

Star-galaxy Classification Using Convolutional Neural Networks

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ABSTRACT

Most existing star-galaxy classifiers use the reduced summary information from catalogs, requiring careful feature extraction and selection. The latest advances in machine learning using deep convolutional neural networks allow a machine to automatically learn the features directly from data, minimizing need for input from human experts. We present a star-galaxy classification framework that uses a deep convolutional neural network (ConvNet) directly on the raw pixel values. Using data from the Sloan Digital Sky Survey (SDSS) and the Canada-France-Hawaii Telescope Lensing Survey (CFHTLenS), we demonstrate that ConvNet is able to produce accurate and well-calibrated probabilistic classifications that are competitive with conventional machine learning techniques. Future advances in deep learning may bring more success in currently ongoing and forthcoming photometric surveys, such as the Dark Energy Survey (DES) and the Large Synoptic Survey Telescope (LSST), because deep neural networks require very little feature engineering by hand.

Key words: methods: data analysis – methods: statistical – surveys – stars: statistics – galaxies: statistics.

1 INTRODUCTION

Currently ongoing and forthcoming large-scale photometric surveys, such as the Dark Energy Survey (DES) and the Large Synoptic Survey Telescope (LSST), aim to collect photometric data for hundreds of millions to billions of stars and galaxies. Due to the sheer volume of data, it is not possible for human experts to manually classify them, and the separation of photometric catalogs into stars and galaxies has to be automated. Furthermore, any classification approach must be probabilistic in nature. A fully probabilistic classifier enables a user to adopt probability cuts to obtain a pure sample for population studies, or to optimize the allocation of observing time by selecting objects for follow-up. However, ideally, the probability estimates themselves would be retained for all sources and used in subsequent analyses to improve or enhance a particular measurement (Ross et al. 2011; Seo et al. 2012).

With machine learning, we can use algorithms to automatically create accurate source catalogs with well-calibrated posterior probabilities. Machine learning techniques have been a popular tool in many areas of astronomy (Ball et al. 2007; Ball et al. 2008; Banerji et al. 2010; Carrasco Kind & Brunner 2013, 2014a,b; Ivezić et al. 2014; Kamdar et al. 2016a,b). Artificial neural networks were first applied to the problem of star-galaxy classification in the work of Odewahn et al. (1992), which has become a core part of the astronomical image processing software SExtractor (Bertin & Arnouts 1996). Other successfully implemented examples of applying machine learning to the star-galaxy classification problem

include decision trees (Weir et al. 1995; Suchkov et al. 2005; Ball et al. 2006; Sevilla-Noarbe & Etayo-Sotos 2015), Support Vector Machines (Fadely et al. 2012), and classifier combination strategies (Kim et al. 2015).

Almost all star-galaxy classifiers published in the literature use the reduced summary information available from astronomical catalogs. Constructing catalogs requires careful engineering and considerable domain expertise to transform the raw pixel values of an image to suitable features, such as magnitudes or shape information of an object. In a branch of machine learning called deep learning, features are not designed by human experts; they are learned from data by deep neural networks. Deep learning has been applied successfully to galaxy morphological classification in Sloan Digital Sky Survey (SDSS; Dieleman et al. 2015) and Cosmic Assembly Near-infrared Deep Extragalactic Legacy Survey (CANDELS; Huertas-Company et al. 2015) and to photometric redshift estimation (Hoyle 2015), but it has never been applied to the problem of source classification.

In this paper, we present a star-galaxy classification framework that uses a convolutional neural network (ConvNet) model directly on the images from SDSS and Canada-France-Hawaii Telescope Lensing Survey (CFHTLenS). We compare its performance with a standard machine learning technique that uses the reduced summary information from catalogs, and demonstrate that our ConvNet model is able to produce accurate and well-calibrated probabilistic classifications with very little feature engineering by hand. In Section 2, we describe the data sets used in this paper and the pre-processing steps for preparing the image data sets. We provide a brief overview of deep learning and ConvNets in Section 3, and

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discuss our strategy for preventing overfitting in Section 4. In Section 5, we describe a state-of-the-art tree-based machine learning algorithm, to which the performance of our ConvNet model is compared. We present the main results of our ConvNet model in Section 6, and we outline our conclusions in Section 7.

2 DATA

2.1 Sloan Digital Sky Survey

The Sloan Digital Sky Survey (SDSS; York et al. 2000) phases I–III obtained photometric data in five bands: u , g , r , i , and z , covering 14,555 square degrees, more than one-third of the entire sky. The resulting catalog contains photometry of over 300 million stars and galaxies with a limiting magnitude of $r \approx 22$, making the SDSS one of the largest sky surveys ever undertaken. The SDSS also conducted an expansive spectroscopic follow-up of more than three million stars and galaxies (Eisenstein et al. 2011). In this paper, we use a subset of the photometric and spectroscopic data contained within the Data Release 12 (DR12; Alam et al. 2015), which is publicly available through the online CasJobs server (Li & Thakar 2008)¹.

Using the CasJobs server, we randomly select 65,000 stars and galaxies. We exclude some bad photometric observations as follows. We consider only objects whose r band magnitude is less than 40; there are no warning flags in the spectroscopic measurement (`zWarning` = 0); the half-light radius in the r band is less than 30 arc seconds as measured by the exponential and de Vaucouleurs light profiles; the error on the spectroscopic redshift measurement is less than 0.1; and the spectroscopic redshift is less than 2.

To create training images, we obtain the image FITS files for SDSS fields containing these objects in five photometric bands: u , g , r , i , and z . We use the astrometry information in the FITS headers in the Montage² software to align each image to the reference (r -band) image. We then use SExtractor to find the pixel positions of the 65,000 objects we have selected, and to center each object in the cutout image. We also convert the flux values to inverse hyperbolic sine magnitudes (also known as luptitudes; Lupton et al. 1999). Finally, in order to account for the effect of galactic dust, galactic extinction corrections in magnitudes are applied following Schlegel et al. (1998). In the end, we have cutout images of size 48×48 pixels with luptitude values in each pixel. We note that we have experimented with increasing the pixel dimensions to 60×60 and 72×72 pixels, but do not find noticeable improvement in the performance of our model.

In the end, we have 17 344 stars and 47 656 galaxies available for the training and testing processes. We randomly split the objects into training, validation, and test sets of 40 000, 10 000, and 15 000, respectively. We note that we perform a blind test, and the test set is not used in any to train or calibrate the algorithms.

2.2 Canada-France-Hawaii Telescope Lensing Survey

We also use photometric data from the Canada-France-Hawaii Telescope Lensing Survey (CFHTLenS³; Heymans et al. 2012; Erben et al. 2013; Hildebrandt et al. 2012). This catalog consists of

more than twenty five million objects with a limiting magnitude of $i_{AB} \approx 25.5$. It covers a total of 154 square degrees in the four fields (named W1, W2, W3, and W4) of CFHT Legacy Survey (CFHTLS; Gwyn 2012) observed in the five photometric bands: u , g , r , i , and z .

We have cross-matched reliable spectroscopic galaxies from the Deep Extragalactic Evolutionary Probe Phase 2 (DEEP2; Davis et al. 2003; Newman et al. 2013), the Sloan Digital Sky Survey Data Release 10 (Alam et al. 2015, SDSS-DR10), the Visible imaging Multi-Object Spectrograph (VIMOS) Very Large Telescope (VLT) Deep Survey (VVDS; Le Fèvre et al. 2005; Garilli et al. 2008), and the VIMOS Public Extragalactic Redshift Survey (VIPERS; Garilli et al. 2014). We have selected only sources with very secure redshifts and no bad flags (quality flags -1, 3, and 4 for DEEP2; quality flag 0 for SDSS; quality flags 3, 4, 23, and 24 for VIPERS and VVDS).

We obtain FITS images for each 1 square degree CFHTLenS pointing that contains objects with spectroscopic labels. We create cutout images of size 96×96 pixels by using a similar method to that described in Section 2.1. Finally, images are downsampled to 48×48 pixels to reduce computational cost.

In the end, we have 8 545 stars and 57 843 galaxies available for the training and testing processes. We randomly split the objects into training, validation, and test sets of size 40 000, 10 000, and 13 278, respectively.

3 DEEP LEARNING

3.1 Neural Networks

A neuron in the human brain receives signals from other neurons through synaptic connections. If the combination of these signals exceeds a certain threshold, the neuron will fire and send a signal to other neurons. Intelligence is believed to be the collective effect of approximately 10^{11} neurons firing. An artificial neuron in most artificial neural networks is represented as a mathematical function that models a biological neural structure (Figure 1a). Let \mathbf{x} be a vector of inputs to a given neuron, \mathbf{w} be a vector of weights, and b be the bias. Then, the output of the neuron is

$$y = \sigma(\mathbf{w} \cdot \mathbf{x} + b), \quad (1)$$

where σ is the activation function (or *non-linearity*).

The sigmoid function, $\sigma(x) = 1 / (1 + e^{-x})$, has frequently been used as activation function, but it has recently fallen out of favor, and the hyperbolic tangent function, $\sigma(x) = \tanh(x)$ is almost always used instead. The most popular non-linearity at present, however, is the rectified linear unit (ReLU; Nair & Hinton 2010), $\sigma(x) = \max(0, x)$, ReLUs generally allow much faster training of deep neural networks with many layers. However, ReLU units can sometimes result in dead neurons whose output is always zero. To mitigate this problem, we use leaky ReLUs that have a small negative slope in the negative region,

$$\sigma(x) = \begin{cases} x & \text{if } x \geq 0 \\ 0.01x & \text{if } x < 0. \end{cases} \quad (2)$$

Many deep learning models use feedforward neural network architectures with multiple layers, where each neuron in one layer is connected to the neurons of the subsequent layer. A schematic representation is shown in Figure 1b. All layers except the input and output layers are conveniently called hidden layers. With multiple hidden layers, deep neural networks can model complex non-linear relationships, and they have had great success in multimedia

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³ <http://www.cfhtlens.org/>



Figure 1. (a) A mathematical model of a biological neuron. (b) A schematic diagram of a neural network with one hidden layer of two neurons and one output layer with two neurons.

tasks where humans traditionally outperformed computers: speech recognition, language processing, and image classification.

The goal of learning is to find a set of weights and biases such that the output from the network $\mathbf{y} = \{y_1, y_2, \dots, y_n\}$ approximates the desired output $\hat{\mathbf{y}} = \{\hat{y}_1, \hat{y}_2, \dots, \hat{y}_n\}$ as closely as possible for all input \mathbf{x} . We can formulate this as the minimization of a loss function $L(\mathbf{x}, \hat{\mathbf{y}})$ over the training data. In this work, we use *cross-entropy*,

$$L(y, \hat{y}) = -\hat{y} \log_2 y - (1 - \hat{y}) \log_2 (1 - y), \quad (3)$$

where \hat{y} is the actual truth value (e.g., 0 or 1) and y is the probability prediction made by the model. We compute the loss function by taking the average of all cross-entropies in the sample. Given N samples, the loss function becomes

$$L(y, \hat{y}) = -\frac{1}{N} \sum_{i=1}^N \hat{y}_i \log_2 y_i + (1 - \hat{y}_i) \log_2 (1 - \hat{y}_i). \quad (4)$$

where \hat{y}_i is the truth value and probability estimate of the i -th data, respectively.

To find the weights \mathbf{w} and biases \mathbf{b} which minimize the loss, we use a technique called *gradient descent*, where we use the following rules to update the parameters in each layer j :

$$\mathbf{w}_j \rightarrow \mathbf{w}'_j = \mathbf{w}_j - \eta \frac{\partial L}{\partial \mathbf{w}_j} \quad (5)$$

$$\mathbf{b}_j \rightarrow \mathbf{b}'_j = \mathbf{b}_j - \eta \frac{\partial L}{\partial \mathbf{b}_j}, \quad (6)$$

where η is a small, positive number known as the *learning rate*. A common approach to speed up training is to split the training data into mini-batches and compute the gradients in Equation 6 for each mini-batch separately instead of the entire training data. This results in much faster convergence, as training examples are usually correlated and the gradient computed from a randomly chosen mini-batch is a good approximation of the overall gradient. We define an *epoch* as a single, complete pass through the training data, and full training usually requires many epochs. At the end of each epoch, we evaluate the loss function on the validation set, and the model that minimizes the loss is chosen as the best model.

3.2 Convolutional Neural Networks

The Convolutional neural network (ConvNet; Fukushima 1980; LeCun et al. 1998) is a type of deep, feedforward neural network that has recently become the dominant approach in the computer vision

community. In a typical ConvNet, the first few stages are composed of two types of layers: convolutional layers and pooling layers.

The input to a convolutional layer is an image with a certain number of color channels or *feature maps*. To produce output feature maps, we convolve each feature map with a set of weights called *filters*, and apply a non-linearity such as ReLU to the weighted sum of these convolutions. Different feature maps use different sets of filters, but all neurons in a feature map share the same set of filters. Mathematically, we replace the dot product in Equation 1 with a sum of convolutions. The k -th feature map is given by

$$\mathbf{y}^k = \sigma \left(\sum_j \mathbf{w}_j^k * \mathbf{x}_j + b^k \right), \quad (7)$$

where we sum over the set of filters, $*$ is the convolution operator, and \mathbf{w}_j^k represent the filters.

A typical pooling layer computes the maximum of a local 2×2 patch in a feature map. Since the pooling layer aggregates the activations of neighboring units from the previous layer, it reduces the dimensionality of the feature maps and makes the model invariant to small shifts and distortions. Two or more layers of convolution and pooling are stacked, followed by more convolutional and fully-connected layers.

3.3 Neural Network Architecture

We present the overall architecture of our ConvNet model in Table 1. The network consists of eleven trainable layers. The first convolutional layer filters the $5 \times 44 \times 44$ input image (i.e., 44×44 images in five bands *ugriz*) with 32 square filters of size $5 \times 5 \times 5$. The leaky ReLU non-linearity is applied to the output of the first convolutional layer (and all subsequent layers), and the second convolutional layer filters it with 32 filters of $32 \times 3 \times 3$. In the second convolutional layer (and all subsequent convolutional layers), we pad the input with zeros spatially on the border (i.e., the zero-padding is 1 pixel for 3×3 convolutional layers) such that the spatial resolution is preserved after convolution. Max-pooling with filters of size 2×2 follows the second convolutional layer. A stack of six additional convolutional layers, all with filters of size 3×3 , is followed by three fully-connected layers. The first two fully-connected layers have 2048 channels each, and the third performs binary classification.

Table 1. Summary of hyperparameters. Note that pooling layers have no learnable parameters.

type	filters	filter size	padding	non-linearity	initial weights	initial biases
convolutional	32	5×5	-	leaky ReLU	orthogonal	0.1
convolutional	32	3×3	1	leaky ReLU	orthogonal	0.1
pooling	-	2×2	-	-	-	-
convolutional	64	3×3	1	leaky ReLU	orthogonal	0.1
convolutional	64	3×3	1	leaky ReLU	orthogonal	0.1
convolutional	64	3×3	1	leaky ReLU	orthogonal	0.1
pooling	-	2×2	-	-	-	-
convolutional	128	3×3	1	leaky ReLU	orthogonal	0.1
convolutional	128	3×3	1	leaky ReLU	orthogonal	0.1
convolutional	128	3×3	1	leaky ReLU	orthogonal	0.1
pooling	-	2×2	-	-	-	-
fully-connected	2048	-	-	leaky ReLU	orthogonal	0.01
fully-connected	2048	-	-	leaky ReLU	orthogonal	0.01
fully-connected	2	-	-	softmax	orthogonal	0.01

The output of the final fully-connected layer is fed to a softmax function. The softmax function is given by

$$P(y_i | \mathbf{x}) = \frac{e^{\mathbf{x} \cdot \mathbf{w}_{y_i}}}{\sum_k e^{\mathbf{x} \cdot \mathbf{w}_k}}, \quad (8)$$

where we interpret its output as the posterior probability that an object is a galaxy (or a star). We note that we could also try to solve a regression problem, e.g., by normalizing the output values that the network produces for each class. However, we find that solving a regression problem instead of using the softmax function results in significantly worse performance.

In addition to hyperparameter optimization, we have explored more than 100 different architectures and have found that the architecture described in this section provides the best performance on the validation data. For example, the architecture of [Krizhevsky et al. \(2012\)](#) uses relatively large receptive fields (11×11) in the first convolutional layers. [Zeiler & Fergus \(2014\)](#) and [Dieleman et al. \(2015\)](#) also use large receptive fields of 7×7 and 6×6 in the first convolution layer, respectively. However, we find that using a receptive field larger than 5×5 in the first convolutional layer leads to worse performance. This result is in agreement with [Simonyan & Zisserman \(2014\)](#), which features an extremely homogeneous architecture that only performs 3×3 convolutions. Using a large receptive field instead of a stack of multiple 3×3 convolutions leads to a shallower network, and it is often preferable to increase the depth by using smaller receptive fields. However, we find that replacing the first layer with a stack of two 3×3 convolutional layers increases the validation error, but we still follow [Simonyan & Zisserman \(2014\)](#) and add many 3×3 convolutions (with zero-padding) in the remaining layers.

3.4 Training

The choice of momentum, learning rate, and initial weights is crucial for achieving high predictive performance and speeding up the learning process ([Sutskever et al. 2013](#)). To train our models, we use mini-batch gradient descent with a batch size of 128 and Nesterov momentum ([Bengio et al. 2013](#)) of 0.9. We initialize the learning rate η at 0.003 for all layers and decrease it linearly with the number of epochs from 0.003 to 0.0001 over 750 epochs. We also initialize the weights in each layer with random orthogonal initial conditions ([Saxe et al. 2013](#)). We use a slightly positive value $b = 0.1$ for all biases. We find initializing biases to a small constant

value helps eliminate dead neurons by ensuring that all ReLU neurons fire in the beginning. We note that our network takes about 40 hours to train the networks on a NVIDIA Tesla K40 GPU.

4 REDUCING OVERFITTING

Our convolution neural network has 11×10^6 learnable parameters, while there are only 5×10^4 images in the training set. As a result, the model is very likely to *overfit* without regularization. In this section, we describe the techniques used to combat overfitting.

4.1 Data Augmentation

One common method to combat overfitting is to artificially increase the number of training data by using label-preserving transformations. Each image is transformed as follows:

- **Rotation:** Rotating an image does not change whether the object is a star or a galaxy. We exploit this rotational symmetry and randomly rotate each image by a multiple of 90° .
- **Reflection:** We flip each image horizontally with a probability of 0.5 to exploit mirror symmetry.
- **Translation:** We also have translational symmetry in the images. Given an image of size 48×48 pixels, we extract a random contiguous crop of size 44×44 . Each cropping is equivalent to randomly shifting a 44×44 image by up to 4 pixels vertically and horizontally.
- **Gaussian noise:** We introduce random Gaussian noise to each pixel values by using a similar method to [Krizhevsky et al. \(2012\)](#).

These data augmentation schemes add almost no computational cost, as they are performed on the CPU while the GPU is training the ConvNets on images.

4.2 Dropout

We use a regularization technique called dropout ([Hinton et al. 2012](#)) in the fully-connected layers. Dropout consists of randomly setting to zero the output of each hidden neuron of the previous layer with probability 0.5. The weights of the remaining neurons are multiplied by 0.5 to preserve the scale of input values to the next layer. Since a neuron can be removed at any time, it cannot

rely on the presence of other neurons in the same layer and is forced to learn more robust features.

4.3 Model Combination

To make final classifications, we use our ConvNet model to make 64 sets of predictions for 64 transformations of the input images: 4 rotations, 4 horizontal translations, and 4 vertical translations (with random horizontal reflections). Although we use an identical network architecture for all transformations, we consider each set of predictions as separate results from different models. Finally, we use a model combination technique known as Bayesian Model Combination (BMC; Monteith et al. 2011), which uses Bayesian principles to generate an ensemble combination of different models. Although the data augmentation step 4.1 should make our ConvNet model invariant to these types of transformations, we find that applying BMC still results in a significant decrease in validation error.

The posterior probability that a source is a star is given by

$$P(S|x, \mathbf{D}, \mathbf{M}, \mathbf{E}) = \sum_{e \in E} P(S|x, \mathbf{M}, e) P(e|\mathbf{D}), \quad (9)$$

where \mathbf{D} is the data set, and e is an element in the ensemble space E of possible model combinations. By Bayes' Theorem, the posterior probability of e given \mathbf{D} is given by

$$P(e|\mathbf{D}) = \frac{P(e)}{P(\mathbf{D})} \prod_{d \in \mathbf{D}} P(d|e) \propto P(e) \prod_{d \in \mathbf{D}} P(d|e). \quad (10)$$

Here, $P(e)$ is the prior probability of e , which we assume to be uniform. The product of $P(d|e)$ is over all individual data d in the training data \mathbf{D} , and $P(\mathbf{D})$ is merely a normalization factor and not important. For probabilistic classifiers, we can directly use the probabilistic predictions and write Equation 10 as

$$P(e|\mathbf{D}) \propto P(e) \prod_{i=0}^{N-1} \hat{y}_i y_i + (1 - \hat{y}_i)(1 - y_i). \quad (11)$$

Although the space E of potential model combinations is in principle infinite, we can produce a reasonable finite set of potential model combinations by using sampling techniques. In our implementation, the weights of each combination of the base classifiers is obtained by sampling from a Dirichlet distribution. We first set all alpha values of a Dirichlet distribution to unity. We then sample this distribution q times to obtain q sets of weights. For each combination, we assume a uniform prior and calculate $P(e|\mathbf{D})$ using Equation 11. We select the combination with the highest $P(e|\mathbf{D})$, and update the alpha values by adding the weights of the most probable combination to the current alpha values. The next q sets of weights are drawn using the updated alpha values.

We continue the sampling process until we reach a predefined number of combinations, and finally use Equation 9 to compute the posterior probability that a source is a star (or a galaxy). In this paper, we use a q value of three, and 1,000 model combinations are considered.

5 TREES FOR PROBABILISTIC CLASSIFICATIONS

To compare the performance of ConvNets with machine learning algorithms that use standard photometric features, we use a machine learning framework called Trees for Probabilistic Classifications (TPC). Although a complete description of TPC is beyond the

scope of this paper, we provide a brief description in this section. For more details, we refer the reader to Carrasco Kind & Brunner (2013) and Kim et al. (2015).

TPC is a parallel, supervised machine learning algorithm that uses prediction trees and random forest techniques (Breiman et al. 1984; Breiman 2001) to produce a star-galaxy classification. TPC is a part of a publicly available software package called MLZ⁴ (Machine Learning for Photo-z).

TPC uses classification trees, a type of prediction trees that are designed to provide a classification or predict a discrete category. Prediction trees are built by asking a sequence of questions that recursively split the data into branches until a terminal leaf is created that meets a stopping criterion (e.g., a minimum leaf size). The optimal split dimension is decided by choosing the attribute that maximizes the *Information Gain* (I_G), which is defined as

$$I_G(D_{\text{node}}, X) = I_d(D_{\text{node}}) - \sum_{x \in \text{values}(X)} \frac{|D_{\text{node},x}|}{|D_{\text{node}}|} I_d(D_{\text{node},x}), \quad (12)$$

where D_{node} is the training data in a given node, X is one of the possible dimensions (e.g., magnitudes or colors) along which the node is split, and x are the possible values of a specific dimension X . $|D_{\text{node}}|$ and $|D_{\text{node},x}|$ are the size of the total training data and the number of objects in a given subset x within the current node, respectively. I_d is the impurity degree index, and TPC can calculate I_d from any of the three standard different impurity indices: *information entropy*, *Gini impurity*, and *classification error*. In this work, we use the information entropy, which is defined similarly to the thermodynamic entropy:

$$I_d(D) = -f_g \log_2 f_g - (1 - f_g) \log_2 (1 - f_g), \quad (13)$$

where f_g is the fraction of galaxies in the training data. At each node in our tree, we scan all dimensions to identify the split point that maximizes the information gain as defined by Equation 12, and select the attribute that maximizes the impurity index overall.

In a technique called random forest, we create bootstrap samples (i.e., N randomly selected objects with replacement) from the input training data by sampling repeatedly from the magnitudes and colors using their measurement errors. We use these bootstrap samples to construct multiple, uncorrelated prediction trees whose individual predictions are aggregated to produce a star-galaxy classification for each source.

We train two TPC models on the SDSS data set using different sets of attributes. The first model, which we denote TPC_{phot}, is trained with only nine photometric attributes: the extinction-corrected model magnitudes in five bands (u , g , r , i , z) and their corresponding colors ($u - g$, $g - r$, $r - i$, $i - z$). The second model, which we denote TPC_{morph}, is trained with the concentration parameter in each band in addition to the magnitudes and colors, for a total of fifteen dimensions. The concentration is defined as the difference between the cmodel and PSF magnitude, i.e., $\text{concentration} \equiv \text{psfMag} - \text{cModelMag}$. The SDSS pipeline uses a parametric method based on the concentration, i.e., an object is classified as a galaxy if $\text{concentration} > 0.145$. We find that the concentration is an excellent morphological feature for star-galaxy separation, and including more morphological features does not show noticeable improvement in performance. The concentration is a good example of carefully handcrafted feature extraction, and

⁴ <http://lcdm.astro.illinois.edu/code/mlz.html>

we show in Section 6 that ConvNets do not require such feature engineering.

We also train two models on the CFHTLenS data set. TPC_{phot} is trained with the five magnitudes and their corresponding colors, $u, g, r, i, z, u-g, g-r, r-i$, and $i-z$. Since the CFHTLenS catalog does not provide the concentration parameter, $\text{TPC}_{\text{morph}}$ uses SExtractor's FLUX_RADIUS (the half-light radius), A_WORLD (the semi-major axis), B_WORLD (the semi-minor axis) for morphological features, in addition to the five magnitudes and their corresponding colors, for a total of twelve dimensions.

6 RESULTS AND DISCUSSION

In this section, we present the classification performance of our ConvNet model and compare it with the performance of TPC.

6.1 Classification Metrics

Probabilistic classification models can be considered as functions that output a probability estimate of each source to be in one of the classes (e.g., a star or a galaxy). The simplest way to use the probability output is to convert it into a class label by using a threshold (a probability cut). Although many studies often choose the threshold by setting it to a fixed value, e.g., $p_{\text{cut}} = 0.5$ (e.g., Henrion et al. 2011; Fadely et al. 2012), choosing 0.5 as a threshold is not the best choice for an unbalanced data set, where galaxies outnumber stars. Furthermore, setting a fixed threshold ignores the operating condition (e.g., science requirements, stellar distribution, misclassification costs) where the model will be applied.

6.1.1 Receiver Operating Characteristic Curve

When we have no information about the operating condition when evaluating the performance of classifiers, there are effective tools such as the Receiver Operating Characteristic (ROC) curve (Swets, Dawes & Monahan 2000). An ROC curve is a graphical plot that illustrates the true positive rate versus the false positive rate of a binary classifier as its classification threshold is varied. The Area Under the Curve (AUC) summarizes the curve information in a single number, and can be used as an assessment of the overall performance.

6.1.2 Completeness and Purity

In astronomical applications, the operating condition usually translates to the completeness and purity requirements of the star or galaxy sample. We define the galaxy *completeness* c_g (also known as recall or sensitivity) as the fraction of the number of true galaxies classified as galaxies out of the total number of true galaxies,

$$c_g = \frac{N_g}{N_g + M_g}, \quad (14)$$

where N_g is the number of true galaxies classified as galaxies, and M_g is the number of true galaxies classified as stars. We define the galaxy *purity* p_g (also known as precision or positive predictive value) as the fraction of the number of true galaxies classified as galaxies out of the total number of objects classified as galaxies,

$$p_g = \frac{N_g}{N_g + M_s}, \quad (15)$$

where M_s is the number of true stars classified as galaxies. Star completeness and purity are defined in a similar manner.

One of the advantages of a probabilistic classification is that the threshold can be adjusted to produce a more complete but less pure sample, or a less complete but more pure one. We can compare the performance of different classification techniques by assuming an arbitrary operating condition. For example, weak lensing science measurements of the DES require $c_g > 0.960$ and $p_g > 0.778$ to control both the statistical and systematic errors on the cosmological parameters, and $c_s > 0.250$ and $p_s > 0.970$ for stellar Point Spread Function (PSF) calibration (Soumagnac et al. 2015). Although these values will likely be different for the science cases of the CFHTLenS data, we adopt these values to compare the classification performance at a reasonable operating condition. Thus, we compute p_g at $c_g = 0.960$ and c_s at $p_s = 0.250$.

6.1.3 Mean Squared Error

We also use the mean squared error (MSE; also known as Brier score (Brier 1950)) as a performance metric. We define MSE as

$$\text{MSE} = \frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2, \quad (16)$$

The MSE can be considered as both a score function that quantifies how well a set of probabilistic predictions are calibrated, or a loss function.

6.1.4 Calibration Error

A fully probabilistic classifier predicts not only the class label, but also its confidence level on the prediction. In a well-calibrated classifier, the posterior class probability estimates should coincide with the proportion of objects that truly belong to a certain class. Probability *calibration curves* (or reliability curves; DeGroot & Fienberg 1983) are often used to display this relationship, where we bin the probability estimates and plot the fraction of positive examples versus the predicted probability in each bin (see Figures 5 and fig:xxx).

The problem with binning approach is either too few or too many bins can distort the evaluation of calibration performance. Thus, we adopt a calibration measure based on overlapping binning (Caruana & Niculescu-Mizil 2004). We order the predicted values P_{class} and put the first 1000 elements in the first bin. We calculate the true probability P_{gal} by counting the true galaxies in this bin. The calibration error for this bin is $|P_{\text{gal}} - P_{\text{class}}|$. We then repeat this for the second bin (2 to 1001), the third bin (3 to 1002), and so on, and average the binned calibration errors. Thus, the overall calibration error is given by

$$\text{CAL} = \frac{1}{N-s} \sum_{b=1}^{N-s} \sum_{i=b}^{b+s-1} \left| P_{\text{class},i} - \frac{\sum_{i=b}^{b+s-1} P_{\text{gal},i}}{s} \right| \quad (17)$$

where $s = 1000$ is the bin length.

6.1.5 Number of galaxies

Ideally, the probabilistic output of a classifier would be used in subsequent scientific analyses. For example, one can weight each object by the probability that it is a galaxy when measuring auto-correlation functions of luminous galaxies (Ross et al. 2011). In other words, given a well-calibrated classifier, instead of counting

Table 2. The definition of the classification performance metrics.

Metric	Meaning
AUC	Area under the Receiver Operating Curve
MSE	Mean squared error
c_g	Galaxy completeness
p_g	Galaxy purity
c_s	Star completeness
p_s	Star purity
$p_g(c_g = x)$	Galaxy purity at x galaxy completeness
$p_s(c_s = x)$	Star purity at x star completeness
CAL	Calibration error with overlapping binning
$ \Delta N_g /N_g$	Absolute error in number of galaxies

each galaxy equally, a galaxy could be counted as P_{class} , the probability estimate. This should, in principle, remove the contamination effect of stars. For a perfect classifier, we can count the number of galaxies by summing the values of P_{class} . Thus, we measure the reliability of the classifier output by the absolute error in the estimation of number of galaxies,

$$\frac{|\Delta N_g|}{N_g} = \frac{|N_g - \sum_{i=1}^N P_{\text{class}}|}{N_g} \quad (18)$$

6.2 CFHTLenS

We present in Table 3 a summary of the results obtained by applying ConvNet and TPC on the CFHTLenS data set. The bold entries highlight the best technique for any particular metric. ConvNet outperforms TPC_{morph} in four metrics (AUC, p_g , CAL, and $|\Delta N_g|/N_g$), while TPC_{morph} performs better in two metrics (MSE and c_g). It is not surprising that TPC_{phot} performs significantly worse than both ConvNet and TPC_{phot}, as morphology is critical in separating stars from galaxies. This suggests that ConvNet is able to learn the morphological features automatically from the images.

In Figure 2, we compare the galaxy completeness and star purity values for ConvNet and TPC as functions of i -band magnitude for the differential counts. We use the kernel density estimation (KDE Silverman 1986) with the Gaussian kernel. As the first panel shows, KDE is able to smooth the fluctuations in the distribution without binning. While ConvNet shows a slightly better performance than TPC_{morph} in galaxy purity, the star completeness plots for ConvNet and TPC are nearly identical. Again, TPC_{phot} performs significantly worse than both ConvNet and TPC, and this suggests that ConvNets are able to learn the shape information automatically from the images. We note that, at these operating conditions ($c_g = 0.96$, $p_s = 0.97$), both ConvNet and TPC_{morph} outperform the star-galaxy classification provided by the CFHTLenS pipeline Hildebrandt et al. (2012) across all magnitudes. We do not show the CFHTLenS classifications to avoid cluttering the plots.

In Figure 3, we show the overall galaxy purity and star completeness values as functions of magnitude for the integrated counts. ConvNet is able to maintain a galaxy purity of 0.9972 up to $i \sim 24.5$, while the galaxy purity of TPC_{morph} drops to 0.9963. However, TPC_{morph} performs better than ConvNet in terms of star completeness, maintaining a purity of 0.9252 up to $i \sim 24.5$, while ConvNet drops to 0.8966.

We also show the galaxy purity and star completeness values as functions of $g - r$ color in Figure 4. TPC_{morph} provides slightly better completeness and purity than ConvNet between

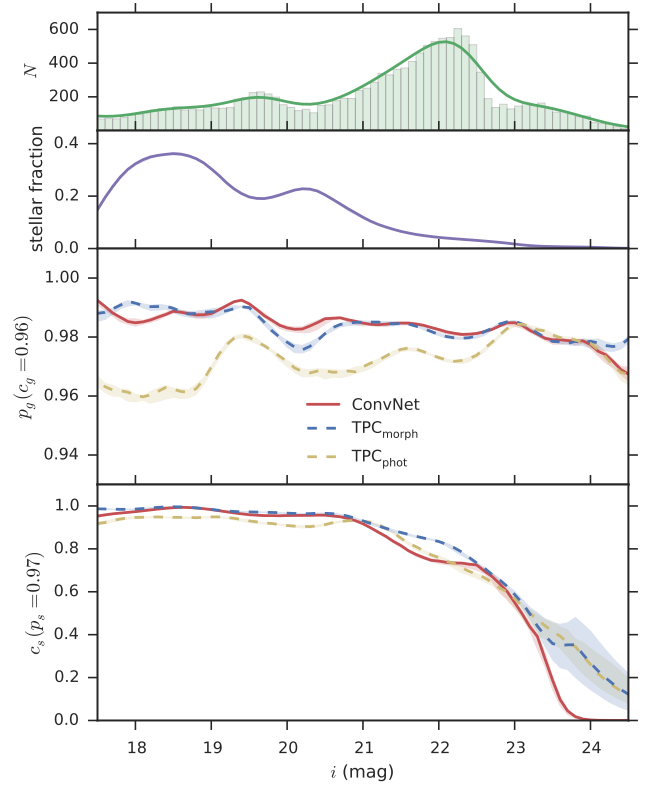


Figure 2. Galaxy completeness and star purity values as a function of the i -band magnitude as estimated by the kernel density estimation (KDE) method for the differential counts. The top panel shows the histogram with a bin size of 0.1 mag and the KDE for objects in the test set. The second panel shows the fraction of stars estimated by KDE as a function of magnitude. The bottom two panels compare the galaxy purity and star completeness values for ConvNet (red solid line), TPC_{morph} (blue dashed line), and TPC_{phot} (yellow dashed line) as functions of magnitude. The 1σ confidence bands are estimated by bootstrap sampling.

$0.8 \lesssim g - r \lesssim 1.6$ while ConvNet outperforms TPC_{morph} or is similar to TPC_{morph} in the remaining regions.

Figure 5 shows the calibration curve that compares P_{gal} , the fraction of objects that are galaxies (as determined from their spectra) to P_{conv} the probabilistic output that our ConvNet model produces. The calibration curve is nearly diagonal, which implies that ConvNet is well-calibrated and we can treat P_{conv} as the probability that an object is a galaxy. Figure 6 shows the calibration curve for the probabilistic output of TPC, which is apparently not as well-calibrated as ConvNet. These calibration curves visually confirm the results in Table 3 that the calibration error of ConvNet is about 20% lower than that of TPC. While probabilistic predictions can be further calibrated by using, e.g., isotonic calibration (Zadrozny & Elkan 2001), we do not consider additional probability calibration in this work.

It is informative to visualize how an input image activates the neurons in the convolutional layers. Figures 7 and 8 show the activations of the network when images of a galaxy and a star are fed into the network. The size of feature maps decreases with depth, and layers near the input layer have fewer filters while the later layers have more. The low-level features

When highly optimized features (e.g., the concentration of SDSS) are not readily available from the catalog, a ConvNet model becomes more attractive.

Table 3. A summary of the classification performance metrics as applied to the CFHTLenS data. The definition of the metrics is summarized in Table 2. The bold entries highlight the best performance values within each column.

classifier	AUC	MSE	$p_g(c_g = 0.96)$	$c_s(p_s = 0.97)$	CAL	$ \Delta N_g /N_g$
ConvNet	0.9948	0.0112	0.9972	0.8971	0.0197	0.0029
TPC _{morph}	0.9924	0.0109	0.9963	0.9268	0.0245	0.0056
TPC _{phot}	0.9876	0.0189	0.9927	0.8044	0.0266	0.0101

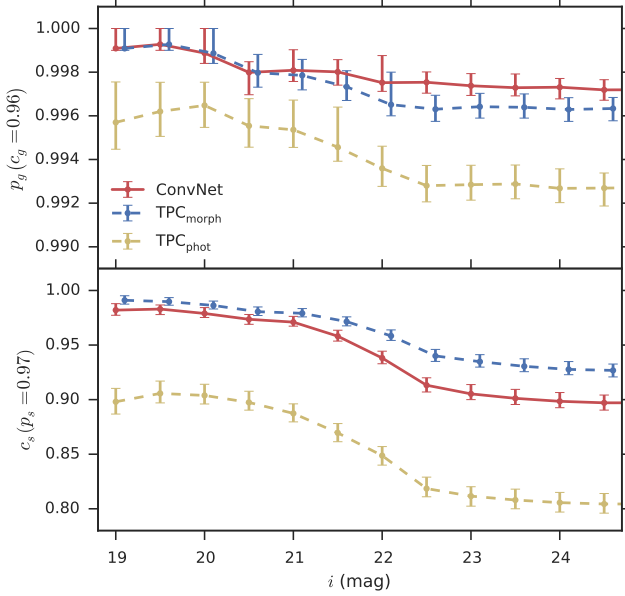


Figure 3. Galaxy purity and star completeness as functions of the i -band magnitude for the integrated counts. The upper panel compares the galaxy purity values for ConvNet (red solid line), TPC_{morph} (blue dashed line), and TPC_{phot} (yellow dashed line). The lower panel compares the star completeness. The 1σ error bars are computed following the method of Paterno (2003) to avoid the unphysical errors of binomial or Poisson statistics.

6.3 SDSS

We have also trained and tested our ConvNet model on the SDSS data set, and we present in Table 4 the same six metrics for ConvNet, TPC_{morph}, and TPC_{phot}. The bold entries highlight the best technique for any particular metrics. In contrast with the CFHTLenS data set in the previous section, it is apparent that TPC_{morph} outperforms ConvNet in all metrics except the CAL. Both ConvNet and TPC_{morph} still outperform TPC_{phot} in all six metrics by a significant amount.

In Figure 9, we compare the galaxy completeness and star purity values for ConvNet and TPC as functions of i -band magnitude for the differential counts. We note that TPC_{morph} outperforms the star-galaxy classifier used by the SDSS pipeline (i.e., an object is classified as a galaxy if the concentration parameter is greater than 0.145) across all magnitudes. We do not show the SDSS classifications to avoid cluttering the plots. While ConvNet shows a similar but slightly worse performance than TPC_{morph}, the galaxy purity and star completeness values of ConvNet begin to drop at faint magnitudes $i \lesssim 21$. Again, TPC_{phot} performs significantly worse than both ConvNet and TPC at bright magnitudes. One reason that ConvNet fails to outperform TPC_{phot}, especially at faint magnitudes, might be its over-reliance on morphological features. Near a survey's limit, the measurement uncertainties gen-

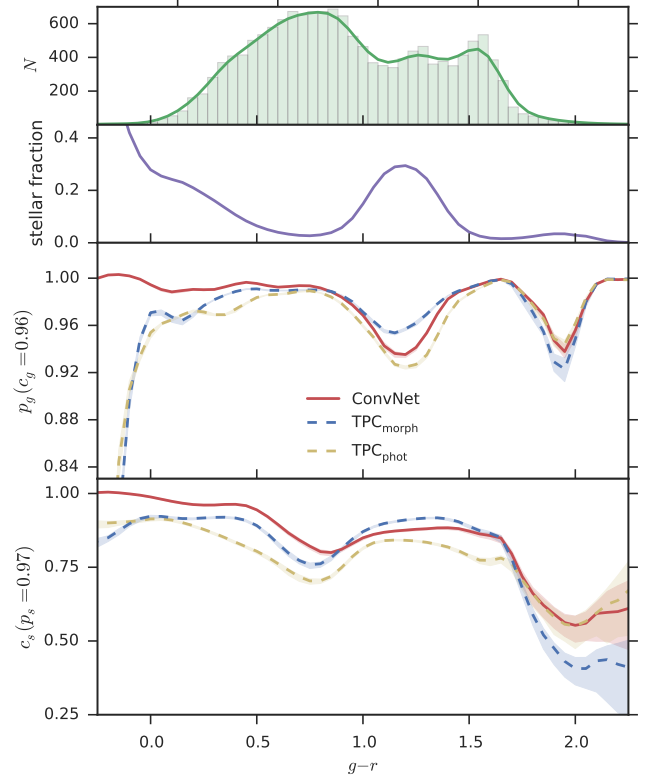


Figure 4. Similar to Figure 2 but as a function of $g-r$ color. The bin size of histogram in the top panel is 0.05.

erally increase, and morphology is not a reliable metric for star-galaxy classification.

In Figure 10, we show the overall galaxy purity and star completeness values as functions of magnitude for the integrated counts. ConvNet is able to maintain a galaxy purity of 0.9915 up to $i \sim 22.5$, while TPC_{morph} provides a galaxy purity of 0.9977. TPC_{morph} also outperforms ConvNet in terms of star completeness, maintaining a purity of 0.9810 up to $i \sim 22.5$, while the star completeness of ConvNet drops to 0.9500.

We also show the galaxy purity and star completeness values as functions of $g-r$ color in Figure 11. TPC_{morph} provides slightly better completeness and purity than ConvNet between $0.8 \lesssim g-r \lesssim 1.6$ while ConvNet outperforms TPC_{morph} or is similar to TPC_{morph} in the remaining regions.

Figure 12 shows the calibration curve that compares P_{gal} , the fraction of objects that are galaxies (as determined from their spectra) to P_{conv} the probabilistic output that our ConvNet model produces. The calibration curve is nearly diagonal, which implies that ConvNet is well-calibrated and we can treat P_{conv} as the probability that an object is a galaxy. Figure 13 shows the calibration curve for the probabilistic output of TPC, which is apparently not as well-

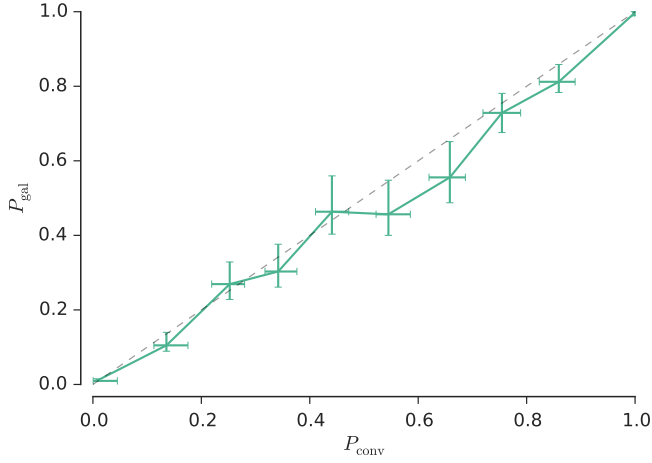


Figure 5. Calibration curve for ConvNet as applied to the CFHTLenS data set. p_{gal} is the fraction of objects that are galaxies. p_{conv} is the probabilistic output generated by ConvNet. The dashed line displays the relationship $p_{\text{gal}} = p_{\text{conv}}$. The 1σ error bars are computed following the method of [Paterno \(2003\)](#).

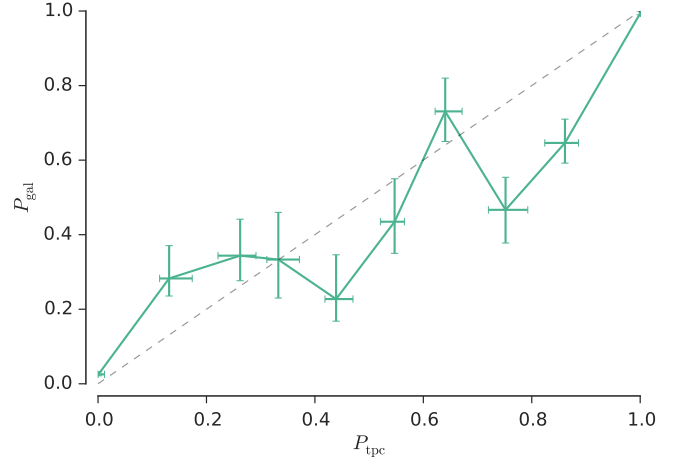


Figure 6. Calibration curve for TPC as applied to the CFHTLenS data set.

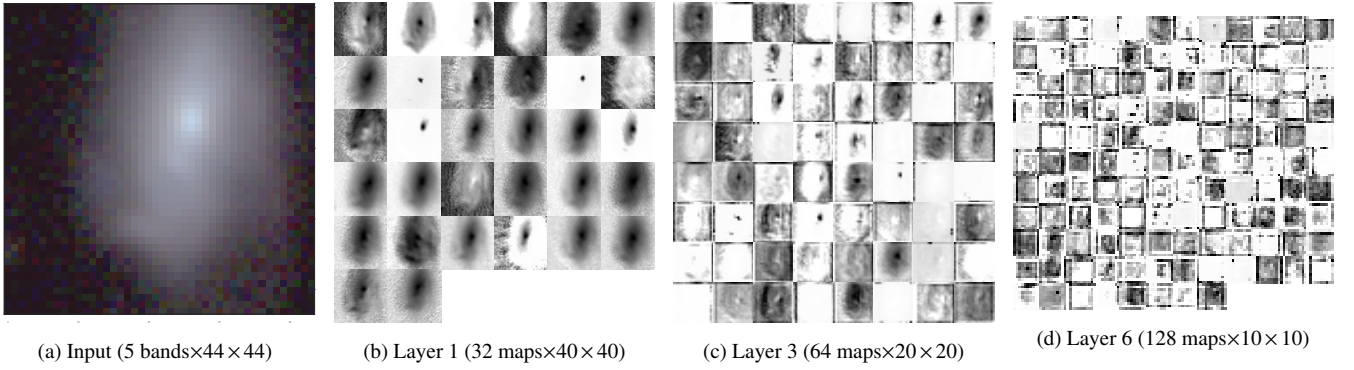


Figure 7. (a) A sample 44×44 RGB image of a CFHTLenS galaxy. The RGB image is created by mapping $R \rightarrow g$ band magnitude, $G \rightarrow r$ band magnitude, and $B \rightarrow i$ band magnitude. (b) Activations on the first convolutional layer when a $5 \times 44 \times 44$ image is fed into the network. (c) Activations on the third convolutional layer. (d) Activations on the sixth convolutional layer. Each image in (a), (b), and (c) is a feature map corresponding to the output for one of the learned features.

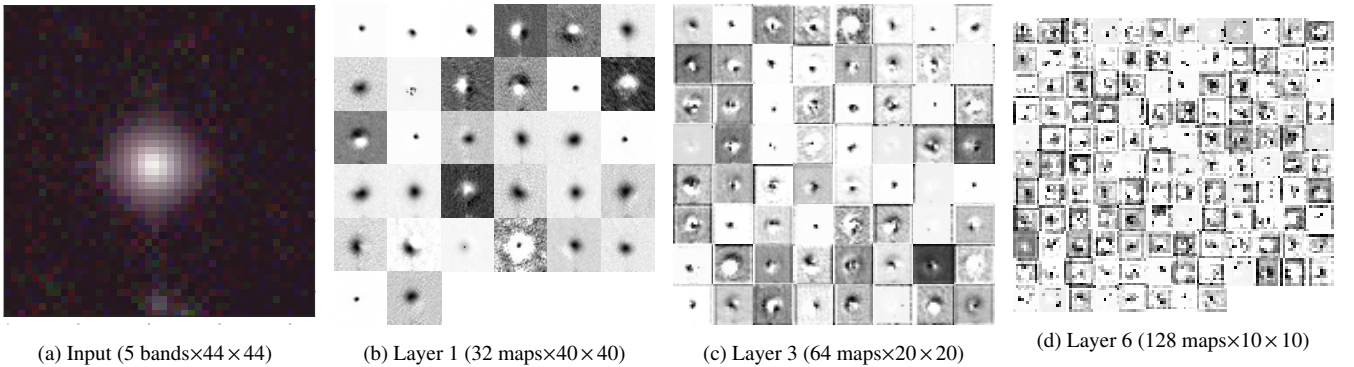


Figure 8. Same as Figure 7 but for a CFHTLenS star.

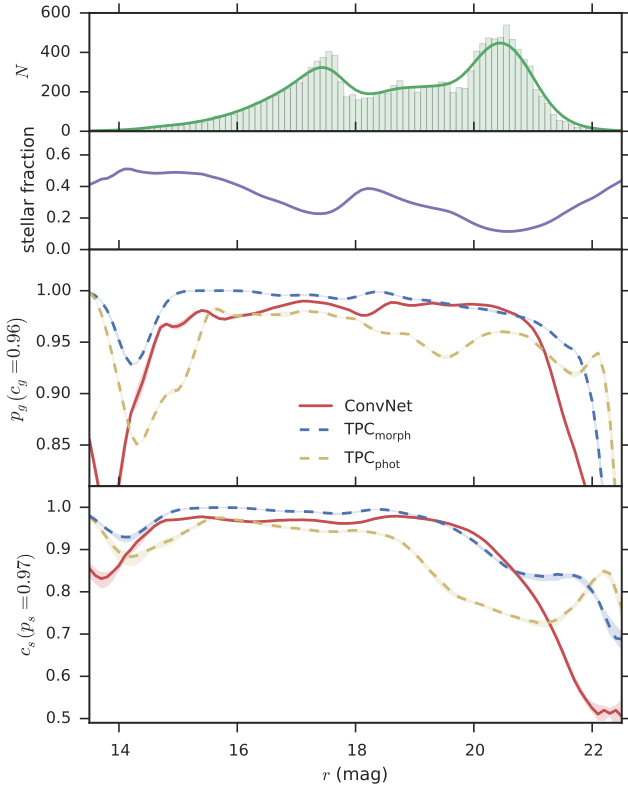
calibrated as ConvNet. These calibration curves visually confirm the results in Table 4 that the calibration error of ConvNet is about 20% lower than that of TPC.

7 CONCLUSIONS

We have presented a convolutional neural network for classifying stars and galaxies in the SDSS and CFHTLenS photometric images. In the interest of scientific reproducibility, we make all our code available at <https://github.com/EdwardJKim/dl4astro>. For

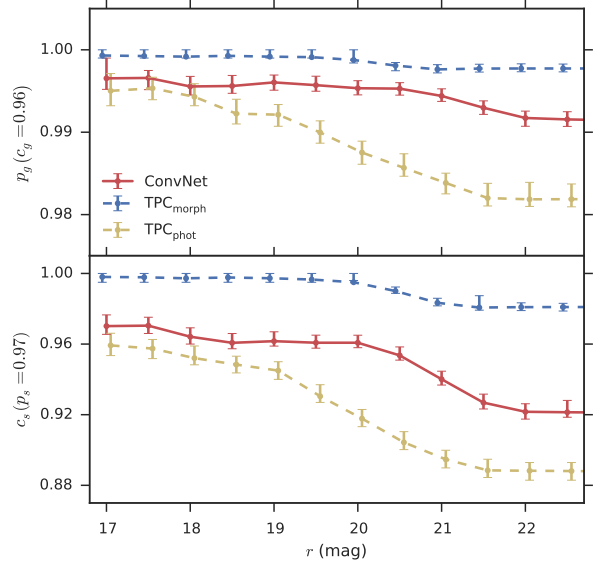
Table 4. A summary of the classification performance metrics as applied to the SDSS data.

classifier	AUC	MSE	$p_g(c_g = 0.96)$	$c_s(p_s = 0.97)$	CAL	$ \Delta N_g /N_g$
ConvNet	0.9952	0.0182	0.9915	0.9500	0.0243	0.0157
TPC _{morph}	0.9967	0.0099	0.9977	0.9810	0.0254	0.0044
TPC _{phot}	0.9886	0.0283	0.9819	0.8879	0.0316	0.0160

**Figure 9.** Completeness and purity in the SDSS as a function of the r -band magnitude for the differential counts.

the CFHTLenS data set, the network is able to provide a classification that is as accurate as a random forest algorithm (TPC), while the probability estimates of our ConvNet model appear to be better calibrated. When the same network architecture is applied to the SDSS data set, the network fails to outperform TPC, but the probabilities are still slightly better calibrated. The major advantage of ConvNets is that useful features are learned automatically from raw pixel values, while traditional machine learning algorithms require feature engineering as a separate process to provide accurate classifications.

ConvNets have recently achieved record-breaking results in many image classification tasks (LeCun et al. 2015) and have been quickly and widely adopted by the computer vision community. One of the main reasons for the success is that ConvNets are general-purpose algorithms that are applicable to a variety of problems without the need for designing a feature extractor. The lack of requirement for feature extraction is a huge advantage e.g., when the task is to classify 1 000 classes in the ImageNet data set (Rusakovsky et al. 2015), as a good feature extractor for identifying images of cats would of little use for classifying sailboats, and it is impractical to design a feature extractor for each class. However,

**Figure 10.** Completeness and purity in the SDSS as a function of the r -band magnitude for the integrated counts.

when there already exists a good feature extractor for the problem at hand, e.g., the concentration parameter, the weight-averaged spread_model parameter from the Dark Energy Survey (Desai et al. 2012; Crocce et al. 2016), or even the SExtractor software, conventional machine learning algorithms that are proven to be effective, such as TPC (Carrasco Kind & Brunner 2013; Kim et al. 2015), remain a viable option. As the "no free lunch" theorem (Wolpert 1996) states, there is no one model that works for every problem. For the CFHTLenS data set, our ConvNet model outperforms TPC trained on the output of SExtractor. Since the SDSS catalog provides the concentration parameter that is highly optimized for star-galaxy classification, TPC works better for SDSS.

Although we used various techniques to combat overfitting, it is possible that our ConvNet model has overfit the data. Overfitting could explain why our ConvNet model with maximal information fails to significantly outperform a standard machine learning algorithm that uses the reduced summary information from catalogs. The most effective way to prevent overfitting would be to simply collect more training images with spectroscopic follow-up, as the performance of ConvNets apparently improves with more training data. However, spectroscopic observations are expensive and time-consuming, and it is unclear if sufficient training data will be available in future photometric surveys. If enough training data become available in DES or LSST, ConvNets become an attractive option because it can be applied immediately on raw images to produce well-calibrated posterior probabilities.

Deep learning is a rapidly developing field and recent devel-

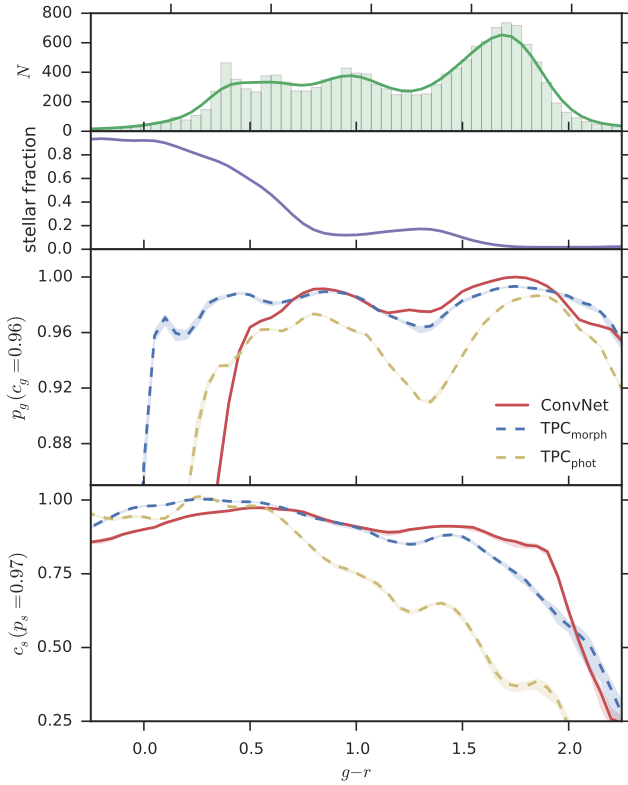


Figure 11. Similar to Figure 9 but as a function of $g-r$ color. The bin size of histogram in the top panel is 0.05.

opments include improved network architectures. For future work, we plan to train more ConvNet variants, such as the Inception Module (Szegedy et al. 2015) and Residual network (He et al. 2015). To improve the predictive performance, we have combined the predictions of different models across multiple transformations of the input images (Section 4.3). To further improve the performance, we could also train several networks with different architectures and combine the models. The winning solution of Dieleman et al. (2015) for the Galaxy Zoo challenge was based on a ConvNet model, and it required averaging many sets of predictions from models with different neural network architectures. It is likely that the performance will be improved by, not only training multiple network architectures, but also combining with different star-galaxy classifiers. In Kim et al. (2015), we combined a purely morphological classifier, a supervised machine learning method (TPC), an unsupervised machine learning method based on self-organizing maps, and a hierarchical Bayesian template fitting method, and demonstrated that our combination technique improves the overall performance over any individual classification method. ConvNets could be included as a different machine learning paradigm in this classifier combination framework to produce further improvements in predictive performance.

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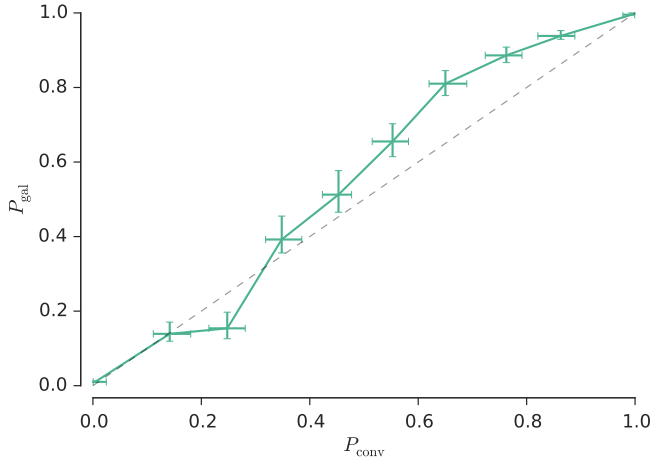


Figure 12. Calibration curve for ConvNet as applied to the SDSS data set.

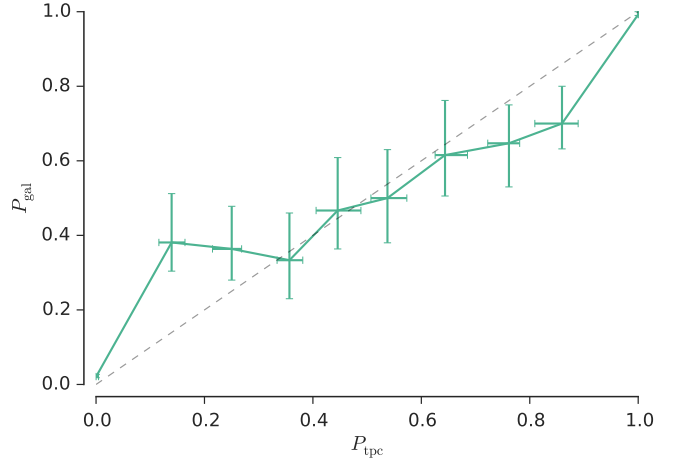


Figure 13. Calibration curve for TPC as applied to the CFHTLenS data set.

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