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# Correct Integer Operations With Minimal Runtime Penalties

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## 1. Introduction

This library is intended as a drop-in replacement for all built-in integer types in any program which must:

- be demonstrably and verifiably correct.
- detect every user error such as input, assignment, etc.
- be efficient as possible subject to the constraints above.

### 1.1. Problem

Arithmetic operations in C++ are NOT guaranteed to yield a correct mathematical result. This feature is inherited from the early days of C. The behavior of `int`, `unsigned int` and others were designed to map closely to the underlying hardware. Computer hardware implements these types as a fixed number of bits. When the result of arithmetic operations exceeds this number of bits, the result will not be arithmetically correct. The following example illustrates this problem.

```
int f(int x, int y){  
    // this returns an invalid result for some legal values of x and y !  
    return x + y;  
}
```

It is incumbent up the C/C++ programmer to guarantee that this behavior does not result in incorrect or unexpected operation of the program. There are no language facilities which do this. They have to be explicitly addressed in the program code. There are a number of ways to do this. Sees[\[INT-32C\]](#) seems to recommend the following approach.

```
int f(int x, int y){  
    if (((y > 0) && (x > (INT_MAX - y)))  
        || ((y < 0) && (x < (INT_MIN - y)))) {  
        /* Handle error */  
    }  
    return x + y;  
}
```

This will indeed trap the error. However, it would be tedious and laborious for a programmer to do alter his code to do. Altering code in this way for all arithmetic operations would likely render the code unreadable and add another source of potential programming errors. This approach is clearly not functional when the expression is even a little more complex as is shown in the following example.

```
int f(int x, int y, int z){  
    // this returns an invalid result for some legal values of x and y !  
    return x + y * z;  
}
```

```
}
```

This example addresses only the problem of undefined/erroneous behavior related to overflow of the addition operation. Similar problems occur with other built-in integer types such as unsigned, long, etc. and other operations such as subtraction, multiplication etc. . C/C++ often automatically and silently convert some integer types to others in the course of implementing binary operations and similar problems occur in this case as well. Since the problems and their solution are similar, We'll confine the current discussion to just this example.

## 1.2. Solution

This library implements special versions of int, unsigned, etc. which behave exactly like the original ones EXCEPT that the results of these operations are guaranteed to be either arithmetically correct or invoke an error. Using this library, the above example would be rendered as:

```
#include <boost/safe_numeric/safe_integer.hpp>
using namespace boost::numeric;
safe<int> f(safe<int> x, safe<int> y){
    return x + y; // throw exception if correct result cannot be returned
}
```



### Note

Library code in this document resides in the name space `boost::numeric`. This name space has generally been eliminated from text, code and examples in order to improve readability of the text.

The addition expression is checked at runtime or (if possible) at compile time to trap any possible errors resulting from incorrect arithmetic behavior. This will permit one to write arithmetic expressions that cannot produce an erroneous result. Instead, one and only one of the following is guaranteed to occur.

- the expression will yield the correct mathematical result
- the expression will emit a compilation error.
- the expression will invoke a runtime exception.

In other words, the *library absolutely guarantees that no arithmetic expression will yield incorrect results.*

## 1.3. Implementation

The library implements special versions of int, unsigned, etc. named `safe<int>`, `safe<unsigned int>` etc. These behave exactly like the underlying types EXCEPT that expressions using these types fulfill the above guarantee. These types are meant to be "drop-in" replacements for the built-in types they are meant to replace. So things which are legal - such as assigning an signed to unsigned value are not trapped at compile time - as they are legal C/C++ code - but rather checked at runtime to trap the case where this (legal) operation would lead to an arithmetically incorrect result.

Note that the library addresses arithmetical errors generated by straightforward C/C++ expressions. Some of these arithmetic errors are defined as conforming to the C/C++ standards while others are not. So characterizing this library as addressing undefined behavior of C/C++ numeric expressions is misleading.

Facilities particular to C++14 are employed to minimize any runtime overhead required to make this guarantee. In many cases there is no runtime overhead at all. In other cases, a using program can be slightly altered to achieve the above guarantee without any runtime overhead.

## 1.4. Additional Features

Operation of safe types is determined by template parameters which specify a pair of [policy classes](#) which specify the behavior for type promotion and error handling. In addition to the usage serving as a drop-in replacement for standard integer types, users of the library can:

- Select or define an exception policy class to specify handling of exceptions.
  - throw exception or runtime, trap at compile time.
  - trap at compiler time all operations which might fail at runtime.
  - specify custom functions which should be called at runtime
- Select or define a promotion policy class to alter the C++ type promotion rules. This can be used to
  - use C++ native type promotion rules so that, except for throwing/trapping of exceptions on operations resulting in incorrect arithmetic behavior, programs will operate identically when using/not using safe types.
  - replace C++ native promotion rules with ones which are arithmetically equivalent but minimize the need for runtime checking of arithmetic results.
  - replace C++ native promotion rules with ones which emulate other machine architectures. This is designed to permit the testing of C++ code destined to be run on another machine on one's development platform. Such a situation often occurs while developing code for embedded systems.
- Enforce of other program requirements using ranged integer types. The library includes types `safe_..._range<Min, Max>` and `safe_literal(...)`. These types can be used to improve program correctness and performance.

## 1.5. Requirements

This library is composed entirely of C++ Headers. It requires a compiler compatible with the C++14 standard.

The following Boost Libraries must be installed in order to use this library

- Mpl
- Integer
- Config
- Concept Checking
- Tribool
- Enable\_if

The safe numerics library is delivered with an exhaustive suite of test programs. Users who choose to run this test suite will also need to install the Boost.Preprocessor library.

## 1.6. Scope

This library currently applies only to built-in integer types. Analogous issues arise for floating point types but they are not currently addressed by this version of the library. User or Library defined types such as arbitrary precision integers can also have this problem. Extension of this library to these other types is not currently under development but may be addressed in the future. This is one reason why the library name is "safe numeric" rather than "safe integer" library.

## 2. Eliminating Runtime Penalty

Up until now, we've focused on detecting when incorrect results are produced and handling these occurrences either by throwing an exception or invoking some designated function. We've achieved our goal of enforcing arithmetically correct behavior - but at what cost. For many C++ programmers any runtime penalty is unacceptable. Whether or not one agrees with this trade off, its a fact that many C++ programmers feel this way. So the question arises as to how we alter our program to minimize or eliminate any runtime penalty.

The first step is to determine what parts of a program might invoke exceptions. The following program is similar to previous examples but uses a special exception policy: [trap\\_exception](#).

```
#include <iostream>

#include "../include/safe_integer.hpp"
#include "../include/exception.hpp" // include exception policies
#include "safe_format.hpp" // prints out range and value of any type

using safe_t = boost::numeric::safe<
    int,
    boost::numeric::native,
    boost::numeric::trap_exception // note use of "trap_exception" policy!
>;

safe_t f(const safe_t & x, const safe_t & y){
    // each statement below will fail to compile !
    safe_t z = x + y;
    std::cout << "(x + y)" << safe_format(x + y) << std::endl;
    std::cout << "(x - y)" << safe_format(x - y) << std::endl;
    return z;
}

int main(int argc, const char * argv[]){
    std::cout << "example 81:\n";
    safe_t x(INT_MAX); // will fail to compile
    safe_t y(2);       // will fail to compile
    std::cout << "x" << safe_format(x) << std::endl;
    std::cout << "y" << safe_format(y) << std::endl;
    std::cout << "z" << safe_format(f(x, y)) << std::endl;
    return 0;
}
```

Now, any expression which ***MIGHT*** fail at runtime is flagged with a compile time error. There is no longer any need for try/catch blocks. Since this program does not compile, the **library absolutely guarantees that no arithmetic expression will yield incorrect results**. This is our original goal. Now all we need to do is make the program work. There are a couple of ways to do this.

### 2.1. Using Automatic Type Promotion

The C++ standard describes how binary operations on different integer types are handled. Here is a simplified version of the rules:

- promote any operand smaller than int to an int or unsigned int.
- if the signed operand is larger than the signed one, the result will be signed, otherwise the result will be unsigned.
- expand the smaller operand to the size of the larger one

So the result of the sum of two integer types will result in another integer type. If the values are large, they will exceed the size that the resulting integer type can hold. This is what we call "overflow". Standard C/C++ does just truncates the result to fit into the result type - which sometimes will make the result arithmetically incorrect.

The complete signature for a safe integer type is:

```
template <
    class T,                // underlying integer type
    class P = native,       // type promotion policy class
    class E = throw_exception // error handling policy class
>
safe;
```

The standard C++ type promotion rules are consistent with the default "native" type promotion policy. Up until now, we've focused on detecting when this happens and invoking an interrupt or other kind of error handler.

But now we look at another option. Using the "automatic" type promotion policy, we can change the rules of C++ arithmetic for safe types to something like the following:

- for any C++ numeric types, we know from `std::numeric::limits` what the maximum and minimum values that a variable can be - this defines a closed interval.
- For any binary operation on these types, we can calculate the interval of the result at compile time.
- From this interval we can select a new type which can be guaranteed to hold the result and use this for the calculation. This is more or less equivalent to the following code:

```
int x, y;
int z = x + y           // could overflow

int x, y;
long z = (long)x + (long)y; // can never overflow
```

One could do this by editing his code manually, but such a task would be tedious, error prone, and leave the resulting code hard to read and verify. Using the "automatic" type promotion policy will achieve the equivalent result without these problems

- Since the result type is guaranteed to hold the result, there is no need to check for errors - they can't happen !!! The usage of "trap\_exception" exception policy enforces this guarantee
- Since there can be no errors, there is no need for try/catch blocks.
- The only runtime error checking we need to do is when safe values are initialized or assigned using smaller types. These are infrequent occurrences which generally have little or no impact on program running time. And many times, one can make small adjustments in selecting the types in order to eliminate all runtime penalties.

In short, given a binary operation, we promote the types of the operands to a larger so that the result type cannot overflow. This is a fundamental departure from the C++ Standard behavior.

If the interval of the result cannot be contained in the largest type that the machine can handle (usually 64 bits these days), the largest available integer type with the correct result sign is used. So even with our "automatic" type promotion scheme, it's still possible to overflow. In this case, and only this case, is runtime error checking code generated. Depending on the application, it should be rare to generate error checking code, and even more rare to actually invoke it. Any such instances are detected by the "trap\_exception" exception policy.

This small example illustrates how to use automatic type promotion to eliminate all runtime penalty.

```
#include <iostream>

#include "../include/safe_integer.hpp"
#include "../include/automatic.hpp"
#include "safe_format.hpp" // prints out range and value of any type

using safe_t = boost::numeric::safe<
    int,
    boost::numeric::automatic, // note use of "automatic" policy!!!
    boost::numeric::trap_exception
>;

auto f(const safe_t & x, const safe_t & y){ // note use of "auto"
    auto z = x + y; // note change to "auto"
    std::cout << "(x + y) = " << safe_format(x + y) << std::endl;
    std::cout << "(x - y) = " << safe_format(x - y) << std::endl;
    return z;
}

int main(int argc, const char * argv){
    std::cout << "example 82:\n";
    safe_t x(INT_MAX);
    safe_t y = 2;
    std::cout << "x = " << safe_format(x) << std::endl;
    std::cout << "y = " << safe_format(y) << std::endl;
    std::cout << "z = " << safe_format(f(x, y)) << std::endl;
    return 0;
}
```

The above program produces the following output:

```
example 82:
x = <int>[-2147483648,2147483647] = 2147483647
y = <int>[-2147483648,2147483647] = 2
z = (x + y) = <long>[-4294967296,4294967294] = 2147483649
(x - y) = <long>[-4294967295,4294967295] = 2147483645
<long>[-4294967296,4294967294] = 2147483649
```

The output uses a custom output manipulator for safe types to display the underlying type and its range as well as current value. Note that:

- automatic type promotion policy has rendered the result of the some of two integers as a long type.
- our program compiles without error - even when using the trap\_exception exception policy
- We do not need to use try/catch idiom to handle arithmetic errors - we will have none.
- We only needed to change two lines of code to achieve our goal

## 2.2. Using **safe\_range**

Instead of relying on automatic type promotion, we can just create our own types in such a way that we known they won't overflow. In the example below, we presume we happen to know that the values we want to work with fall in the closed

range of -24,82. So we "know" the program will always result in a correct result. But since we trust no one, and since the program could change and the expressions be replaced with other ones, we'll still use the `"trap_exception" exception policy` to verify at compile time that what we "know" to be true is in fact true.

```
#include <iostream>

#include "../include/safe_range.hpp"
#include "../include/safe_literal.hpp"
#include "../include/native.hpp"
#include "../include/exception.hpp"

#include "safe_format.hpp" // prints out range and value of any type

using namespace boost::numeric; // for safe_literal

// create a type for holding small integers. We "know" that C++ type
// promotion rules will work such that operations on this type
// will never overflow. If change the program to break this, the
// usage of the trap_exception promotion policy will prevent compilation.
using safe_t = safe_signed_range<
    -24,
    82,
    native,          // C++ type promotion rules work OK for this example
    trap_exception   // catch problems at compile time
>;

auto f(const safe_t & x,    const safe_t & y){
    //safe_t z = x + y; // depending on values of x & y COULD fail
    auto z = x + y;      // due to C++ type promotion rules,
                        // we know that this cannot fail
    std::cout << "(x + y) = " << safe_format(x + y) << std::endl;
    std::cout << "(x - y) = " << safe_format(x - y) << std::endl;
    return z;
}

int main(int argc, const char * argv[]){
    std::cout << "example 83:\n";
    // constexpr const safe_t z = 3; // fails to compile
    const safe_t x(safe_literal<2>{});
    const safe_t y = safe_literal<2>(); // to avoid runtime penalty
    std::cout << "x = " << safe_format(x) << std::endl;
    std::cout << "y = " << safe_format(y) << std::endl;
    std::cout << "z = " << safe_format(f(x, y)) << std::endl;
    return 0;
}
```

which produces the following output.

```
example 83:
x = <signed char>[-24,82] = 2
y = <signed char>[-24,82] = 2
z = (x + y) = <int>[-48,164] = 4
(x - y) = <int>[-106,106] = 0
<int>[-48,164] = 4
```

- In this example, standard C++ type promotion rules are used. These promote operands to int before invoking the addition operation. So addition operation itself won't overflow. The result of addition is another unnamed safe type guaranteed to

be able to hold the some of any pair of safe types. In this example the result is a safe type based on the C++ built-in type of short.

- So when we try to assign the result to z we could get an error. This is because our custom `safe_t` cannot be guaranteed to hold the some of all possible pairs of `safe_t` instances. We fix the by using an "auto" for the sum.
- We now have a problem when we try to initialize our `safe_t` variable with an initial literal value. This operation could overflow at runtime. To our disappointment, our attempt to fix the problem by using `constexpr` fails. The fix for this is to use `safe_literal` to initialize safe types. `safe_literal` is a special safe type which wraps a constant defined at compile time. It cannot be assigned to, or changed. Subject to this restriction, it can participate in safe arithmetic operations.

We've used simple expressions in this illustration. But since binary operations on safe types result in other safe types, expressions can be made arbitrarily elaborate - just as they can be with intrinsic integer types. That is, safe integer types are drop in replacements for intrinsic integer types. We are guaranteed never to produce an incorrect result regardless of how elaborate the expression might be.

## 2.3. Mixing Approaches

For purposes of exposition, we've divided the discussion of how to eliminate runtime penalties by the different approaches available. A realistic program would likely include all techniques mentioned above. Consider the following:

```
#include <stdexcept>
#include <iostream>

#include "../include/safe_range.hpp"
#include "../include/automatic.hpp"
#include "../include/exception.hpp"

#include "safe_format.hpp" // prints out range and value of any type

using namespace boost::numeric;

using safe_t = safe_signed_range<
    -24,
    82,
    automatic,
    trap_exception
>;

// define variables use for input
using input_safe_t = safe_signed_range<
    -24,
    82,
    automatic, // we don't need automatic in this case
    throw_exception // these variables need to
>;

// function arguments can never be outside of limits
auto f(const safe_t & x, const safe_t & y){
    auto z = x + y; // we know that this cannot fail
    std::cout << "z = " << safe_format(z) << std::endl;
    std::cout << "(x + y) = " << safe_format(x + y) << std::endl;
    std::cout << "(x - y) = " << safe_format(x - y) << std::endl;
    return z;
}

int main(int argc, const char * argv[]){
```



```
std::cout << "example 84:\n";
try{
    input_safe_t x, y;
    std::cin >> x >> y; // read variables, throw exception
    std::cout << "x" << safe_format(x) << std::endl;
    std::cout << "y" << safe_format(y) << std::endl;
    std::cout << safe_format(f(x, y)) << std::endl;
}
catch(const std::exception & e){
    // none of the above should trap. Mark failure if they do
    std::cout << e.what() << std::endl;
    return false;
}
return 0;
}
```

- As before we define a `safe_t` to reflect our view of legal values for this program. This uses automatic type policy as well as trapping exception policy to enforce elimination of runtime penalties.
- In addition we define `input_safe_t` to be used when reading variables from the program console. Clearly, these can only be checked at runtime so they use the `throw_exception` policy.
- When variables are read from the console and assigned to `safe_t` variables `x` and `y`, they are checked for legal values. We need ad hoc code to do this, as these types are guaranteed to contain legal values and will throw an exception when this guarantee is violated. In other words, we automatically get checking of input variables with no additional programming.
- On calling of the function `f`, the variables of type `input_safe_t` are converted to variables of `safe_t`. This conversion invokes any needed checking. In this case there is none necessary. If checker were necessary, the usage of the `trap_exception` policy for `safe_t` types would cause a compile time error.
- The function `f` accepts only `safe_t` types so we have no need to check the input types. This performs the functionality of *programming by contract* with no runtime cost. Due to our usage of `trap_exception` as a policy in `safe_t`, any violation in our "contract" will result in a runtime error.

Here is the output from the program when values 12 and 32 are input from the console:

```
example 84:
12 32
x<signed char>[-24,82] = 12
y<signed char>[-24,82] = 32
z = <short>[-48,164] = 44
(x + y) = <short>[-48,164] = 44
(x - y) = <short>[-106,106] = -20
<short>[-48,164] = 44
```

## 3. Notes

This library is really a re-implementation of the facilities provided by [David LeBlanc's SafeInt Library](http://safeint.codeplex.com) [http://safeint.codeplex.com] using [Boost and C++14](http://www.boost.org) [www.boost.org]. I found this library very well done in every way. My main usage was to run unit tests for my embedded systems projects on my PC. Still, I had a few issues.

- It was a lot of code in one header - 6400 lines. Very unwieldy to understand, modify and maintain.
- I couldn't find separate documentation other than that in the header file.
- It didn't use [Boost](http://www.boost.org) [www.boost.org] conventions for naming.

- It required porting to different compilers.
- It had a very long license associated with it.
- I could find no test suite for the library.

This version addresses these issues. It exploits [Boost](http://www.boost.org) [www.boost.org] facilities such as template metaprogramming to reduce the number of lines of source code to approximately 4700. It exploits the Boost Preprocessor Library to generate exhaustive tests.

All concepts, types and functions documented are declared in the name space `boost::numeric`.

## 4. Rationale and FAQ

- 4.1. Is this really necessary? If I'm writing the program with the requisite care and competence, problems noted in the introduction will never arise. Should they arise, they should be fixed "at the source" and not with a "band aid" to cover up bad practice.

This surprised me when it was first raised. But some of the feedback I've received makes me think that it's a widely held view. The best answer is to consider the cases in the section [Tutorials and Motivating Examples](#).

- 4.2. Can safe types be used as drop-in replacement for built-in types?

Almost. Replacing all built-in types with their safe counterparts should result in a program that will compile and run as expected. In some cases compile time errors will occur and adjustments to the source code will be required. Typically these will result in code which is more correct. See [drop-in replacement](#).

- 4.3. Why is Boost.Convert not used?

I couldn't figure out how to use it from the documentation.

- 4.4. Why is the library named "safe ..." rather than something like "checked ..." ?

I used "safe" in large part this is what has been used by other similar libraries. Maybe a better word might have been "correct" but that would raise similar concerns. I'm not inclined to change this. I've tried to make it clear in the documentation what the problem that the library addressed is

- 4.5. Given that the library is called "numerics" why is floating point arithmetic not addressed?

Actually, I believe that this can/should be applied to any type T which satisfies the type requirement "Numeric" type as defined in the documentation. So there should be specializations `safe<float>` et. al. and eventually `safe<fixed_decimal>` etc. But the current version of the library only addresses integer types. Hopefully the library will evolve to match the promise implied by its name.

- 4.6. Isn't putting a defensive check just before any potential undefined behavior is often considered a bad practice?

By whom? Is leaving code which can produce incorrect results better? Note that the documentation contains references to various sources which recommend exactly this approach to mitigate the problems created by this C/C++ behavior. See [\[Seacord\]](#), [Software Engineering Institute - Carnegie Mellon University](#) [https://www.cert.org]

- 4.7. It looks like the implementation presumes two's complement arithmetic at the hardware level. So this library is not portable - correct? What about other hardware architectures?

As far as is known as of this writing, the library does not presume that the underlying hardware is two's complement. However, this has yet to be verified in a rigorous way.

**4.8.** Why do you specialize `numeric_limits` for "safe" types? Do you need it?

`safe<T>` behaves like a "number" just as `int` does. It has `max`, `min`, etc. Any code which uses numeric limits to test a type `T` should work with `safe<T>`. `safe<T>` is a drop-in replacement for `T` so it has to implement all the operations.

**4.9.** According to C/C++ standards, unsigned integers cannot overflow - they are modular integers which "wrap around". Yet the safe numerics library detects and traps this behavior as errors. Why is that?

The guiding purpose of the library is to trap incorrect arithmetic behavior - not just undefined behavior. Although a savvy user may understand and keep present in his mind that an unsigned integer is really a modular type, the plain reading of an arithmetic expression conveys the idea that all operands are plain integers. Also in many cases, unsigned integers are used in cases where modular arithmetic is not intended, such as array indexes. Finally, the modulus for such an integer would vary depending upon the machine architecture. For these reasons, in the context of this library, an unsigned integer is considered to be a representation of a subset of integers which is expected to provide correct integer results. Note that this decision is consistent with INT30-C, "Ensure that unsigned integer operations do not wrap" in the CERT C Secure Coding Standard [Seacord 2008].

## 5. Current Status

The library is currently in the [Boost Review Queue](http://www.boost.org/community/review_schedule.html) [http://www.boost.org/community/review\_schedule.html]. The proposal submission can be found in the [Boost Library Incubator](http://blincubator.com/bi_library/safe-numerics/?gform_post_id=426) [http://blincubator.com/bi\_library/safe-numerics/?gform\_post\_id=426]

- The library is currently limited to integers.
- Conversions to safe integer types from floating point types is not explicitly addressed.
- Note that standard library stream conversion functions such as `strtoi` etc. DO check for valid input and throw the exception `std::out_of_range` if the string cannot be converted to the specified integer type. In other words, `strtoi` already contains some of the functionality that `safe<int>` provides.
- Although care was taken to make the library portable, it's likely that at least some parts of the implementation - particularly checked arithmetic - depend upon two's complement representation of integers. Hence the library is probably not currently portable to other architectures.
- Currently the library permits a `safe<int>` value to be uninitialized. This supports the goal of "drop-in" replacement of C++/C built-in types with safe counterparts. On the other hand, this breaks the "always valid" guarantee.
- The library is not quite a "drop-in" replacement for all built-in integer types. In particular, C/C++ implements implicit conversions and promotions between certain integer types which are not captured by the operation overloads used to implement the library. In practice these cases are few and can be addressed with minor changes to the user program to avoid these silent implicit conversions.

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