# Feedback — IV. Linear Regression with Multiple

**Variables** Help Center

You submitted this quiz on **Mon 26 Jan 2015 10:00 AM CET**. You got a score of **5.00** out of **5.00**.

### **Question 1**

Suppose m=4 students have taken some class, and the class had a midterm exam and a final exam. You have collected a dataset of their scores on the two exams, which is as follows:

midterm exam	(midterm exam) <sup>2</sup>	final exam
89	7921	96
72	5184	74
94	8836	87
69	4761	78

You'd like to use polynomial regression to predict a student's final exam score from their midterm exam score. Concretely, suppose you want to fit a model of the form  $h_{\theta}(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2$ , where  $x_1$  is the midterm score and  $x_2$  is (midterm score)<sup>2</sup>. Further, you plan to use both feature scaling (dividing by the "max-min", or range, of a feature) and mean normalization.

What is the normalized feature  $x_2^{(4)}$ ? (Hint: midterm = 89, final = 96 is training example 1.) Please enter your answer in the text box below. If applicable, please provide at least two digits after the decimal place.

#### You entered:

-0.46982

Your Answer		Score	Explanation
-0.46982	<b>~</b>	1.00	
Total		1.00 / 1.00	

#### **Question Explanation**

The mean of  $x_2$  is 6675.5 and the range is 8836 - 4761 = 4075 So  $x_1^{(4)}$  is  $\frac{4761 - 6675.5}{4075} = -0.47$ .

## **Question 2**

You run gradient descent for 15 iterations with  $\alpha=0.3$  and compute  $J(\theta)$  after each iteration. You find that the value of  $J(\theta)$  decreases quickly then levels off. Based on this, which of the following conclusions seems most plausible?

Your Answer	Score	Explanation
Rather than use the current value of $\alpha$ , it'd be more promising to try a smaller value of $\alpha$ (say $\alpha=0.1$ ).		
Rather than use the current value of $\alpha$ , it'd be more promising to try a larger value of $\alpha$ (say $\alpha=1.0$ ).		
$\alpha = 0.3$ is an effective choice of learning rate.	<b>✓</b> 1.00	We want gradient descent to quickly converge to the minimum, so the current setting of $\alpha$ seems to be good.
Total	1.00 / 1.00	

### **Question 3**

Suppose you have m=14 training examples with n=3 features (excluding the additional allones feature for the intercept term, which you should add). The normal equation is  $\theta=(X^TX)^{-1}X^Ty$ . For the given values of m and n, what are the dimensions of  $\theta$ , X, and y in this equation?

Your Answer		Score	Explanation
• $X$ is $14 \times 4$ , $y$ is $14 \times 1$ , $\theta$ is $4 \times 1$	~	1.00	
$\bigcirc X \text{ is } 14 \times 3, y \text{ is } 14 \times 1, \theta \text{ is } 3 \times 3$			
$\bigcirc X \text{ is } 14 \times 4, y \text{ is } 14 \times 4, \theta \text{ is } 4 \times 4$			
$\bigcirc X \text{ is } 14 \times 3, y \text{ is } 14 \times 1, \theta \text{ is } 3 \times 1$			
Total		1.00 / 1.00	

#### **Question Explanation**

X has m rows and n+1 columns (+1 because of the  $x_0=1$  term). y is an m-vector.  $\theta$  is an ( n+1)-vector.

## **Question 4**

Suppose you have a dataset with m=1000000 examples and n=200000 features for each example. You want to use multivariate linear regression to fit the parameters  $\theta$  to our data. Should you prefer gradient descent or the normal equation?

Your Answer	Score	Explanation
Gradient descent, since it will always converge to the optimal $\theta$ .		
• Gradient descent, since $(X^TX)^{-1}$ will be very slow to compute in the normal equation.	✔ 1.00	With $n=200000$ features, you will have to invert a $200001\times200001$ matrix to compute the normal equation. Inverting such a large matrix is computationally expensive, so gradient descent is a good choice.
The normal equation, since gradient descent might be unable to find the optimal $\theta$ .		
The normal equation, since it provides an efficient way to directly find the solution.		
Total	1.00 / 1.00	

### **Question 5**

Which of the following are reasons for using feature scaling?

**Your Answer** 

Score Explanation

✓ It speeds up gradient descent by making it require fewer iterations to get to a good solution.	✔ 0.25	Feature scaling speeds up gradient descent by avoiding many extra iterations that are required when one or more features take on much larger values than the rest.
It prevents the matrix $X^TX$ (used in the normal equation) from being noninvertable (singular/degenerate).	✔ 0.25	$X^TX$ can be singular when features are redundant or there are too few examples. Feature scaling does not solve these problems.
☐ It speeds up gradient descent by making each iteration of gradient descent less expensive to compute.	✔ 0.25	The magnitude of the feature values are insignifican in terms of computational cost.
$\ \square$ It speeds up solving for $ heta$ using the normal equation.	✔ 0.25	The magnitude of the feature values are insignifican in terms of computational cost.
Total	1.00 1.00	