

1) No, CNF can't have one state and one alphabet like 0A or 1B

It should be transferred to

$$S \rightarrow AB$$

$$A \rightarrow CA \mid 0$$

$$B \rightarrow DB \mid 1$$

$$C \rightarrow 0$$

$$D \rightarrow 1$$

2) a) C has no terminal string, B derives C and no terminal string. In addition,  $S \rightarrow C$ . So S has no terminal string. S, C and B derive nothing

b)

$$S \rightarrow AB | CD$$

$$A \rightarrow BC | a$$

$$B \rightarrow AC | C^x$$

$$C \rightarrow AB | CD$$

$$D \rightarrow AC | d$$

$$S \rightarrow AB | CD | AC$$

$$A \rightarrow Bc^x | a | cc^x$$

$$\Rightarrow B \rightarrow AC^x$$

$$B \rightarrow C \text{ is unit production} \quad C \rightarrow AB | CD | AC^x$$

$$D \rightarrow AC^x | d$$

$\Rightarrow$  C doesn't have terminal string

$$S \rightarrow AB^x$$

$$A \rightarrow a$$

$\Rightarrow$  S derives nothing and the language is empty

3)

a)

$$S \rightarrow 0A0 \mid 1B1 \mid BB$$

$$A \rightarrow C$$

$$B \rightarrow S \mid A$$

$$C \rightarrow S \mid \epsilon^x$$

$\Rightarrow$

eliminate

$$C \rightarrow \epsilon$$

$$S \rightarrow 0A0 \mid 1B1 \mid BB$$

$$A \rightarrow C \mid \epsilon^x$$

$$B \rightarrow S \mid A$$

$$C \rightarrow S$$

$$S \rightarrow 0A0 \mid 1B1 \mid BB \mid 00$$

$\Rightarrow$

$$A \rightarrow C$$

eliminate

$$B \rightarrow S \mid A \mid \epsilon$$

$$A \rightarrow \epsilon$$

$$C \rightarrow S$$

$$S \rightarrow 0A0 \mid 1B1 \mid BB \mid 00 \mid 11 \mid B$$

$\Rightarrow$

eliminate

$$A \rightarrow C$$

$$B \rightarrow S \mid A$$

$$B \rightarrow \epsilon$$

$$C \rightarrow S$$

$$\begin{aligned}
 b) \quad S &\rightarrow 0A0 \mid 1B1 \mid BB \mid 00 \mid 11 \mid B \\
 A &\rightarrow C \\
 B &\rightarrow S \mid A \\
 C &\rightarrow S
 \end{aligned}$$

$$\begin{aligned}
 \Rightarrow \quad S &\rightarrow 0A0 \mid 1B1 \mid BB \mid 00 \mid 11 \mid B \\
 B \rightarrow S \\
 C \rightarrow S \\
 A \rightarrow C \\
 B &\rightarrow 0A0 \mid 1B1 \mid BB \mid 00 \mid 11 \mid B \mid A \\
 C &\rightarrow 0A0 \mid 1B1 \mid BB \mid 00 \mid 11 \mid B
 \end{aligned}$$

$$\begin{aligned}
 \Rightarrow \text{eliminate} \quad S &\rightarrow 0A0 \mid 1B1 \mid BB \mid 00 \mid 11 \\
 S \rightarrow B \\
 A \rightarrow B \\
 C \rightarrow B \\
 B \rightarrow A \\
 C &\rightarrow 0A0 \mid 1B1 \mid BB \mid 00 \mid 11
 \end{aligned}$$

$$c) S \rightarrow \overset{D}{0A0} | \overset{E}{1B1} | BB | 00 | 11$$

$$A \rightarrow 0A0 | 1B1 | BB | 00 | 11$$

$$B \rightarrow 0A0 | 1B1 | BB | 00 | 11$$

$$C \rightarrow 0A0 | 1B1 | BB | 00 | 11$$

$$\Rightarrow S \rightarrow \overset{F}{D0} | \overset{G}{E1} | BB | 00 | 11$$

$$A \rightarrow D0 | E1 | BB | 00 | 11$$

$$B \rightarrow D0 | E1 | BB | 00 | 11$$

$$C \rightarrow D0 | E1 | BB | 00 | 11$$

$$D \rightarrow 0A$$

$$E \rightarrow 1B$$

$S \rightarrow DF | EG | BB | FF | GG$

$A \rightarrow DF | EG | BB | FF | GG$   $\times$  unreachable

$B \rightarrow DF | EG | BB | FF | GG$

$C \rightarrow DF | EG | BB | FF | GG$   $\times$

$D \rightarrow FA$

$E \rightarrow GB$

$F \rightarrow 0$

$G \rightarrow 1$

$S \rightarrow DF | EG | BB | FF | GG$

$B \rightarrow DF | EG | BB | FF | GG$

$D \rightarrow FA$

$E \rightarrow GB$

$F \rightarrow 0$

$G \rightarrow 1$

d)

$S \rightarrow DF \mid EG \mid BB \mid FF \mid GG$

$B \rightarrow DF \mid EG \mid BB \mid FF \mid GG$

$D \rightarrow FA$

$E \rightarrow GB$

$F \rightarrow O$

$G \rightarrow I$