

```

Clear[L, a, phi, theta, m, k, w, yp]
f[θ_] := a Cos[θ + φ] + Sqrt[L^2 - (yp - a Sin[θ + φ])^2]
f'[θ](*First derivative*)
f''[θ](*Second derivative*)
(*f[0], intial time , no time taking into account*)
deltax[θ_] := f[θ] - f[0]
(*Force of the Plancks*)
Fplanks[θ_] := -k * deltax[θ] (*where k is an arbitrary constant*)
Fplanks[θ]
Frodx[θ_] := m f''[θ] + Fplanks[θ]
Frodx[θ] // FullSimplify

```

Out[65]=

$$-a \sin\left[\frac{7\pi}{60} + \theta\right] + \frac{a \cos\left[\frac{7\pi}{60} + \theta\right] \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)}{\sqrt{L^2 - \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)^2}}$$

Out[66]=

$$-a \cos\left[\frac{7\pi}{60} + \theta\right] - \frac{a^2 \cos^2\left[\frac{7\pi}{60} + \theta\right] \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)^2}{\left(L^2 - \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)^2\right)^{3/2}} -$$

$$\frac{a^2 \cos^2\left[\frac{7\pi}{60} + \theta\right]}{\sqrt{L^2 - \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)^2}} - \frac{a \sin\left[\frac{7\pi}{60} + \theta\right] \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)}{\sqrt{L^2 - \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)^2}}$$

Out[69]=

$$-k \left(-a \cos\left[\frac{7\pi}{60}\right] + a \cos\left[\frac{7\pi}{60} + \theta\right] - \sqrt{L^2 - \left(yp - a \sin\left[\frac{7\pi}{60}\right]\right)^2} + \sqrt{L^2 - \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)^2} \right)$$

Out[71]=

\$Aborted

```

In[48]:= Clear[L, a, phi, theta, m, k, w, yp]
xr[θ_] := a Cos[θ + φ]
Ftot = Frodx[θ]/((f[θ] - xr[θ])/L)
Ftot // FullSimplify
(*Setting values for the constants*)
{w = -5, L = 1, a = 0.02, k = 100, yp = .3,
 m = 70, φ = 21 (Pi / 180)}
Plot[Ftot, {θ, 0, 2 Pi}]

```

Out[50]=

$$\begin{aligned}
 & \left(L \left(m \left(-a \cos\left[\frac{7\pi}{60} + \theta\right] - \frac{a^2 \cos^2\left[\frac{7\pi}{60} + \theta\right] \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)^2}{\left(L^2 - \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)^2\right)^{3/2}} - \right. \right. \right. \\
 & \quad \left. \frac{a^2 \cos^2\left[\frac{7\pi}{60} + \theta\right]}{\sqrt{L^2 - \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)^2}} - \frac{a \sin\left[\frac{7\pi}{60} + \theta\right] \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)}{\sqrt{L^2 - \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)^2}} \right) - \\
 & \quad \left. k \left(-a \cos\left[\frac{7\pi}{60}\right] + a \cos\left[\frac{7\pi}{60} + \theta\right] - \sqrt{L^2 - \left(yp - a \sin\left[\frac{7\pi}{60}\right]\right)^2} + \sqrt{L^2 - \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)^2} \right) \right) \Bigg) / \\
 & \quad \left(\sqrt{L^2 - \left(yp - a \sin\left[\frac{7\pi}{60} + \theta\right]\right)^2} \right)
 \end{aligned}$$

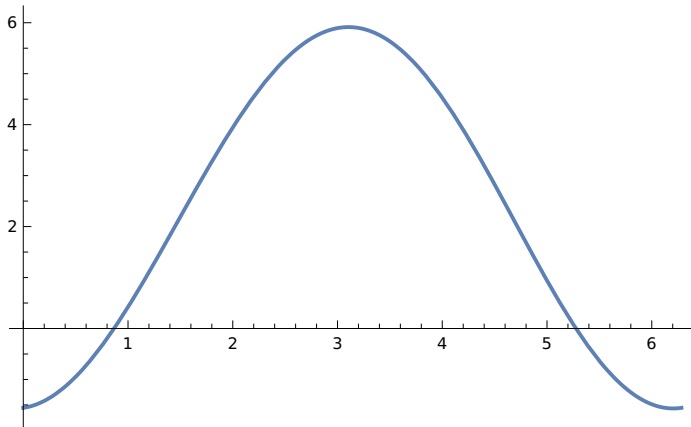
Out[51]=

\$Aborted

Out[52]=

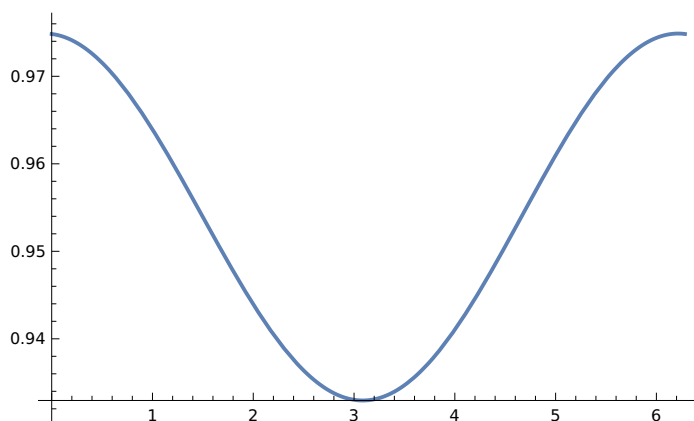
$\{-5, 1, 0.02, 100, 0.3, 70, \frac{7\pi}{60}\}$

Out[53]=



In[15]:= `Plot[f[θ], { θ , 0, 2 Pi}]`

Out[15]=



In[72]:= (*Expression for the total force copied from 'try 2'*)

Clear[L, a, phi, theta, m, k, w, yp]

$$f_{\text{tot}} = \left(L \left(a m w^2 \left(-\cos[\phi + \theta] - \frac{a L^2 \cos[\phi + \theta]^2}{\left(L^2 - (y_p - a \sin[\phi + \theta])^2 \right)^{3/2}} + \frac{\sin[\phi + \theta] (-y_p + a \sin[\phi + \theta])}{\sqrt{L^2 - (y_p - a \sin[\phi + \theta])^2}} \right) + k \left(a \cos[\phi] - a \cos[\phi + \theta] + \sqrt{L^2 - (y_p - a \sin[\phi])^2} - \sqrt{L^2 - (y_p - a \sin[\phi + \theta])^2} \right) \right) / \left(\sqrt{L^2 - (y_p - a \sin[\phi + \theta])^2} \right)$$

(*Expression for xp*)

xp = a Cos[theta + phi] + Sqrt[L^2 - (yp - a Sin[theta + phi])^2]

Out[73]=

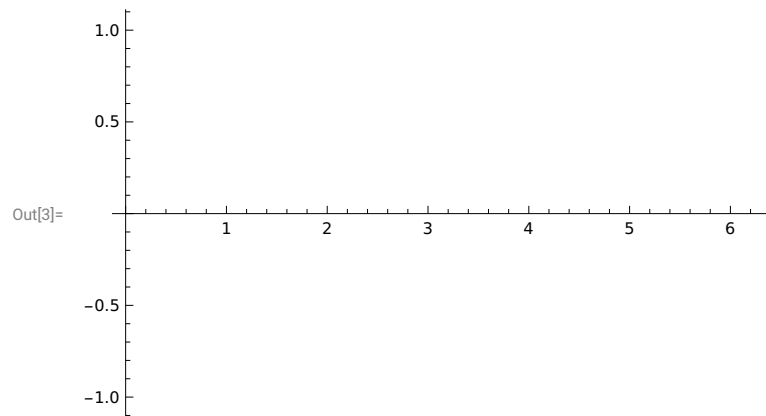
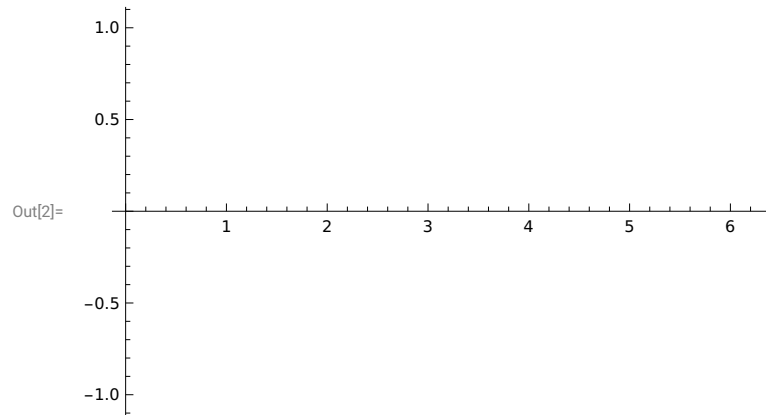
$$\left(L \left(a m w^2 \left(-\cos[\phi + \theta] - \frac{a L^2 \cos[\phi + \theta]^2}{\left(L^2 - (y_p - a \sin[\phi + \theta])^2 \right)^{3/2}} + \frac{\sin[\phi + \theta] (-y_p + a \sin[\phi + \theta])}{\sqrt{L^2 - (y_p - a \sin[\phi + \theta])^2}} \right) + k \left(a \cos[\phi] - a \cos[\phi + \theta] + \sqrt{L^2 - (y_p - a \sin[\phi])^2} - \sqrt{L^2 - (y_p - a \sin[\phi + \theta])^2} \right) \right) \right) / \left(\sqrt{L^2 - (y_p - a \sin[\phi + \theta])^2} \right)$$

Out[74]=

$$a \cos[\phi + \theta] + \sqrt{L^2 - (y_p - a \sin[\phi + \theta])^2}$$

```
In[1]:= {w2 = -5, L = 1, a = 0.02, k = 100, yp = .3 + 0.05 Sin[w2*theta], m = 70, phi = 20 (Pi / 180)}
Plot[ftot, {theta, 0, 2 Pi}] (*Plotting the total force over theta*)
Plot[xp, {theta, 0, 2 Pi}] (*Plotting xp over theta*)
```

```
Out[1]= {-5, 1, 0.02, 100, 0.3 - 0.05 Sin[5 theta], 70,  $\frac{\pi}{9}$ }
```



In[154]:=

```

Clear[L, a, phi, theta, m, k, w, yp]
f[theta_] := a Cos[theta + phi] + Sqrt[L^2 - (yp - a Sin[theta + phi])^2]
f'[theta](*First derivative*)
f''[theta](*Second derivative*)
(*f[0], initial time , no time taking into account*)
deltax[theta_] := f[theta] - f[0]
(*Force of the Plancks*)
Fplanks[theta_] := -k * deltax[theta] (*where k is an arbitrary constant*)
Fplanks[theta]

Fx[theta_] := m f''[theta] + Fplanks[theta]
Fx[theta] // FullSimplify
{w2 = -5, L = 1, a = 0.02, k = 100, yp = .3 + 0.05 Sin[w2 * theta], m = 70, phi = 20 (Pi / 180)}
Plot[Fx[theta], {theta, 0, 2 Pi}] (*Plotting the total force over theta*)

```

Out[156]=

$$-a \sin[\phi + \theta] + \frac{a \cos[\phi + \theta] (yp - a \sin[\phi + \theta])}{\sqrt{L^2 - (yp - a \sin[\phi + \theta])^2}}$$

Out[157]=

$$-a \cos[\phi + \theta] - \frac{a^2 \cos[\phi + \theta]^2 (yp - a \sin[\phi + \theta])^2}{(L^2 - (yp - a \sin[\phi + \theta])^2)^{3/2}} - \frac{a^2 \cos[\phi + \theta]^2}{\sqrt{L^2 - (yp - a \sin[\phi + \theta])^2}} - \frac{a \sin[\phi + \theta] (yp - a \sin[\phi + \theta])}{\sqrt{L^2 - (yp - a \sin[\phi + \theta])^2}}$$

Out[160]=

$$-k \left(-a \cos[\phi] + a \cos[\phi + \theta] - \sqrt{L^2 - (yp - a \sin[\phi])^2} + \sqrt{L^2 - (yp - a \sin[\phi + \theta])^2} \right)$$

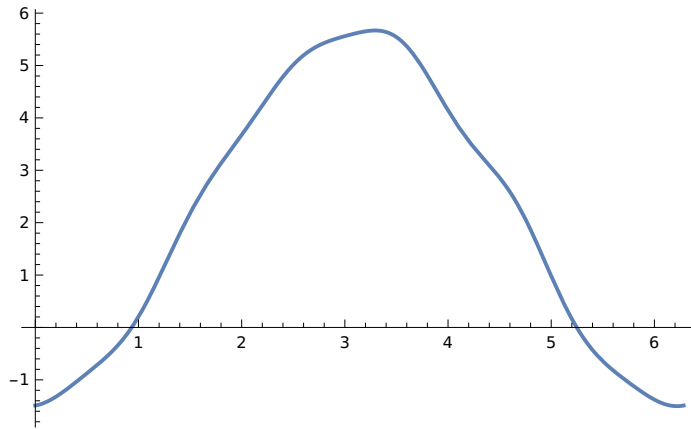
Out[162]=

$$a m \left(-\cos[\phi + \theta] - \frac{a L^2 \cos[\phi + \theta]^2}{(L^2 - (yp - a \sin[\phi + \theta])^2)^{3/2}} + \frac{\sin[\phi + \theta] (-yp + a \sin[\phi + \theta])}{\sqrt{L^2 - (yp - a \sin[\phi + \theta])^2}} \right) + k \left(a \cos[\phi] - a \cos[\phi + \theta] + \sqrt{L^2 - (yp - a \sin[\phi])^2} - \sqrt{L^2 - (yp - a \sin[\phi + \theta])^2} \right)$$

Out[163]=

$$\{-5, 1, 0.02, 100, 0.3 - 0.05 \sin[5 \theta], 70, \frac{\pi}{9}\}$$

Out[164]=



In[282]:=

```
Clear[L, a, phi, theta, m, k, w, yp]
(*Solving for Fy*)
```

$$f_{\text{tot}} = \left(L \left(a m w^2 \left(-\cos[\phi + \theta] - \frac{a L^2 \cos[\phi + \theta]^2}{(L^2 - (yp - a \sin[\phi + \theta])^2)^{3/2}} + \frac{\sin[\phi + \theta] (-yp + a \sin[\phi + \theta])}{\sqrt{L^2 - (yp - a \sin[\phi + \theta])^2}} \right) + k (a \cos[\phi] - a \cos[\phi + \theta] + \sqrt{L^2 - (yp - a \sin[\phi])^2} - \sqrt{L^2 - (yp - a \sin[\phi + \theta])^2}) \right) / \left(\sqrt{L^2 - (yp - a \sin[\phi + \theta])^2} \right) \right)$$

```
(*Finding the torque*)
```

```
{w = -5, w2 = -5, L = 1, a = 0.02, k = 100,
```

```
yp = .3 + 0.0 Sin[w2 * theta], m = 70, phi = 0 (Pi / 180)}
```

```
x = a Cos[theta + phi]
```

```
y = a Sin[theta + phi]
```

```
Fy = ftot * ((yp - y) / L)
```

```
torque = Fx[theta] * y + Fy * x
```

```
Plot[-Fx[theta] * y - Fy * x, {theta, 0, Pi}] (*Plotting the total force over theta*)
```

```
Plot[-Fx[theta] * y + Fy * x, {theta, Pi, 2 Pi}]
```

Out[283]=

$$\left(L \left(a m w^2 \left(-\text{Cos}[\text{phi} + \text{theta}] - \frac{a L^2 \text{Cos}[\text{phi} + \text{theta}]^2}{(L^2 - (y p - a \text{Sin}[\text{phi} + \text{theta})]^2)^{3/2}} + \frac{\text{Sin}[\text{phi} + \text{theta}] (-y p + a \text{Sin}[\text{phi} + \text{theta}])}{\sqrt{L^2 - (y p - a \text{Sin}[\text{phi} + \text{theta})]^2}} \right) + k \left(a \text{Cos}[\text{phi}] - a \text{Cos}[\text{phi} + \text{theta}] + \sqrt{L^2 - (y p - a \text{Sin}[\text{phi}])^2} - \sqrt{L^2 - (y p - a \text{Sin}[\text{phi} + \text{theta})]^2} \right) \right) \Bigg) / \left(\sqrt{L^2 - (y p - a \text{Sin}[\text{phi} + \text{theta})]^2} \right)$$

Out[284]=

{-5, -5, 1, 0.02, 100, 0.3, 70, 0}

Out[285]=

0.02 Cos[theta]

Out[286]=

0.02 Sin[theta]

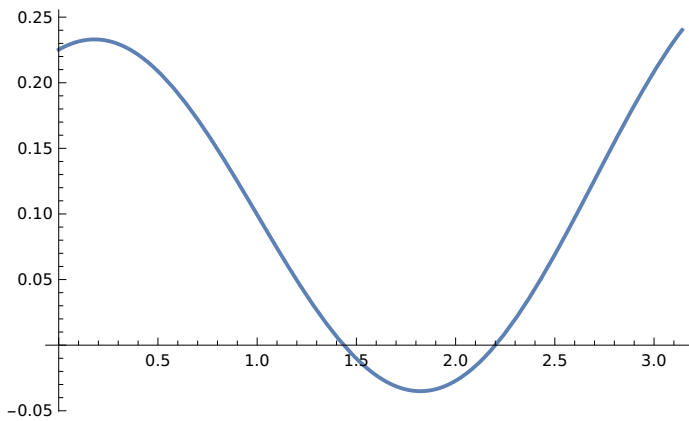
Out[287]=

$$\left((0.3 - 0.02 \text{Sin}[\text{theta}]) \left(100 \left(0.973939 - 0.02 \text{Cos}[\text{theta}] - \sqrt{1 - (0.3 - 0.02 \text{Sin}[\text{theta}])^2} \right) + 35. \left(-\text{Cos}[\text{theta}] - \frac{0.02 \text{Cos}[\text{theta}]^2}{(1 - (0.3 - 0.02 \text{Sin}[\text{theta}])^2)^{3/2}} + \frac{(-0.3 + 0.02 \text{Sin}[\text{theta}]) \text{Sin}[\text{theta}]}{\sqrt{1 - (0.3 - 0.02 \text{Sin}[\text{theta}])^2}} \right) \right) \right) / \left(\sqrt{1 - (0.3 - 0.02 \text{Sin}[\text{theta}])^2} \right)$$

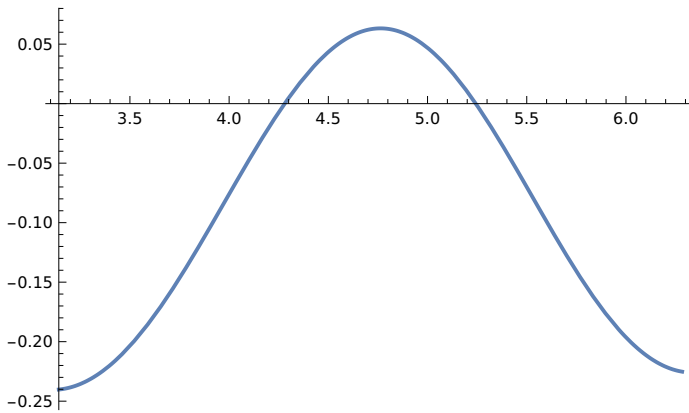
Out[288]=

$$0.02 \sin[\theta] \left(100 \left(0.973939 - 0.02 \cos[\theta] - \sqrt{1 - (0.3 - 0.02 \sin[\theta])^2} \right) + \right. \\ \left. 1.4 \left(-\cos[\theta] - \frac{0.02 \cos[\theta]^2}{(1 - (0.3 - 0.02 \sin[\theta])^2)^{3/2}} + \frac{(-0.3 + 0.02 \sin[\theta]) \sin[\theta]}{\sqrt{1 - (0.3 - 0.02 \sin[\theta])^2}} \right) + \right. \\ \left. \left(0.02 \cos[\theta] (0.3 - 0.02 \sin[\theta]) \right) \right. \\ \left. \left(100 \left(0.973939 - 0.02 \cos[\theta] - \sqrt{1 - (0.3 - 0.02 \sin[\theta])^2} \right) + \right. \right. \\ \left. \left. 35. \left(-\cos[\theta] - \frac{0.02 \cos[\theta]^2}{(1 - (0.3 - 0.02 \sin[\theta])^2)^{3/2}} + \frac{(-0.3 + 0.02 \sin[\theta]) \sin[\theta]}{\sqrt{1 - (0.3 - 0.02 \sin[\theta])^2}} \right) \right) \right) / \\ \left(\sqrt{1 - (0.3 - 0.02 \sin[\theta])^2} \right)$$

Out[289]=



Out[290]=



```

(*Going back for "t"*)
Clear[L, a, ϕ, t, m, k, w, w2, yp]
f[t_] := a Cos[w t + ϕ] + Sqrt[L^2 - (yp - a Sin[w t + ϕ])^2]
(*Solve for the first and second derivative for xp*)
f'[t] (*First derivative*)
f''[t] (*Second derivative*)
delta[t_] = f[t] - f[0]
Fplanks[t_] := -k * delta[t]
Fx[t_] := m f''[t] + Fplanks[t]
Fx[t] // FullSimplify
xr[t_] := a Cos[w t + ϕ]
yr[t_] := a Sin[w t + ϕ]
Ftot = Fx[t] / ((f[t] - xr[t]) / L)
Fy = Ftot * ((yp - yr[t]) / L)
torque = Fx[t] * yr[t] + Fy * xr[t]
(*Give values for the variables*)
{w = 5, L = 1, a = 0.02, k = 100, yp = 0.2, m = 70, ϕ = 21 (Pi / 180)}
Plot[-Fx[t] * yr[t] - Fy * xr[t], {t, 0, Pi}, Axes → True, AxesLabel → {t, Torque}]
(*Plotting the torque over time*)
Plot[-Fx[t] * yr[t] + Fy * xr[t], {t, Pi, 2 Pi}, Axes → True, AxesLabel → {t, Torque}]

```

Out[151]=

$$-a \cos[\phi] + a \cos[t w + \phi] - \sqrt{L^2 - (yp - a \sin[\phi])^2} + \sqrt{L^2 - (yp - a \sin[t w + \phi])^2}$$

Out[154]=

$$a m w^2 \left(-\cos[t w + \phi] - \frac{a L^2 \cos[t w + \phi]^2}{(L^2 - (yp - a \sin[t w + \phi])^2)^{3/2}} + \frac{\sin[t w + \phi] (-yp + a \sin[t w + \phi])}{\sqrt{L^2 - (yp - a \sin[t w + \phi])^2}} \right) +$$

$$k \left(a \cos[\phi] - a \cos[t w + \phi] + \sqrt{L^2 - (yp - a \sin[\phi])^2} - \sqrt{L^2 - (yp - a \sin[t w + \phi])^2} \right)$$

Out[157]=

$$\left(L \left(m \left(-a w^2 \cos[t w + \phi] - \frac{a^2 w^2 \cos[t w + \phi]^2 (yp - a \sin[t w + \phi])^2}{(L^2 - (yp - a \sin[t w + \phi])^2)^{3/2}} - \right. \right. \right.$$

$$\left. \left. \frac{a^2 w^2 \cos[t w + \phi]^2}{\sqrt{L^2 - (yp - a \sin[t w + \phi])^2}} - \frac{a w^2 \sin[t w + \phi] (yp - a \sin[t w + \phi])}{\sqrt{L^2 - (yp - a \sin[t w + \phi])^2}} \right) - \right.$$

$$\left. \left. k \left(-a \cos[\phi] + a \cos[t w + \phi] - \sqrt{L^2 - (yp - a \sin[\phi])^2} + \sqrt{L^2 - (yp - a \sin[t w + \phi])^2} \right) \right) \right) /$$

$$\left(\sqrt{L^2 - (yp - a \sin[t w + \phi])^2} \right)$$

Out[158]=

$$\left((yp - a \sin[tw + \phi]) \left(m \left(-a w^2 \cos[tw + \phi] - \frac{a^2 w^2 \cos[tw + \phi]^2 (yp - a \sin[tw + \phi])^2}{(L^2 - (yp - a \sin[tw + \phi])^2)^{3/2}} - \frac{a^2 w^2 \cos[tw + \phi]^2}{\sqrt{L^2 - (yp - a \sin[tw + \phi])^2}} - \frac{a w^2 \sin[tw + \phi] (yp - a \sin[tw + \phi])}{\sqrt{L^2 - (yp - a \sin[tw + \phi])^2}} \right) - k \left(-a \cos[\phi] + a \cos[tw + \phi] - \sqrt{L^2 - (yp - a \sin[\phi])^2} + \sqrt{L^2 - (yp - a \sin[tw + \phi])^2} \right) \right) \right) / \left(\sqrt{L^2 - (yp - a \sin[tw + \phi])^2} \right)$$

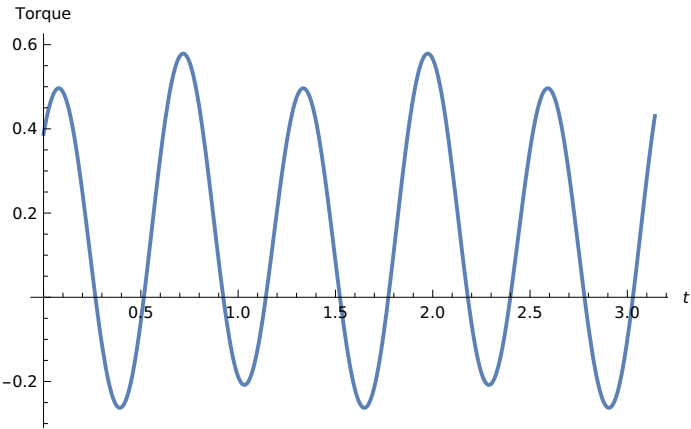
Out[159]=

$$a \sin[tw + \phi] \left(m \left(-a w^2 \cos[tw + \phi] - \frac{a^2 w^2 \cos[tw + \phi]^2 (yp - a \sin[tw + \phi])^2}{(L^2 - (yp - a \sin[tw + \phi])^2)^{3/2}} - \frac{a^2 w^2 \cos[tw + \phi]^2}{\sqrt{L^2 - (yp - a \sin[tw + \phi])^2}} - \frac{a w^2 \sin[tw + \phi] (yp - a \sin[tw + \phi])}{\sqrt{L^2 - (yp - a \sin[tw + \phi])^2}} \right) - k \left(-a \cos[\phi] + a \cos[tw + \phi] - \sqrt{L^2 - (yp - a \sin[\phi])^2} + \sqrt{L^2 - (yp - a \sin[tw + \phi])^2} \right) \right) + \left(a \cos[tw + \phi] (yp - a \sin[tw + \phi]) \left(m \left(-a w^2 \cos[tw + \phi] - \frac{a^2 w^2 \cos[tw + \phi]^2 (yp - a \sin[tw + \phi])^2}{(L^2 - (yp - a \sin[tw + \phi])^2)^{3/2}} - \frac{a^2 w^2 \cos[tw + \phi]^2}{\sqrt{L^2 - (yp - a \sin[tw + \phi])^2}} - \frac{a w^2 \sin[tw + \phi] (yp - a \sin[tw + \phi])}{\sqrt{L^2 - (yp - a \sin[tw + \phi])^2}} \right) - k \left(-a \cos[\phi] + a \cos[tw + \phi] - \sqrt{L^2 - (yp - a \sin[\phi])^2} + \sqrt{L^2 - (yp - a \sin[tw + \phi])^2} \right) \right) \right) / \left(\sqrt{L^2 - (yp - a \sin[tw + \phi])^2} \right)$$

Out[160]=

$$\left\{ 5, 1, 0.02, 100, 0.2, 70, \frac{7\pi}{60} \right\}$$

Out[161]=



Out[162]=

