

This problem involves a solitaire card game invented just for this question. You will write a program that tracks the progress of a game. You only need to complete part (g), but parts (a)–(f) are provided as hints. A game is played with a **card-list and a goal**. The player has a list of held cards, initially empty. The player makes a move by either drawing, which means removing the first card in the card-list from the card-list and adding it to the held-cards, or discarding, which means choosing one of the held-cards to remove. The game ends either when **the player chooses to make no more moves** or when the **sum of the values of the held-cards is greater than the goal**. The objective is to end the game with a low score (0 is best). Scoring works as follows: Let *sum* be the **sum of the values of the held-cards**. If *sum* is greater than *goal*, the preliminary score is three times (*sum*–*goal*), else the preliminary score is (*goal*–*sum*). The score is the preliminary score **unless** all the held-cards are the same color, in which case the score is the preliminary score divided by 2 (and rounded down as usual with integer division; use ML’s `div` operator).

- (a) Write a function `card_color`, which takes a card and returns its color (spades and clubs are black, diamonds and hearts are red). Note: **One case-expression** is enough.
- (b) Write a function `card_value`, which takes a card and returns its value (numbered cards have their number as the value, aces are 11, everything else is 10). Note: One case-expression is enough.
- (c) Write a function `remove_card`, which takes a list of cards *cs*, a card *c*, and an exception *e*. It returns a list that has all the elements of *cs* except *c*. If *c* is in the list more than once, remove only the first one. If *c* is not in the list, raise the exception *e*. You can **compare cards with =**.
- (d) Write a function `all_same_color`, which takes a list of cards and returns `true` if all the cards in the list are the same color.
- (e) Write a function `sum_cards`, which takes a list of cards and returns the sum of their values. You may use a locally defined helper function that is **tail recursive**, but this is not a requirement.
- (f) Write a function `score`, which **takes a card list (the held-cards) and an int (the goal)** and computes the score as described above.

(g) Write a function `officiate`, which “runs a game.” **It takes a card list (the card-list) a move list (what the player “does” at each point), and an int (the goal)** and returns the score at the end of the game after processing (some or all of) the moves in the move list in order. You can use a locally defined recursive helper **function that takes several arguments that together represent the current state of the game**. As described above:

- The game starts with the held-cards being the empty list.
- The game ends if there are no more moves. **(The player chose to stop since the move list is empty.)**

- If the player discards some card *c*, play continues (i.e., make a recursive call) with the held cards not having *c* and the card-list unchanged. If *c* is not in the held-cards, raise the `IllegalMove` exception.
- If the player draws and the card-list is (already) empty, the game is over. Else if drawing causes the sum of the held-cards to exceed the goal, the game is over (after drawing). Else play continues with a larger held-cards and a smaller card-list. Note: For the problem, the following datatypes have been defined:

```
datatype suit = Clubs | Diamonds | Hearts | Spades
datatype rank = Jack | Queen | King | Ace | Num of int
type card = suit * rank
datatype color = Red | Black
datatype move = Discard of card | Draw
```

```
exception IllegalMove
```

You do not need to copy these code into your solution.