$\eta\mathcal{H}/c$ compared to analytical approximations