

## Feedback — II. Linear regression with one variable

[Help Center](#)

You submitted this quiz on **Sat 24 Jan 2015 8:46 AM CET**. You got a score of **5.00** out of **5.00**.

### Question 1

Consider the problem of predicting how well a student does in her second year of college/university, given how well they did in their first year. Specifically, let  $x$  be equal to the number of "A" grades (including A-, A and A+ grades) that a student receives in their first year of college (freshmen year). We would like to predict the value of  $y$ , which we define as the number of "A" grades they get in their second year (sophomore year).

Questions 1 through 4 will use the following training set of a small sample of different students' performances. Here each row is one training example. Recall that in linear regression, our hypothesis is  $h_{\theta}(x) = \theta_0 + \theta_1 x$ , and we use  $m$  to denote the number of training examples.

$x$	$y$
3	2
1	2
0	1
4	3

For the training set given above, what is the value of  $m$ ? In the box below, please enter your answer (which should be a number between 0 and 10).

You entered:

Your Answer

Score

Explanation

4



1.00

Total

1.00 / 1.00

### Question Explanation

$m$  is the number of training examples. In this example, we have  $m=4$  examples.

## Question 2

Consider the following training set of  $m = 4$  training examples:

$x$	$y$
1	0.5
2	1
4	2
0	0

Consider the linear regression model  $h_{\theta}(x) = \theta_0 + \theta_1 x$ . What are the values of  $\theta_0$  and  $\theta_1$  that you would expect to obtain upon running gradient descent on this model? (Linear regression will be able to fit this data perfectly.)

Your Answer	Score	Explanation
<input type="radio"/> $\theta_0 = 0.5, \theta_1 = 0$		
<input type="radio"/> $\theta_0 = 0.5, \theta_1 = 0.5$		
<input checked="" type="radio"/> $\theta_0 = 0, \theta_1 = 0.5$	✓ 1.00	
<input type="radio"/> $\theta_0 = 1, \theta_1 = 1$		
Total	1.00 / 1.00	

### Question Explanation

As  $J(\theta_0, \theta_1) = 0, y = h_{\theta}(x) = \theta_0 + \theta_1 x$ . Using any two values in the table, solve for  $\theta_0, \theta_1$ .

## Question 3

Consider the training set below with only  $m = 3$  training examples:

$x$	$y$
1	1
2	2
3	3

Recall the gradient descent algorithm used to update  $\theta_0$  and  $\theta_1$ :

$$\theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})$$

$$\theta_1 := \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) \cdot x^{(i)}$$

Now let's assume we choose  $\theta_0 = 0$  and  $\theta_1 = 0.5$  as our starting point, and we choose  $\alpha$  to be 0.1. After you perform one iteration of gradient descent, what will be the new values for  $\theta_0$  and  $\theta_1$ ?

Your Answer	Score	Explanation
<input type="radio"/> $\theta_0 = 0$ and $\theta_1 = 1$		
<input type="radio"/> $\theta_0 = 0.1$ and $\theta_1 = 0.713$		
<input type="radio"/> $\theta_0 = 0.15$ and $\theta_1 = 0.632$		
<input checked="" type="radio"/> $\theta_0 = 0.1$ and $\theta_1 = 0.733$	✓ 1.00	
Total	1.00 / 1.00	

#### Question Explanation

Remember to update both  $\theta_0$  and  $\theta_1$  simultaneously. So,

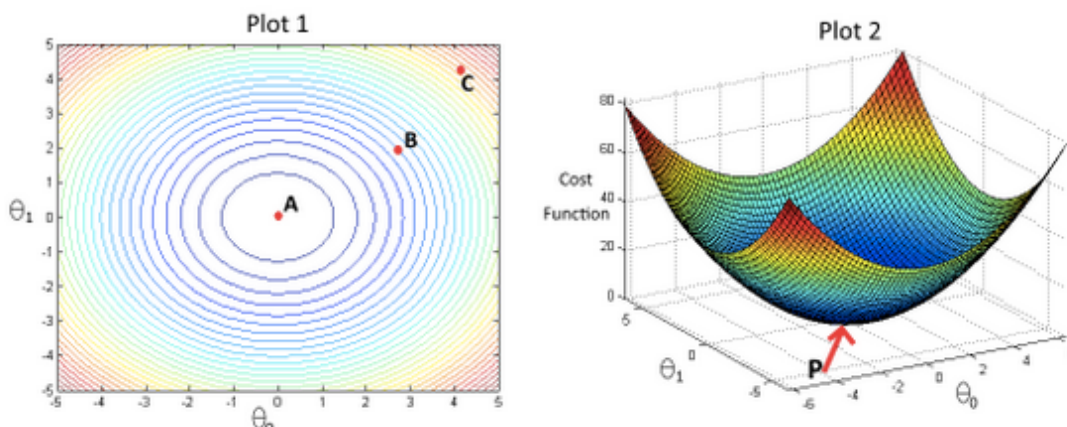
$$\theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) = 0 - 0.1 \times (1/3) \times ((0.5 \times 1 - 1) + (0.5 \times 2 - 2) + (0.5 \times 3 - 3)) = 0.1$$

$$\theta_1 := \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) \cdot x^{(i)} = 0.5 - 0.1 \times (1/3) \times ((0.5 \times 1 - 1) \times 1 + (0.5 \times 2 - 2) \times 2 + (0.5 \times 3 - 3) \times 3) = 0.733$$

## Question 4

In the given figure, the cost function  $J(\theta_0, \theta_1)$  has been plotted against  $\theta_0$  and  $\theta_1$ , as shown in 'Plot 2'. The contour plot for the same cost function is given in 'Plot 1'. Based on the figure, choose the correct options (check all that apply).

Plots for Cost Function  $J(\theta_0, \theta_1)$



Your Answer	Score	Explanation
<input checked="" type="checkbox"/> Point P (the global minimum of plot 2) corresponds to point A of Plot 1.	<input checked="" type="checkbox"/> 0.20	Correct. Plot 2 is a 3-D surface plot for cost function $J(\theta_0, \theta_1)$ against $\theta_0$ and $\theta_1$ , whereas Plot 1 is the 2-D contour plot for the same cost function. Hence, the correspondence of the two plots can be understood.
<input type="checkbox"/> If we start from point B, gradient descent with a well-chosen learning rate will eventually help us reach at or near point C, as the value of cost function $J(\theta_0, \theta_1)$ is minimum at point C.	<input checked="" type="checkbox"/> 0.20	
<input type="checkbox"/> Point P (The global minimum of plot 2) corresponds to point C of Plot 1.	<input checked="" type="checkbox"/> 0.20	
<input type="checkbox"/> If we start from point B, gradient descent with a well-chosen learning rate will eventually help us reach at or near point A, as the value of cost function $J(\theta_0, \theta_1)$ is maximum at point A.	<input checked="" type="checkbox"/> 0.20	
<input checked="" type="checkbox"/> If we start from point B, gradient descent with a well-chosen learning rate will eventually help us reach at or near point A, as the value of cost function $J(\theta_0, \theta_1)$ is minimum at A.	<input checked="" type="checkbox"/> 0.20	Correct. Correct implementation of Gradient Descent Algorithm will help us minimizing the cost function $J(\theta_0, \theta_1)$ . Since point A represents the global minimum of the cost function, gradient descent should lead us to reach at or near point A.
Total	1.00 / 1.00	

## Question 5

Suppose that for some linear regression problem (say, predicting housing prices as in the lecture), we have some training set, and for our training set we managed to find some  $\theta_0, \theta_1$  such that  $J(\theta_0, \theta_1) = 0$ . Which of the statements below must then be true? (Check all that apply.)

Your Answer	Score	Explanation
<input type="checkbox"/> We can perfectly predict the value of $y$ even for new examples that we have not yet seen. (e.g., we can perfectly predict prices of even new houses that we have not yet seen.)	✓ 0.25	Even though we can fit our training set perfectly, this does not mean that we'll always make perfect predictions on houses in the future/on houses that we have not yet seen.
<input checked="" type="checkbox"/> Our training set can be fit perfectly by a straight line, i.e., all of our training examples lie perfectly on some straight line.	✓ 0.25	If $J(\theta_0, \theta_1) = 0$ , that means the line defined by the equation " $y = \theta_0 + \theta_1 x$ " perfectly fits all of our data.
<input type="checkbox"/> For this to be true, we must have $y^{(i)} = 0$ for every value of $i = 1, 2, \dots, m$ .	✓ 0.25	So long as all of our training examples lie on a straight line, we will be able to find $\theta_0$ and $\theta_1$ so that $J(\theta_0, \theta_1) = 0$ . It is not necessary that $y^{(i)} = 0$ for all of our examples.
<input type="checkbox"/> For this to be true, we must have $\theta_0 = 0$ and $\theta_1 = 0$ so that $h_\theta(x) = 0$	✓ 0.25	If $J(\theta_0, \theta_1) = 0$ , that means the line defined by the equation " $y = \theta_0 + \theta_1 x$ " perfectly fits all of our data. There's no particular reason to expect that the values of $\theta_0$ and $\theta_1$ that achieve this are both 0 (unless $y^{(i)} = 0$ for all of our training examples).
Total	1.00 / 1.00	

---