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EXTENDS Naturals, FiniteSets, Sequences, TLC
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Is leader ALIVE or CRASHED

Variable leaderState

Helper variable tracking the number of times the leader node has failed VARIABLE nodedownIndex

A collection of 'nodedown' messages the leader has sent.

In Erlang, when a monitored node crashes, the 'nodedown' message is sent to the follower.

The value of a message is not a part of the implementation and

represents the number of times the node has failed.

Variable nodedownMessages

 $nodedownInfo \triangleq \langle nodedownMessages, nodedownIndex \rangle$

Heartbeat messages the leader has sent

The value of a message is not a part of the implementation and

represents the number of times a heartbeat message was sent.

VARIABLE heartbeatMessages

Helper variable tracking the number of sent heartbeat messages

Variable heartbeatIndex

 $heartbeatInfo \triangleq \langle heartbeatMessages, heartbeatIndex \rangle$

Whether the follower timed out

VARIABLE is Timeout

 $vars \triangleq \langle leaderState, nodedownInfo, heartbeatInfo, isTimeout \rangle$

The leader crashes and doesn't recover

 $CrashLeader \triangleq$

 \land leaderState = "ALIVE"

 $\land leaderState' = "CRASHED"$

Erlang sends the NODEDOWN message if the leader was monitored

 $\land nodedownMessages' = Append(nodedownMessages, nodedownIndex)$

 $\land nodedownIndex' = nodedownIndex + 1$

∧ UNCHANGED ⟨heartbeatInfo, isTimeout⟩

Helper function to remove a message from a sequence of messages

 $RemoveMessage(i, seq) \triangleq$

 $[j \in 1...Len(seq) - 1 \mapsto \text{if } j < i \text{ then } seq[j] \text{ else } seq[j+1]]$

The network drops a heartbeat message

 $DropHeartbeat \triangleq$

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\land Len(heartbeatMessages) > 0
        \land \exists i \in 1 .. Len(heartbeatMessages) :
            heartbeatMessages' = RemoveMessage(i, heartbeatMessages)
        ∧ UNCHANGED ⟨leaderState, heartbeatIndex, nodedownInfo, isTimeout⟩
The follower receives a heartbeat message from the leader.
ReceiveHeartbeat \triangleq
        \wedge Len(heartbeatMessages) > 0
        \land \exists i \in 1 .. Len(heartbeatMessages) :
            heartbeatMessages' = RemoveMessage(i, heartbeatMessages)
        \land UNCHANGED \langle leaderState, heartbeatIndex, nodedownInfo, isTimeout \rangle
The leader sends a heartbeat message to the follower.
SendHeartbeat \triangleq
        \land leaderState = "ALIVE"
        \land heartbeatMessages' = Append(heartbeatMessages, heartbeatIndex)
        \land heartbeatIndex' = heartbeatIndex + 1
        \land UNCHANGED \langle leaderState, nodedownInfo, isTimeout \rangle
The network drops a nodedown message.
DropNodedown \triangleq
        \land Len(nodedownMessages) > 0
        \land \exists i \in 1 ... Len(nodedownMessages) :
            nodedownMessages' = RemoveMessage(i, nodedownMessages)
        \land UNCHANGED \langle leaderState, nodedownIndex, heartbeatInfo, isTimeout \rangle
 The follower receives a nodedown message from the leader which causes it time out immediately.
ReceiveNodedown \triangleq
        \land Len(nodedownMessages) > 0
        \land \exists i \in 1 .. Len(nodedownMessages) :
            nodedownMessages' = RemoveMessage(i, nodedownMessages)
        \wedge isTimeout' = TRUE
        \land UNCHANGED \langle leaderState, nodedownIndex, heartbeatInfo \rangle
Timeout \triangleq
         \land isTimeout = False
          \wedge isTimeout' = TRUE
         ∧ UNCHANGED ⟨leaderState, heartbeatInfo, nodedownInfo⟩
Initial state of model
Init \stackrel{\triangle}{=} \land leaderState = "ALIVE"
         \land \ nodedownIndex = 0
         \land nodedownMessages = \langle \rangle
         \wedge heartbeatIndex = 0
         \land heartbeatMessages = \langle \rangle
         \land isTimeout = False
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 \begin{array}{ccc} \text{Next state function} \\ Next & \triangleq & \lor DropHeartbeat \end{array}
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 \lor SendHeartbeat

 $\lor Receive Heart be at$

 $\lor DropNodedown$

 $\lor ReceiveNodedown$

 $\lor \mathit{CrashLeader}$

 $\lor \ Timeout$

 $Spec \stackrel{\triangle}{=} Init \wedge \Box [Next]_{vars} \wedge WF_{vars}(Next)$