

Creating a Data Type in C

Rational Numbers

For this assignment, you will use the `struct` mechanism in C to implement a data type that represents rational numbers. A set can be modeled using the C `struct`:

```
struct _Rational {
    int Top;        // numerator
    int Bottom;     // denominator
};
typedef struct _Rational Rational;
```

A *rational number* is any number Q that can be represented as a ratio of two integers, N and D , such that D is not zero, so the `struct` type above seems to be entirely appropriate.

How will we deal with representation issues? For example, all of the following rational numbers (written in the usual mathematical fashion) are equal:

$$\frac{-3}{4} = \frac{3}{-4} = \frac{-9}{12} = \frac{75}{-100}$$

Will we represent all of them the same way, or differently? If we represent them all the same way, what will that be? This can be characterized as a question of *normalization*; that is, will we adopt some standard (normal) scheme for representation?

How will we deal with a client who tries to create a `Rational` variable with denominator set equal to 0? Mathematically, such an expression violates the definition of a rational number. Implementing this in an OO language, we would probably consider responding by throwing an exception; that's not an option in C. So, what will we do? There are ways to force a runtime error...

These decisions are left to you; how I handle them in my implementation will be discussed in class, but you are not required to follow my lead. I will guarantee that I will not test your implementation by ever setting a denominator to 0.

A *data type* consists of a collection of values and a set of operations that may be performed on those values. For a rational number type, it would make sense to provide the common arithmetic operations; for example:

```
/**
 * Compute the sum of Left and Right.
 * Pre:
 *     Left and Right have been properly initialized.
 * Returns:
 *     A Rational object X equal to Left + Right.
 */
Rational Rational_Add(const Rational Left, const Rational Right);
```

The design of `Rational_Add()` follows the expected semantics of addition; when you add two values, neither of those is modified and a new value is produced.

The design also avoids using pointers and (apparently) dynamic allocation. `Rational` objects are small, 8 bytes, and so it's fine to pass them into the function by copy and avoid the overhead of pointer accesses. The function must create a new `Rational` object and return it; since the function must always create exactly one object, there's no need or reason to allocate that object dynamically. Since dynamic allocation costs extra time at runtime, the design wisely avoids using dynamic allocation.

We will copy one aspect of an OO design; it's useful to provide a function that will create a new `Rational` object:

```
/**
 * Creates and initializes a new Rational object.
 * Pre:
 *     Denominator != 0
 * Returns:
 *     A Rational object X such that X.Top == Numerator
 *     and X.Bottom = Denominator.
 */
Rational Rational_Construct(int Numerator, int Denominator);
```

To some degree, this plays the role of a constructor in an OO implementation; the basic difference is that this is actually responsible for creating the new object (but not dynamically). In contrast, in a Java implementation, you would call `new` to allocate memory for the object dynamically and then call the constructor to initialize that memory correctly.

The other required functions are:

```
Rational Rational_Negate(const Rational R);
int Rational_Floor(const Rational R);
int Rational_Ceiling(const Rational R);
int Rational_Round(const Rational R);

Rational Rational_Add(const Rational Left, const Rational Right);
Rational Rational_Subtract(const Rational Left, const Rational Right);
Rational Rational_Multiply(const Rational Left, const Rational Right);
Rational Rational_Divide(const Rational Left, const Rational Right);

bool Rational_Equals(const Rational Left, const Rational Right);
bool Rational_NotEquals(const Rational Left, const Rational Right);
bool Rational_LessThan(const Rational Left, const Rational Right);
bool Rational_LessThanOrEqual(const Rational Left, const Rational Right);
bool Rational_GreaterThan(const Rational Left, const Rational Right);
bool Rational_GreaterThanOrEqual(const Rational Left, const Rational Right);
```

The file `Rational.h`, posted on the course website, includes header comments for each of these. Pay attention to the comments in the header file. All the stated pre- and post-conditions are part of the assignment. Pay particular attention to avoiding memory leaks. You should use the posted header file as your starting point, and place your implementation in a file named `Rational.c`.

You should consider implementing additional "helper" functions. Those should be private to your C file, so make them `static`; they will be invisible to the testing code and never called directly from outside your file.

Your solution will be compiled with a test driver, using the supplied header file, so if you do not conform to the specified interfaces there will very likely be compilation and/or linking errors.

What to Submit

You will submit a single `.c` file, containing the implementations of the specified C functions and any private helper functions you write. Be sure to conform to the specified function interfaces.

Your submission will be compiled with a test driver and graded according to how many cases your solution handles correctly.

This assignment will be graded automatically. You will be allowed up to ten submissions for this assignment. Test your function thoroughly before submitting it. Make sure that your function produces correct results for every test case you can think of.

Some requirements may be checked manually by a TA after the assignment is closed. Any shortcomings will be assessed a penalty, which will be applied to your score from the Curator.

The course policy is that the submission that yields the highest score will be checked. If several submissions are tied for the highest score, the earliest of those will be checked.

The *Student Guide* and other pertinent information, such as the link to the proper submit page, can be found at:

<http://www.cs.vt.edu/curator/>

Pledge:

Each of your program submissions must be pledged to conform to the Honor Code requirements for this course. Specifically, you **must** include the following pledge statement in the submitted file:

```
//    On my honor:
//
//    - I have not discussed the C language code in my program with
//      anyone other than my instructor or the teaching assistants
//      assigned to this course.
//
//    - I have not used C language code obtained from another student,
//      or any other unauthorized source, either modified or unmodified.
//
//    - If any C language code or documentation used in my program
//      was obtained from another source, such as a text book or course
//      notes, that has been clearly noted with a proper citation in
//      the comments of my program.
//
//    - I have not designed this program in such a way as to defeat or
//      interfere with the normal operation of the Curator System.
//
//    <Student Name>
```

Failure to include this pledge in a submission is a violation of the Honor Code.