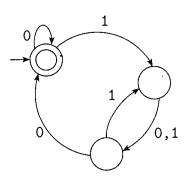
Decidability

Answer all parts for the following DFA ${\cal M}$ and give reasons for your answers.

1)



- a. Is $\langle M, 0100 \rangle \in A_{\mathsf{DFA}}$?
- **b.** Is $\langle M, 011 \rangle \in A_{\mathsf{DFA}}$?
- **c.** Is $\langle M \rangle \in A_{\mathsf{DFA}}$?

- **d.** Is $\langle M, 0100 \rangle \in A_{\mathsf{REX}}$?
- **e.** Is $\langle M \rangle \in E_{\mathsf{DFA}}$?
- **f.** Is $\langle M, M \rangle \in EQ_{\mathsf{DFA}}$?

2) Let $A_{\epsilon_{CFG}} = \{ \ < G > \ | \ G \ \ \text{is a CFG that generates the empty string } \}$

Show that $A\epsilon_{\text{CFG}}$ is decidable.

Decidability

3) Show that the following language is decidable

$$ALL_{DFA} = \{ \langle A \rangle | A \text{ is a DFA and } L(A) = \Sigma^* \}$$

4) Show that the following language is Turing-recognizable

 $A_{\exists} = \{ \ < M > | \ M \ \text{is a Turing Machine that accepts some string in } \Sigma^n \}$