

## 9.2. REDUCED BASES

Table 9.2.5.1. The parameters  $D = \mathbf{b} \cdot \mathbf{c}$ ,  $E = \mathbf{a} \cdot \mathbf{c}$  and  $F = \mathbf{a} \cdot \mathbf{b}$  of the 44 lattice characters ( $A = \mathbf{a} \cdot \mathbf{a}$ ,  $B = \mathbf{b} \cdot \mathbf{b}$ ,  $C = \mathbf{c} \cdot \mathbf{c}$ )

The character of a lattice given by its reduced form (9.2.2.1) is the first one that agrees when the 44 entries are compared with that reduced form in the sequence given below (suggested by Gruber). Such a logical order is not always obeyed by the widely used character numbers (first column), which therefore show some reversals, e.g. 4 and 5.

No.	Type	$D$	$E$	$F$	Lattice symmetry	Bravais type‡	Transformation to a conventional basis (cf. Table 9.2.5.2, footnote **)
$A = B = C$							
1	I	$A/2$	$A/2$	$A/2$	Cubic	$cF$	$\bar{1}\bar{1}1/11\bar{1}/\bar{1}\bar{1}1$
2	I	$D$	$D$	$D$	Rhombohedral	$hR$	$\bar{1}\bar{1}0/\bar{1}01/\bar{1}\bar{1}\bar{1}$
3	II	0	0	0	Cubic	$cP$	100/010/001
5	II	$-A/3$	$-A/3$	$-A/3$	Cubic	$cI$	101/110/011
4	II	$D$	$D$	$D$	Rhombohedral	$hR$	$\bar{1}\bar{1}0/\bar{1}01/\bar{1}\bar{1}\bar{1}$
6	II	$D^*$	$D$	$F$	Tetragonal	$tI$	011/101/110
7	II	$D^*$	$E$	$E$	Tetragonal	$tI$	101/110/011
8	II	$D^*$	$E$	$F$	Orthorhombic	$oI$	$\bar{1}\bar{1}0/\bar{1}0\bar{1}/0\bar{1}\bar{1}$
$A = B$ , no conditions on $C$							
9	I	$A/2$	$A/2$	$A/2$	Rhombohedral	$hR$	100/ $\bar{1}$ 10/ $\bar{1}\bar{1}$ 3
10	I	$D$	$D$	$F$	Monoclinic	$mC$	110/1 $\bar{1}$ 0/00 $\bar{1}$
11	II	0	0	0	Tetragonal	$tP$	100/010/001
12	II	0	0	$-A/2$	Hexagonal	$hP$	100/010/001
13	II	0	0	$F$	Orthorhombic	$oC$	110/ $\bar{1}$ 10/001
15	II	$-A/2$	$-A/2$	0	Tetragonal	$tI$	100/010/112
16	II	$D^*$	$D$	$F$	Orthorhombic	$oF$	$\bar{1}\bar{1}0/1\bar{1}0/112$
14	II	$D$	$D$	$F$	Monoclinic	$mC$	110/ $\bar{1}$ 10/001
17	II	$D^*$	$E$	$F$	Monoclinic	$mC$	$\bar{1}\bar{1}0/110/\bar{1}0\bar{1}$
$B = C$ , no conditions on $A$							
18	I	$A/4$	$A/2$	$A/2$	Tetragonal	$tI$	0 $\bar{1}$ 1/ $\bar{1}\bar{1}\bar{1}$ /100
19	I	$D$	$A/2$	$A/2$	Orthorhombic	$oI$	$\bar{1}\bar{1}0/0\bar{1}\bar{1}/\bar{1}\bar{1}1$
20	I	$D$	$E$	$E$	Monoclinic	$mC$	011/0 $\bar{1}\bar{1}$ / $\bar{1}$ 00
21	II	0	0	0	Tetragonal	$tP$	010/001/100
22	II	$-B/2$	0	0	Hexagonal	$hP$	010/001/100
23	II	$D$	0	0	Orthorhombic	$oC$	011/0 $\bar{1}\bar{1}$ /100
24	II	$D^*$	$-A/3$	$-A/3$	Rhombohedral	$hR$	121/0 $\bar{1}\bar{1}$ /100
25	II	$D$	$E$	$E$	Monoclinic	$mC$	011/0 $\bar{1}\bar{1}$ /100
No conditions on $A, B, C$							
26	I	$A/4$	$A/2$	$A/2$	Orthorhombic	$oF$	100/ $\bar{1}$ 20/ $\bar{1}$ 02
27	I	$D$	$A/2$	$A/2$	Monoclinic	$mC$	$\bar{1}$ 20/ $\bar{1}$ 00/0 $\bar{1}\bar{1}$
28	I	$D$	$A/2$	$2D$	Monoclinic	$mC$	$\bar{1}\bar{1}0/\bar{1}$ 02/010
29	I	$D$	$2D$	$A/2$	Monoclinic	$mC$	100/120/00 $\bar{1}$
30	I	$B/2$	$E$	$2E$	Monoclinic	$mC$	010/01 $\bar{2}$ / $\bar{1}$ 00
31	I	$D$	$E$	$F$	Triclinic	$aP$	100/010/001
32	II	0	0	0	Orthorhombic	$oP$	100/010/001
40	II	$-B/2$	0	0	Orthorhombic	$oC$	0 $\bar{1}$ 0/012/ $\bar{1}$ 00
35	II	$D$	0	0	Monoclinic	$mP$	0 $\bar{1}$ 0/ $\bar{1}$ 00/00 $\bar{1}$
36	II	0	$-A/2$	0	Orthorhombic	$oC$	100/ $\bar{1}$ 0 $\bar{2}$ /010
33	II	0	$E$	0	Monoclinic	$mP$	100/010/001
38	II	0	0	$-A/2$	Orthorhombic	$oC$	$\bar{1}\bar{1}0/120/00\bar{1}$
34	II	0	0	$F$	Monoclinic	$mP$	$\bar{1}\bar{1}0/00\bar{1}/0\bar{1}0$
42	II	$-B/2$	$-A/2$	0	Orthorhombic	$oI$	$\bar{1}\bar{1}0/0\bar{1}0/112$
41	II	$-B/2$	$E$	0	Monoclinic	$mC$	0 $\bar{1}\bar{2}$ /0 $\bar{1}0/\bar{1}$ 00
37	II	$D$	$-A/2$	0	Monoclinic	$mC$	102/100/010
39	II	$D$	0	$-A/2$	Monoclinic	$mC$	$\bar{1}$ 20/ $\bar{1}$ 00/00 $\bar{1}$
43	II	$D^\dagger$	$E$	$F$	Monoclinic	$mI$	$\bar{1}\bar{1}0/\bar{1}\bar{1}\bar{2}/0\bar{1}0$
44	II	$D$	$E$	$F$	Triclinic	$aP$	100/010/001

\*  $2|D + E + F| = A + B$ .

† As footnote \* plus  $|2D + F| = B$ .

‡ For symbols for Bravais types see footnote \* to Table 9.1.7.1 and de Wolff *et al.* (1985). The capital letter of the symbols in this column indicates the centring type of the cell as obtained by the transformation in the last column. For this reason, the standard symbols  $mS$  and  $oS$  are not used here.