ShOpt.jl: A Julia Package for Empirical Point Spread Function Characterization of JWST NIRCam Data

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Summary

When astronomers capture images of the night sky, several factors – ranging from diffraction and optical aberrations to atmospheric turbulence and telescope jitter – affect the incoming light. The resulting distortion and blurring are summarized in the image's point spread function (PSF), the response of an optical system to an idealized point source. The PSF can obscure or even mimic the astronomical signal of interest, making its accurate characterization essential. By effectively modeling the PSF, we can predict image distortions at any location and proceed to deconvolve the PSF, ultimately reconstructing distortion-free images.

The PSF characterization methods used by astronomers fall into two main classes: forward-modeling approaches, which use physical optics propagation based on models of the optics, and empirical approaches, which use stars as fixed points to model and interpolate the PSF across the rest of the image. (Stars are essentially point sources before their light passes through the atmosphere and telescope, so the shape and size of their surface brightness profiles define the PSF at that location.) Empirical PSF characterization proceeds by first cataloging the observed stars, separating the catalog into validation and training samples, and interpolating the training stars across the field of view of the camera. After training, the PSF model can be validated by comparing the reserved stars to the PSF model's prediction.

Shear Optimization with ShOpt.jl introduces modern techniques, tailored to James Webb Space Telescope (JWST) imaging, for empirical PSF characterization across the field of view. ShOpt has two modes of operation: approximating stars with analytic profiles, and a more realistic pixel-level representation. Both modes take as input a catalog with image cutouts – or "vignettes" – of the stars targeted for analysis.
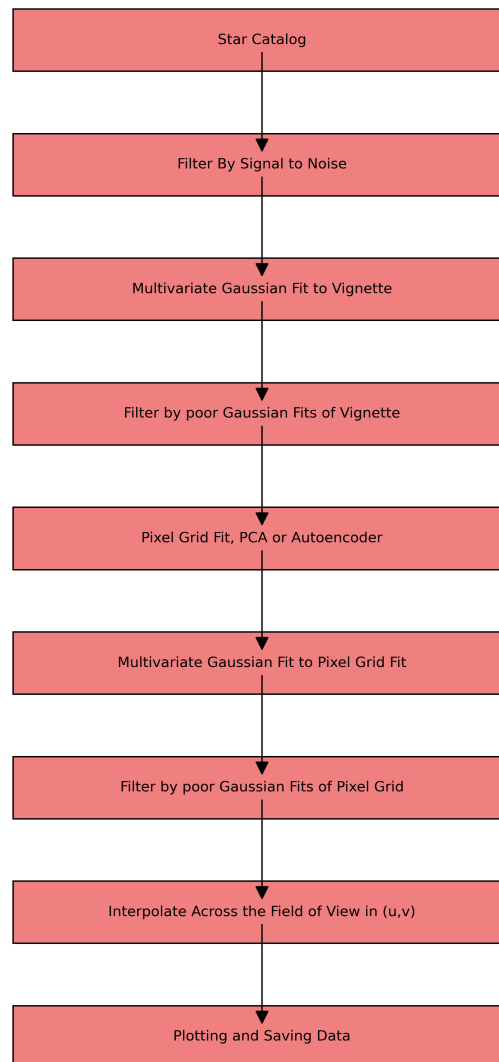
Figure 1: ShOpt Workflow

Statement of need

Empirical PSF characterization tools like PSFEx (Bertin, 2011) and PIFF (Jarvis et al., 2020) are widely popular in astrophysics. However, the quality of PIFF and PSFEx models tends to be quite sensitive to the parameter values used to run the software, with optimization sometimes relying on brute-force guess-and-check runs. PIFF is also notably inefficient for large, well-sampled images, taking hours in the worst cases. The James Webb Space Telescope's (JWST) Near Infrared Camera (NIRCam) offers vast scientific opportunities (Casey, Kartaltepe, et al., 2023); at the same time, this unprecedented data brings new challenges for PSF modeling:

(1) Analytic functions like Gaussians are incomplete descriptions of the NIRCam PSF, as evident from Figure 2. This calls for well-thought-out, non-parametric modeling and diagnostic tools that can capture the full dynamic range of the NIRCam PSF. ShOpt

38   provides these models and diagnostics out of the box.

39   (2) The NIRCam detectors have pixel scales of 0.03 (short wavelength channel) and 0.06
40   (long wavelength channel) arcseconds per pixel (Beichman et al., 2012; Rieke et al.,
41   2003, 2005). At these pixel scales, star vignettes need to be at least 131 by 131 pixels
42   across to fully capture the wings of the PSFs (4-5 arcseconds). These vignette sizes are
43   3-5 times larger than the ones used in surveys such as DES (Jarvis et al., 2020) and
44   SuperBIT (McCleary et al., 2023) and force us to evaluate how well existing PSF fitters
45   scale to this size. Sh0pt has been designed for computational efficiency and aims to
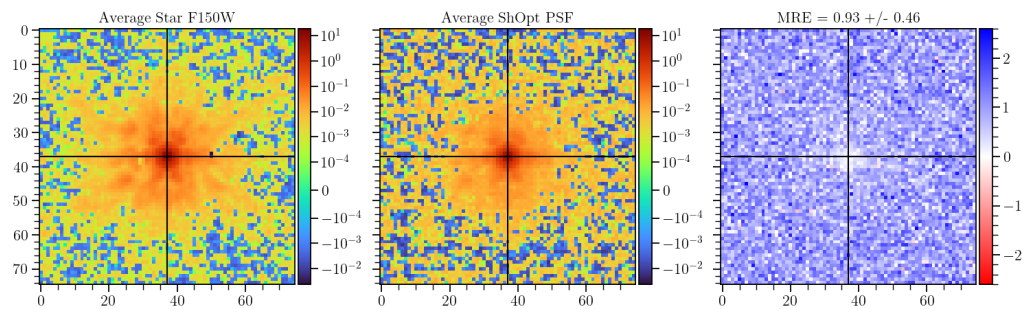46   meet the requirements of detectors like NIRCam.

Figure 2: The plot on the left shows the average cutout of all stars in a supplied catalog. The plot in the middle shows the average point spread function model for each star. The plot on the right shows the average normalized error between the observed star cutouts and the point spread function model.

47 Sh0pt bridges the speed of PSFex with the features of PIFF using fewer configurable hyperpa-
48 rameters. Sh0pt employs a myriad of techniques to optimize the speed of the program. First
49 and foremost, Sh0pt is equipped with support for multithreading. Polynomial interpolation
50 is used for handling PSF variations across the field of view. The polynomials given to each
51 basis element of the PSF are independent of one another and therefore can be distributed to
52 different CPU threads to be run in parallel. Sh0pt also introduces new methods for fitting
53 both analytic profiles and pixel based profiles. If an analytic profile is used to model the PSF,
54 then there are 3 basis elements parameterizing the model. We choose 2D elliptical Gaussians
55 for these analytic profiles because they are cheap to compute. Moreover, we use the Limited
56 Memory Broyden–Fletcher–Goldfarb–Shanno algorithm (LBFGS) to find these paramters. This
57 is faster but more memory intensive than Conjugate Gradient, the algorithm used in PIFF.
58 Moreover, the 3 basis elements are constrained to the manifold $B_2(r) \times \mathbb{R}_+$. We constructed
59 a function that maps any point in $\mathbb{R}^3$ into $B_2(r) \times \mathbb{R}_+$. The LBFGS algorithm uses successive
60 iterations to converge to a solution for the 3 basis elements, and so we use this function to
61 ensure that our update steps in LBFGS do not leave the constraint. For the pixel basis, both
62 PIFF and PSFex approximate the PSF by minimizing the reduced χ^2 between a grid of pixels
63 and a star vignette. PCA can quickly achieve the same purpose of approximating the input
64 vignette without overfitting to background noise. We also provide an autoencoder mode, which
65 uses deep learning to reconstruct the image. The weights and biases are not reset between
66 stars, so the knowledge of how to reconstruct one star is transfered to the next. This in turn
67 leads to less training iterations. Finally, Sh0pt is written in Julia. Julia uses a just in time
68 compiler which makes it faster than intepreted languages such as Python and has shown to be
69 a good choice for performance critical code (Stanitzki & Strube, 2021).

State of the Field

The JWST captures images at high resolution and at wavelengths of light that have been previously unexplored (Gardner et al., 2006). With these images we are seeing farther into the early universe than we ever have before. The difficulties of producing good PSF models for the JWST are emblemetic of a larger problem: Our data sets are getting bigger and existing software was not built to scale. That is to say, the advancements in software are falling behind the advances in instrumentation. Not only does Sh0pt produces PSF models for JWST NIRCam images, it also sets the precedent for designing software that scales.

There are several existing empirical PSF fitters, in addition to a forward model of the JWST PSFs developed by STScI (Jarvis et al., 2020 ; Bertin, 2011; Perrin et al., 2014 ; Perrin et al., 2012). We describe them here and draw attention to their strengths and weaknesses to further motivate the development of Sh0pt.jl. As described in the statement of need, PSFex was one of the first precise and general purpose tools used for empirical PSF fitting. However, the Dark Energy Survey collaboration reported small but noticeable discrepancies between the sizes of PSFex models and the sizes of observed stars. They also reported ripple-like patterns in the spatial variation of star-PSF residuals across the field of view (Jarvis et al., 2020), which they attributed to the astrometric distortion solutions for the Dark Energy Camera.

These findings motivated the Dark Energy Survey's development of PIFF (Point Spread Functions in the Full Field of View). PIFF works in sky coordinates on the focal plane, as opposed to image pixel coordinates used in PSFex, which minimized the ripple patterns in the star-PSF residuals and the PSF model size bias. (Based on the DES findings, Sh0pt also works directly in sky coordinates.) PIFF is written in Python, a language with a large infrastructure for astronomical data analysis, for example Astropy (Astropy Collaboration et al., 2022) and Galsim (Rowe et al., 2015). The choice of language makes PIFF software more accessible to programmers in the astrophysics community than PSFex, which was first written in C twenty-five years ago and much less approachable for a community of open source developers. One of the motivations of Sh0pt was to write astrophysics specific software in Julia, because Julia provides a good balance of readability and speed with its high-level functional paradigm and just-in-time compiler (Stanitzki & Strube, 2021). Julia ranks behind Python, IDL, Matlab, and Fortran in full-text mentions in astronomical literature (Collaboration et al., 2022). We are optimistic that Sh0pt will demonstrate that Julia is an appealing choice for programming in astronomy despite its low adoption to date. There is also recent work on using PSFr for PSF reconstructions that has been applied to JWST data (Ding et al., 2022; Merlin et al., 2022; Santini et al., 2023; Yang et al., 2022). Similar to Sh0pt, PSFr begins its PSF modeling by stacking stars to form an initial guess. However, rather than using polynomial interpolation to address spatial variations, PSFr employs an iterative process of shifting the pixels in its PSF model. This process continues until the model can adequately represent all of the stars in the catalog. There is future work to be done to benchmarking all of these empirical approaches on JWST NIRCam data.

While WebbPSF provides highly precise forward models of the JWST PSF, these models are defined for single-epoch exposures (Perrin et al., 2014, 2012). Much of the NIRCam science is accomplished with image mosaics – essentially, the combination of single exposure detector images into a larger, deeper image. The rotation of the camera between exposures, the astrometric transformations and resampling of images before their combination into a mosaic, and the mosaic's large area all make the application of WebbPSF models to mosaics a non-trivial procedure. This has been done quite effectively (Ji et al., 2023), however, it is not as easy to reproduce compared to running an empirical characterization tool like Sh0pt.

As outlined in the state of the field, Sh0pt is a tool built with the user experience in mind that attempts to bridge the strengths of existing PSF fitters. Sh0pt's combination of speed, user friendliness, and accuracy enable the science goals of the COSMOS-Web survey, detailed below.

The COMOS-Web survey is the largest cycle 1 JWST extragalactic survey according to area and prime time allocation (Casey, Kartaltepe, et al., 2023), and takes up $0.54\ deg^2$ (Beichman et al., 2012; Rieke et al., 2023). Among other science goals, the COMOS-Web survey will use the JWST to detect thousands of galaxies in the Epoch of Reionization ($6 \sim z \sim 11$) to create one of the highest resolution large scale structure maps of the early universe (Casey, Kartaltepe, et al., 2023). JWST data has also been used to pick out active galactic nuclei from host galaxies (Zhuang & Shen, 2023) and indentify 15 candidate galaxies whose luminosities push the limits of our ΛCDM galaxy formation models (Casey, Akins, et al., 2023). These science cases all rely upon good PSF modeling and underscore the importance of Sh0pt.

Acknowledgements

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