

MM5425 HomeworkPlus: Linear Regression

Objectives:

- Gently get started with how to use Pandas in python
- Check the attributes' relevance using the correlation
- Predict accurately the insurance cost with multivariate linear regression
- Check the performance metrics of the linear regression model

Part I: Python Basics ~ function

```
# function defining in python with def and :
def greet(name):
    return f"Hello, {name}!" # return "Hello" + ' ' + name+'!'

# calling the function
message = greet("Wenting")
print(message) # output: Hello, Wenting!
```

Exercise 1.1: Sales Tax Calculator

Write a function called calculate_sales_tax that takes two arguments: the price of an item and the sales tax rate (as a percentage). The function should return the total price including sales tax. Call the function and display the total for \$170 with 12.5% tax rate.

Exercise 1.2: Employee Bonus Calculator

Task: Write a function called calculate_bonus that takes two arguments: the employee's salary and the performance rating (an integer from 1 to 5). The function should return the bonus amount based on the following criteria:

Rating 5: 20% of salary
 Rating 4: 15% of salary
 Rating 3: 10% of salary
 Rating 2: 5% of salary
 Rating 1: 0% of salary

Try the function to calculate the bonus for an employee with salary 28000 and performance rating is 3.

Part II: Linear Regression with Excel

Download the dataset insurance.csv from Blackboard in WK4. Open the file and check the contents.

This dataset has 1 target variable and 6 independent variables:

Age: age of primary beneficiary.

Gender: insurance contractor gender, female, male.

BMI: Body mass index, providing an understanding of body weights that are relatively high or low relative to height, objective index of body weight (kg/m^2) using the ratio of height to weight, ideally 18.5 to 24.9.

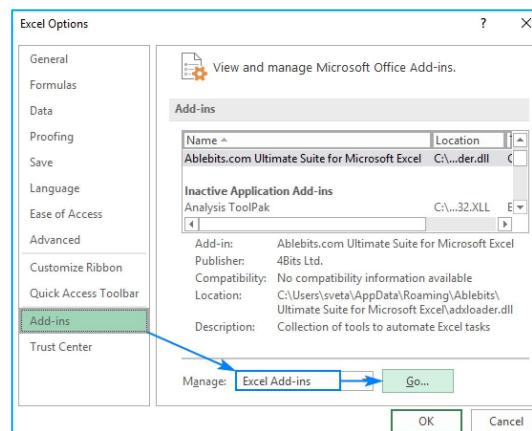
Children: Number of children covered by health insurance/Number of dependents.

Smoker: Is the person a smoker or not.

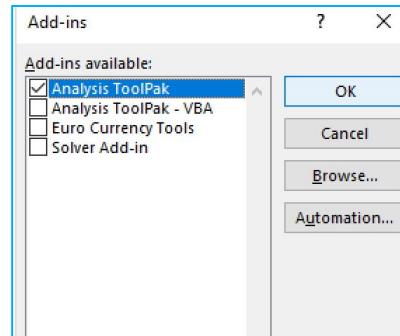
Region: the beneficiary's residential area in the US, northeast, southeast, southwest, northwest.

Charges: Individual medical costs billed by health insurance.

1. Open file insurance.csv
2. Select "Data" from the toolbar. The "Data" menu displays.
3. Select "Data Analysis". The Data Analysis - Analysis Tools dialog box displays.
 - If you don't see 'Data Analysis',
for Windows system, you need:
 1. In your Excel, click File > Options.
 2. In the Excel Options dialog box, select Add-ins on the left sidebar, make sure Excel Add-ins is selected in the Manage box, and click Go.



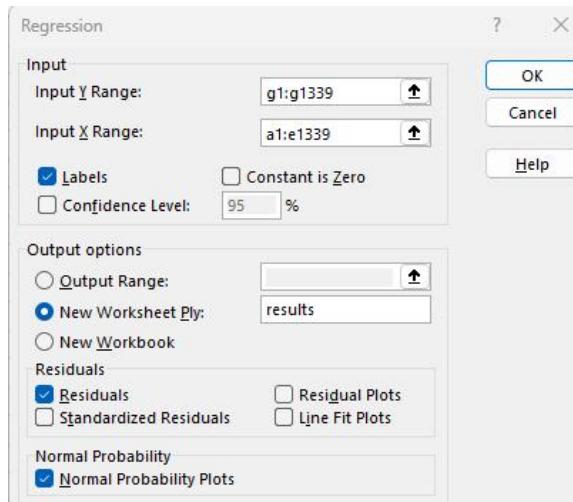
3. In the Add-ins dialog box, tick Analysis Toolpak, and click OK.
That will add Data Analysis tools to the Data tab to your excel



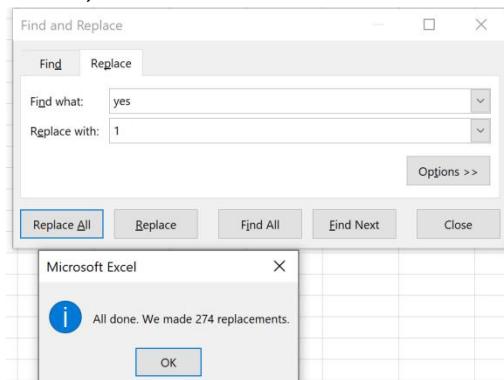
For iOS:

- ➔ Start Excel for Mac.
 - ➔ Click Tools, and then click Add-Ins.
 - ➔ Click the Data Analysis ToolPak or Solver option to enable it. Then, click OK.
 - ➔ Locate Data Analysis ToolPak or Solver on the Data tab.
-

4. From the menu, select "Regression" and click "OK".
5. In the Regression dialog box, click the "Input Y Range" box and select the dependent variable data. Try the following options:



- There's an error message showing that only numerical data can be used in the linear regression. Therefore, pressing **ctrl+f** keys, we replace 'yes' with 1, 'no' with 0, 'female' with 0, 'male' with 1



(Question: what do we do with column region?)

- Try the regression dialog box again.
- Check the results in excel. Look for the following statistics:

Adjusted R square: _____

Coefficient of the intercept: _____ and its p value: _____

Coefficient of age: _____ and its p value: _____

Coefficient of gender: _____ and its p value: _____

Coefficient of bmi: _____ and its p value: _____

Coefficient of children: _____ and its p value: _____

Coefficient of smoker: _____ and its p value: _____

With the calculated p-value, which attributes can be excluded in the model?

1	SUMMARY OUTPUT
2	
3	Regression Statistics
4	Multiple R 0.865865
5	R Square 0.749723
6	Adjusted R 0.748783
7	Standard Er 6069.725
8	Observatio 1338
9	
10	ANOVA
11	df SS MS F Significance F
12	Regression 5 1.47E+11 2.94E+10 798.0185 0
13	Residual 1332 4.91E+10 36841565
14	Total 1337 1.96E+11
15	
16	Coefficients Standard Error t Stat P-value Lower 95% Upper 95% Lower 95.0% Upper 95.0%
17	Intercept -12052.5 951.2604 -12.67 8.1E-35 -13918.6 -10186.3 -13918.6 -10186.3
18	X Variable 1 257.735 11.90389 21.65133 2.59E-89 234.3826 281.0874 234.3826 281.0874
19	X Variable 2 -128.64 333.3605 -0.38589 0.699641 -782.609 525.329 -782.609 525.329
20	X Variable 3 322.3642 27.4186 11.75714 1.95E-30 268.5759 376.1526 268.5759 376.1526
21	X Variable 4 474.4111 137.8558 3.441358 0.000597 203.973 744.8493 203.973 744.8493
22	X Variable 5 23823.39 412.5234 57.75041 0 23014.13 24632.66 23014.13 24632.66

In the first part, the Adjusted R square is the factor used in indicating how good the model fits.

In the second part of ANOVA (analysis of variance), the df is the degree of freedom, F is the F statistic.

The most useful component in this section is Coefficients. We can see that gender ($p = 0.6996$) is not statistically significant at $\alpha = 0.05$.

Part III: Linear regression with Python:

Introduction to Pandas

- Python Pandas provides high level, flexible and fast sets of tools to manipulate data into the right format. Pandas Focuses on loading/reading data, exploring data, basic data operations, data selection, data transformation, handling missing values, data visualization and etc..
 - DataFrame provides rectangular table of data containing an ordered collection of columns of different value types (numeric, string, boolean...)
 - For each column in the dataframe, we may refer it with the column name: df.age or df['age']
 - The data statistics of different columns can use: df.age.mean()
 - We can check the correlation between the numerical variables: df.corr()
 - We will try some Pandas built in plotting functions: plot(), hist(), boxplot()
 - Other common operations:
 - Replace values: df.gender.replace(['M', 'F'], [1,0])
 - drop_duplicates(): df.drop_duplicates()
 - check the missing values: df.isnull().sum()
 - drop the missing values: df.dropna(inplace = True)
1. Start your jupyter notebook or google colab
 2. Import the following packages: pandas, seaborn and pyplot from matplotlib

```
import pandas as pd
```

3. Read the data set and preview the data

```
# Load the data
df = pd.read_csv('insurance.csv')

# preview data columns
df.info()

# data descriptive statistics
df.describe()

df.head(3)
```

(For students who use colab, you need save the insurance.csv to your google drive, and add the

drive to colab. Please use the following as reference:

```
[1] 1 # in colab, we need mount google drive to access the files
2 # upon running the code, make sure to follow the steps and allow access in the pop-up window
3 from google.colab import drive
4 drive.mount('/content/drive')
```

→ Drive already mounted at /content/drive; to attempt to forcibly remount, call drive.mount("/content

Step 1: importing the packages

```
[2] 1 import pandas as pd
```

Step 2: read the file

```
[3] 1 # Load the data (the insurance.csv is in a folder MM5425 in this example)
2 df = pd.read_csv('/content/drive/My Drive/MM5425/insurance.csv')
```

4. In the data preparation, we replace the categorical values of Gender and Smoker to be values of 1 or 0

```
df.gender = df.gender.replace(['male','female'],[0,1])
df.smoker = df.smoker.replace(['yes','no'],[1,0])
```

5. For another categorical values of Region, we need use dummy variables

```
#3.5: handle other categorical data:
# Create dummy variables for the 'region' column
df = pd.get_dummies(df, columns=['region'])
df.head(3)
```

6. To use the linear regression model, we need find the target variable and the dependent variables <https://www.timeanddate.com/worldclock/hong-kong/hong-kong>

```
# 4.1 define X and y:
# target variable
y=df.charges
# independent variables
X=df.drop('charges', axis = 1)
```

7. (optional) We will split the data for training and testing in our model training:

```
# 4.2 split data into training and testing sets:
# import the package for splitting data into training and testing:
from sklearn.model_selection import train_test_split
# split the data into 80% training and 20% testing
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2)
```

8. Train the model

```
from sklearn.linear_model import LinearRegression  
model = LinearRegression()  
# feed in data for model training  
model.fit(X,y)
```

9. At this step, we simply check the intercept and slopes in Step 5:

```
# check the value of R^2  
model.score(X,y)  
  
# check the model's intercept and coefficient  
model.intercept_  
  
# check the model's coefficients  
model.coef_
```

10. To have a summary of the model:

```
import statsmodels.api as sm  
  
#fit linear regression model  
model_ols = sm.OLS(y_train, X_train).fit()  
  
#view model summary  
print(model_ols.summary())
```

11. Is the result consistent with that from Excel? What is the charges equation as predicted?

Charges =

12. If you have a new customer who is 32 years old male with bmi=28.9, two children, non-smoking, from southeast district. How much is the predicted insurance charge for him?

```
import numpy as np  
new_customer = np.array([32,1,28.9,2,0,0,0,1,0]).reshape(1,-1)  
print(model.predict(new_customer))
```

Submission: please submit your Jupyter notebook file with results