

# ShOpt.jl | A Julia Library for Empirical Point Spread Function Characterization of JWST NIRCам Data

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## Summary

### Introduction

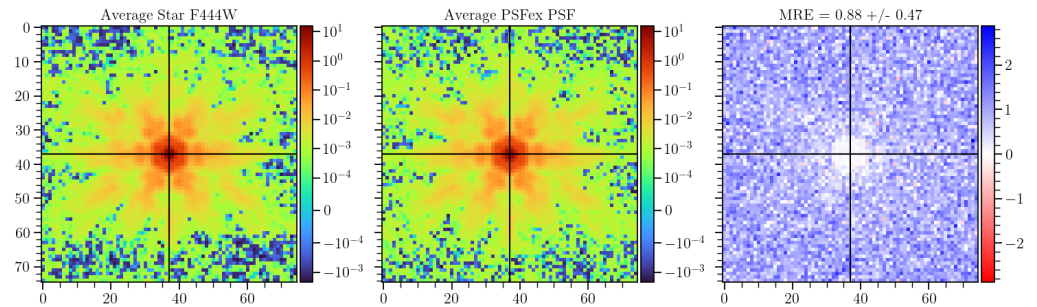
When astronomers capture images of the night sky, several factors – ranging from diffraction and optical aberrations to atmospheric turbulence and telescope jitter – affect the incoming light. The resulting distortions are summarized in the image's point spread function (PSF), a mathematical model that describes the response of an optical system to an idealized point of light. The PSF can obscure or even mimic the astronomical signal of interest, making its accurate characterization essential. By effectively modeling the PSF, we can predict image distortions at any location and proceed to deconvolve the PSF, ultimately reconstructing distortion-free images.

The PSF characterization methods used by astronomers fall into two main classes: forward-modeling approaches, which use physical optics propagation based on models of the optics, and empirical approaches, which use stars as fixed points to model and interpolate the PSF across the rest of the image. (Stars are essentially point sources before their light passes through the atmosphere and telescope, so the shape and size of their surface brightness profiles define the PSF at that location.) Empirical PSF characterization proceeds by first cataloging the observed stars, separating the catalog into validation and training samples, and interpolating the training stars across the field of view of the camera. After training, the PSF model can be validated by comparing the reserved stars to the PSF model's prediction.

Shear Optimization with ShOpt.jl introduces modern techniques, tailored to James Webb Space Telescope (JWST) imaging, for empirical PSF characterization across the field of view. ShOpt has two modes of operation: approximating stars with analytic profiles, and a more realistic pixel-level representation. Both modes take as input a catalog with image cutouts – or “vignettes” – of the stars targeted for analysis.

### Analytic profile mode

A rough idea of the size and shape of the PSF can be obtained by fitting stars with analytic profiles. We adopt a multivariate Gaussian profile, as it is computationally cheap to fit one to an image. That is, Gaussian profiles are easy to differentiate and don't involve any numeric integration or other costly steps to calculate. Fitting other common models, such as a Kolmogorov profile, involves numeric integration and thus take much longer to fit. Moreover, the JWST point spread function is very “spikey” (cf. Figure 1). As a result, analytic profiles are limited in their ability to model the point spread function anyway, making the usual advantages of a more expensive analytic profile moot.



**Figure 1:** The plot on the left shows the average cutout of all stars in a supplied catalog. The plot in the middle shows the average point spread function model for each star. The plot on the right shows the average normalized error between the observed star cutouts and the point spread function model.

Our multivariate gaussian is parameterized by three variables,  $[s, g_1, g_2]$ , where  $s$  corresponds to size and  $g_1, g_2$  correspond to shear. A shear matrix has the form

$$\begin{pmatrix} 1 + g_1 & g_2 \\ g_2 & 1 - g_1 \end{pmatrix}$$

. Given a point  $[u, v]$ , we obtain coordinates  $[u', v']$  by applying a shear and then a scaling by  $\frac{s}{\sqrt{1-g_1^2-g_2^2}}$ . Then, we choose  $f(r) := Ae^{-r^2}$  to complete our fit, where  $A$  makes the fit sum to unity over the cutout of our star. After we fit this function to our stars with `Optim.jl` (Mogensen & Riseth, 2018) and `ForwardDiff.jl` (Revels et al., 2016), we interpolate the parameters across the field of view according to position. Essentially, each star is a datapoint, and the three variables are treated as polynomials in the focal plane. We express positions in sky (astrometric) coordinates  $(u, v)$ , as opposed to pixel coordinates  $(x, y)$  measured in detector pixels.

## Notation

1. For the set  $B_2(r)$ , we have:

$$B_2(r) \equiv \{[x, y] : x^2 + y^2 < 1\} \subset \mathbb{R}^2$$

2. For the set  $\mathbb{R}_+$ , we have:

$$\mathbb{R}_+ \equiv \{x : x > 0\} \subset \mathbb{R}$$

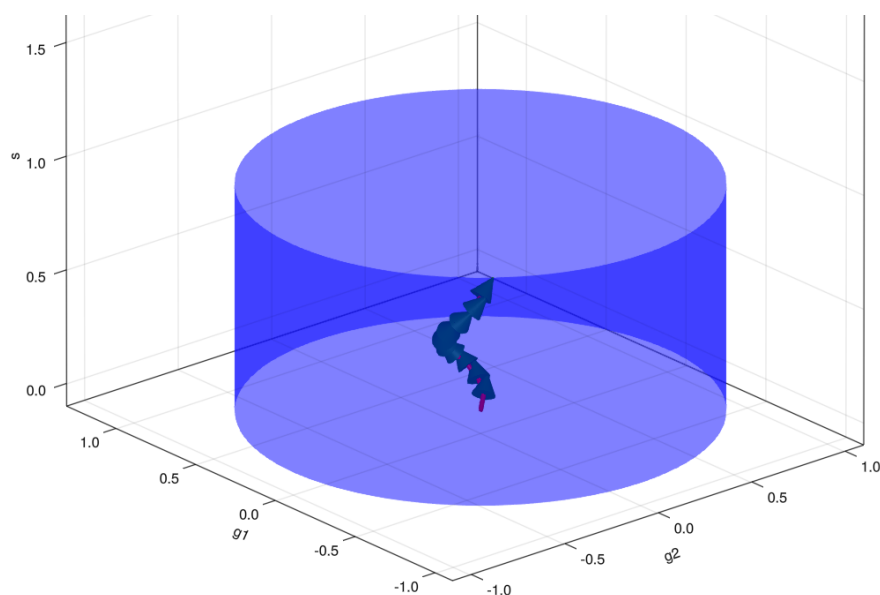
3. For the Cartesian product of sets  $A$  and  $B$ , we have:

$$A \times B \equiv \{(a, b) : a \in A, b \in B\}$$

## Analytic methods

ShOpt.jl's analytic profile fitting takes inspiration from a number of algorithms outside of astronomy, notably SE-Sync (Rosen et al., 2019), an algorithm that solves the robotic

mapping problem by considering the manifold properties of the data. With sufficiently clean data, the SE-Sync algorithm will descend to a global minimum constrained to the manifold  $SE(d)^n / SE(d)$ . Following suit, we are able to put a constraint on the solutions we obtain to  $[s, g_1, g_2]$  to a manifold. The solution space to  $[s, g_1, g_2]$  is constrained to the manifold  $B_2(r) \times \mathbb{R}_+$  (Bernstein & Jarvis, 2002). The existence of the constraint on shear is well known; nevertheless, the parameter estimation task is usually framed as an unconstrained problem (Jarvis et al., 2020). For a more rigorous treatment of optimization on manifolds see (Absil et al., 2008) and (Boumal, 2023). Julia offers support for working with manifolds through the Manopt framework, which we may leverage in future releases (Bergmann, 2022).



**Figure 2:** LFBGS algorithm used to find parameters subject to the cylindrical constraint.  $s$  is arbitrarily capped at 1 as a data cleaning method.

## 64 Pixel grid mode

A more complete description of the PSF can be obtained using the image pixels themselves as a basis, with an interpolation function to model PSF variation across the field of view. `Sh0pt.jl` provides two modes for these pixel grid fits: PCA mode and Autoencoder mode. PCA mode, outlined below, reconstructs its images using the first  $n$  principal components. Autoencoder mode uses a neural network to reconstruct the image from a lower dimensional latent space. The network code written with `Flux.jl` is also outlined below (Innes, 2018). Both modes provide the end user with tunable parameters that allow for both perfect reconstruction of star cutouts and low dimensional representations. The advantage of these modes is that they provide good reconstructions of the distorted images that can learn the key features of the point spread function without overfitting the background noise. In this way it generates a datapoint for our algorithm to train on and denoises the image in one step. In both cases, the input star data is cleaned by first fitting an analytic (Gaussian) PSF profile and rejecting size outliers. As in the analytic profile case, star positions are expressed directly in sky (astrometric) coordinates  $(u, v)$  rather than pixel coordinates  $(x, y)$ . In the pixel grid modes, we also model each pixel in the star stamp as polynomial to be interpolated across the field of view. That is, each pixel in position  $(i, j)$  of a star cutout gets its own polynomial, interpolated over  $k$  different star cutouts at different locations in the focal plane.

82 **Pixel grid methods**

## 83 PCA mode

```
function pca_image(image, ncomponents)
  #Load img Matrix
  img_matrix = image

  # Perform PCA
  M = fit(PCA, img_matrix; maxoutdim=ncomponents)

  # Transform the image into the PCA space
  transformed = MultivariateStats.transform(M, img_matrix)

  # Reconstruct the image
  reconstructed = reconstruct(M, transformed)

  # Reshape the image back to its original shape
  reconstructed_image = reshape(reconstructed, size(img_matrix)...)
end
```

84 Autoencoder mode

```
# Encoder
encoder = Chain(
  Dense(r*c, 128, leakyrelu),
  Dense(128, 64, leakyrelu),
  Dense(64, 32, leakyrelu),
)

#Decoder
decoder = Chain(
  Dense(32, 64, leakyrelu),
  Dense(64, 128, leakyrelu),
  Dense(128, r*c, tanh),
)

#Full autoencoder
autoencoder = Chain(encoder, decoder)

#x_hat = autoencoder(x)
loss(x) = mse(autoencoder(x), x)

# Define the optimizer
optimizer = ADAM()
```

## 85 Statement of need

86 Empirical PSF characterization tools like PSFEx (Bertin, 2011) and PIFF (Jarvis et al., 2020)  
87 are widely popular in astrophysics. However, the quality of PIFF and PSFEx models tends  
88 to be quite sensitive to the parameter values used to run the software, with optimization  
89 sometimes relying on brute-force guess-and-check runs. PIFF is also notably inefficient for large,  
90 well-sampled images, taking hours in the worst cases. The James Webb Space Telescope's  
91 (JWST) Near Infrared Camera (NIRCam) offers vast scientific opportunities (e.g., (Casey et al.,  
92 2023)); at the same time, this unprecedented data brings new challenges for PSF modeling:

- 93 (1) Analytic functions like Gaussians are incomplete descriptions of the NIRCam PSF, as  
94 evident from Figure 1. This calls for well-thought-out, non-parametric modeling and  
95 diagnostic tools that can capture the full dynamic range of the NIRCam PSF. ShOpt  
96 provides these models and diagnostics out of the box.
- 97 (2) The NIRCam detectors have pixel scales of 0.03 (short wavelength channel) and 0.06

(long wavelength channel) arcseconds per pixel (Beichman et al., 2012a; Rieke et al., 2003, 2005). At these pixel scales, star vignettes need to be at least 131 by 131 pixels across to fully capture the wings of the PSFs (4-5 arcseconds). These vignette sizes are 3-5 times larger than the ones used in surveys such as DES (Jarvis et al., 2020) and SuperBIT (McCleary et al., 2023) and force us to evaluate how well existing PSF fitters scale to this size. Sh0pt has been designed for computational efficiency and aims to meet the requirements of detectors like NIRCcam.

## State of the Field

There are several existing empirical PSF fitters, in addition to a forward model of the JWST PSFs developed by STScI (Jarvis et al., 2020; Bertin, 2011; Perrin et al., 2014; Perrin et al., 2012). We describe them here and draw attention to their strengths and weaknesses to motivate the development of Sh0pt.jl. As described in the statement of need, PSFex was one of the first precise and general purpose tools used for empirical PSF fitting. However, the Dark Energy Survey collaboration reported small but noticeable discrepancies between the sizes of PSFex models and the sizes of observed stars. They also reported ripple-like patterns in the spatial variation of star-PSF residuals across the field of view (Jarvis et al., 2020), which they attributed to the astrometric distortion solutions for the Dark Energy Camera.

These findings motivated the Dark Energy Survey's development of PIFF (Point Spread Functions in the Full Field of View). PIFF works in sky coordinates on the focal plane, as opposed to image pixel coordinates used in PSFex, which minimized the ripple patterns in the star-PSF residuals and the PSF model size bias. (Based on the DES findings, Sh0pt also works directly in sky coordinates.) PIFF is written in Python, a language with a large infrastructure for astronomical data analysis, for example Astropy (Astropy Collaboration et al., 2022) and Galsim (Rowe et al., 2015). The choice of language makes PIFF software more accessible to programmers in the astrophysics community than PSFex, which was first written in C twenty-five years ago and much less approachable for a community of open source developers. As an aside, one of the motivations of Sh0pt was to write astrophysics specific software in Julia, because Julia provides a nice balance of readability and speed with its high-level functional paradigm and just-in-time compiler.

While WebbPSF provides highly precise forward models of the JWST PSF, these models are defined for single-epoch exposures (Perrin et al., 2014, 2012). Much of the NIRCcam science is accomplished with image mosaics – essentially, the combination of single exposure detector images into a larger, deeper image. The rotation of the camera between exposures, the astrometric transformations and resampling of images before their combination into a mosaic, and the mosaic's large area all make the application of WebbPSF models to mosaics a non-trivial procedure. Additionally, some recent work being done to generate hybrid PSF models, which add an empirical correction to forward-model PSFs, for single-epoch exposures (Lin et al., 2023). At the time of writing, there is no widely available software to do this.

## Future Work

The COMOS-Web survey is the largest JWST extragalactic survey according to area and prime time allocation (Casey et al., 2023), and takes up  $0.54 \text{ deg}^2$  (Beichman et al., 2012b; Rieke et al., 2023). This is a large enough portion of the sky that we should prepare to see significant PSF variation across the field of view because of astrometric distortions. Thus, COSMOS-Web data provides Sh0pt with an opportunity to validate PIFF's correction for handling PSF variations and test how impactful (or not impactful) PSFex's size bias is.

We speculate that petal diagrams may be able to approximate the spikey natures of JWST PSFs. Consider  $r = A \cos(k\theta + \gamma)$ , shown below in figure 3 for different  $[A, k]$  values where  $\gamma = 0$ . In practice,  $[A, k, \gamma]$  could be learnable parameters. Moreover, we could do this for a

series of trigonometric functions to get petals of different sizes. We could then choose some  $f(r) \propto \frac{1}{r}$  such that the gray fades from black to white. We would define  $f(r)$  piece wise such that it is 0 outside of the petal and decreases radially with  $r$  inside the petal.

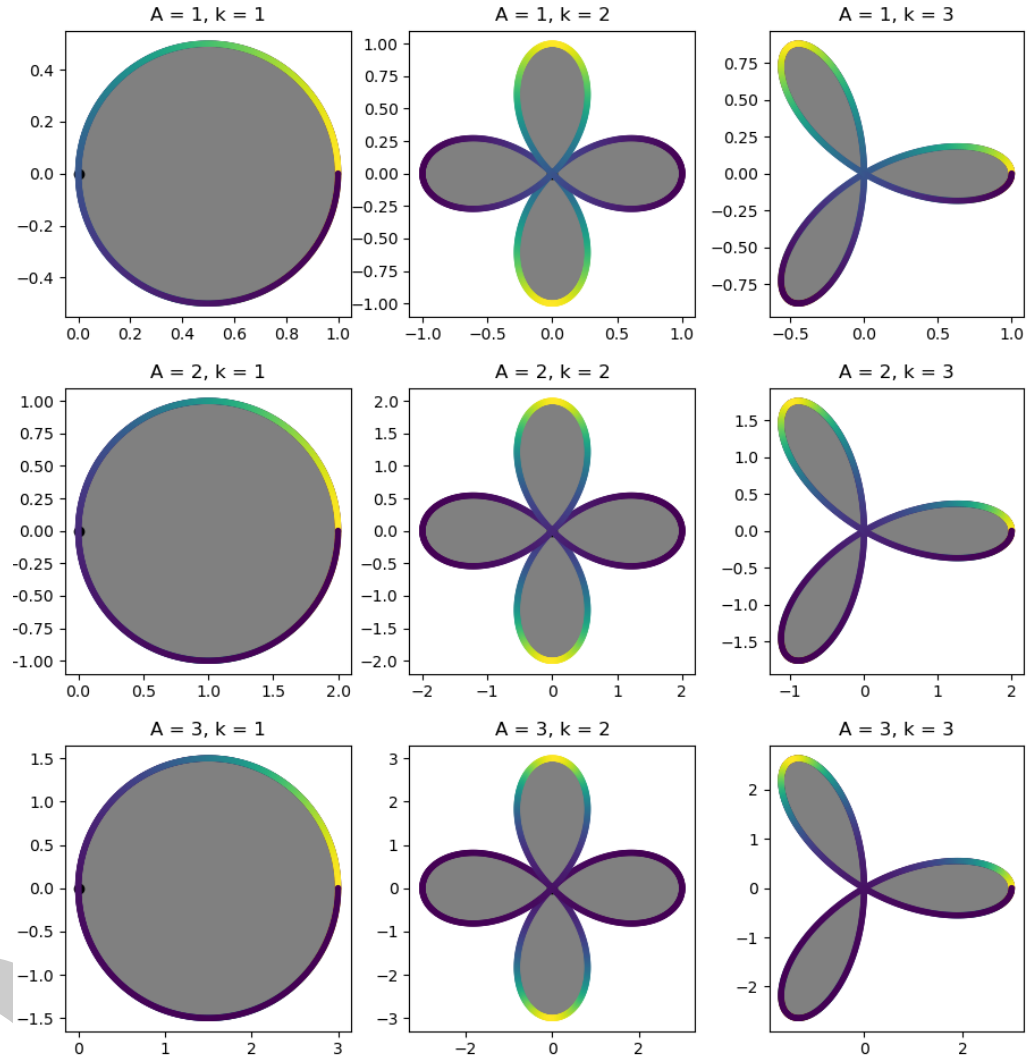


Figure 3: Petal Diagram

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