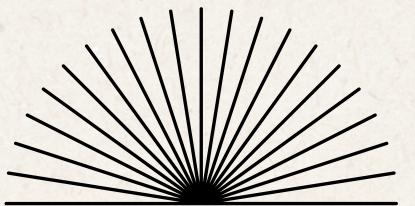


# **PROJECT MILESTONE**

**By Edward Raphael & Harry Chiu**

**NAME OF PROJECT:**  
**Lightning Modelling and  
Simulation in Python**



# Agenda

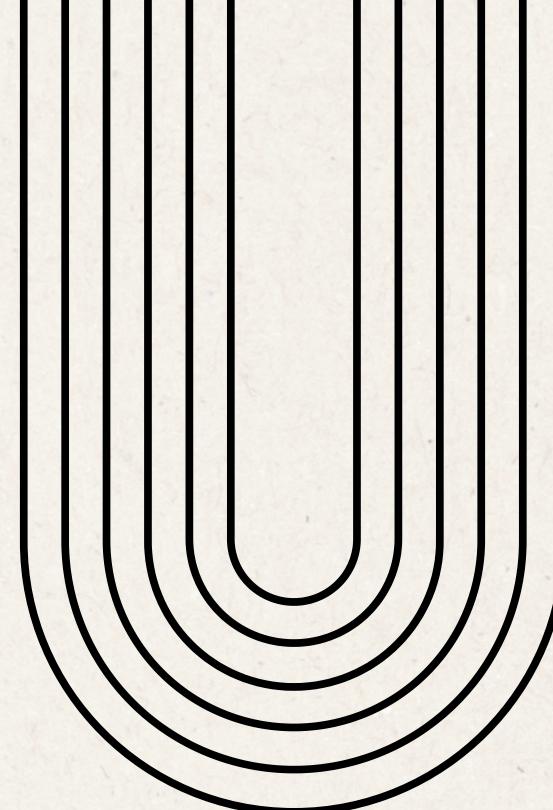
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<b>03</b>	<b>Objectives</b>
<b>04</b>	<b>Descriptions</b>
<b>06</b>	<b>Timeline &amp; Gantt Chart</b>
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# Objectives and Goals



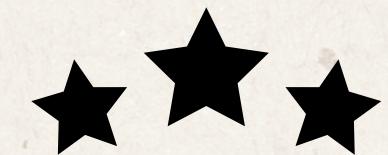
## Goal # 1

Simulate lightning formation using recursive fractal algorithms.



## Goal # 2

Integrate physical principles, particularly electric field influence.



## Goal # 3

Visualize natural lightning behavior with 2D plots and animations.



## Goal # 4

Analyze behavior under environmental variations (e.g., pressure, humidity).

## 01 What Causes Lightning?

Collisions between the ice particles and water droplets causes there to be a separation of positive and negative charges. This buildup of said charges creates an electric field between the clouds and the ground strong enough to generate lightning. The lightning is produced once the field exceeds a certain threshold where air becomes ionized and plasma channels form.

## 02 Fractal Segment Construction:

- Midpoint:  $M = (A + B) / 2$
- Normal Vector:  $n = [-(yB - yA), xB - xA] / ||...||$
- Offset Midpoint:  $M' = M + \text{offset} * n$
- Recursive Subdivision builds complexity (generations)

### Branching Mechanics:

- Probability: branch if  $\text{random()} < p_{\text{branch}}$
- Rotation Matrix: rotates branch direction  $R(\theta)$
- Segment Decay:  $L_{\text{new}} = L_{\text{old}} * \text{decay\_factor}$

# Description

### 03 Electric Field Approximation:

- $E(y) = 1 - y / \text{MAX\_Y}$
- y: height of midpoint, MAX\_Y: total canvas height
- Simulates stronger field near ground ( $y = 0$ )

Growth Constraint:

- Segment only forms if  $E(y) > E_{\text{threshold}}$
- Branching only occurs in high-field zones

Purpose:

- Models lightning propagation toward ground
- Adds realism based on physics principles

### Tested Variables

Test Variables: generations, max\_offset, decay\_factor, E\_THRESHOLD, p\_branch.

Constants: MAX\_Y = 200, angle ranges, random seed (for testing).

Computed  
segment midpoints, normal vectors, field strength.

- Vary one test variable at a time and observe effects.

# Timeline

05/10

Milestone	Description	Owner	Status
Research About Lightning	Conduct a comprehensive review of studies literature on lightning phenomena. Understanding the fundamental physics and behavior that cause the phenomena. This forms the foundation for our project by identifying variables and factors.	Harry	Done
Choose Appropriate Model	Select the appropriate computational model that will be used for simulating lightning. This involves evaluating different algorithms based on their accuracy, efficiency, and compatibility that suits our research.	Edward	Done
Implement Basic Code (Simulation)	Develop and run an initial simulation based on the chosen model. This includes setting up the environment, ensuring basic functionalities are working and coding the simulation parameters.	Edward	Done
Add Constraints and Variables	Introduce physical constraints and parameters to the simulation to enhance the simulation accuracy. This involves integrating known physics principles related to electricity, atmospheric conditions, and lightning behavior into the model.	Harry	Done
Animate & Visualize	Create accurate visual representations of the simulation results. Includes generating simple animations that depict lightning strikes and visualizing the data in a way to make it comprehensible.	Edward	In Progress
Final Fixes & Report	Perform final adjustments to the simulation parameters to optimize accuracy and performance. Compile the results, analyses, and visuals into a report that summarizes the findings and implications of the research.	Harry	Not Done

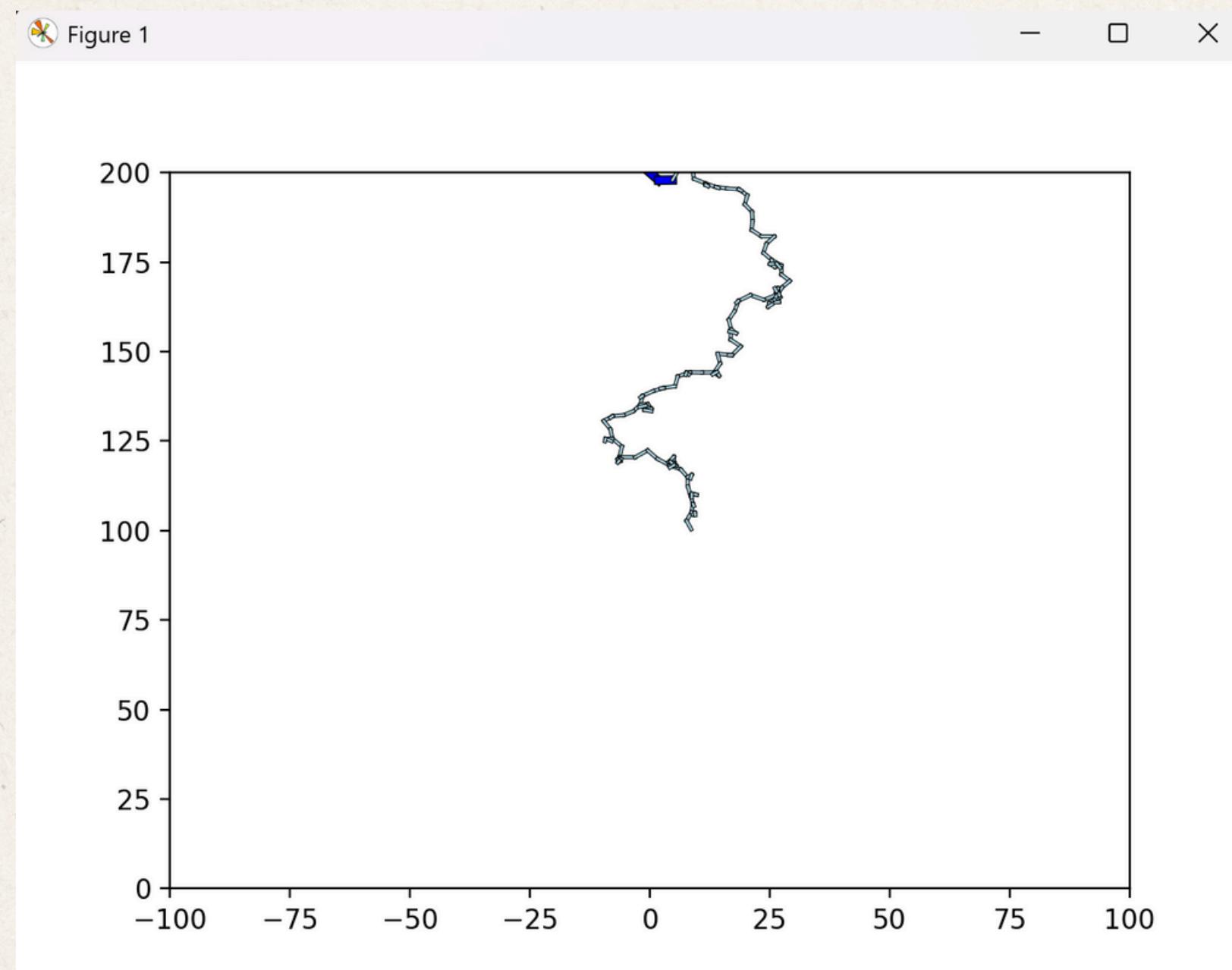
# Gantt Chart

Display of our work timeline

Tasks	March				April				May				June
	W1	W2	W3	W4	W1	W2	W3	W4	W1	W2	W3	W4	W1
Research Lightning													
Choose Model													
Implement Base Simulation													
Add Physics Constraint													
Animate & Visualize													
Final Tuning & Report													

- Completed
- In Progress
- Not complete
- Hiatus

# Visualizations



# Program

```
1 import numpy as np
2 import matplotlib.pyplot as plt
3 from matplotlib.animation import FuncAnimation
4
5 # Constants
6 E_THRESHOLD = 0.3 # Threshold for electric field strength
7 MAX_Y = 200 # Maximum height for the simulation
8
9 def get_electric_field(point):
10
11     y = point[1]
12     return y / MAX_Y # Normalized field strength (0 at top, 1 at bottom)
13
14 def create_segments(segments, generations, max_offset, decay_factor):
15     if generations == 0:
16         return segments
17
18     new_segments = []
19
20     for segment in segments:
21         start, end = segment
22         mid = 0.5 * (start + end)
23
24         # Check if the electric field at the midpoint is sufficient
25         E_field = get_electric_field(mid)
26         if E_field < E_THRESHOLD:
27             continue
28
```

```
29         # Calculate the normal vector for offsetting
30         normal = np.array([- (end[1] - start[1]), end[0] - start[0]], dtype=float)
31         normal /= np.linalg.norm(normal)
32         offset = np.random.uniform(-max_offset, max_offset)
33         mid += normal * offset
34
35         new_segments.append((start, mid))
36         new_segments.append((mid, end))
37
38         if np.random.rand() < 0.3 and E_field > E_THRESHOLD + 0.1:
39             direction = end - start
40             direction /= np.linalg.norm(direction)
41             angle = np.random.uniform(-np.pi / 4, np.pi / 4)
42             rot_matrix = np.array([
43                 [np.cos(angle), -np.sin(angle)],
44                 [np.sin(angle), np.cos(angle)]
45             ])
46             direction = rot_matrix @ direction
47             branch_end = mid + direction * decay_factor
48             new_segments.append((mid, branch_end))
49
50     return create_segments(new_segments, generations - 1, max_offset / 2, decay_factor)
51
```

# **Thank you**

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# References

<https://siliconwit.com/modelling-and-simulation-in-python/lightning-strike>

**Riousset, J. A., Pasko, V. P., Krehbiel, P. R., Thomas, R. J., & Rison, W. (2007). Three-dimensional fractal modeling of intracloud lightning discharge in a New Mexico thunderstorm and comparison with lightning mapping observations. Journal of Geophysical Research Atmospheres, 112(D15).**

<https://doi.org/10.1029/2006jd007621>

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