β-dependence for polynomial degree p with $\lambda = 2$