

模糊方法实验

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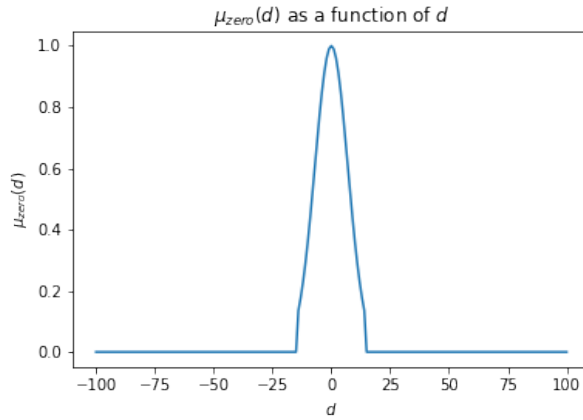
Course: 图象分析与理解 – Professor: 季续
Due date: 5月8日, 2022年

1. 模糊边界提取

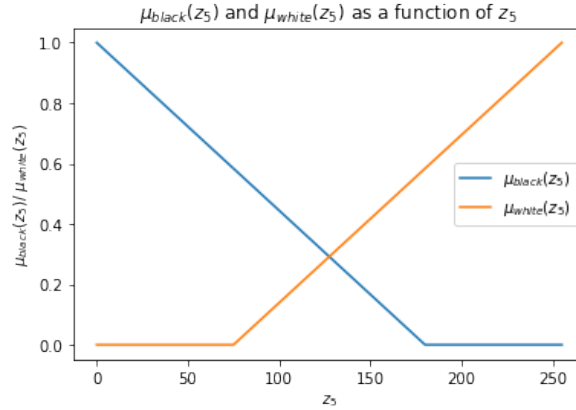
Solution.

1. Definitions of membership functions

- (a) The change of $\mu_{zero}(d)$ with respect to d is shown in Figure 1a.
- (b) The change of $\mu_{black}(z_5)$ and $\mu_{white}(z_5)$ as a function of z_5 is shown in Figure 1b.



(a) Membership function of the fuzzy set *zero*



(b) Membership functions of the fuzzy sets *black* and *white*

Figure 1: Membership functions

2. Rule-based Inference

- (a) Results of fuzzy spatial filtering are shown in Figure 2.
- (b) When σ of the input membership function is changed to 10, the corresponding boundaries are less obvious. The bandwidth of the truncated Gaussian is wider, which recognizes neighbours with larger intensity differences as a uniform area.



(a) Boundary extraction ($\sigma = 7$)



(b) Boundary extraction ($\sigma = 10$)

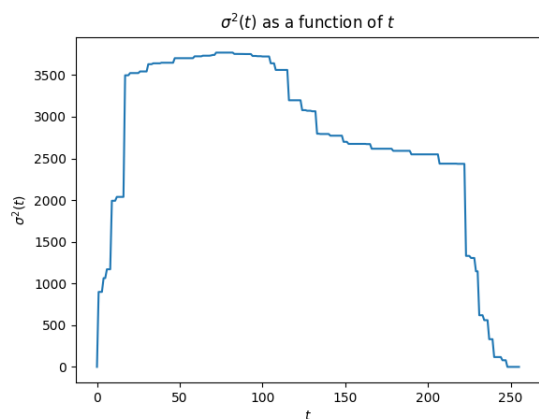
Figure 2: Results of fuzzy spatial filtering

2. 阈值分割

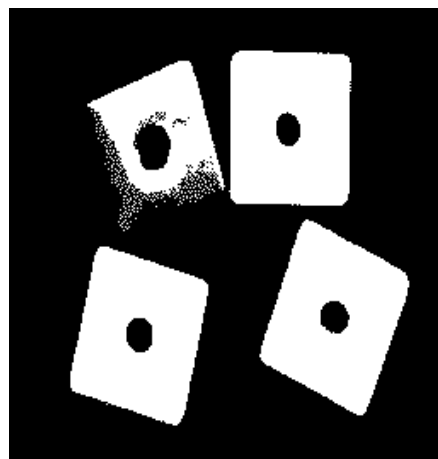
Solution.

1. Otsu's Binarization

- (a) The change of $\sigma^2(t)$ with respect to t is shown in Figure 3a.
- (b) As is shown in Figure 3b, the result after Otsu thresholding is barely satisfactory where the top-left square is not well determined.



(a) between-class variance $\sigma^2(t)$ with respect to t

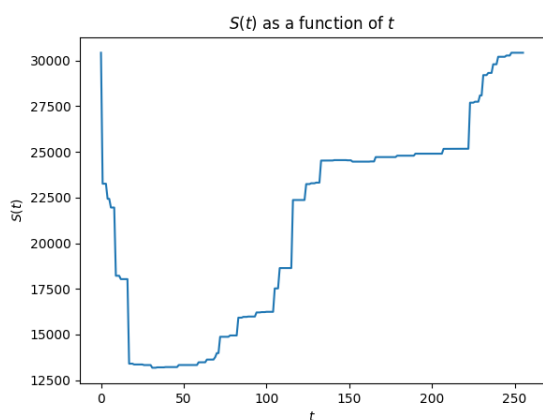


(b) thresholded by Otsu algorithm

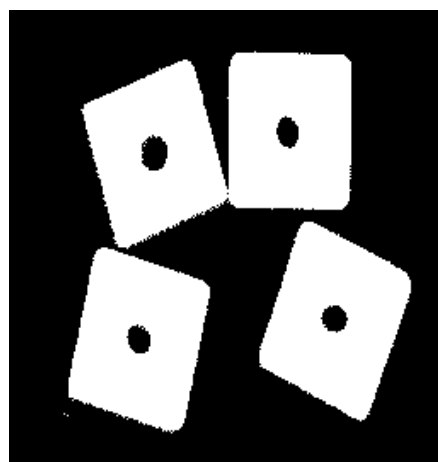
Figure 3: Illustration of Otsu's Binarization

2. Fuzzy thresholding method

- (a) The change of sum of all pixels' entropy $S(t)$ with respect to threshold t is shown in Figure 4a.
- (b) As is shown in Figure 4b, the result after fuzzy thresholding is satisfactory where all the four squares are well segmented from the background.



(a) Entropy $S(t)$ with respect to t



(b) thresholded by fuzzy method

Figure 4: Illustration of fuzzy thresholding