems that some metrics could be correlated and many of them tends to have the same pattern per sectors. That lead us to the question on how to evaluate them in risk mitigation assets, this will be done in the next chapter.

We can see that metrics that clearly show a difference in results per sectors are:

- 1. Debt to equity
- 2. Current ratio
- 3. Interest coverage
- 4. SG&A to revenue
- 5. R&D to revenue
- 6. Intangibles to assets
- 7. Capex to operating cash flow

- 8. Capex to revenue
- 9. ROIC
- 10. Return on tangible assets
- 11. Working capital
- 12. Tangible Asset Value
- 13. Average Inventory
- 14. Days sales outstanding
- 15. Days payables outstanding
- 16. Days of inventory on hand
- 17. Receivables turnover
- 18. Inventory turnover
- 19. ROE

It is important to notice that x-axis is on log scale, that means that other metrics could be included as well

Let's check how these metrics are correlated

```
KeyMetrics %>%
    unnest(data) %>%
    ungroup() %>% #removes grouped data, otherwise select will bring grouped atributes as well
    select(sector, metric, symbol, date, value) %>% # select variables needed to spread
    spread(key = metric, value = value) %>% # spread metrics to column that will be correlated
    select(-sector, -symbol, -date) %>% # remove columns not needed
   drop_na() %>% #Remove any na on metrics data, to fix correlation function return NA
    cor() %>% # Apply correlation function
    as.data.frame() %>% # Convert matrix class to data frame
    rownames to column("Metric") %>% # Include row names id from matrix to a column named data frame
    gather( "metric", "correlation", -Metric) %>% # gather all correlation into a single column
    filter (Metric != metric) %>% # Remove any metrics equal (That results in correlation 1)
    arrange(-correlation) %>% # Arrange correlation, this will be used in id creation later
    filter(correlation >= 0.8) %% # Filter only correlations greater than 0.8
   mutate(id = case_when(Metric == lag(metric, 1) ~ 1, TRUE ~ 0)) %>% # Column created to remove dupli
   filter(id == 1) %>% # Removing duplicates
    select(-id) %>% # Removing aux column
   kable(caption = "Correlation of metrics greather than 80%") %>%
   kable_styling(full_width = F)
```

\begin{table}

\caption{Correlation of metrics greather than 80%}

Metric	metric	correlation
Book Value per Share	Shareholders Equity per Share	1.0000000
Enterprise Value	Market Cap	1.0000000
EV to Operating cash flow	POCF ratio	1.0000000
EV to Free cash flow	PFCF ratio	0.9999999
Enterprise Value over EBITDA	Market Cap	0.9999999
PB ratio	PTB ratio	
Enterprise Value	Enterprise Value over EBITDA	0.9999999
Enterprise Value over EBITDA	PE ratio	0.9999999
PE ratio		0.9999999
	Market Cap	0.9999998
Market Cap	PE ratio	0.9999998
PE ratio	Enterprise Value	0.9999998
Enterprise Value	PE ratio	0.9999998
EV to Sales	Price to Sales Ratio	0.9999993
Enterprise Value over EBITDA	PFCF ratio	0.9999987
PFCF ratio	Market Cap	0.9999986
Market Cap	PFCF ratio	0.9999986
PFCF ratio	Enterprise Value	0.9999986
Enterprise Value	PFCF ratio	0.9999986
PFCF ratio	PE ratio	0.9999986
PE ratio	PFCF ratio	0.9999986
PFCF ratio	EV to Operating cash flow	0.9999986
EV to Operating cash flow	PFCF ratio	0.9999986
PFCF ratio	POCF ratio	0.9999985
Enterprise Value over EBITDA	EV to Free cash flow	0.9999984
EV to Free cash flow	EV to Operating cash flow	0.9999984
EV to Free cash flow	Market Cap	0.9999984
Enterprise Value	EV to Free cash flow	0.9999984
EV to Free cash flow	PE ratio	0.9999983
EV to Free cash flow	POCF ratio	0.9999982
Enterprise Value over EBITDA	EV to Operating cash flow	0.9999974
Enterprise Value over EBITDA	POCF ratio	0.9999973
EV to Operating cash flow	Market Cap	0.9999973
Enterprise Value	EV to Operating cash flow	0.9999973
Market Cap	POCF ratio	0.9999973
POCF ratio	Enterprise Value	0.9999973
Enterprise Value	POCF ratio	0.9999973
EV to Operating cash flow	PE ratio	0.9999972
PE ratio	POCF ratio	0.9999972
	Price to Sales Ratio	0.9999972
Enterprise Value over EBITDA Price to Sales Ratio		
	Market Cap Price to Sales Ratio	0.9999971
Market Cap Price to Sales Ratio		0.9999971
	Enterprise Value	0.9999971
Enterprise Value	Price to Sales Ratio	0.9999971
Price to Sales Ratio	PE ratio	0.9999971
PE ratio	Price to Sales Ratio	0.9999971
Price to Sales Ratio	PFCF ratio	0.9999959
PFCF ratio	Price to Sales Ratio	0.9999959
Price to Sales Ratio	EV to Free cash flow	0.9999956
EV to Free cash flow	Price to Sales Ratio	0.9999956
Enterprise Value over EBITDA	PB ratio	0.9999952
PB ratio	Market Cap	0.9999952
Market Cap	PB ratio	0.9999952
PB ratio	Enterprise Value	0.9999952
Enterprise Value	PB ratio	0.9999952
Enterprise Value over EBITDA	PTB ratio	0.9999952
PB ratio	PE ratio	0.9999951
Market Can	PTR ratio	0.0000051

\end{table}

This is very interesting, it seems that 32 metrics have a correlation with one of these metrics by greather than 80% as we could see in the metrics plots.

That actually makes sense because these metrics formulas are shared or have a common hierarchy formula variable.

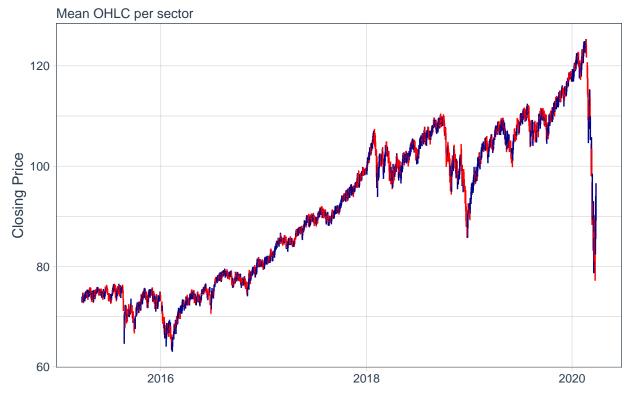
That still lead us the question of risk mitigation on portfolio assets to these metrics, even though they're correlated that doesn't mean that these assets will follow the same pattern. In the next chapter this will be analyzed

Price

Let's take a look on market price in SP500 and per sector.

```
#Candlestick for SP500
HistoricalPrices %>%
   select(sector, Historical_Daily_Price) %>%
   unnest() %>%
   group_by(date) %>%
   summarise(close = mean(close), open = mean(open), low = mean(low), high = mean(high)) %>%
   ggplot(aes(x = date, y = close)) +
   geom_candlestick(aes(open = open, high = high, low = low, close = close)) +
   labs(title = "SP500 Candlestick Chart",
        subtitle = "Mean OHLC per sector",
        y = "Closing Price", x = "") +
   theme_tq()
```

SP500 Candlestick Chart



This candlestick time series plot shows some very interesting analysis:

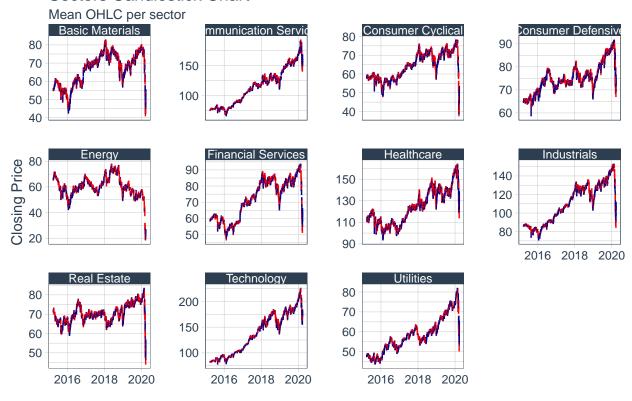
- 1. Huge drop in the market due to coronavirus, it does seem to be one of the worst drops in the market for SP500.
- 2. Market has a lot of drops and ups, but usually shows some trends upwards stoped by some peaked collapses that we know are related to economy breakdowns.

Let's evaluate the same plot per sector

```
#Candlestick per sector
Sector_Daily_OHLC <- HistoricalPrices %>%
    select(sector, Historical_Daily_Price) %>%
    unnest() %>%
    group_by(sector,date) %>%
    summarise(close = mean(close), open = mean(open), low = mean(low), high = mean(high))

Sector_Daily_OHLC %>%
    ggplot(aes(x = date, y = close, group = sector)) +
    geom_candlestick(aes(open = open, high = high, low = low, close = close)) +
    labs(title = "Sectors Candlestick Chart",
        subtitle = "Mean OHLC per sector",
        y = "Closing Price", x = "") +
    facet_wrap(~ sector, ncol = 4, scale = "free_y") +
    theme_tq()
```

Sectors Candlestick Chart



It does seem that all sectors were havily impacted, although technology and communication services were a bit less impacted in percent to its previous downfall price

Another intereseting thing is that some sectors seems to have a similar pattern, by looking at them it seems we have 3 groups of sectors.

Let's take a look on these clusters, we'll use a silhouette method to define the optimal amount of clusters in sectors price

```
Clustering <- function(Cluster_DF, Df_aux){
    require(gridExtra)
    require(ggdendro)
    require(zoo)
    require(purrr)
    require(tsibble)
    require(broom)

# Clustering
    hc <- hclust(dist(t(Df_aux[,-1])), "ave")

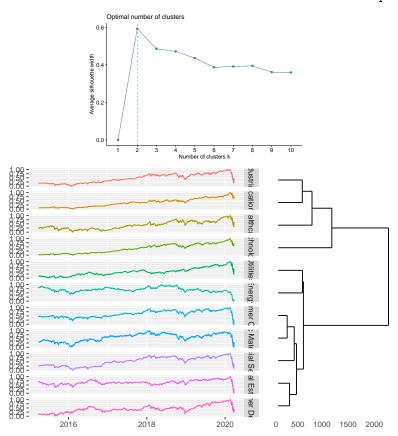
# 8.1 DF clusters
    library(factoextra)
NbClust <- fviz_nbclust(Df_aux[,-1], FUN = hcut, method = "silhouette")

k <- which.max(NbClust$data$y)</pre>
```

```
cut_avg <- cutree(hc, k = k) %>%
    tidy() %>%
    rename("Data"="names", "cluster"="x")
  # Number of clusters plot
  NbClustersPlot <- plot(NbClust)</pre>
  ### Plot
  hcdata <- dendro_data(hc)
  names_order <- hcdata$labels$label</pre>
  # Use the folloing to remove labels from dendogram so not doubling up - but good for checking
  hcdata$labels$label <- ''
  p1 <- ggdendrogram(hcdata, rotate=TRUE, leaf_labels=FALSE)
  # Autoplot only accepts time series data type
  Zoo_DF <- read.zoo(Df_aux)</pre>
  # Scale the time series and plot
  maxs <- apply(Zoo_DF, 2, max)</pre>
  mins <- apply(Zoo_DF, 2, min)
  joined_ts_scales <- scale(Zoo_DF, center = mins, scale = maxs - mins)</pre>
 new data <- joined ts scales[,rev(as.character(names order))]</pre>
 p2 <- autoplot(new data, facets = Series ~ . ) +
    xlab('') + ylab('') + theme(legend.position="none")
  gp1<-ggplotGrob(p1)</pre>
  gp2<-ggplotGrob(p2)</pre>
  grid <- grid.arrange(gp2, gp1, ncol=2, widths=c(4,2))</pre>
  aux <- data.frame(Model_Name = Cluster_DF) %>%
    mutate(Clustered = purrr::map(Model_Name, ~cut_avg),
           hc = purrr::map(Model_Name, ~hc),
           NbClust= purrr::map(Model_Name, ~NbClust),
           NbClustersPlot= purrr::map(Model_Name, ~NbClustersPlot),
           p1= purrr::map(Model_Name, ~p1),
           p2= purrr::map(Model_Name, ~p2),
           grid = purrr::map(Model_Name, ~grid)
    )
 return(aux)
Clust_DF <- Sector_Daily_OHLC %>%
            select(sector, date, close) %>%
            spread(sector, close) %>%
```

```
filter_all(all_vars(!is.na(.)))
Clusters <- Clustering("Sectors", Clust_DF)</pre>
```

Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa



That's interesting! We have 2 groups of clusters, let's organize them:

Now let's see how returns are ocurring annually per sector

```
#Annual returns per sectors
HistoricalPrices %>%
unnest(Monthly_AdjPrice) %>%
group_by(sector) %>%
tq_transmute(select = close, mutate_fun = periodReturn, period = "yearly", type = "arithmetic") %>%
ggplot(aes(x = date, y = yearly.returns, fill = sector)) +
    geom_col() +
    geom_hline(yintercept = 0, color = palette_light()[[1]]) +
    scale_y_continuous(labels = scales::percent) +
```

Table 3: Sector Clusters

sector	cluster
Basic Materials	1
Consumer Cyclical	1
Consumer Defensive	1
Energy	1
Financial Services	1
Real Estate	1
Utilities	1
Communication Services	2
Healthcare	2
Industrials	2
Technology	2

```
labs(title = "Sectors: Annual Returns",
    y = "Annual Returns", x = "") +
facet_wrap(~ sector, ncol = 4, scales = "free_y") +
theme_tq() +
theme(axis.text.x = element_text(angle = 90, hjust = 1),
    legend.position = "none") +
scale_fill_tq()
```





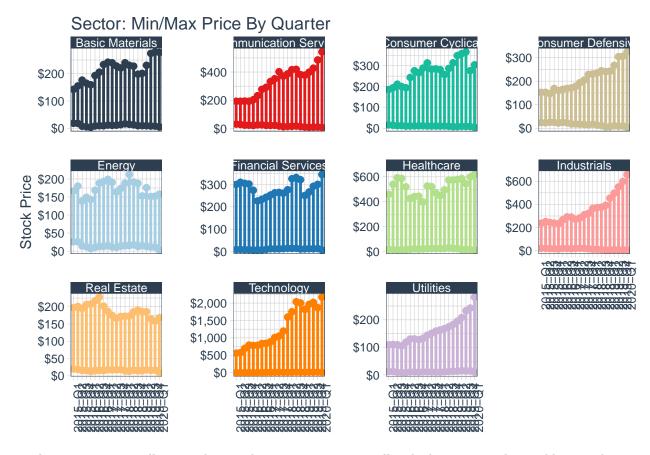
It seems that in general, the market has some downsides and upsides in annual return for all sectors, but it

seems we have a huge drop on return untill this moment of 2020 due to coronavirus.

Another interesting result from this plot is that some sectors have some good percentual margin increase, but thats could be done due to low price being affected by any trend just as it seems to occur with basic materials.

The last analysis is to understand how prices moves quarterly, for that we'll get a min/max quarterly price per sector plot

```
#Quaterly max min per sector
Sector_max_by_qtr <- HistoricalPrices %>%
                      unnest(Historical Daily Price) %>%
                      group_by(sector) %>%
                      tq_transmute(select = close, mutate_fun = apply.quarterly, FUN= max,
                                   col_rename = "max.close") %>%
                      mutate(year.qtr = paste0(lubridate::year(date), "-Q",
                                               lubridate::quarter(date))) %>%
                      select(-date)
Sector_min_by_qtr <- HistoricalPrices %>%
        unnest(Historical_Daily_Price) %>%
        group by(sector) %>%
        tq_transmute(select = close, mutate_fun = apply.quarterly,
                     FUN= min, col_rename = "min.close") %>%
        mutate(year.qtr = paste0(lubridate::year(date), "-Q",
                                 lubridate::quarter(date))) %>%
        select(-date)
Sector_by_qtr <- left_join(Sector_max_by_qtr, Sector_min_by_qtr,</pre>
                           by = c("sector" = "sector", "year.qtr" = "year.qtr"))
Sector_by_qtr %>%
  ggplot(aes(x = year.qtr, color = sector)) +
  geom_segment(aes(xend = year.qtr, y = min.close, yend = max.close),
               size = 1) +
  geom_point(aes(y = max.close), size = 2) +
  geom_point(aes(y = min.close), size = 2) +
  facet_wrap(~ sector, ncol =4, scale = "free_y") +
  labs(title = "Sector: Min/Max Price By Quarter",
       y = "Stock Price", color = "") +
  theme_tq() +
  scale_color_tq() +
  scale_y_continuous(labels = scales::dollar) +
  theme(axis.text.x = element_text(angle = 90, hjust = 1),
        axis.title.x = element_blank(),
        legend.position = "none")
```



This is interesting, all sectors have as low price as zero as well as higher prices. This could mean that companies could be integrated into SP500 quaterly and therefore have low prices due to start in the market, or that the market variability is across all sectors evenly.

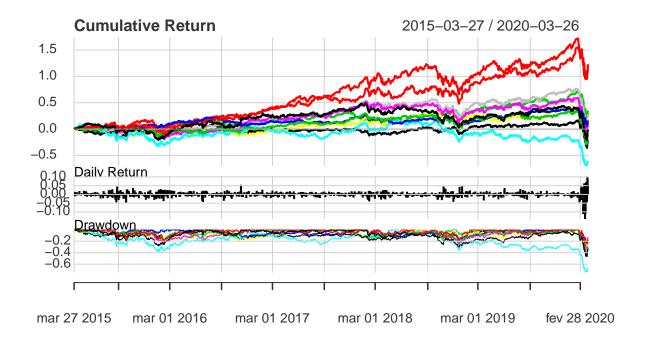
The major difference is that some sectors are more variable than others, and there are those that achieve higher prices in the long run such as technology sectors

Portfolio Analysis

Sectors

Let's make a portfolio with risk mitigation in order to evaluate how the optimization tries to deal with sector returns

Sectors Performance



Let's run the portfolio in order to minimize risk and evaluate it's sector allocation called weight

```
extractWeights() %>%
data.frame(Name = names(.), weights = round(.,3), row.names = NULL) %>%
select(-.)
```

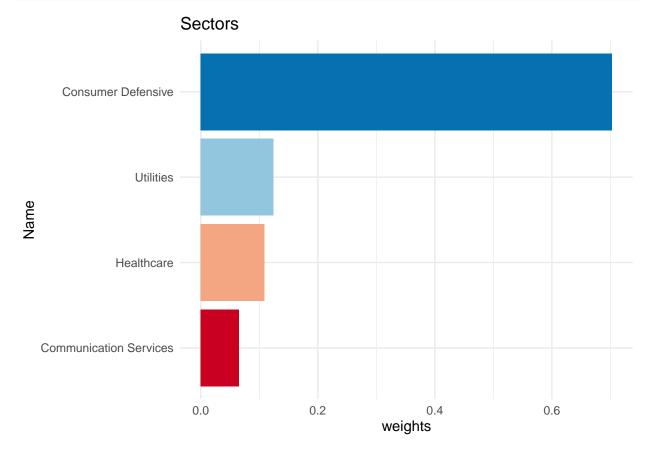
Let's plot these weights

```
plots2 <- function(weights, sector=NULL){

plot <- weights %>%
    mutate(Name = fct_reorder(Name, weights)) %>%
    filter(weights > 0.01) %>%
    ggplot(aes(x = Name, y=weights, fill = Name)) +
    geom_col() +
    scale_fill_brewer(palette = "RdBu") +
    theme_minimal() +
    coord_flip() +
    guides(fill = "none") +
    labs(title = paste0("Sectors ", sector))

return(plot)
}

plots2(SectorReturns)
```

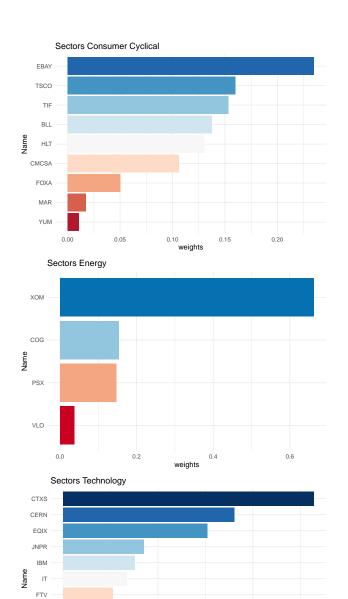


Let's check how each company per sector is structured in this portfolio analysis.

Companies per sector

Since there are 400 countries and the main idea here is to understand how metrics relate to risk mitigation, we'll record only the final result of the best and worst weight allocation of portfolio companies per sector

```
#Since we have to model this grouped per sector, all this piece of script is doing is merging the same
Symbol_Returns <- HistoricalPrices %>%
  select(symbol,sector, Historical_Daily_Price) %>%
  unnest() %>%
  group_by(sector) %>%
  nest() %>%
  mutate(data = map(data, ~..1 %>%
                          select(symbol, date, close) %>%
                          group_by(symbol) %>%
                          tq transmute(select
                                                 = close,
                                       mutate_fun = periodReturn,
                                       period = "daily",
                                       col_rename = "close") %>%
                          spread(symbol, close) %>%
                          filter_all(all_vars(!is.na(.))) %>%
                          tk_xts(data = ., date_var = date, silent = TRUE)))
#Optimizing per each purrr list of sectors
Symbol_Returns <- Symbol_Returns %>%
                  mutate(optimize = map(data, ~Optimize(..1)))
#Simple extract weights and organizing it to be able to plot
Symbol_Returns <- Symbol_Returns %>%
  mutate(weights = map(optimize, extractWeights),
         weights = map(weights, ~data.frame(Name = names(..1),
                                            weights = ..1, row.names = NULL)))
#Extracting worst and best symbols and ploting each sector weights
Symbol_Returns <- Symbol_Returns %>%
       mutate(Best = map(weights, ~ filter(..1, weights == max(weights)) %>%
                            select(Name)),
               Worst = map(weights, ~ filter(..1, weights == min(weights)) %>%
                            select(Name)),
              plots = map(weights, ~plots2(...1, sector)))
walk(Symbol_Returns$plots, plot)
```



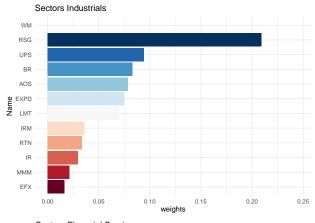
TEL AKAM AMZN EA

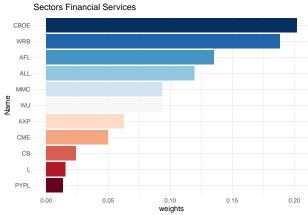
0.0

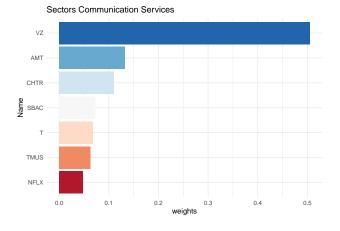
0.1

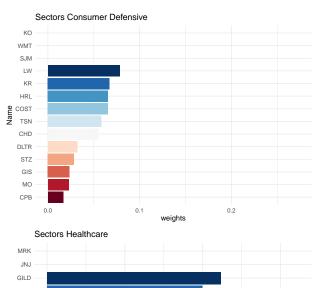
weights

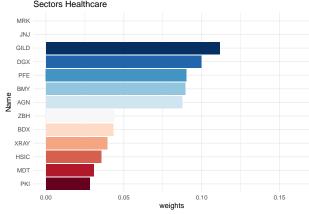
0.2

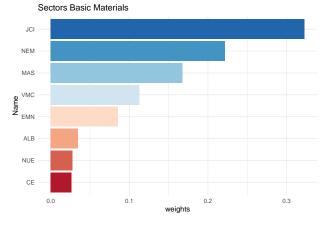


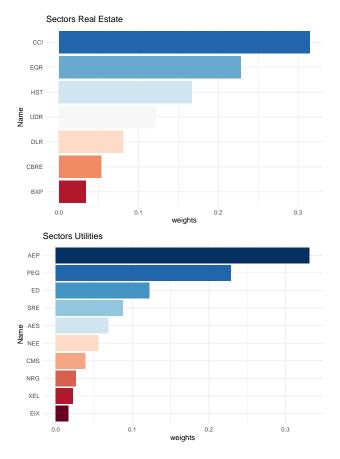












Now we can analyse each metric per best and worst companies allocated portfolio for risk mitigation.

KeyMetrics x Porfolio Mitigation

Best x Worst companies per sector

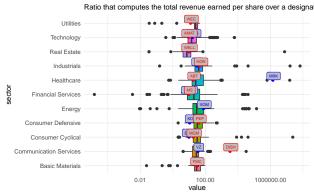
All we have to do know is to include the best and worst companies per sector in the keyMetrics dataset and plot each metric including the position of both best and worst companies in order to understand if these metrics relate to a decision on risk mitigation portfolio

Table 4: Best and Worst company per Porfolio risk mitigation

sector	Best	Worst
Consumer Cyclical	EBAY	MGM
Energy	XOM	FTI
Technology	CTXS	AMAT
Industrials	WM	HON
Financial Services	CBOE	MS
Communication Services	VZ	DISH
Consumer Defensive	KO	PEP
Healthcare	MRK	ABT
Basic Materials	JCI	FMC
Real Estate	CCI	WELL
Utilities	AEP	WEC

Plots

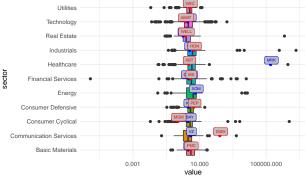




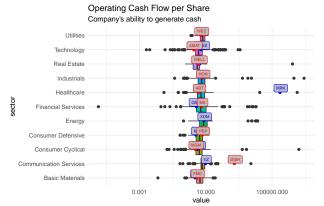
Formula: Total revenue / shares

Net Income per Share

How much of a firm's net income was to each share of common stock



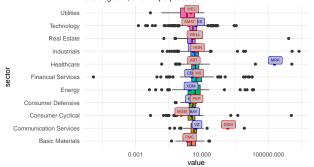
Formula: Net income / average outstanding common shares



Formula: (Operating Cash Flow – Preferred Dividends) / Common Shares Outstanding

Free Cash Flow per Share

How much cash a business generates after accounting for capital expersuch as buildings or equipment. This cash can be used for expansion, creducing debt, or other purposes.



Formula: Free cashflow / # Shares outstanding

Cash per Share

Available cash to a business divided by the number of equity shares ou

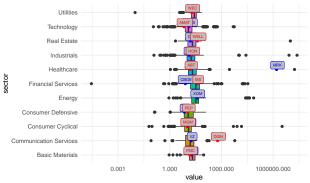
Utilities
Technology
Real Estate
Industrials
Healthcare
Energy
Consumer Defensive
Consumer Cyclical
Communication Services
Basic Materials

0.001
1.000
1000.000
1000000.000

Formula: (Cash Flow – Preferred Dividends) / Shares Outstanding

Book Value per Share

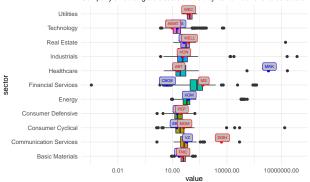
Value of allshares divided by the number of shares issued.



Formula: (Total common stockholders equity – Preferred Stock) / # Common Shares

Tangible Book Value per Share

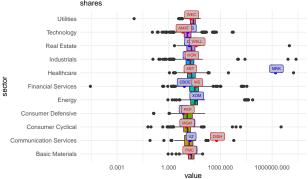
Company's net tangible assets divided by its number of shares outstand



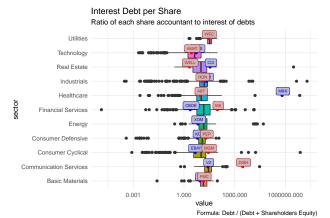
Formula: Tangible Assets/Shares Outstanding

Shareholders Equity per Share

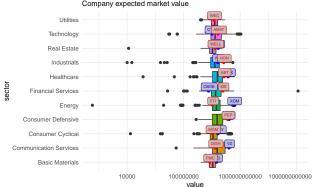
Equity available to common shareholders divided by the number of outs shares



Formula: (Total Equity – Preferred Equity) / Total Shares Outstanding



Market Cap Company expected market value



Formula: Current market price share * Number of Shares

Measure of a company's total value, often used as a more comprehens alternative to equity market capitalization Utilities Technology Real Estate Industrials Healthcare Financial Services Energy Consumer Defensive Consumer Cyclical Communication Services

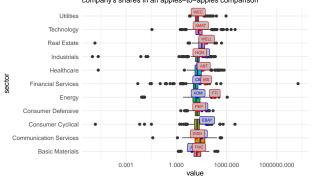
Enterprise Value

value
Formula: Market capitalization + Debt + Minority Shareholders + Preference Shares – Cash & Cash equivalents

100000000000

PE ratio

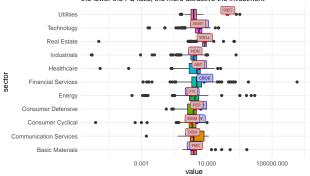
Price to earnings ratio is a measure to determine the relative value of a company's shares in an apples–to–apples comparison



Formula: Earnings per Share / Price per Share

Price to Sales Ratio

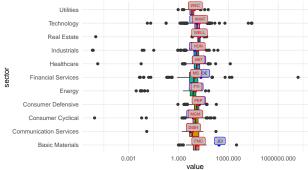
Company's market capitalization divided by the revenue of the past 12 the lower the PS ratio, the more attractive the investment



Formula: Price per share / sales per share

POCF ratio

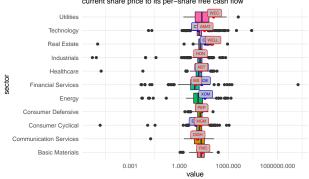
Price to cash flow stock valuation indicator or multiple that measures th of a stock's price relative to its operating cash flow



Formula: Share price / Operating Cash Flow per Share

PFCF ratio

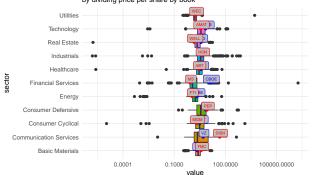
Price to free cash flow ratio is a valuation method used to compare a courrent share price to its per-share free cash flow



Formula: Price per share / (Cash flow / Shares outstanding)

PB ratio

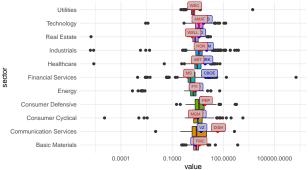
Price to book ratio is to compare a firm's market to book value and is de by dividing price per share by book



Formula: Market price per share / Book value per share

PTB ratio

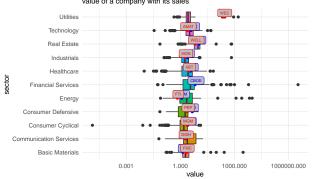
Price to book ratio is to compare a firm's market to book value and is deby dividing price per share by book



Formula: (total assets - total liabilities) / number of shares

EV to Sales

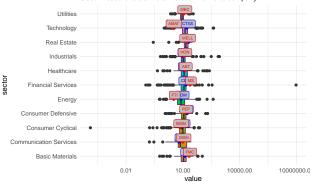
Enterprise value to sales is a business valuation method that compares value of a company with its sales



Formula: (Market Capitalizato + Debt - Cash Cash) / Annual Sales

Enterprise Value over EBITDA

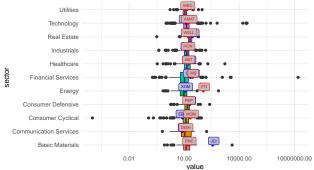
Good measure to estimate the cash flow of a company



Formula: (Market Capitalization + Preferred Shares + Minority Interest + Debt - Total Cash) / EBITDA

EV to Operating cash flow

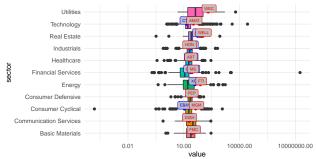
Enteprise value to op cash flow is a good to measure the percentage al operating expenses of current assets



Formula: (Market Capitalization + Total Debt - Cash)/Cash from Operations

EV to Free cash flow

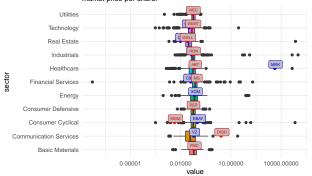
Compares the total valuation of the company with its ability to generate cashflow, he lower the ratio of enterprise value to the free cash flow figithe faster a company can pay back the cost of its acquisition or generat to reinvest in its business



Formula: Free Cash Flow / Enterprise Value

Earnings Yield

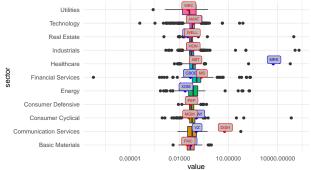
Earnings per share for the most recent 12–month period divided by the market price per share.



Formula: Earnings per Share / Price per Share

Free Cash Flow Yield

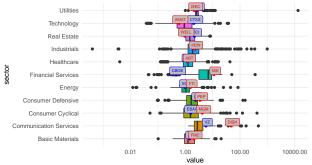
Financial solvency ratio that compares the free cash flow per share a α expected to earn against its market value per share



Formula: Free Cash Flow / Market Capitalization

Debt to Equity

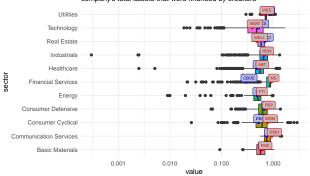
Financial ratio indicating the relative proportion of shareholders' equity debt used to finance a company's assets. Closely related to leveraging, ratio is also known as risk, gearing or leverage



Formula: Total liabilites / total equity

Debt to Assets

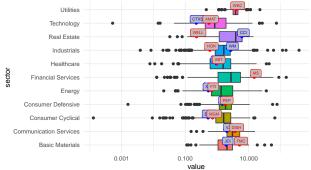
Indicator of a company's financial leverage. It tells you the percentage c company's total assets that were financed by creditors



Formula: Total debts / total assets

Net Debt to EBITDA

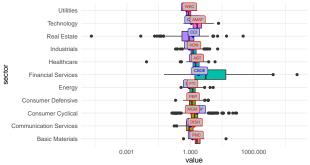
Measurement of leverage, calculated as a company's interest–bearing I minus cash or cash equivalents, divided by its EBITDA



Formula: (Total Debt–Cash&Equivalents) / EBITDA

Current ratio

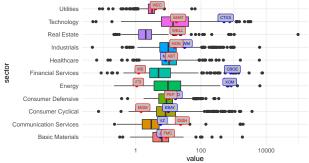
Cincidity ratio that measures whether a firm has enough resources to m short-term obligations. It compares a firm's current assets to its current liabilities



Formula: Current assets / Current Liabilities

Interest Coverage

Measure of a company's ability to meet its interest payments. Interest c ratio is equal to earnings before interest and taxes (EBIT) for a time per often one year, divided by interestexpenses for the same time period



Formula: EBIT / Interest Expense

Income Quality

Proportion of cash flow from operations to net income

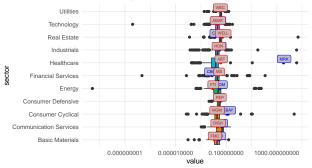
Utilities
Technology
Real Estate
Industrials
Healthcare
Energy
Consumer Opelical
Communication Services
Basic Materials

0.01
0.10
1.00
10.00
100.00

Formula: Net cash from operating activities / Net income

Dividend Yield

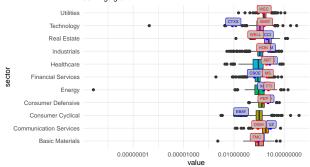
Dividend yield is used to calculate the earning on investment (shares) considering only the returns in the form of total dividends declared by the company during the year



Formula: Annual dividend / Current Stock Pricec

Payout Ratio

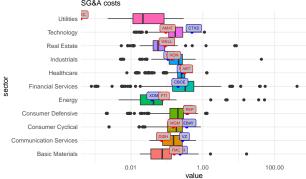
Fraction of net income a firm pays to its stockholders in dividends: The of earnings not paid to investors is left for investment to provide for futuearnings growth



Formula: Total dividend Payments / (Net income + Noncash expenses - Noncash sales)

SG&A to Revenue

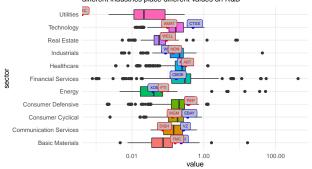
It tells you what percent of every dollar your company earned gets suck SG&A costs



Formula: Total SG&A / Total sales revenue

R&D to Revenue

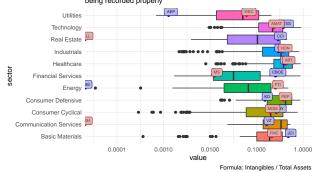
Measures the percentage of sales that is allocated to R&D expenditure is not as effective when looking at companies in different industries bec different industries place different values on R&D



Formula: Total R&D / Total sales revenue

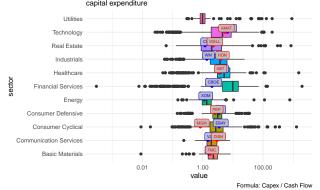
Intangibles to Total Assets

The goodwill to assets ratio is a financial measurement that compares t intangible assets like a brand name, customer list, or unique position in industry to the total assets of the company in an effect to see if goodwil being recorded properly



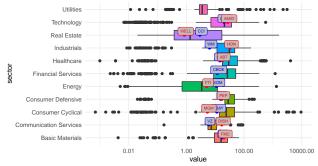
Capex to Operating Cash Flow

Assesses how much of a company's cash flow from operations is being capital expenditure



Capex to Revenue

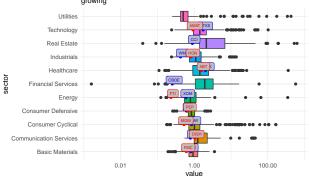
The Capex to Revenue ratio measures a company's investments in projequipment and other capital assets to its total sales. The ratio shows he aggressively the company is re–investing its revenue back into producti



Formula: Capex / Revenue

Capex to Depreciation

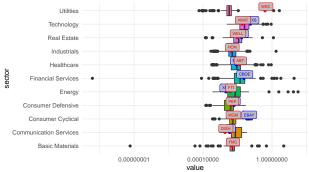
If a company regularly has more CapEx than depreciation, its asset bas



Formula: Capex / Depreciation

Stock-based compensation to Revenue

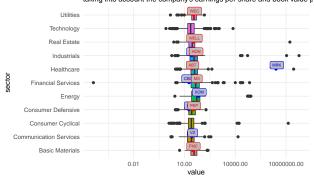
Represents a noncash expense that reduces book income, which isn't the IRS as a deductible expense



Formula: NA

Graham Number

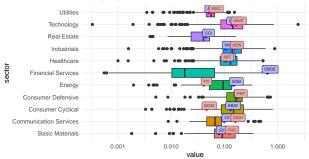
The Graham number is a figure that measures a stock's fundamental vataking into account the company's earnings per share and book value p



Formula: sqrt(22.5 * earnings per share * book value)

ROIC

Return on invested capital, is a ratio used in finance, valuation and accounting, as a measure of the profitability and value-creating potentic companies relative to the amount of capital invested by shareholders are debtholders.



Formula: NA

1.0000

Return on Tangible Assets calculated as Net Income divided by its average total tangible assets

0.0010

Communication Services Basic Materials

0.0001

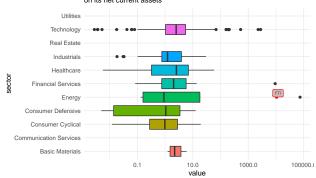
Utilities Technology Real Estate Industrials Healthcare Financial Services Consumer Defensive Consumer Cyclical

0.0100

0.1000 value Formula: Net Income / Average Total Tangible Assets

Graham Net-Net

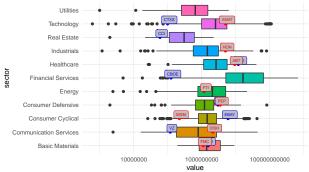
Net-net is a value investing technique in which a company is valued ba on its net current assets



Formula: (Current Assets - Total Liabilities + Preferred Stock / Shares Outstanding

Working Capital

Is a financial metric which represents operating liquidity available to a business, organization, or other entity



Formula: Accounts receivable + Inventory - Accounts payable

Tangible Asset Value

100000000

Basic Materials

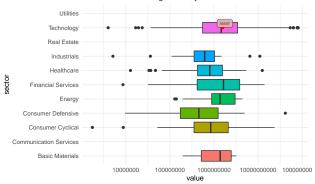
Measure of a company's worth that focuses on the property the firm acl Utilities Technology Real Estate Industrials Healthcare Financial Services Energy Consumer Defensive Communication Services

> 10000000000 value Formula: Total assets - Intangible assets - Total liabilities

1000000000000

Net Current Asset Value

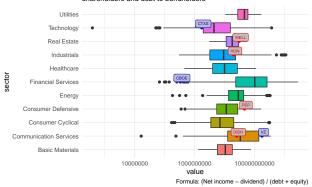
Gives an additional margin of safety versus book value



Formula: Total curret assets - Total current liabilities

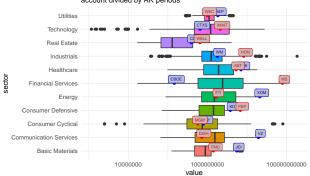
Invested Capital

Total amount of money raised by a company by issuing securities to eq shareholders and debt to bondholders



Average Receivables

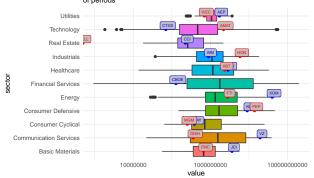
Total amount of money owed to your business by your customers from account divided by AR periods



Formula: Average of Receivables

Average Payables

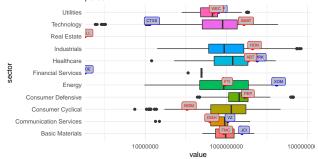
Total amount of money the business owes the customers account divide of periods



Formula: Average of Payables

Average Inventory

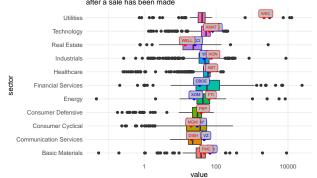
Average inventory is the mean value of an inventory within a certain tim period, which may vary from the median value of the same data set, an computed by averaging the starting and ending inventory values over a period



Formula: Average of inventory

Days Sales Outstanding

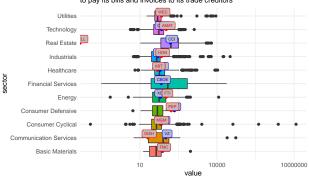
Measure of the average number of days that it takes a company to colle after a sale has been made



Formula: accounts receivable / Total Credits sales * Nperiods

Days Payables Outstanding

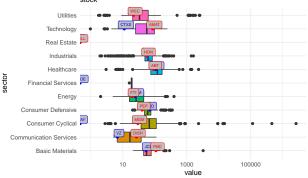
Financial ratio that indicates the average time (in days) that a company to pay its bills and invoices to its trade creditors



Formula: accounts payable / COGS * Nperiods

Days of Inventory on Hand

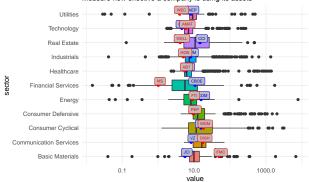
Measure of how quickly a business uses up the average inventory it ker stock



Formula: inventory turnover rate / 365

Receivables Turnover

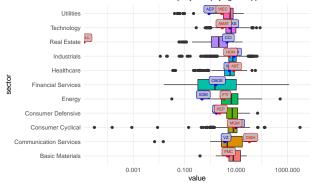
Measure how effective a company is using its assets



Formula: Net credit sales / Avg accounts receivable

Payables Turnover

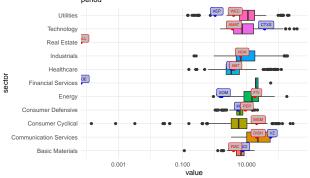
Measure how efficient a company is at paying its suppliers and short-te



Formula: Total supply payables / (Diff Accounts payable / 2)

Inventory Turnover

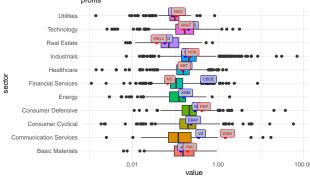
Measure how many times a company has sold and replaced inventory operiod



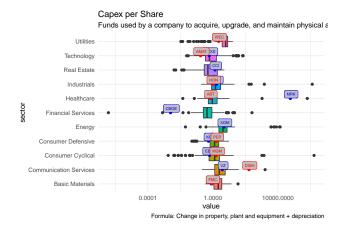
Formula: Cost of sales / Average stock held

ROE

Measure of how effectively management is using a company's assets $\ensuremath{\mathsf{tr}}$ profits



Formula: Net Income / Avg Shareholders equity



Thats awesome!! It does seem that some metrics and sector differ in relation to portfolio risk mitigation.

Let's just remember first that:

- 1. Sectors are correlated and we managed to find 2 clusters between them, this will be ignored in order to evaluate them per each sector
- 2. Metrics are correlated and we found that 32 of them are strongly correlated, but the main goal of this project is to evaluate per metric how they infer as a good result or bad result for risk mitigation. This is important though, if you're willing to analyze any subject including these metrics together, the strongest correlation will bias your model.
- 3. Prices have erratic movement that might injury any machine learning models and must be annomalized, this will be used for last chapter of this project when we model forecast for prices

Model

In order to model this, we'll follow the strategy:

- 1. List group sectors and get symbols weight the porftolio risk mitigation
- 2. Model how each metric value associates to the risk weight

In order to model it we'll use a GLM function from H2O wich consists of the formula:

$$\hat{y} = x^T \beta + \beta_0$$

Let's model it:

```
#Let's create a function with h2o to help us model per sector
h2o.init(max_mem_size = "5g")
##
## H2O is not running yet, starting it now...
## Note: In case of errors look at the following log files:
       C:\Users\EDUARD~1.ALM\AppData\Local\Temp\RtmpABkP1t/h2o_eduardo_almeida_started_from_r.out
       C:\Users\EDUARD~1.ALM\AppData\Local\Temp\RtmpABkP1t/h2o_eduardo_almeida_started_from_r.err
##
##
##
## Starting H20 JVM and connecting: Connection successful!
##
## R is connected to the H2O cluster:
##
       H2O cluster uptime:
                                    3 seconds 491 milliseconds
##
       H20 cluster timezone:
                                    America/Sao_Paulo
##
       H2O data parsing timezone: UTC
##
                                    3.26.0.2
       H20 cluster version:
       H2O cluster version age:
##
                                    8 months !!!
##
       H2O cluster name:
                                    H20_started_from_R_eduardo.almeida_snc915
##
      H2O cluster total nodes:
##
      H2O cluster total memory:
                                   4.44 GB
##
       H2O cluster total cores:
##
       H2O cluster allowed cores: 8
##
       H2O cluster healthy:
                                    TRUE
##
                                   localhost
       H20 Connection ip:
      H2O Connection port:
##
                                    54321
##
       H2O Connection proxy:
                                   NA
##
       H20 Internal Security:
                                   FALSE
##
       H2O API Extensions:
                                    Amazon S3, Algos, AutoML, Core V3, Core V4
       R Version:
                                    R version 3.6.2 (2019-12-12)
h2o.no_progress()
H2o_Model <- function(Data,x, y){</pre>
  require(h2o)
  require(tidyverse)
  require(purrr)
  Data$sector <- as.factor(Data$sector)</pre>
  Data_h2o <- as.h2o(Data)
  set.seed(123)
  automl_glm <- h2o.glm(</pre>
    x = x,
    y = y,
    training_frame = Data_h2o)
  Name_Model <- "H2O_GLM"
  coef <- h2o.coef(automl_glm) %>%
```

```
as.data.frame()
  #Model summary
  CV_Summary <- h2o.performance(automl_glm)</pre>
  \# explainer \leftarrow lime(x = Data[,x],
                       # model = automl qlm)
  \# explanation <- explain(x = Data[,x], explainer = explainer, bin_continuous = TRUE,
                             # feature_select = "auto", n_features = 2)
  # Features_Plot <- plot_features(explanation, cases = 1)</pre>
  aux <- data.frame(Model_Name = Name_Model) %>%
    mutate(Model = map(Model_Name, ~automl_glm),
           coefs = map(Model_Name, ~coef),
           CV_Summary = map(Model_Name, ~CV_Summary)#,
           #explanation = map(Model_Name, ~explanation),
           #Features_Plot = map(Model_Name, ~Features_Plot)
    )
 return(aux)
}
# Let's model
KeyMetrics <- KeyMetrics %>%
               mutate(H2o_Model = map(data2, ~H2o_Model(...1, x = c("value", "sector"),
                                                         y = "weights")))
h2o.shutdown(prompt = F)
## [1] TRUE
#Organize coeficients for kable
Coefiecients <- KeyMetrics %>%
                mutate(coefs = map(H2o Model, ~..1$coefs %>%
                              reduce(as.data.frame) %>%
                              rownames_to_column(var = "Parameter"))) %>%
                ungroup() %>%
                select(metric, coefs) %>%
                unnest(coefs) %>%
                rename("value" = ".") %>%
                mutate(Parameter = gsub(Parameter, pattern = "sector.", replacement = "")) %>%
                spread(key = Parameter, value = value) %>%
                select(metric, Intercept, value, everything()) %>%
                arrange(-Intercept, -value)
```

Let's check the coeficients

```
kable(Coefiecients, caption = "Metrics coeficients per sectors", digits = 3) %>%
kable_styling(bootstrap_options = "striped", full_width = F, font_size = 10)
```

This is great! As showed in the charts before, it does seem that metrics and sectors differs between each other in terms of risk mitigation.

In order to understand this table we must first understand how it works:

- 1. The value is a weight multiplication to the metric value, when it's negative it means that metrics value that are negatives will deliver higher risk mitigation.
- 2. When we get a difference between values and sector weights we can actually see that some sectors tend to increase or decrease the final risk mitigation by the metric

That means that we can actually measure theses metrics by comparing the highest ratio of difference from value to sector values in regards of negative x positive weights in order to understand:

- 1. Metrics that deliver the higher information gain for each sector
- 2. Metrics that deliver higher information gain in overall

This will not be done in this project.

Conclusion

This projects seeked to evaluate how each metric is related to a risk mitigation in a portfolio and how it differs per sectors.

For future projects we can measure:

- 1. Metrics that deliver the higher information gain for each sector
- 2. Metrics that deliver higher information gain in overall
- 3. Impact of other variables such as macroeconomic metrics and sentiment analysis of news
- 4. Predict the future price of models and re-model it for portfolio mitigation
- 5. Compare companies that are not in SP500 or have lower prices but have a good result on metrics and assess how it is used for risk mitigation with a lower price bond

sessionInfo()

```
## R version 3.6.2 (2019-12-12)
## Platform: x86_64-w64-mingw32/x64 (64-bit)
## Running under: Windows 10 x64 (build 18362)
##
## Matrix products: default
##
## locale:
## [1] LC_COLLATE=Portuguese_Brazil.1252 LC_CTYPE=Portuguese_Brazil.1252
## [3] LC_MONETARY=Portuguese_Brazil.1252 LC_NUMERIC=C
  [5] LC_TIME=Portuguese_Brazil.1252
##
## attached base packages:
## [1] stats
                 graphics grDevices utils
                                               datasets methods
                                                                    base
##
## other attached packages:
  [1] factoextra 1.0.6
                                   broom 0.5.4
## [3] tsibble_0.8.6
                                   ggdendro_0.1-20
   [5] gridExtra 2.3
                                   lime 0.5.1
##
##
   [7] h2o_3.26.0.2
                                   ggstatsplot_0.3.1
  [9] cowplot_1.0.0
                                   kableExtra_1.1.0
```

Table 5: Metrics coeficients per sectors

Table 5: Metrics coeficients per sectors							
metric	Intercept	value	Basic Materials	Communication Services	Consumer Cycl		
Debt to Assets	0.041	-0.013	0.035	0.077	-0.		
Working Capital	0.033	0.000	0.035	0.074	-0.		
Payables Turnover	0.033	0.000	0.035	0.075	-0.		
Invested Capital	0.033	0.000	0.035	0.075	-0.		
Net Current Asset Value	0.033	0.000	0.035	0.075	-0.		
Stock-based compensation to Revenue	0.033	-0.001	0.035	0.075	-0.		
Current ratio	0.033	0.000	0.035	0.075	-0.		
Days Payables Outstanding	0.033	0.000	0.035	0.075	-0.		
Days of Inventory on Hand	0.033	0.000	0.035	0.075	-0.		
EV to Sales	0.033	0.000	0.035	0.075	-0.		
Price to Sales Ratio	0.033	0.000	0.035	0.075	-0.		
POCF ratio	0.033	0.000	0.035	0.075	-0.		
EV to Operating cash flow	0.033	0.000	0.035	0.075	-0.		
PB ratio	0.033	0.000	0.035	0.075	-0.		
PTB ratio	0.033	0.000	0.035	0.075	-0.		
Enterprise Value over EBITDA	0.033	0.000	0.035	0.075	-0.		
PE ratio	0.033	0.000	0.035	0.075	-0.		
Market Cap	0.033	0.000	0.035	0.075	-0.		
PFCF ratio	0.033	0.000	0.035	0.075	-0.		
EV to Free cash flow	0.033	0.000	0.035	0.075	-0.		
Enterprise Value	0.033	0.000	0.035	0.075	-0.		
Days Sales Outstanding	0.033	0.000	0.035	0.075	-0.		
Net Debt to EBITDA	0.033	0.000	0.035	0.075	-0.		
SG&A to Revenue	0.033	0.000	0.035	0.075	-0.		
R&D to Revenue	0.033	0.000	0.035	0.075	-0.		
Receivables Turnover	0.033	0.000	0.035	0.075	-0.		
Debt to Equity	0.033	0.000	0.035	0.075	-0.		
Revenue per Share	0.033	0.000	0.035	0.075	-0.		
Capex per Share	0.033	0.000	0.035	0.075	-0.		
Graham Net-Net	0.033	0.000	0.035	0.075	-0.		
ROE	0.033	0.000	0.035	0.075	-0.		
Tangible Book Value per Share	0.033	0.000	0.035	0.075	-0.		
Interest Debt per Share	0.033	0.000	0.035	0.075	-0.		
Net Income per Share	0.033	0.000	0.035	0.075	-0.		
Operating Cash Flow per Share	0.033	0.000	0.035	0.075	-0.		
Free Cash Flow per Share	0.033	0.000	0.035	0.075	-0.		
Free Cash Flow Yield	0.033	0.000	0.035	0.075	-0.		
Cash per Share	0.033	0.000	0.035	0.075	-0.		
Graham Number	0.033	0.000	0.035	0.075	-0.		
Earnings Yield	0.033	0.000	0.035	0.075	-0.		
Shareholders Equity per Share	0.033	0.000	0.035	0.075	-0.		
Book Value per Share	0.033	0.000	0.035	0.075	-0.		
Dividend Yield	0.033	0.000	0.035	0.075	-0.		
Payout Ratio	0.033	0.000	0.035	0.075	-0.		
Income Quality	0.033	0.000	0.035	0.075	-0.		
Capex to Revenue	0.033	0.000	0.035	0.075	-0.		
Interest Coverage	0.033	0.000	0.035	0.075	-0.		
Capex to Operating Cash Flow	0.033	0.000	0.035	0.075	-0.		
Tangible Asset Value	0.033	0.000	0.036	0.075	-0.		
Capex to Depreciation	0.032	0.000	0.035	0.073	-0.		
Average Payables	0.032	0.000	0.036	0.074	-0. -0.		
Inventory Turnover		630.000	0.035	0.074	-0. -0.		
Return on Tangible Assets	0.032	0.015	0.035	0.074	-0. -0.		
Average Persirables	0.052	0.013	0.055	0.070	-0.		

0.032

0.031

0.000

0.019

0.036

0.035

0.074

0.076

-0.

-0.

Average Receivables

ROIC

```
## [11] knitr_1.26
                                    ROI.plugin.quadprog_0.2-5
## [13] ROI.plugin.glpk_0.3-0
                                    ROI_0.3-3
## [15] PortfolioAnalytics 1.1.0
                                    foreach 1.4.7
## [17] tibbletime_0.1.3
                                    timetk_0.1.2
## [19] readxl_1.3.1
                                    anytime_0.3.7
                                    quantmod 0.4-15
## [21] tidyquant 0.5.10
## [23] TTR 0.23-6
                                    PerformanceAnalytics_2.0.4
## [25] xts_0.12-0
                                    zoo 1.8-7
## [27] lubridate_1.7.4
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## [29] janitor_1.2.1
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## [31] stringr_1.4.0
                                    dplyr_0.8.3
## [33] purrr_0.3.3
                                    readr_1.3.1
## [35] tidyr_1.0.2
                                    tibble_2.1.3
## [37] ggplot2_3.3.0
                                    tidyverse_1.3.0
## [39] jsonlite_1.6
                                    httr_1.4.1
##
## loaded via a namespace (and not attached):
##
     [1] estimability 1.3
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##
     [3] multcomp_1.4-12
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##
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##
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                                    callr_3.4.0
                                    webshot_0.5.2
##
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##
                                    httpuv 1.5.2
##
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  [15] gower_0.2.1
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                                    WRS2 1.0-0
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##
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##
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                                    Quandl_2.10.0
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                                    metaBMA 0.6.2
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   [47] lazyeval 0.2.2
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                                    registry_0.5-1
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                                    cellranger 1.1.0
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                                    broomExtra_2.5.0
## [73] lmtest_0.9-37
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```

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   [83] rjson_0.2.20
                                    oompaBase_3.2.9
##
  [85] bitops 1.0-6
                                    parameters 0.6.0
## [87] ggExtra 0.9
                                    shape 1.4.4
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                                    Brobdingnag_1.2-6
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                                    parallel_3.6.2
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## [121] digest 0.6.23
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## [125] jmv 1.2.5
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## [127] car_3.0-6
                                    metafor_2.1-0
## [129] ez_4.4-0
                                    BayesFactor_0.9.12-4.2
                                    metaplus_0.7-11
## [131] performance_0.4.4
## [133] later_1.0.0
                                    psych_1.9.12.31
## [135] effectsize_0.2.0
                                    sjstats_0.17.9
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## [139] fs_1.3.1
                                    splines_3.6.2
## [141] rematch2_2.1.0
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                                    mapproj_1.2.7
## [145] jcolors_0.0.4
                                    xtable_1.8-4
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## [149] zeallot_0.1.0
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## [151] scico_1.1.0
                                    R6 2.4.1
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## [155] htmltools 0.4.0
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## [157] glue_1.3.1
                                    fastmap_1.0.1
## [159] minqa_1.2.4
                                    codetools_0.2-16
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                                    pkgbuild_1.0.6
## [163] mvtnorm_1.0-12
                                    lattice_0.20-38
## [165] numDeriv_2016.8-1.1
                                    curl_4.3
## [167] DescTools_0.99.34
                                    gtools_3.8.1
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                                    zip_2.0.4
## [171] openxlsx_4.1.4
                                    survival_3.1-8
## [173] rmarkdown_2.0
                                    repr_1.1.0
## [175] munsell_0.5.0
                                    iterators_1.0.12
## [177] simisc 2.8.3
                                    haven_2.2.0
## [179] reshape2_1.4.3
                                    gtable_0.3.0
## [181] bayestestR 0.5.2
```