Chapter 1. Safe Numerics

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Table of Contents

1. Introduction	4
1.1. Problem	4
1.2. Solution	5
1.3. How It Works	5
1.4. Additional Features	6
1.5. Requirements	6
1.6. Scope	7
2. Tutorial and Motivating Examples	7
2.1. Arithmetic Expressions Can Yield Incorrect Results	
2.2. Arithmetic Operations Can Overflow Silently	
2.3. Implicit Conversions Can Lead to Erroneous Results	
2.4. Mixing Data Types Can Create Subtle Errors	
2.5. Array Index Value Can Exceed Array Limits	
2.6. Checking of Input Values Can Be Easily Overlooked	. 13
2.7. Cannot Recover From Arithmetic Errors	
2.8. Programming by Contract is Too Slow	
3. Case Studies	
3.1. Eliminating Runtime Penalty	
Using safe_range and safe_literal	
Using Automatic Type Promotion	. 19
Mixing Approaches	
3.2. Composition with Other Libraries	
4. Background	
5. Type Requirements	
5.1. Numeric <t></t>	. 24
Description	. 24
Notation	24
Associated Types	
Valid Expressions	
Models	
Header	
5.2. Integer <t></t>	. 26
Description	
Refinement of	
Notation	
Valid Expressions	
Models	. 28
Header	
5.3. SafeNumeric <t></t>	
Description	
Refinement of	
Notation	
	_

Safe Numerics

	valid Expressions	. 28
	Complexity Guarantees	. 30
	Invariants	
	Models	
	Header	
	5.4. PromotionPolicy <pp></pp>	
	Description	
	Notation	
	Valid Expressions	
	Models	
	Header	
	5.5. ExceptionPolicy <ep></ep>	
	Description	
	Notation	
	Valid Expressions	
	dispatch <ep>(const safe_numerics_error & e, const char * msg)</ep>	
	Models	
. T	Header	
6. I	ypes	
	6.1. safe <t, ep="" pp,=""></t,>	
	Description	
	Notation	
	Associated Types	
	Template Parameters	
	Model of	
	Valid Expressions	
	Examples of use	
	Header	
	6.2. safe_signed_range <min, ep="" max,="" pp,=""> and safe_unsigned_range<min, ep="" max,="" pp,=""></min,></min,>	
	Description	
	Notation	
	Associated Types	
	Template Parameters	
	Model of	. 38
	Valid Expressions	. 38
	Example of use	38
	Header	39
	6.3. safe_signed_literal <value, ep="" pp,=""> and safe_unsigned_literal<value, ep="" pp,=""></value,></value,>	. 39
	Description	
	Associated Types	. 39
	Template Parameters	
	Model of	. 39
	Inherited Valid Expressions	. 40
	New Valid Expression	
	Example of use	
	Header	
	6.4. exception	
	Description	
	enum class safe numerics error	
	enum class safe_numerics_actions	
	See Also	
	Header	
	6.5. exception_policy <ae, idb,="" ub,="" uv=""></ae,>	
	Description	
	Description	+∠

Safe Numerics

Template Parameters	. 42
Model of	43
Inherited Valid Expressions	43
Function Objects	43
Policies Provided by the library	
Header	
6.6. Promotion Policies	
native	
automatic	
cpp <int c,="" i,="" int="" l,="" ll="" s,=""></int>	
7. Exception Safety	
8. Library Implementation	
8.1. checked_result <r></r>	
Description	
Notation	
Template Parameters	
Model of	
Valid Expressions	
<u> </u>	
Example of use	
See Also	
Header	
8.2. Checked Arithmetic	
Synopsis	
Description	
Type requirements	
Complexity	
Example of use	
Notes	
See Also	
Header	
8.3. interval <r></r>	
Description	
Template Parameters	
Notation	55
Associated Types	
Valid Expressions	55
Example of use	
Header	. 57
8.4. safe_compare <t, u=""></t,>	57
Synopsis	57
Description	. 57
Type requirements	. 57
Complexity	57
Example of use	. 58
Header	. 58
9. Performance Tests	
10. Rationale and FAQ	
11. Pending Issues	
12. Acknowledgements	
13. Change Log	
14. Bibliography	

1. Introduction

This library is intended as a drop-in replacement for all built-in integer types in any program which must:

- be demonstrably and verifiably correct.
- detect every user error such as input, assignment, etc.
- be efficient as possible subject to the constraints above.

1.1. Problem

Arithmetic operations in C/C++ are NOT guaranteed to yield a correct mathematical result. This feature is inherited from the early days of C. The behavior of int, unsigned int and others were designed to map closely to the underlying hardware. Computer hardware implements these types as a fixed number of bits. When the result of arithmetic operations exceeds this number of bits, the result will not be arithmetically correct. The following example illustrates just one example where this causes problems.

```
int f(int x, int y){
    // this returns an invalid result for some legal values of x and y !
    return x + y;
}
```

It is incumbent upon the C/C++ programmer to guarantee that this behavior does not result in incorrect or unexpected operation of the program. There are no language facilities which implement such a guarantee. A programmer needs to examine each expression individually to know that his program will not return an invalid result. There are a number of ways to do this. In the above instance, [INT32-C] seems to recommend the following approach:

```
int f(int x, int y){
  if (((y > 0) && (x > (INT_MAX - y)))
  || ((y < 0) && (x < (INT_MIN - y)))) {
    /* Handle error */
  }
  return x + y;
}</pre>
```

This will indeed trap the error. However, it would be tedious and laborious for a programmer to alter his code in this manner. Altering code in this way for all arithmetic operations would likely render the code unreadable and add another source of potential programming errors. This approach is clearly not functional when the expression is even a little more complex as is shown in the following example.

```
int f(int x, int y, int z){
   // this returns an invalid result for some legal values of x and y !
   return x + y * z;
}
```

This example addresses only the problem of undefined/erroneous behavior related to overflow of the addition operation as applied to the type int. Similar problems occur with other built-in integer types such as unsigned, long, etc. And it also applies to other operations such as subtraction, multiplication etc. .C/C++ often automatically and silently converts some integer types to others in the course of implementing binary operations. Sometimes such conversions can silently change arithmetic values which inject errors. The C/C++ standards designate some behavior such as right shifting a negative number as "implementation"

defined behavior". These days machines usually do what the programmer expects - but such behavior is not guaranteed. Relying on such behavior will create a program which cannot be guaranteed to be portable. And then there is undefined behavior. In this case, compiler writer is under no obligation to do anything in particular. Sometimes this will unexpectedly break the program. At the very least, the program is rendered non-portable. Finally there is the case of behavior that is arithmetically wrong to begin with - for example divide by zero. Some runtime environments will just terminate the program, others may throw some sort of exception. In any case, the execution has failed in a manner from which there is no recovery.

All of the above conditions prevent obstacles to creation of a program which will never fail. The Safe Numerics Library addresses all of these conditions, at least as far as integer operations are concerned.

Since the problems and their solution are similar, We'll confine the current discussion to just the one example shown above.

1.2. Solution

This library implements special versions of int, unsigned, etc. which behave exactly like the original ones **except** that the results of these operations are guaranteed to be either arithmetically correct or invoke an error. Using this library, the above example would be rendered as:

```
#include <boost/safe_numeric/safe_integer.hpp>
using namespace boost::numeric;
safe<int> f(safe<int> x, safe<int> y){
  return x + y; // throw exception if correct result cannot be returned
}
```

Note

Library code in this document resides in the namespace boost::numeric. This namespace has generally been eliminated from text, code and examples in order to improve readability of the text.

The addition expression is checked at runtime or (if possible) at compile time to trap any possible errors resulting in incorrect arithmetic behavior. Arithmetic expressions will not produce an erroneous result. Instead, one and only one of the following is guaranteed to occur.

- the expression will yield the correct mathematical result
- the expression will emit a compilation error.
- the expression will invoke a runtime exception.

In other words, the library absolutely guarantees that no integer arithmetic expression will yield incorrect results.

1.3. How It Works

The library implements special versions of int, unsigned, etc. named safe<int>, safe<unsigned int> etc. These behave exactly like the underlying types **except** that expressions using these types fulfill the above guarantee. These "safe" types are meant to be "drop-in" replacements for the built-in types they are meant to replace. So things which are legal - such as assignment of a signed to unsigned value - are not trapped at compile time as they are legal C/C++ code. Instead, they are checked at runtime to trap the case where this (legal) operation would lead to an arithmetically incorrect result.

Note that the library addresses arithmetical errors generated by straightforward C/C++ expressions. Some of these arithmetic errors are defined as conforming to the C/C++ standards while others are not. So characterizing this library as only addressing undefined behavior of C/C++ numeric expressions would be misleading.

Facilities particular to C++14 are employed to minimize any runtime overhead. In many cases there is no runtime overhead at all. In other cases, a program using the library can be slightly altered to achieve the above guarantee without any runtime overhead.

1.4. Additional Features

Operation of safe types is determined by template parameters which specify a pair of policy classes which specify the behavior for type promotion and error handling. In addition to the usage serving as a drop-in replacement for standard integer types, users of the library can:

- Select or define an exception policy class to specify handling of exceptions.
 - Throw exception on runtime, trap at compile time if possible.
 - Trap at compiler time all operations which could possibly fail at runtime.
 - Specify custom functions which should be called in case errors are detected at runtime.
- Select or define a promotion policy class to alter the C/C++ type promotion rules. This can be used to
 - Use C/C++ native type promotion rules so that, except for throwing/trapping of exceptions on operations resulting in incorrect arithmetic behavior, programs will operate identically when using/not using safe types. This might be used if safe types are only enabled during debug and testing.
 - Replace C/C++ native promotion rules with ones which are arithmetically equivalent but minimize the need for runtime checking of arithmetic results. Such a policy will effectively change the semantics of a C++ program. It's not really C++ any more. The program cannot be expected to function the same as when normal integer types are used.
 - Replace C/C++ native promotion rules with ones which emulate other machine architectures. This is designed to permit the testing of C/C++ code destined to be run on another machine on one's development platform. Such a situation often occurs while developing code for embedded systems.
- Enforce other program requirements using bounded integer types. The library includes the types for ranges and literals. Operations which result in operations which violate these requirements will trapped at either compile or runtime and not silently return invalid values. These types can be used to improve program correctness and performance.

1.5. Requirements

This library is composed entirely of C++ Headers. It requires a compiler compatible with the C++14 standard.

The following Boost Libraries must be installed in order to use this library

- MPL
- Integer
- Config
- · Concept Checking
- Tribool
- Enable_if

The Safe Numerics library is delivered with an exhaustive suite of test programs. Users who choose to run this test suite will also need to install the Boost.Preprocessor and Boost.MP11 libraries.

1.6. Scope

This library currently applies only to built-in integer types. Analogous issues arise for floating point types but they are not currently addressed by this version of the library. User or library defined types such as arbitrary precision integers can also have this problem. Extension of this library to these other types is not currently under development but may be addressed in the future. This is one reason why the library name is "safe numeric" rather than "safe integer" library.

2. Tutorial and Motivating Examples

2.1. Arithmetic Expressions Can Yield Incorrect Results

When some operation on signed integer types results in a result which exceeds the capacity of a data variable to hold it, the result is undefined. In the case of unsigned integer types a similar situation results in a value wrap as per modulo arithmetic. In either case the result is different than in integer number arithmetic in the mathematical sense. This is called "overflow". Since word size can differ between machines, code which produces mathematically correct results in one set of circumstances may fail when re-compiled on a machine with different hardware. When this occurs, Most C++ compilers will continue to execute with no indication that the results are wrong. It is the programmer's responsibility to ensure such undefined behavior is avoided.

This program demonstrates this problem. The solution is to replace instances of int type with safe<int> type.

```
#include <cassert>
#include <exception>
#include <iostream>
#include <cstdint>
#include "../include/safe_integer.hpp"
int main(int, const char *[]){
    std::cout << "example 1:";
    std::cout << "undetected erroneous expression evaluation" << std::endl;</pre>
    std::cout << "Not using safe numerics" << std::endl;
    try{
        int x = INT_MAX;
        int y = 2;
        int z;
        // this produces an invalid result !
        std::cout << z << " != " << x << " + " << y << std::endl;
        std::cout << "error NOT detected!" << std::endl;</pre>
    catch(std::exception){
        std::cout << "error detected!" << std::endl;</pre>
    // solution: replace int with safe<int>
    std::cout << "Using safe numerics" << std::endl;
    try{
        using namespace boost::numeric;
        safe < int > x = INT_MAX;
        safe<int> y = 2;
        safe<int> z;
        // rather than producing an invalid result an exception is thrown
    catch(std::exception & e){
        // which we can catch here
```

```
std::cout << "error detected:" << e.what() << std::endl;
}
return 0;
}</pre>
```

```
example 1:undetected erroneous expression evaluation

Not using safe numerics
-2147483647 != 2147483647 + 2

error NOT detected!

Using safe numerics
error detected:addition result too large: positive overflow error
```

2.2. Arithmetic Operations Can Overflow Silently

A variation of the above is when a value is incremented/decremented beyond its domain. This is a common problem with for loops.

```
#include <cassert>
#include <exception>
#include <iostream>
#include "../include/safe_integer.hpp"
int main(int, const char *[]){
    std::cout << "example 2:";</pre>
    std::cout << "undetected overflow in data type" << std::endl;</pre>
    // problem: undetected overflow
    std::cout << "Not using safe numerics" << std::endl;</pre>
    try{
        int x = INT_MAX;
        // the following silently produces an incorrect result
        std::cout << x << " != " << INT MAX << " + 1" << std::endl;
        std::cout << "error NOT detected!" << std::endl;</pre>
    catch(std::exception){
        std::cout << "error detected!" << std::endl;</pre>
    // solution: replace int with safe<int>
    std::cout << "Using safe numerics" << std::endl;</pre>
    try{
        using namespace boost::numeric;
        safe < int > x = INT_MAX;
        // throws exception when result is past maximum possible
        assert(false); // never arrive here
    catch(std::exception & e){
        std::cout << e.what() << std::endl;</pre>
        std::cout << "error detected!" << std::endl;</pre>
    return 0;
}
```

```
example 2:undetected overflow in data type
Not using safe numerics
```

```
-2147483648 != 2147483647 + 1
error NOT detected!
Using safe numerics
addition result too large
error detected!
```

When variables of unsigned integer type are decremented below zero, they "roll over" to the highest possible unsigned version of that integer type. This is a common problem which is generally never detected.

2.3. Implicit Conversions Can Lead to Erroneous Results

At CPPCon 2016 Jon Kalb gave a very entertaining (and disturbing) lightning talk related to C++ expressions.

The talk included a very, very simple example similar to the following:

```
#include <exception>
#include <iostream>
#include "../include/safe_integer.hpp"
int main(){
    std::cout << "example 4: ";</pre>
    std::cout << "implicit conversions change data values" << std::endl;</pre>
    std::cout << "Not using safe numerics" << std::endl;</pre>
    // problem: implicit conversions change data values
    try{
        signed int a\{-1\};
        unsigned int b{1};
        std::cout << "a is " << a << " b is " << b << '\n';
        if(a < b){
            std::cout << "a is less than b\n";
        else{
            std::cout << "b is less than a\n";
        std::cout << "error NOT detected!" << std::endl;</pre>
    catch(std::exception){
        // never arrive here - just produce the wrong answer!
        std::cout << "error detected!" << std::endl;</pre>
        return 1;
    // solution: replace int with safe<int> and unsigned int with safe<unsigned int>
    std::cout << "Using safe numerics" << std::endl;</pre>
    try{
        using namespace boost::numeric;
        safe<signed int> a\{-1\};
        safe<unsigned int> b{1};
        std::cout << "a is " << a << " b is " << b << '\n';
        if(a < b){
            std::cout << "a is less than b\n";
        else{
            std::cout << "b is less than a\n";
```

```
std::cout << "error NOT detected!" << std::endl;
    return 1;
}
catch(std::exception & e){
    // never arrive here - just produce the correct answer!
    std::cout << e.what() << std::endl;
    std::cout << "error detected!" << std::endl;
}
return 0;
}</pre>
```

```
example 3: implicit conversions change data values

Not using safe numerics
a is -1 b is 1
b is less than a
error NOT detected!

Using safe numerics
a is -1 b is 1
converted negative value to unsigned: domain error
error detected!
```

A normal person reads the above code and has to be dumbfounded by this. The code doesn't do what the text - according to the rules of algebra - says it does. But C++ doesn't follow the rules of algebra - it has its own rules. There is generally no compile time error. You can get a compile time warning if you set some specific compile time switches. The explanation lies in reviewing how C++ reconciles binary expressions (a < b is an expression here) where operands are different types. In processing this expression, the compiler:

- Determines the "best" common type for the two operands. In this case, application of the rules in the C++ standard dictate that this type will be an unsigned int.
- Converts each operand to this common type. The signed value of -1 is converted to an unsigned value with the same bit-wise contents, 0xFFFFFFFF, on a machine with 32 bit integers. This corresponds to a decimal value of 4294967295.
- Performs the calculation in this case it's <, the "less than" operation. Since 1 is less than 4294967295 the program prints "b is less than a".

In order for a programmer to detect and understand this error he should be pretty familiar with the implicit conversion rules of the C++ standard. These are available in a copy of the standard and also in the canonical reference book *The C++ Programming Language* (both are over 1200 pages long!). Even experienced programmers won't spot this issue and know to take precautions to avoid it. And this is a relatively easy one to spot. In the more general case this will use integers which don't correspond to easily recognizable numbers and/or will be buried as a part of some more complex expression.

This example generated a good amount of web traffic along with everyone's pet suggestions. See for example a blog post with everyone's favorite "solution". All the proposed "solutions" have disadvantages and attempts to agree on how handle this are ultimately fruitless in spite of, or maybe because of, the emotional content. Our solution is by far the simplest: just use the safe numerics library as shown in the example above.

Note that in this particular case, usage of the safe types results in no runtime overhead in using the safe integer library. Code generated will either equal or exceed the efficiency of using primitive integer types.

2.4. Mixing Data Types Can Create Subtle Errors

C++ contains signed and unsigned integer types. In spite of their names, they function differently which often produces surprising results for some operands. Program errors from this behavior can be exceedingly difficult to find. This has lead to

recommendations of various ad hoc "rules" to avoid these problems. It's not always easy to apply these "rules" to existing code without creating even more bugs. Here is a typical example of this problem:

```
#include <iostream>
#include <cstdint>
#include "../include/safe_integer.hpp"
using namespace std;
using namespace boost::numeric;
void f(const unsigned int & x, const int8_t & y){
    cout << x * y << endl;</pre>
void safe_f(
    const safe<unsigned int> & x,
    const safe<int8_t> & y
) {
    cout << x * y << endl;</pre>
}
int main(){
    cout << "example 4: ";</pre>
    cout << "mixing types produces surprising results" << endl;</pre>
    try {
        std::cout << "Not using safe numerics" << std::endl;</pre>
        // problem: arithmetic operations can yield incorrect results.
        f(100, 100); // works as expected
        f(100, -100); // wrong result - unnoticed
        cout << "error NOT detected!" << endl;;</pre>
    catch(const std::exception & e){
        // never arrive here
        cout << "error detected:" << e.what() << endl;;</pre>
    try {
        // solution: use safe types
        std::cout << "Using safe numerics" << std::endl;</pre>
        safe_f(100, 100); // works as expected
        safe_f(100, -100); // throw error
        cout << "error NOT detected!" << endl;;</pre>
    catch(const std::exception & e){
        cout << "error detected:" << e.what() << endl;;</pre>
    return 0;
}
```

Here is the output of the above program:

```
example 4: mixing types produces surprising results
Not using safe numerics
10000
4294957296
error NOT detected!
Using safe numerics
10000
```

```
error detected!converted negative value to unsigned: domain error
```

This solution is simple, just replace instances of int with safe<int>.

2.5. Array Index Value Can Exceed Array Limits

Using an intrinsic C++ array, it's very easy to exceed array limits. This can fail to be detected when it occurs and create bugs which are hard to find. There are several ways to address this, but one of the simplest would be to use safe_unsigned_range;

```
#include <stdexcept>
#include <iostream>
#include <array>
#include "../include/safe_integer_range.hpp"
void detected_msg(bool detected){
    std::cout << (detected ? "error detected!" : "error NOT detected! ") << std::endl;
int main(int, const char *[]){
    // problem: array index values can exceed array bounds
    std::cout << "example 5: ";</pre>
    std::cout << "array index values can exceed array bounds" << std::endl;</pre>
    std::cout << "Not using safe numerics" << std::endl;</pre>
    std::array<int, 37> i_array;
    // unsigned int i_index = 43;
    // the following corrupts memory.
    // This may or may not be detected at run time.
    // i_array[i_index] = 84; // comment this out so it can be tested!
    std::cout << "error NOT detected!" << std::endl;</pre>
    // solution: replace unsigned array index with safe_unsigned_range
    std::cout << "Using safe numerics" << std::endl;
    try{
         using namespace boost::numeric;
         using i_index_t = safe_unsigned_range<0, i_array.size() - 1>;
         i_index_t i_index;
        i_index = 36; // this works fine
        i_array[i_index] = 84;
         i_index = 43; // throw exception here!
         \mathtt{std}::\mathtt{cout} << \mathtt{"error} \ \mathtt{NOT} \ \mathtt{detected}! \mathtt{"} << \mathtt{std}::\mathtt{endl}; \ // \ \mathtt{so} \ \mathtt{we} \ \mathtt{never} \ \mathtt{arrive} \ \mathtt{here}
    catch(std::exception & e){
         std::cout << "error detected:" << e.what() << std::endl;</pre>
    return 0;
}
```

```
example 5: array index values can exceed array bounds
Not using safe numerics
error NOT detected!
Using safe numerics
error detected:Value out of range for this safe type: domain error
```

Collections like standard arrays and vectors do array index checking in some function calls and not in others so this may not be the best example. However it does illustrate the usage of safe_range<T> for assigning legal ranges to variables. This will guarantee that under no circumstances will the variable contain a value outside of the specified range.

2.6. Checking of Input Values Can Be Easily Overlooked

It's way too easy to overlook the checking of parameters received from outside the current program.

```
#include <stdexcept>
#include <sstream>
#include <iostream>
#include "../include/safe_integer.hpp"
int main(int, const char *[]){
    // problem: checking of externally produced value can be overlooked
    std::cout << "example 6: ";
    std::cout << "checking of externally produced value can be overlooked" << std::endl;
    std::cout << "Not using safe numerics" << std::endl;</pre>
    std::istringstream is("12317289372189 1231287389217389217893");
    try{
        int x, y;
        is >> x >> y; // get integer values from the user
        std::cout << x << ' ' << y << std::endl;
        std::cout << "error NOT detected!" << std::endl;</pre>
    catch(std::exception){
        std::cout << "error detected!" << std::endl;</pre>
    // solution: assign externally retrieved values to safe equivalents
    std::cout << "Using safe numerics" << std::endl;</pre>
        using namespace boost::numeric;
        safe<int> x, y;
        is.seekg(0);
        try{
            is >> x >> y; // get integer values from the user
            std::cout << x << ' ' << y << std::endl;
            std::cout << "error NOT detected!" << std::endl;</pre>
        catch(std::exception & e){
            std::cout << "error detected:" << e.what() << std::endl;</pre>
    return 0;
```

```
example 6: checking of externally produced value can be overlooked
Not using safe numerics
2147483647 0
error NOT detected!
Using safe numerics
error detected:error in file input: domain error
```

Without safe integer, one will have to insert new code every time an integer variable is retrieved. This is a tedious and error prone procedure. Here we have used program input. But in fact this problem can occur with any externally produced input.

2.7. Cannot Recover From Arithmetic Errors

If a divide by zero error occurs in a program, it's detected by hardware. The way this manifests itself to the program can and will depend upon

- data type int, float, etc
- · setting of compile time command line switches
- invocation of some configuration functions which convert these hardware events into C++ exceptions

It's not all that clear how one would detect and recover from a divide by zero error in a simple portable way. Usually, users just ignore the issue which usually results in immediate program termination when this situation occurs.

This library will detect divide by zero errors before the operation is invoked. Any errors of this nature are handled according to the ErrorPolicy selected by the library user.

```
#include <stdexcept>
#include <iostream>
#include "../include/safe_integer.hpp"
int main(int, const char *[]){
    // problem: cannot recover from arithmetic errors
    std::cout << "example 7: ";</pre>
    std::cout << "cannot recover from arithmetic errors" << std::endl;</pre>
    std::cout << "Not using safe numerics" << std::endl;</pre>
    try{
        int x = 1;
        int y = 0;
        // can't do this as it will crash the program with no
        // opportunity for recovery - comment out for example
        //std::cout << x / y;
        std::cout << "error NOT detectable!" << std::endl;</pre>
    }
    catch(std::exception){
        std::cout << "error detected!" << std::endl;</pre>
    }
    // solution: replace int with safe<int>
    std::cout << "Using safe numerics" << std::endl;</pre>
    try{
        using namespace boost::numeric;
        safe < int > x = 1;
        safe < int > y = 0;
        std::cout << x / y;
        std::cout << " error NOT detected!" << std::endl;</pre>
    catch(std::exception & e){
        std::cout << "error detected:" << e.what() << std::endl;</pre>
    return 0;
```

```
example 7: cannot recover from arithmetic errors

Not using safe numerics
error NOT detectable!

Using safe numerics
error detected:divide by zero: domain error
```

2.8. Programming by Contract is Too Slow

Programming by Contract is a highly regarded technique. There has been much written about it and it has been proposed as an addition to the C++ language [Garcia][Crowl & Ottosen]. It (mostly) depends upon runtime checking of parameter and object values upon entry to and exit from every function. This can slow the program down considerably which in turn undermines the main motivation for using C++ in the first place! One popular scheme for addressing this issue is to enable parameter checking only during debugging and testing which defeats the guarantee of correctness which we are seeking here! Programming by Contract will never be accepted by programmers as long as it is associated with significant additional runtime cost.

The Safe Numerics Library has facilities which, in many cases, can check guaranteed parameter requirements with little or no runtime overhead. Consider the following example:

```
#include <cassert>
#include <stdexcept>
#include <sstream>
#include <iostream>
#include "../include/safe_integer_range.hpp"
// NOT using safe numerics - enforce program contract explicitly
// return total number of minutes
unsigned int contract_convert(
    const unsigned int & hours,
    const unsigned int & minutes
) {
    // check that parameters are within required limits
    // invokes a runtime cost EVERYTIME the function is called
    // and the overhead of supporting an interrupt.
    // note high runtime cost!
    if(minutes > 59)
        throw std::domain_error("minutes exceeded 59");
    if(hours > 23)
        throw std::domain_error("hours exceeded 23");
    return hours * 60 + minutes;
}
// Use safe numeric to enforce program contract automatically
// define convenient typenames for hours and minutes hh:mm
using hours_t = boost::numeric::safe_unsigned_range<0, 23>;
using minutes_t = boost::numeric::safe_unsigned_range<0, 59>;
using minutes_total_t = boost::numeric::safe_unsigned_range<0, 59>;
// return total number of minutes
// type returned is safe_unsigned_range<0, 24*60 - 1>
auto convert(const hours_t & hours, const minutes_t & minutes) {
    // no need to test pre-conditions
    // input parameters are guaranteed to hold legitimate values
    // no need to test post-conditions
    // return value guaranteed to hold result
    return hours * 60 + minutes;
```

```
}
unsigned int test1(unsigned int hours, unsigned int minutes){
    // problem: checking of externally produced value can be expensive
    // invalid parameters - detected - but at a heavy cost
    return contract_convert(hours, minutes);
auto test2(unsigned int hours, unsigned int minutes){
    // solution: use safe numerics
    // safe types can be implicitly constructed base types
    // construction guarentees corectness
    // return value is known to fit in unsigned int
    return convert(hours, minutes);
}
auto test3(unsigned int hours, unsigned int minutes){
    // actually we don't even need the convert function any more
    return hours_t(hours) * 60 + minutes_t(minutes);
}
int main(int, const char *[]){
    std::cout << "example 7: ";
    std::cout << "enforce contracts with zero runtime cost" << std::endl;</pre>
    unsigned int total_minutes;
    try {
        total_minutes = test3(17, 83);
        std::cout << "total minutes = " << total_minutes << std::endl;</pre>
    catch(std::exception e){
        std::cout << "parameter error detected" << std::endl;</pre>
    try {
        total_minutes = test3(17, 10);
        std::cout << "total minutes = " << total_minutes << std::endl;</pre>
    catch(std::exception e){
        // should never arrive here
        std::cout << "parameter error erroneously detected" << std::endl;</pre>
    return 0;
}
```

```
example 8:
enforce contracts with zero runtime cost
parameter error detected
```

In the example above, the function convert incurs significant runtime cost every time the function is called. By using "safe" types, this cost is moved to the moment when the parameters are constructed. Depending on how the program is constructed, this may totally eliminate extraneous computations for parameter requirement type checking. In this scenario, there is no reason to suppress the checking for release mode and our program can be guaranteed to be always arithmetically correct.

3. Case Studies

3.1. Eliminating Runtime Penalty

Up until now, we've focused on detecting when incorrect results are produced and handling these occurrences either by throwing an exception or invoking some designated function. We've achieved our goal of detecting and handling arithmetically incorrect behavior - but at what cost? It is a fact that many C++ programmers will find this trade-off unacceptable. So the question arises as to how we might minimize or eliminate this runtime penalty.

The first step is to determine what parts of a program might invoke exceptions. The following program is similar to previous examples but uses a special exception policy: loose_trap_policy.

```
#include <iostream>
#include "../include/safe_integer.hpp"
#include "../include/exception_policies.hpp" // include exception policies

using safe_t = boost::numeric::safe<
    int,
    boost::numeric::native,
    boost::numeric::loose_trap_policy // note use of "loose_trap_exception" policy!

>;

int main(int argc, const char * argv[]){
    std::cout << "example 81:\n";
    safe_t x(INT_MAX);
    safe_t y(2);
    safe_t z = x + y; // will fail to compile !
    return 0;
}</pre>
```

Now, any expression which *might* fail at runtime is flagged with a compile time error. There is no longer any need for try/catch blocks. Since this program does not compile, the **library absolutely guarantees that no arithmetic expression will yield incorrect results**. Furthermore, it is **absolutely guaranteed that no exception will ever be thrown**. This is our original goal.

Now all we need to do is make the program work. There are a couple of ways to achieve this.

Using safe_range and safe_literal

Instead of relying on automatic type promotion, we can just create our own types in such a way that we know they won't overflow. In the example below, we presume we know that the values we want to work with fall in the range [-24,82]. So we "know" the program will always result in a correct result. But since we trust no one, and since the program could change and the expressions be replaced with other ones, we'll still use the <code>loose_trap_policy</code> exception policy to verify at compile time that what we "know" to be true is in fact true.

```
#include <iostream>
#include "../include/safe_integer_range.hpp"
#include "../include/safe_integer_literal.hpp"
#include "../include/exception.hpp"
#include "../include/native.hpp"
#include "safe_format.hpp" // prints out range and value of any type
using namespace boost::numeric;
// create a type for holding small integers in a specific range
```

```
using safe_t = safe_signed_range<
    -24,
    82,
                      // C++ type promotion rules work OK for this example
    native.
    loose_trap_policy // catch problems at compile time
>;
// create a type to hold one specific value
template<int I>
using const_safe_t = safe_signed_literal<I, native, loose_trap_policy>;
// We "know" that C++ type promotion rules will work such that
// addition will never overflow. If we change the program to break this,
// the usage of the loose_trap_policy promotion policy will prevent compilation.
int main(int, const char *[]){
    std::cout << "example 83:\n";
    constexpr const const_safe_t<10> x;
    std::cout << "x = " << safe_format(x) << std::endl;</pre>
    constexpr const const_safe_t<67> y;
    std::cout << "y = " << safe_format(y) << std::endl;</pre>
    constexpr const safe_t z = x + y;
    std::cout << "x + y = " << safe_format(x + y) << std::endl;
    std::cout << "z = " << safe_format(z) << std::endl;</pre>
    return 0;
}
```

- safe_signed_range defines a type which is limited to the indicated range. Out of range assignments will be detected at compile time if possible (as in this case) or at run time if necessary.
- A safe range could be defined with the same minimum and maximum value effectively restricting the type to holding one specific value. This is what safe_signed_literal does.
- Defining constants with safe_signed_literal enables the library to correctly anticipate the correct range of the results of arithmetic expressions.
- The usage of loose_trap_policy will mean that any assignment to z which could be outside its legal range will result in a compile time error.
- All safe integer operations are implemented as constant expressions. The usage of constexpr will guarantee that z will be available at compile time for any subsequent use.
- So if this program compiles, it's guaranteed to return a valid result.

The output uses a custom output manipulator, safe_format, for safe types to display the underlying type and its range as well as current value. This program produces the following run time output.

```
example 83:

x = <signed char>[10,10] = 10

y = <signed char>[67,67] = 67

x + y = <int>[77,77] = 77

z = <signed char>[-24,82] = 77
```

Take note of the various variable types:

- x and y are safe types with fixed ranges which encompass one single value. They can hold only that value which they have been assigned at compile time.
- ullet The sum x + y can also be determined at compile time.

• The type of z is defined so that It can hold only values in the closed range -24,82. We can assign the sum of x + y because it is in the range that z is guaranteed to hold. If the sum were not known at compile time, or it could not be guaranteed to fall in the range of z, we would get a compile time error due to the fact we are using the loose_trap_policy exception policy.

All this information regarding the range and values of variables has been determined at compile time. There is no runtime overhead. The usage of safe types does not alter the calculations or results in anyway. So safe_t and const_safe_t could be redefined to int and const int respectively and the program would operate identically - although it might We could compile the program for another machine - as is common when building embedded systems and know (assuming the target machine architecture was the same as our native one) that no erroneous results would ever be produced.

Using Automatic Type Promotion

The C++ standard describes how binary operations on different integer types are handled. Here is a simplified version of the rules:

- promote any operand smaller than int to an int or unsigned int.
- if the size of the signed operand is larger than the size of the signed operand, the type of the result will be signed. Otherwise, the type of the result will be unsigned.
- Convert the type each operand to the type of the result, expanding the size as necessary.
- Perform the operation the two resultant operands.

So the type of the result of some binary operation may be different than the types of either or both of the original operands.

If the values are large, the result can exceed the size that the resulting integer type can hold. This is what we call "overflow". The C/C++ standard characterizes this as undefined behavior and leaves to compiler implementors the decision as to how such a situation will be handled. Usually, this means just truncating the result to fit into the result type - which sometimes will make the result arithmetically incorrect. However, depending on the compiler and compile time switch settings, such cases may result in some sort of run time exception or silently producing some arbitrary result.

The complete signature for a safe integer type is:

The promotion rules implemented in the default native type promotion policy are consistent with those of standard C++

Up until now, we've focused on detecting when an arithmetic error occurs and invoking an exception or other kind of error handler.

But now we look at another option. Using the automatic type promotion policy, we can change the rules of C++ arithmetic for safe types to something like the following:

- for any C++ numeric type, we know from std::numeric_limits what the maximum and minimum values that a variable can be this defines a closed interval.
- For any binary operation on these types, we can calculate the interval of the result at compile time.
- From this interval we can select a new type which can be guaranteed to hold the result and use this for the calculation. This is more or less equivalent to the following code:

```
int x, y;
```

One could do this by editing his code manually as above, but such a task would be tedious, error prone, non-portable and leave the resulting code hard to read and verify. Using the automatic type promotion policy will achieve the equivalent result without these problems.

Using the automatic type promotion policy, given a binary operation, we silently promote the types of the operands to a wider result type so the result cannot overflow. This is a fundamental departure from the C++ Standard behavior.

If the interval of the result cannot be guaranteed to fit in the largest type that the machine can handle (usually 64 bits these days), the largest available integer type with the correct result sign is used. So even with our "automatic" type promotion scheme, it's still possible to overflow. So while our automatic type promotion policy might eliminate exceptions in our example above, it wouldn't be guaranteed to eliminate them for all programs.

Using the loose_trap_policy exception policy will produce a compile time error anytime it's possible for an error to occur.

This small example illustrates how to use automatic type promotion to eliminate all runtime penalty.

```
#include <iostream>
#include "../include/safe integer.hpp"
#include "../include/exception_policies.hpp"
#include "../include/automatic.hpp"
#include "safe_format.hpp" // prints out range and value of any type
using safe_t = boost::numeric::safe<
    int,
    boost::numeric::automatic, // note use of "automatic" policy!!!
    boost::numeric::loose_trap_policy
>;
int main(int, const char *[]){
    std::cout << "example 82:\n";</pre>
    safe_t x(INT_MAX);
    safe_t y = 2;
    std::cout << "x = " << safe_format(x) << std::endl;
    std::cout << "y = " << safe_format(y) << std::endl;</pre>
    std::cout << "x + y = " << safe_format(x + y) << std::endl;
    return 0;
}
```

- the automatic type promotion policy has rendered the result of the sum of two integers as a safe<long> type.
- our program compiles without error even when using the loose_trap_policy exception policy. This is because since a long can always hold the result of the sum of two integers.
- We do not need to use the try/catch idiom to handle arithmetic errors we will have no exceptions.
- We only needed to change two lines of code to achieve our goal of guaranteed program correctness with no runtime penalty.

The above program produces the following output:

```
example 82:
x = <int>[-2147483648,2147483647] = 2147483647
```

```
y = <int>[-2147483648,2147483647] = 2
x + y = <long>[-4294967296,4294967294] = 2147483649
```

Note that if any time in the future we were to change safe<int> to safe<long long> the program could now overflow. But since we're using loose_trap_policy the modified program would fail to compile. At this point we'd have to alter our yet program again to eliminate run time penalty or set aside our goal of zero run time overhead and change the exception policy to default_exception_policy.

Mixing Approaches

For purposes of exposition, we've divided the discussion of how to eliminate runtime penalties by the different approaches available. A realistic program would likely include all techniques mentioned above. Consider the following:

```
#include <stdexcept>
#include <iostream>
#include "../include/safe_integer.hpp"
#include "../include/safe_integer_range.hpp"
#include "../include/automatic.hpp"
#include "../include/exception.hpp"
#include "safe_format.hpp" // prints out range and value of any type
using namespace boost::numeric;
using safe_t = safe_signed_range<
    -24,
    82,
    automatic,
    loose_trap_policy
>;
// define variables used for input
using input_safe_t = safe_signed_range<</pre>
    -24,
    82,
    automatic, // we don't need automatic in this case
    loose_exception_policy // assignment of out of range value should throw
>;
// function arguments can never be outside of limits
auto f(const safe_t & x, const safe_t & y){
    auto z = x + y; // we know that this cannot fail
    std::cout << "z = " << safe_format(z) << std::endl;</pre>
    std::cout << "(x + y) = " << safe_format(x + y) << std::endl;
    std::cout << "(x - y) = " << safe_format(x - y) << std::endl;
    return z;
}
int main(int argc, const char * argv[]){
    std::cout << "example 84:\n";
    input_safe_t x, y;
    try{
        std::cout << "type in values in format x y:" << std::flush;
        std::cin >> x >> y; // read varibles, maybe throw exception
    catch(const std::exception & e){
        // none of the above should trap. Mark failure if they do
```

```
std::cout << e.what() << std::endl;
    return 1;
}
std::cout << "x" << safe_format(x) << std::endl;
std::cout << "y" << safe_format(y) << std::endl;
std::cout << safe_format(f(x, y)) << std::endl;
return 0;
}</pre>
```

- As before, we define a type safe_t to reflect our view of legal values for this program. This uses the automatic type promotion policy as well as the loose_trap_policy exception policy to enforce elimination of runtime penalties.
- The function f accepts only arguments of type safe_t so there is no need to check the input values. This performs the functionality of *programming by contract* with no runtime cost.
- In addition, we define input_safe_t to be used when reading variables from the program console. Clearly, these can only be checked at runtime so they use the throw_exception policy. When variables are read from the console they are checked for legal values. We need no ad hoc code to do this, as these types are guaranteed to contain legal values and will throw an exception when this guarantee is violated. In other words, we automatically get checking of input variables with no additional programming.
- On calling of the function f, arguments of type input_safe_t are converted to values of type safe_t. In this particular example, it can be determined at compile time that construction of an instance of a safe_t from an input_safe_t can never fail. Hence, no try/catch block is necessary. The usage of the loose_trap_policy policy for safe_t types guarantees this to be true at compile time.

Here is the output from the program when values 12 and 32 are input from the console:

```
example 84:
type in values in format x y:33 45
x<signed char>[-24,82] = 33
y<signed char>[-24,82] = 45
z = <short>[-48,164] = 78
(x + y) = <short>[-48,164] = 78
(x - y) = <signed char>[-106,106] = -12
<short>[-48,164] = 78
```

3.2. Composition with Other Libraries

For many years, Boost has included a library to represent and operate on rational numbers. Its well crafted, has good documentation and is well maintained. Using the rational library is as easy as construction an instance with the expression rational r(n, d) where n and d are integers of the same type. From then on it can be used pretty much as any other number. Reading the documentation with safe integers in mind one finds

Limited-precision integer types [such as int] may raise issues with the range sizes of their allowable negative values and positive values. If the negative range is larger, then the extremely-negative numbers will not have an additive inverse in the positive range, making them unusable as denominator values since they cannot be normalized to positive values (unless the user is lucky enough that the input components are not relatively prime pre-normalization).

Which hints of trouble. Examination of the code reveals which suggest that care has been taken implement operations so as to avoid overflows, catch divide by zero, etc. But the code itself doesn't seem to consistently implement this idea. So we make a small demo program:

```
#include <iostream>
#include <limits>
```

```
#include <boost/rational.hpp>
#include <safe_integer.hpp>
int main(int, const char *[]){
   // simple demo of rational library
   const boost::rational<int> r {1, 2};
    std::cout << "r = " << r << std::endl;
    const boost::rational<int> q {-2, 4};
    std::cout << "q = " << q << std::endl;
    // display the product
   std::cout << "r * q = " << r * q << std::endl;
   // problem: rational doesn't handle integer overflow well
    const boost::rational<int> c {1, INT_MAX};
    std::cout << "c = " << c << std::endl;
   const boost::rational<int> d {1, 2};
    std::cout << "d = " << d << std::endl;
    // display the product - wrong answer
    std::cout << "c * d = " << c * d << std::endl;
    // solution: use safe integer in rational definition
    using safe_rational = boost::rational <
       boost::numeric::safe<int>
   // use rationals created with safe_t
    const safe_rational sc {1, INT_MAX};
    std::cout << "c = " << sc << std::endl;
    const safe_rational sd {1, 2};
    std::cout << "d = " << sd << std::endl;
    std::cout << "c * d = ";
    try {
        // multiply them. This will overflow
       std::cout << sc * sd << std::endl;
    catch (std::exception const& e) {
       // catch exception due to multiplication overflow
        std::cout << e.what() << std::endl;</pre>
   return 0;
}
```

which produces the following output

```
 \begin{array}{l} r = 1/2 \\ q = -1/2 \\ r * q = -1/4 \\ c = 1/2147483647 \\ d = 1/2 \\ c * d = 1/-2 \\ c = 1/2147483647 \\ d = 1/2 \\ c * d = multiplication overflow: positive overflow error \\ \end{array}
```

The rational library documentation is quite specific as to the type requirements placed on the underlying type. Turns out the our own definition of an integer type fulfills (actually surpasses) these requirements. So we have reason to hope that we can use

safe<int> as the underlying type to create what we might call a "safe_rational". This we have done in the above example where we demonstrate how to compose the rational library with the safe numerics library in order to create what amounts to a safe_rational library - all without writing a line of code! Still, things are not perfect. Since the rational numbers library implements its own checking for divide by zero by throwing an exception, the safe numerics code for handling this - included exception policy will not be respected. To summarize:

- In some cases safe types can be used as template parameters to other types to inject the concept of "no erroneous results" into the target type.
- Such composition is not guaranteed to work. The target type must be reviewed in some detail.

4. Background

This library started out as a re-implementation of the facilities provided by David LeBlanc's SafeInt Library. I found this library to be well done in every way. My main usage was to run unit tests for my embedded systems projects on my PC. Still, from my perspective it had a few issues.

- It was a lot of code in one header 6400 lines. Very unwieldy to understand, modify and maintain.
- I couldn't find separate documentation other than that in the header file.
- It didn't use **Boost** conventions for naming.
- It required porting to different compilers.
- · It had a very long license associated with it.
- I could find no test suite for the library.

Using later versions of C++ and the its standard library, template metaprogramming and Boost libraries I managed to (re)implement similar functionality in under 2000 ? lines of code. I promoted this version as a possible submission to the Boost. The feedback I received convinced me that no such library would be considered acceptable to the large majority of C++ programmers. It seems that the desire for maximum performance overrides any requirement that a program be known to be free of bugs. By this time I had a better idea of the opportunities available with the latest version of C++ (C++14) and resolved to address this issue by creating a library which would provide all the facilities of safe numerics at minimal runtime cost. The result is what you see here. The library now consists of 7000 lines of code, approximately 50 separate tests and more than 60 pages of documentation and examples.

5. Type Requirements

5.1. Numeric<T>

Description

A type is Numeric if it has the properties of a number.

More specifically, a type T is Numeric if there exists a specialization of std::numeric_limits<T>. See the documentation for the standard library class numeric_limits. The standard library includes such specializations for all the built-in numeric types. Note that this concept is distinct from the C++ standard library type traits is_integral and is_arithmetic. These latter fulfill the requirement of the concept Numeric. But there are types T which fulfill this concept for which is_arithmetic<T>::value == false. For example see safe_signed_integer<int>.

Notation

T, U, V	A type that is a model of Numeric	
---------	-----------------------------------	--

t, u	An object of a type modeling Numeric
os	An object of type std::base_ostream
is	An object of type std::base_istream

Associated Types

std::numeric_limits <t></t>	The numeric_limits class template provides a C++ program with information about various properties of the implementation's representation of the arithmetic types. See C++ standard 18.3.2.2.
-----------------------------	---

Valid Expressions

In addition to the expressions defined in Assignable the following expressions must be valid. Any operations which result in integers which cannot be represented as some Numeric type will throw an exception.

Table 1.1. General

Expression	Return Value
std::numeric_limits <t>::is_bounded</t>	true or false
std::numeric_limits <t>::is_specialized</t>	true or false
std::numeric_limits <t>::is_integer</t>	true or false
std::numeric_limits <t>::is_signed</t>	true or false
os << t	os &
is >> t	is &

Table 1.2. Unary Operators

Expression	Return Type	Semantics
-t	Т	Invert sign
+t	Т	unary plus - a no op
t	Т	post decrement
t++	Т	post increment
t	Т	pre decrement
++t	Т	pre increment

Table 1.3. Binary Operators

Expression	Return Type	Semantics
t - u	V	subtract u from t
t + u	V	add u to t
t * u	V	multiply t by u
t / u	Т	divide t by u
t % u	Т	t modulus u
t < u	bool	true if t less than u, false otherwise
t <= u	bool	true if t less than or equal to u, false otherwise
t > u	bool	true if t greater than u, false otherwise
t >= u	bool	true if t greater than or equal to u, false otherwise
t == u	bool	true if t equal to u, false otherwise
t != u	bool	true if t not equal to u, false otherwise
t = u	Т	assign value of u to t
t += u	Т	add u to t and assign to t
t -= u	Т	subtract u from t and assign to t
t *= u	Т	multiply t by u and assign to t
t /= u	Т	divide t by u and assign to t

Models

int, float, safe_signed_integer<int>, safe_signed_range<int>, etc.

Header

#include <boost/numeric/safe_numerics/concepts/numeric.hpp>

5.2. Integer<T>

Description

A type fulfills the requirements of an Integer if it has the properties of a integer.

More specifically, a type T is Integer if there exists a specialization of $std::numeric_limits<T>$ for which $std::numeric_limits<T>$. is_integer is equal to true. See the documentation for standard library class

numeric_limits. The standard library includes such specializations for all built-in numeric types. Note that this concept is distinct from the C++ standard library type traits is_integral and is_arithmetic. These latter fulfill the requirements of the concept Numeric. But there are types which fulfill this concept for which is_arithmetic<T>::value == false. For example see safe<int>.

Refinement of

Numeric

Notation

T, U, V	A type that is a model of the Integer	
t, u	An object of type modeling Integer	

Valid Expressions

In addition to the expressions defined in Numeric the following expressions must be valid.

Table 1.4. General

Expression	Value
std::numeric_limits <t>::is_inte</t>	g én ne

Expression	Return Type	Semantics
~t	Т	bitwise complement
t << u	Т	shift t left u bits
t >> u	Т	shift t right by u bits
t & u	V	and of t and u padded out to max # bits in t, u
t u	V	or of t and u padded out to max # bits in t, u
t^u	V	exclusive or of t and u padded out to max # bits in t, u
t <<= u	T	left shift the value of t by u bits
t >>= u	Т	right shift the value of t by u bits
t &= u	Т	and the value of t with u and assign to t
t = u	Т	or the value of t with u and assign to t
t ^= u	Т	exclusive or the value of t with u and assign to t

Models

int, safe<int>, safe_unsigned_range<0, 11>, etc.

Header

#include <boost/numeric/safe_numerics/concepts/integer.hpp>

5.3. SafeNumeric<T>

Description

This holds an arithmetic value which can be used as a replacement for built-in C++ arithmetic values. These types differ from their built-in counter parts in that the are guaranteed not to produce invalid arithmetic results. These operations return safe types rather than built-in types.

Refinement of

Numeric or Integer

Notation

Symbol	Description	
т, и	Types fulfilling Numeric or Integer type requirements.	
t, u	objects of types T, U	
S	A type fulfilling SafeNumeric type requirements	
s, s1, s2	objects of types S	
op	C++ infix operator supported by underlying type T	
prefix_op	C++ prefix operator: -, +, ~, ++, supported by underlying type T	
postfix_op	C++ postfix operator:++, supported by underlying type T	
assign_op	C++ assignment operator	

Valid Expressions

Expression	Result Type	Description
s op t	unspecified S	invoke C++ operator op and return another SafeNumeric type.
t op s	unspecified S	invoke C++ operator op and return another SafeNumeric type.
s1 op s2	unspecified S	invoke C++ operator op and return another SafeNumeric type.
prefix_op S	unspecified S	invoke C++ operator prefix_op and return another SafeNumeric type.

Expression	Result Type	Description
S postfix_op	unspecified S	invoke C++ operator postfix_op and return another SafeNumeric type.
s assign_op t	S &	convert t to type S and assign it to s.
t assign_op s	Т &	convert s to type T and assign it to s. If the value t cannot be represented as an instance of type S, it is an error.
S(t)	S	construct an instance of S from a value of type T. In this case, T is referred to as the base type of S. If the value t cannot be represented as an instance of type S, it is an exception condition is invoked.
S	S	construct an uninitialized instance of S.
T(s)	Т	implicit conversion of the value of s to type T. If the value of s cannot be correctly represented as a type T, an exception condition is invoked.
static_cast <t>(s)</t>	Т	convert the value of s to type T. If the value of s cannot be correctly represented as a type T, an exception condition is invoked.
is_safe <s></s>	std::true_type	type trait to query whether any type S fulfills the requirements for a SafeNumeric type.
base_type <s>::type</s>	Т	Retrieve the base type of a given safe type.
base_value(s)	Т	Retrieve the value of an instance of a safe type. This is equivalent to static_cast base_type <s>>(s).</s>

- The result of any binary operation where one or both of the operands is a SafeNumeric type is also a SafeNumeric type.
- All the expressions in the above table are constexpr expressions.
- Binary expressions which are not assignments and whose operands are both safe types require that promotion and exception policies of the operands be identical.
- Operations on safe types are supported if and only if the same operation is supported on the underlying types. For example, the binary operations |, &, ^ and ~ operations defined for safe unsigned integer types. But they are not defined for floating point types. Currently the are also defined for signed integer types. It's not clear that this is the correct decision. On one hand, usage of these operators on signed types is almost certainly an error in program logic. But trapping this as an error conflicts with the goal of making safe types "drop-in" replacements for the corresponding built-in types. In light of this, these operators are currently supported as they are for normal built-in types.
- Safe Numeric types will be implicitly converted to built-in types when appropriate. Here's an example:

This behavior supports the concept of safe<T> as being a "drop-in" replacement for a T.

Complexity Guarantees

There are no complexity guarantees explicitly enforced here. However, it would be very surprising if any implementation were to be more complex that O(0);

Invariants

The fundamental requirement of a SafeNumeric type is that it implements all C++ operations permitted on its base type in a way the prevents the return of an incorrect arithmetic result. Various implementations of this concept may handle circumstances which produce such results differently (throw exception, compile time trap, etc..). But no implementation should return an arithmetically incorrect result.

Models

```
safe<T>
safe_signed_range<-11, 11>
safe_unsigned_range<0, 11>
safe_signed_literal<4>
```

Header

#include <boost/numeric/safe_numerics/concepts/safe_numeric.hpp>

5.4. PromotionPolicy<PP>

Description

In C++, arithmetic operations result in types which may or may not be the same as the constituent types. A promotion policy determines the type of the result of an arithmetic operation. For example, in the following code

```
int x;
char y;
auto z = x + y
```

the type of z will be an int. This is a consequence for the standard rules for type promotion for C/C++ arithmetic. A key feature of library permits one to specify his own type promotion rules via a PromotionPolicy class.

Notation

PP	A type that full fills the requirements of a PromotionPollicy	
T, U	A type that is a model of the Numeric concept	
R	An object of type modeling Numeric which can be used to construct a SafeNumeric type.	

Valid Expressions

Any operations which result in integers which cannot be represented as some Numeric type will throw an exception. These expressions return a type which can be used as the basis create a SafeNumeric type.

Expression	Return Value
PP::addition_result <t, u="">::type</t,>	unspecified Numeric type
PP::subtraction_result <t, u="">::type</t,>	unspecified Numeric type
PP::multiplication_result <t, u="">::type</t,>	unspecified Numeric type
PP::division_result <t, u="">::type</t,>	unspecified Numeric type
PP::modulus_result <t, u="">::type</t,>	unspecified Numeric type
PP::comparison_result <t, u="">::type</t,>	bool
PP::left_shift_result <t, u="">::type</t,>	unspecified Numeric type
PP::right_shift_result <t, u="">::type</t,>	unspecified Numeric type
PP::bitwise_or_result <t, u="">::type</t,>	unspecified Numeric type
PP::bitwise_and_result <t, u="">::type</t,>	unspecified Numeric type
PP::bitwise_xor_result <t, u="">::type</t,>	unspecified Numeric type

Models

The library contains a number of pre-made promotion policies:

• boost::numeric::native

Use the normal C/C++ expression type promotion rules.

```
int x;
char y;
auto z = x + y; // could result in overflow
safe<int, native> sx;
auto sz = sx + y; // standard C++ code which detects errors
```

Type sz will be a SafeNumeric type based on int. If the result exceeds the maximum value that can be stored in an int, an error is detected.

The native policy is documented in Promotion Policies - native.

• boost::numeric::automatic

Use optimizing expression type promotion rules. These rules replace the normal C/C++ type promotion rules with other rules which are designed to result in more efficient computations. Expression types are promoted to the smallest type which can be guaranteed to hold the result without overflow. If there is no such type, the result will be checked for overflow. Consider the following example:

```
int x;
char y;
auto z = x + y; // could result in overflow
```

```
safe<int, automatic> sx;
auto sz = sx + y;
    // sz is a safe type based on long
    // hence sz is guaranteed not to overflow.
safe_unsigned_range<1, 4> a;
safe_unsigned_range<2, 4> b;
auto c = a + b; // c will be a safe type with a range [3,8] and cannot overflow
```

Type sz will be a SafeNumeric type which is guaranteed to hold he result of x + y. In this case that will be a long int (or perhaps a long long) depending upon the compiler and machine architecture. In this case, there will be no need for any special checking on the result and there can be no overflow.

Type of c will be a signed character as that type can be guaranteed to hold the sum so no overflow checking is done.

This policy is documented in Promotion Policies - automatic

Header

#include <boost/numeric/safe_numerics/concepts/promotion_policy.hpp>

5.5. ExceptionPolicy<EP>

Description

The exception policy specifies what is to occur when a safe operation cannot return a valid result. A type is an ExceptionPolicy if it has functions for handling exceptional events that occur in the course of safe numeric operations.

Notation

EP	A type that fulfills the requirements of an ExceptionPolicy	
e	A code from safe_numerics_error	
message	A const char * which refers to a text message about the cause of an exception	

Valid Expressions

Whenever an operation yield an invalid result, one of the following functions will be invoked.

Expression	Retu Valu	nfinvoked when: ne
<pre>EP::on_arithmetic_error(e, message)</pre>	void	The operation cannot produce valid arithmetic result such as overflows, divide by zero, etc.
EP::on_undefined_behavior(e, message)	void	The result is undefined by the C++ standard
<pre>EP::on_implementation_defined_behavior message)</pre>	(evpid	The result depends upon implementation defined behavior according to the C++ standard
<pre>EP::on_uninitialized_value(e, message)</pre>	void	A variable is not initialized

dispatch<EP>(const safe_numerics_error & e, const char * msg)

This function is used to invoke the exception handling policy for a particular exception code.

Synopsis

```
template<class EP>
constexpr void
dispatch<EP>(const boost::numeric::safe_numerics_error & e, char const * const & msg);
```

Example of use

```
#include <boost/safe_numerics/exception_policies.hpp"

dispatch<boost::numeric::loose_exception_policy>(
    boost::numeric::safe_numerics_error::positive_overflow_error,
    "operation resulted in overflow"
);
```

Models

The library header <boost/numerics/safe_numerics/exception_policies.hpp> contains a number of pre-made exception policies:

• boost::numeric::loose_exception_policy

Throw on arithmetic errors, ignore other errors. Some applications ignore these issues and still work and we don't want to update them.

• boost::numeric::loose_trap_policy

Same as above in that it doesn't check for various undefined behaviors but traps at compile time for hard arithmetic errors. This policy would be suitable for older embedded systems which depend on bit manipulation operations to work.

• boost::numeric::strict_exception_policy

Permit just about anything, throw at runtime on any kind of error. Recommended for new code. Check everything at compile time if possible and runtime if necessary. Trap or Throw as appropriate. Should guarantee code to be portable across architectures.

• boost::numeric::strict_trap_policy

Same as above but requires code to be written in such a way as to make it impossible for errors to occur. This naturally will require extra coding effort but might be justified for embedded and/or safety critical systems.

• boost::numeric::default_exception_policy

Alias for strict_exception_policy, One would use this first. After experimentation, one might switch to one of the above policies or perhaps use a custom policy.

Header

#include <boost/numeric/safe_numerics/concepts/exception_policy.hpp>

6. Types

6.1. safe<T, PP, EP>

Description

A safe<T, PP, EP can be used anywhere a type T can be used. Any expression which uses this type is guaranteed to return an arithmetically correct value or to trap in some way.

Notation

Symbol	Description	
Т	Underlying type from which a safe type is being derived	

Associated Types

PP	A type which specifies the result type of an expression using safe types.
EP	A type containing members which are called when a correct result cannot be returned

Template Parameters

Parameter Type Requirements		Description
Т	Integer <t></t>	The underlying type. Currently only integer types are supported
PP	PromotionPolicy <pp></pp>	Default value is boost::numeric::native
EP	Exception Policy <ep></ep>	Default value is boost::numeric::default_exception_policy

See examples below.

Model of

Integer

SafeNumeric

Valid Expressions

Implements all expressions and only those expressions defined by the SafeNumeric<T> type requirements. Note that all these expressions are constexpr. Thus, the result type of such an expression will be another safe type. The actual type of the result of such an expression will depend upon the specific promotion policy template parameter.

When a binary operand is applied to two instances of safe<T, PP, EP>on of the following must be true:

- The promotion policies of the two operands must be the same or one of them must be void
- The exception policies of the two operands must be the same or one of them must be void

If either of the above is not true, a compile error will result.

Examples of use

The most common usage would be safe<T> which uses the default promotion and exception policies. This type is meant to be a "drop-in" replacement of the intrinsic integer types. That is, expressions involving these types will be evaluated into result types which reflect the standard rules for evaluation of C++ expressions. Should it occur that such evaluation cannot return a correct result, an exception will be thrown.

There are two aspects of the operation of this type which can be customized with a policy. The first is the result type of an arithmetic operation. C++ defines the rules which define this result type in terms of the constituent types of the operation. Here we refer to these rules as "type promotion" rules. These rules will sometimes result in a type which cannot hold the actual arithmetic result of the operation. This is the main motivation for making this library in the first place. One way to deal with this problem is to substitute our own type promotion rules for the C++ ones.

As a Drop-in replacement for standard integer types.

The following program will throw an exception and emit an error message at runtime if any of several events result in an incorrect arithmetic type. Behavior of this program could vary according to the machine architecture in question.

```
#include <exception>
#include <iostream>
#include <boost/numeric/safe.hpp>

void f(){
    using namespace boost::numeric;
    safe<int> j;
    try {
        safe<int> i;
        std::cin >> i; // could overflow !
        j = i * i; // could overflow
    }
    catch(std::exception & e){
        std::cout << e.what() << std::endl;
    }
    std::cout << j;
}</pre>
```

The term "drop-in replacement" reveals the aspiration of this library. In most cases, this aspiration is realized. In the following example, the normal implicit conversions function the same for safe integers as they do for built-in integers.

When the safe<long> is implicitly converted to an int when calling f, the value is checked to be sure that it is within the legal range of an int and will invoke an exception if it cannot. We can easily verify this by altering the exception handling policy in the above example to loose_trap_policy. This will invoke a compile time error on any conversion might invoke a runtime exception.

```
#include #include <safe_integer.hpp>
using namespace boost::numeric;

int f(int i){
    return i;
}

using safe_t = safe<long, native, loose_trap_policy>;

int main(){
    const long x = 97;
    f(x); // OK - implicit conversion to int
    const safe_t y = 97;
    f(y); // Would be OK, but will invoke compile time error
    return 0;
}
```

But this raises it's own questions. We can see that in this example, the program can never fail:

- The value 97 is assigned to y
- · y is converted to an int
- · and used as an argument to f

The conversion can never fail because the value of 97 can always fit into an int. But the library code can't detect this and emits the checking code even though it's not necessary.

This can be addressed by using a safe_literal. A safe literal can contain one and only one value. All the functions in this library are marked constexpr. So it can be determined at compile time that conversion to an int can never fail and no runtime checking code need be emitted. Making this small change will permit the above example to run with zero runtime overhead while guaranteeing that no error can ever occur.

With this trivial example, such efforts would hardly be deemed necessary. But in a more complex case, perhaps including compile time arithmetic expressions, it could be much more difficult to verify that the constant is valid and/or no checking code is needed. And there is also possibility that over the life time of the application, the compile time constants might change, thus rendering any ad hoc analyse obsolete. Using safe_literal will future-proof your code against well-meaning, but code-breaking updates.

Adjust type promotion rules.

Another way to avoid arithmetic errors like overflow is to promote types to larger sizes before doing the arithmetic.

Stepping back, we can see that many of the cases of invalid arithmetic wouldn't exist if the result types were larger. So we can avoid these problems by replacing the C++ type promotion rules for expressions with our own rules. This can be done by specifying a non-default type promotion policy automatic. The policy stores the result of an expression in the smallest size that can accommodate the largest value that an expression can yield. All the work is done at compile time - no checking for exceptions is necessary (input is of course an exception). The following example illustrates this.

```
#include <boost/numeric/safe.hpp>
#include <iostream>
int main(int, char[]){
    using safe_int = safe<
        int, boost::numeric::automatic,
        boost::numeric::default_exception_policy
    >;
    safe_int i;
    std::cin >> i; // might throw exception
    auto j = i * i; // won't ever trap - result type can hold the maximum value of i * i
    static_assert(boost::numeric::is_safe<decltype(j)>::value); // result is another safe type
    static_assert(
        std::numeric_limits<decltype(i * i)>::max() >=
        std::numeric_limits<safe_int>::max() * std::numeric_limits<safe_int>::max()
    ); // always true
   return 0;
}
```

Header

#include <boost/numeric/safe_numerics/safe_integer.hpp>

6.2. safe_signed_range<MIN, MAX, PP, EP> and safe_unsigned_range<MIN, MAX, PP, EP>

Description

This type holds a signed or unsigned integer in the closed range [MIN, MAX]. A safe_signed_range<MIN, MAX, PP, EP> or safe_unsigned_range<MIN, MAX, PP, EP> can be used anywhere an arithmetic type is permitted. Any expression which uses either of these types is guaranteed to return an arithmetically correct value or to trap in some way.

Notation

Symbol	Description
MIN, MAX	Minimum and maximum values that the range can represent.

Associated Types

PP	Promotion Policy. A type which specifies the result type of an expression using safe types.
EP	Exception Policy. A type containing members which are called when a correct result cannot be returned

Template Parameters

Parameter	Requirements	Description
MIN	must be a non-negative literal	The minimum non-negative integer value that this type may hold
MAX	must be a non-negative literal	The maximum non-negative integer value that this type may hold
	MIN <= MAX	must be a valid closed range
PP	PromotionPolicy <pp></pp>	Default value is boost::numeric::native
EP	Exception Policy <ep></ep>	Default value is boost::numeric::default_exception_policy

Model of

Integer

SafeNumeric

Valid Expressions

Implements all expressions and only those expressions defined by the SafeNumeric type requirements. Thus, the result type of such an expression will be another safe type. The actual type of the result of such an expression will depend upon the specific promotion policy template parameter.

Example of use

```
#include <type_traits>
#include <../include/safe_integer.hpp>
#include <../include/safe_range.hpp>

#include <../include/utility.hpp>

using namespace boost::numeric;

void f(){
    safe_unsigned_range<7, 24> i;
    // since the range is included in [0,255], the underlying type of i
    // will be an unsigned char.
    i = 0; // throws out_of_range exception
    i = 9; // ok
    i *= 9; // throws out_of_range exception
```

```
i = -1; // throws out_of_range exception
std::uint8_t j = 4;
auto k = i + j;

// if either or both types are safe types, the result is a safe type
// determined by promotion policy. In this instance
// the range of i is [7, 24] and the range of j is [0,255].
// so the type of k will be a safe type with a range of [7,279]
static_assert(
    is_safe<decltype(k)>::value
    && std::numeric_limits<decltype(k)>::min() == 7
    && std::numeric_limits<decltype(k)>::max() == 279,
    "k is a safe range of [7,279]"
);
}
```

Header

#include <boost/numeric/safe_numerics/safe_range.hpp>

6.3. safe_signed_literal<Value, PP, EP> and safe_unsigned_literal<Value, PP, EP>

Description

A safe type which holds a literal value. This is required to be able to initialize other safe types in such a way that an exception code is not generated. It is also useful when creating constexpr versions of safe types. It contains one immutable value known at compile time and hence can be used in any constexpr expression.

Associated Types

PP	A type which specifies the result type of an expression using safe types.
EP	A type containing members which are called when a correct result cannot be returned

Template Parameters

Parameter	Type Requirements	Description
Value	Integer	value used to initialize the literal
PP	PromotionPolicy <pp></pp>	Default value is void
EP	Exception Policy <ep></ep>	Default value is void

Model of

Integer

SafeNumeric

LiteralType

Inherited Valid Expressions

safe literal types are immutable. Hence they only inherit those valid expressions which don't change the value. This excludes assignment, increment, and decrement and all unary operators except unary -, + and ~. Other than that, they can be used anywhere a SafeNumeric type can be used. Note that the default promotion and exception policies are void. This is usually convenient since when a safe literal is used in a binary operation, this will inherit the policies of the other type. On the other hand, this can be inconvenient when operands of a binary expression are both safe literals. This will fail to compile since there are no designated promotion and exception policies. They way to address this to assign specific policies as in this example.

```
template<typename T>
using compile_time_value = safe_signed_literal<T>;

constexpr compile_time_value<1000> x;
constexpr compile_time_value<0> y;

// should compile and execute without problem

std::cout << x << '\n';

// all the following statements should fail to compile
constexpr safe<int> z = x / y;
```

New Valid Expression

Expression	Result Type	Description
t op s	unspecified S	invoke C++ operator op and return another SafeNumeric type.
s1 op s2	unspecified S	invoke C++ operator op and return another SafeNumeric type.
prefix_op S	unspecified S	invoke C++ operator prefix_op and return another SafeNumeric type.
S postfix_op	unspecified S	invoke C++ operator postfix_op and return another SafeNumeric type.
s assign_op t	S1	convert t to type S and assign it to s. If the value t cannot be represented as an instance of type S, it is an error.
S(t)	unspecified S	construct an instance of S from a value of type T. If the value t cannot be represented as an instance of type S, it is an error.
S	S	construct an uninitialized instance of S.
is_safe <s></s>	std::true_type Or std::false_type	type trait to query whether any type S fulfills the requirements for a SafeNumeric type.
static_cast <t>(s)</t>	Т	convert the value of s to type T. If the value of s cannot be correctly represented as a type T, it is an error.

Example of use

```
#include <boost/numeric/safe_numerics/safe_literal.hpp>
```

constexpr boost::numeric::safe_signed_literal<42> x;

Header

#include <boost/numeric/safe_numerics/safe_literal.hpp>

6.4. exception

Description

Here we describe the data types used to refer to exceptional conditions which might occur. Note that when we use the word "exception", we don't mean the C++ term which refers to a data type, but rather the colloquial sense of a anomaly, irregularity, deviation, special case, isolated example, peculiarity, abnormality, oddity; misfit, aberration or out of the ordinary occurrence. This concept of "exception" is more complex that one would thing and hence is not manifested by a single simple type. A small number of types work together to implement this concept within the library.

We've leveraged on the std::error_code which is part of the standard library. We don't use all the facilities that it offers but it's not an exact match, but it's useful for our purposes.

enum class safe_numerics_error

The following values are those which a numeric result might return. They resemble the standard error codes used by C++ standard exceptions. This resemblance is coincidental and they are wholly unrelated to any codes of similar names. The reason for the resemblance is that the library started it's development using the standard library codes. But as development progressed it became clear that the original codes weren't sufficient so now they stand on their own. Here are a list of error codes. The description of what they mean is

Symbol	Description
success	successful operation - no error returned
positive_overflow_error	A positive number is too large to be represented by the data type
negative_overflow_error	The absolute value of a negative number is too large to be represented by the data type.
domain_error	the result of an operation is outside the legal range of the result.
range_error	an argument to a function or operator is outside the legal range - e.g. sqrt(-1).
precision_overflow_erro	r precision was lost in the course of executing the operation.
underflow_error	A number is too close to zero to be represented by the data type.
uninitialized_value	According to the C++ standard, the result may be defined by the application. e.g. $16 >> 10$ will result the expected result of 0 on most machines.

The above listed codes can be transformed to a instance of type std::error_code with the function:

std::error_code make_error_code(safe_numerics_error e)

This object can be

enum class safe_numerics_actions

The above error codes are classified into groups according to how such exceptions should be handled. The following table shows the possible actions that an error could be mapped to.

Symbol	Description
no_action	successful operation - no action action required
uninitialized_value	report attempt to use an uninitialized value - not currently used
arithmetic_error	report an arithmetic error
implementation_defined_	betport am operation which the C++ standard permits but fails to specify
undefined_behavior	report an operation whose result is undefined by the C++ standard.

Translation of a safe_numerics_error into the corresponding safe_numerics_action can be accomplished with the following function:

```
constexpr enum safe_numerics_actions
make_safe_numerics_action(const safe_numerics_error & e);
```

See Also

- C++ Standard Library version The C++ standard error handling utilities.
- Thinking Asynchronously in C++ Another essential reference on the design and usage of the error_code

Header

#include <boost/numeric/safe_numerics/exception.hpp>

6.5. exception_policy<AE, IDB, UB, UV>

Description

Create a valid exception policy from 4 function objects. This specifies the actions to be taken for different types of invalid results.

Template Parameters

Paran	nellerpe Requirements	Invoked when:
AE	Function object callable with the expression AE(e, message)	The operation cannot produce valid arithmetic result such as overflows, divide by zero, etc.
UB	Function object callable with the expression UB(e, message)	The result is undefined by the C++ standard

Paran	ne Te rpe Requirements	Invoked when:
IDB	Function object callable with the expression IDB(e,	The result depends upon implementation defined behavior according to the C++ standard
UV	Function object callable with the expression UV(e, message)	A variable is not initialized

Model of

ExceptionPolicy

Inherited Valid Expressions

This class implements all the valid operations from the type requirements ExceptionPolicy. Aside from these, there are no other operations implemented.

Function Objects

In order to create an exception policy, one needs some function objects. The library includes some appropriate examples of these:

Name	Description
ignore_exception	Ignore any runtime exception and just return - thus propagating the error. This is what would happen with unsafe data types
throw_exception	throw an exception of type std::system_error
trap_exception	Invoke a function which is undefined. Compilers will include this function if and only if there is a possibility of a runtime error. Conversely, This will create a compile time error if there is any possibility that the operation will fail at runtime. Use the action to guarantee that your application will never produce an invalid result. Any operation invoke

But of course one is free to provide his own. Here is an example of a function object which would could be used exception conditions.

Policies Provided by the library

The above function object can be composed into an exception policy by this class. The library provides common policies all ready to use. In the table below, the word "loose" is used to indicate that implementation defined and undefined behavior is not considered an exceptional condition, while "strict" means the opposite. The word "exception" means that a runtime exception will be thrown. The word "trap" means that the mere possibility of an error condition will result in a compile time error.

Name	Description
loose_exception_policy	Throws runtime exception on any arithmetic error. Undefined and implementation defined behavior is permitted as long as it does not produce an arithmetic error.
loose_trap_policy	Invoke a compile time error in any case where it's possible to result in an arithmetic error.
strict_exception_policy	Throws runtime exception on any arithmetic error. Any undefined or implementation defined behavior also results in throwing an exception.
strict_trap_policy	Invoke a compile time error in any case where it's possible to result in an arithmetic error, undefined behavior or implementation defined behavior
default_exception_polic	yan alias for strict_exception_policy

If none of the above suit your needs, you're free to create your own. Here is one where use the logging function object defined above as a component in a loose exception policy which logs any arithmetic errors and ignores any other types of errors.

Header

#include <boost/numeric/safe_numerics/concept/exception_policy.hpp>

6.6. Promotion Policies

native

Description

This type contains the functions to return a safe type corresponding to the C++ type resulting from a given arithmetic operation.

Usage of this policy with safe types will produce the exact same arithmetic results that using normal unsafe integer types will. Hence this policy is suitable as a drop-in replacement for these unsafe types. Its main function is to trap incorrect arithmetic results when using C++ for integer arithmetic.

Model of

PromotionPolicy

As an example of how this works consider C++ rules from section 5 of the standard - "usual arithmetic conversions".

```
void int f(int x, int y){
  auto z = x + y; // z will be of type "int"
  return z;
}
```

According to these rules, z will be of type int. Depending on the values of x and y, z may or may not contain the correct arithmetic result of the operation x + y.

```
using safe_int = safe<int, native>;
void int f(safe_int x, safe_int y){
   auto z = x + y; // z will be of type "safe_int"
   return z;
}
```

Example of use

The following example illustrates the native type being passed as a template parameter for the type safe<int>. This example is slightly contrived in that safe<int> has native as its default promotion parameter so explicitly using native is not necessary.

```
#include <cassert>
#include <boost/numeric/safe_numerics/safe_integer.hpp>
#include <boost/numeric/safe_numerics/native.hpp>
int main(){
   using namespace boost::numeric;
    // use native promotion policy where C++ standard arithmetic
    // might lead to incorrect results
   using safe_int8 = safe<std::int8_t, native>;
    try{
        safe_int8 x = 127;
        safe_int8 y = 2;
       safe_int8 z;
        // rather than producing an invalid result an exception is thrown
        z = x + y;
       assert(false); // never arrive here
    catch(std::exception & e){
        // which we can catch here
       std::cout << e.what() << std::endl;</pre>
   }
    // When result is an int, C++ promotion rules guarentee
    // that there will be no incorrect result.
   // In such cases, there is no runtime overhead from using safe types.
   safe_int8 x = 127;
   safe_int8 y = 2;
   safe<int, native> z; // z can now hold the result of the addition of any two 8 bit numbers
    z = x + y; // is guaranteed correct without any runtime overhead or exception.
   return 0;
}
```

Notes

See Chapter 5, Expressions, C++ Standard

Header

#include <boost/numeric/safe_numerics/native.hpp>

automatic

Description

This type contains the meta-functions to return a type with sufficient capacity to hold the result of a given binary arithmetic operation.

The standard C/C++ procedure for executing arithmetic operations on operands of different types is:

- Convert operands to some common type using a somewhat elaborate elaborate rules defined in the C++ standard.
- Execute the operation.
- If the result of the operation cannot fit in the common type of the operands, discard the high order bits.

The automatic promotion policy replaces the standard C/C++ procedure for the following one:

- Convert operands to some common type using to the following rules.
 - For addition. If the operands are both unsigned the common type will be unsigned. Otherwise it will be signed.
 - For subtraction, the common type will be signed.
 - For left/right shift, the sign of the result will be the sign of the left operand.
 - For all other types of operants, if both operands are unsigned the common type will be unsigned. Otherwise, it will be signed.
- Determine the smallest size of the signed or unsigned type which can be guaranteed hold the result.
- If this size exceeds the maximum size supported by the compiler, use the maximum size supported by the compiler.
- Execute the operation.
 - Convert each operand to the common type.
 - If the result cannot be contained in the result type as above, invoke an error procedure.
 - Otherwise, return the result in the common type

This type promotion policy is applicable only to safe types whose base type is an Integer type.

Model of

PromotionPolicy

Example of use

The following example illustrates the automatic type being passed as a template parameter for the type safe<int>.

#include <boost/safe_numerics/safe_integer.hpp>

```
#include <boost/safe_numerics/automatic.hpp>
int main(){
    using namespace boost::numeric;
    // use automatic promotion policy where C++ standard arithmetic
    // might lead to incorrect results
    using safe_t = safe<std::int8_t, automatic>;

    // In such cases, there is no runtime overhead from using safe types.
    safe_t x = 127;
    safe_t y = 2;
    // z is guaranteed correct without any runtime overhead or exception.
    auto z = x + y;
    return 0;
}
```

Header

#include <boost/numeric/safe_numerics/automatic.hpp>

cpp<int C, int S, int I, int L, int LL>

Description

This policy is used to promote safe types in arithmetic expressions according to the rules in the C++ standard. But rather than using the native C++ standard types supported by the compiler, it uses types whose length in number of bits is specified by the template parameters.

This policy is useful for running test programs which use C++ portable integer types but which are destined to run on an architecture which is different than the one on which the test program is being built and run. This can happen when developing code for embedded systems. Algorithms developed or borrowed from one architecture but destined for another can be tested on the desktop.

Note that this policy is only applicable to safe types whose base type is a type fulfilling the type requirements of Integer.

Template Parameters

Parameter	Туре	Description	
С	int	Number of bits in a char	
S	int	Number of bits in a short	
I	int	Number of bits in an integer	
L	int	Number of bits in a long	
LL	int	Number of bits in a long long	

Model of

PromotionPolicy

Example of Use

Consider the following problem. One is developing software which uses a very small microprocessor and a very limited C compiler. The chip is so small, you can't print anything from the code, log, debug or anything else. One debugs this code by using the "burn" and "crash" method - you burn the chip (download the code), run the code, observe the results, make changes and try again. This is a crude method which is usually the one used. But it can be quite time consuming.

Consider an alternative. Build and compile your code in testable modules. For each module write a test which exercises all the code and makes it work. Finally download your code into the chip and - voilà - working product. This sounds great, but there's one problem. Our target processor - in this case a PIC162550 from Microchip Technology is only an 8 bit CPU. The compiler we use defines INT as 8 bits. This (and a few other problems), make our algorithm testing environment differ from our target environment. We can address this by defining INT as a safe integer with a range of 8 bits. By using a custom promotion policy, we can force the evaluation of C++ expressions in the test environment to be the same as that in the target environment. Also in our target environment, we can trap any overflows or other errors. So we can write and test our code on our desktop system and download the code to the target knowing that it just has to work. This is a huge time saver and confidence builder. The following code is taken from a real project which has used this method.

```
#include "../include/safe_integer.hpp"
#include "../include/cpp.hpp"
// Stepper Motor Control
// emululate evironment for pic162550
// data widths used by the CCS compiler for pic 16xxx series
using pic16_promotion = boost::numeric::cpp<
   8, // char
      // short - not used by pic 16xxxx
      // int
   16, // long
   32 // long long
>;
template <typename T> // T is char, int, etc data type
using safe_t = boost::numeric::safe<
   Τ,
   pic16_promotion,
   boost::numeric::loose_trap_policy // use for compiling and running tests
using int8 = safe_t<std::int8_t>;
using int16 = safe t<std::int16 t>;
using int32 = safe_t<std::int32_t>;
using uint8 = safe_t<std::uint8_t>;
using uint16 = safe_t<std::uint16_t>;
using uint32 = safe_t<std::uint32_t>;
// Mock defines, functions etc which are in the "real application"
// return value in steps
/*
Use the formula:
   stopping dist = v **2 / a / 2
```

```
uint16 get_stopping_distance(LEMPARAMETER velocity){
   int32 d;
   d = velocity;
   d *= velocity;
   d /= lem.acceleration;
   d /= 2;
   return d;
}
```

Note the usage of the compile time trap policy in order to detect at compile time any possible error conditions. As I write this, this is still being refined. Hopefully this will be available by the time you read this.

Header

#include <boost/numeric/safe_numerics/cpp.hpp>

7. Exception Safety

All operations in this library are exception safe and meet the strong guarantee.

8. Library Implementation

This library should compile and run correctly on any conforming C++14 compiler.

The Safe Numerics library is implemented in terms of some more fundamental software components described here. It is not necessary to know about these components to use the library. This information has been included to help those who want to understand how the library works so they can extend it, correct bugs in it, or understand its limitations. These components are also interesting in their own right. For all these reasons, they are documented here.

In general terms, the library works in the following manner:

- The library defines "safe" versions of C++ primitive arithmetic types such as int, unsigned int, etc.
- Arithmetic operators are defined for these "safe" types. These operators are enhanced versions of the standard C/C++ implementations. These operators are declared and implemented in the files "safe_base.hpp" and "safe_base_operations.hpp".
- For binary operators, verify that both operands have the same promotion and and exception handling policies. If they don't, invoke compilation error.
- Retrieve range of values for each operand of type T from std::numeric_limits<T>::min() and std::numeric_limits<T>::max(). A range is a pair of values representing a closed interval with a minimum and maximum value.
- These ranges are cast to equivalent values of the result type, R. It's possible that values cannot be cast to the result type so the result of the cast is returned as a variant type, checked_result<R>. checked_result<R> may hold either a value of type R or a safe_numerics_error value indicating why the cast could not be accomplished. Ranges are represented as a pair of values of the type checked_result<R>.
- <a href="checked_result<R">checked_result<R> can be considered enhanced versions of the underlying type R. Operations which are legal on values of type R such as +, -, ... are also legal on values of <a href="checked_result<R">checked_result<R>. The difference is that the latter can record operation failures and propagate such failures to subsequent operations.checked_result<a href="checked_result<R">checked_result. Is implemented in the header file "checked_result.hpp". Operations on such types are implemented in "checked_result_operations.hpp".
- Given the ranges of the operands, determine the range of the result of the operation using compile-time interval arithmetic. The constexpr facility of C++14 permits the range of the result to be calculated at compile time. Interval arithmetic is

implemented in the header file "interval.hpp". The range of the result is also represented as a pair of values of the type checked_result<R>.

- If the range of the result type includes only arithmetically valid values, the operation is guaranteed to produce an arithmetically correct result and no runtime checking is necessary. The operation invokes the original built-in C/C++ operation and returns the result value.
- Otherwise, operands are cast to the result type, R, according to the selected promotion policy. These "checked" cast operations return values of type checked_result<R>.
- If either of the casting operations fails, an exception is handled in accordance with the exception policy.
- Otherwise, the operation is performed as another "checked operation". These free functions mirror the normal operators +, -, *, ... except that rather than returning values of type R, they return values of the type checked_result<R>. They are defined in files "checked_default.hpp", "checked_integer.hpp", "checked_float.hpp".
- If the operation is not successful, the designated exception policy function is invoked.
- Otherwise, the result value is returned.
- In all cases, result values are returned as a safe<R> type with the above calculated result range.

The following components realize the design described here.

8.1. checked result<R>

Description

checked_result is a special kind of variant class designed to hold the result of some operation. It can hold either the result of the operation or information on why the operation failed to produce a valid result. It is similar to other types proposed for and/or included to the C++ standard library or Boost such as expected, variant, optional and outcome.

- All instances of checked_result<R> are immutable. That is, once constructed, they cannot be altered.
- There is no default constructor.
- checked_result<R> is never empty.
- binary operations can be invoked on a pair of checked_result<R> instances if and only if the underlying type (R) is identical for both instances.
- Comparison operations will return a boost::logic::tribool. Other binary operations will a value of the same type as the arguments.
- unary operations can be invoked on checked_result<R> instances. They will return a value of the same type.

Think of checked<R> as an "extended" version of R which can hold all the values that R can hold in addition other "special values". For example, consider checked<int>.

Notation

Symbol	Description	
R	Underlying type	
r	An instance of type R	

Symbol	Description	
c, c1, c2	an instance of checked_result <r></r>	
t	an instance of checked_result <t> for some type T not necessarily the same as R</t>	
е	An instance of type safe_numerics_error	
os	A type convertible to std::basic_ostream	
os	An instance of type convertible to std::basic_ostream	

Template Parameters

R must model the type requirements of Numeric

Parameter	Description
R	Underlying type

Model of

Numeric

Valid Expressions

All expressions are constexpr.

Expression	Return Type	Semantics
checked_result(r)	checked_result<	Reonstructor with valid instance of R
checked_result <r>(t)</r>	checked_result<	Reonstructor with checked_result <t> where T is not R. T must be convertible to R.</t>
checked_result(e, msg)	checked_result<	Reonstructor with error information
static_cast <r>(c)</r>	R	extract wrapped value - compile time error if not possible
static_cast <safe_numerics_error< td=""><td>> \$afe_numerics_e</td><td>restract wrapped value - may return safe_numerics_error::success if there is no error</td></safe_numerics_error<>	> \$a fe_numerics_e	restract wrapped value - may return safe_numerics_error::success if there is no error
static_cast <const *="" char="">(c)</const>	const char *	returns pointer to the included error message
c.exception()	bool	true if checked_result contains an error condition.
<pre>c < t c >= t c > t c <= t c == t c != t</pre>	boost::logic::t	rcompare the wrapped values of two checked_result instances. If either one contains an error_type value, return boost::logic::tribool::indeterminant.

Expression	Return Type	Semantics
c1 + c2 c1 - c2 c1 * c2 c1 / c2 c1 % c2 c1 c2 c1 & c2 c1 ^ c2 c1 ^ c2 c1 << c2 c1 << c2	checked_result<	Rreturns a new instance of checked_result <r>.</r>
os << c	os	writes result to output stream. If the result is an error it writes the string corresponding to the error message. Otherwise, it writes the numeric value resulting from the operation. Returns reference to output stream.

Example of use

```
#include <exception>
#include <iostream>
#include "../include/checked_result.hpp"
#include "../include/checked_result_operations.hpp"
int main(){
   using ext_uint = boost::numeric::checked_result<unsigned int>;
   const ext_uint x{4};
   const ext_uint y{3};
   // operation is a success!
   std::cout << "success! x - y = " << x - y;
   // subtraction would result in -1, and invalid result for an unsigned value
   std::cout << "problem: y - x = " << y - x;
   const ext_uint z = y - x;
   std::cout << "z = " << z;
   // sum of two negative overflows is a negative overflow.
   std::cout << "z + z" << z + z;
   return 0;
}
```

See Also

ExceptionPolicy

Header

```
#include <boost/numeric/safe_numerics/checked_result.hpp>
#include <boost/numeric/safe_numerics/checked_result_operations.hpp>
```

8.2. Checked Arithmetic

Synopsis

```
// safe casting on primitive types
template<class R, class T>
checked_result<R> constexpr checked::cast(const T & t);
// safe addition on primitive types
template < class R>
checked_result<R> constexpr checked::add(const R & t, const R & u);
// safe subtraction on primitive types
template<class R>
checked_result<R> constexpr checked::subtract(const R & t, const R & u);
// safe multiplication on primitive types
template<class R>
checked_result<R> constexpr checked::multiply(const R & t, const R & u);
// safe division on primitive types
template<class R>
checked_result<R> constexpr checked::divide(const R & t, const R & u);
// safe modulus on primitive types
template<class R>
checked_result<R> constexpr checked::modulus(const R & t, const R & u);
// safe less than predicate on primitive types
template<class R>
bool constexpr checked::less_than(const R & t, const R & u);
// safe greater_than_equal predicate on primitive types
template<class R>
bool constexpr checked::greater_than_equal(const R & t, const R & u);
// safe greater_than predicate on primitive types
template<class R>
bool constexpr checked::greater_than(const R & t, const R & u);
// safe less_than_equal predicate on primitive types
template<class R>
bool constexpr checked::less_than_equal(const R & t, const R & u);
// safe equal predicate on primitive types
template<class R>
bool constexpr checked::equal(const R & t, const R & u);
// left shift
template<class R>
checked_result<R> constexpr checked::left_shift(const R & t, const R & u);
// right shift
template<class R>
checked_result<R> constexpr checked::right_shift(const R & t, const R & u);
// bitwise operations
template<class R>
```

```
checked_result<R> constexpr checked::bitwise_or(const R & t, const R & u);

template<class R> checked_result<R> constexpr checked::bitwise_and(const R & t, const R & u);

template<class R> checked_result<R> constexpr checked::bitwise_xor(const R & t, const R & u);
```

Description

Perform binary operations on arithmetic types. Return either a valid result or an error code. Under no circumstances should an incorrect result be returned.

Type requirements

All template parameters of the functions must model Numeric type requirements.

Complexity

Each function performs one and only one arithmetic operation.

Example of use

```
#include <boost/numeric/safe_numerics/checked_default.hpp>
checked_result<int> r = checked::multiply<int>(24, 42);
```

Notes

Some compilers have command line switches (e.g. -ftrapv) which enable special behavior such that erroneous integer operations are detected at run time. The library has been implemented in such a way that these facilities are not used. It's possible they might be helpful in particular environment. These could be exploited by re-implementing some functions in this library.

See Also

checked_result<R>

Header

```
#include <boost/numeric/safe_numerics/checked_default.hpp>
#include <boost/numeric/safe_numerics/checked_integer.hpp>
#include <boost/numeric/safe_numerics/checked_float.hpp>
```

8.3. interval<R>

Description

A closed arithmetic interval represented by a pair of elements of type R. In principle, one should be able to use Boost.Interval library for this. But the functions in this library are not constexpr. Also, this Boost.Interval is more complex and does not

support certain operations such bit operations. Perhaps some time in the future, Boost.Interval will be used instead of this interval<R> type.

Template Parameters

R must model the type requirements of Numeric. Note this in principle includes any numeric type including floating point numbers and instances of checked_result<R>.

Notation

Symbol	Description	
I	An interval type	
i, j	An instance of interval type	
R	Numeric types which can be used to make an interval	
r	An instance of type R	
р	An instance of std::pair <r, r=""></r,>	
1, u	Lowermost and uppermost values in an interval	
os	std::basic_ostream <class chart,="" class="" traits="std::char_traits<CharT">></class>	

Associated Types

checked_result	holds either the result of an operation or information as to why it failed
----------------	--

Valid Expressions

Note that all expressions are constexpr.

Expression	Return Type	Semantics
interval <r>(1, u)</r>	interval <r></r>	construct a new interval from a pair of limits
interval <r>(p)</r>	interval <r></r>	construct a new interval from a pair of limits
interval <r>(i)</r>	interval <r></r>	copy constructor
make_interval <r>()</r>	interval <r></r>	return new interval with std::numric_limits <r>::min() and std::numric_limits<r>::max()</r></r>
make_interval <r>(c R &r)</r>	onistterval <r></r>	return new interval with std::numric_limits <r>::min() and std::numric_limits<r>::max()</r></r>
i.1	R	lowermost value in the interval i
i.u	R	uppermost value in the interval i

Expression	Return Type	Semantics		
i.includes(j)	boost::logic::trib	boost::logic::tribometurn true if interval i includes interval j		
i.excludes(j)	boost::logic::trib	oodturn true if interval i includes interval j		
i.includes(t)	bool	return true if interval i includes value t		
i.excludes(t)	bool	return true if interval i includes value t		
i + j	interval <r></r>	add two intervals and return the result		
i - j	interval <r></r>	subtract two intervals and return the result		
i * j	interval <r></r>	multiply two intervals and return the result		
i / j	interval <r></r>	divide one interval by another and return the result		
i % j	interval <r></r>	calculate modulus of one interval by another and return the result		
i << j	interval <r></r>	calculate the range that would result from shifting one interval by another		
i >> j	interval <r></r>	calculate the range that would result from shifting one interval by another		
i j	interval <r></r>	range of values which can result from applying \mid to any pair of operands from I and j		
i & j	interval <r></r>	range of values which can result from applying & to any pair of operands from I and j		
i ^ j	interval <r></r>	range of values which can result from applying ^ to any pair of operands from I and j		
t < u	boost::logic::trib	odnue if every element in t is less than every element in u		
t > u	boost::logic::trib	otatue if every element in t is greater than every element in u		
t <= u	boost::logic::trib	odaue if every element in t is less than or equal to every element in u		
t >= u	boost::logic::trib	odaue if every element in t is greater than or equal to every element in u		
t == u	bool	true if limits are equal		
t != u	bool	true if limits are not equal		
os << i	os &	print interval to output stream		

Example of use

```
#include <iostream>
#include <cstdint>
#include <cassert>
```

```
#include <boost/numeric/safe_numerics/interval.hpp>
int main(){
    std::cout << "test1" << std::end1;
    interval<std::int16_t> x = {-64, 63};
    std::cout << "x = " << x << std::end1;
    interval<std::int16_t> y(-128, 126);
    std::cout << "y = " << y << std::end1;
    assert(static_cast<interval<std::int16_t>>(add<std::int16_t>(x,x)) == y);
    std::cout << "x + x =" << add<std::int16_t>(x, x) << std::end1;
    std::cout << "x - x = " << subtract<std::int16_t>(x, x) << std::end1;
    return 0;
}</pre>
```

Header

#include <boost/numeric/safe_numerics/interval.hpp>

8.4. safe_compare<T, U>

Synopsis

```
// compare any pair of integers
template<class T, class U>
bool constexpr safe_compare::less_than(const T & lhs, const U & rhs);

template<class T, class U>
bool constexpr safe_compare::greater_than(const T & lhs, const U & rhs);

template<class T, class U>
bool constexpr safe_compare::less_than_equal(const T & lhs, const U & rhs);

template<class T, class U>
bool constexpr safe_compare::greater_than_equal(const T & lhs, const U & rhs);

template<class T, class U>
bool constexpr safe_compare::equal(const T & lhs, const U & rhs);

template<class T, class U>
bool constexpr safe_compare::equal(const T & lhs, const U & rhs);
```

Description

Compare two primitive integers. These functions will return a correct result regardless of the type of the operands. Specifically it is guaranteed to return the correct arithmetic result when comparing signed and unsigned types of any size. It does not follow the standard C/C++ procedure of converting the operands to some common type then doing the compare. So it is not equivalent to the C/C++ binary operations <, >, >=, <=, ==, !=. The functions are free functions defined inside the namespace boost::numeric::safe_compare.

Type requirements

All template parameters of the functions must be C/C++ built-in integer types, char, int

Complexity

Each function performs one and only one arithmetic operation.

Example of use

```
#include <cassert>
#include <safe_compare.hpp>

using namespace boost::numeric;
const short int x = -64;
const unsigned int y = 42000;

assert(x < y); // fails
assert(safe_compare::less_than(x, y)); // OK</pre>
```

Header

#include <boost/numeric/safe_numerics/safe_compare.hpp>

9. Performance Tests

Our goal is to create facilities which make it possible to write programs known to be correct. But we also want programmers to actually use the facilities we provide here. This won't happen if using these facilities impacts performance to a significant degree. Although we've taken precautions to avoid doing this, the only real way to know is to create and run some tests.

So far we've only run one explicit performance test - test_performance.cpp. This runs a test from the Boost Multiprecision library to count prime numbers and uses on integer arithmetic. We've run the tests with unsigned integers and with safe<unsigned> on two different compilers.. No other change was made to the program. We list the results without further comment.

```
g++ (GCC) 6.2.0
Testing type unsigned:
time = 17.6215
count = 1857858
Testing type safe<unsigned>:
time = 22.4226
count = 1857858

clang-802.0.41
Testing type unsigned:
time = 16.9174
count = 1857858
Testing type safe<unsigned>:
time = 36.5166
count = 1857858
```

10. Rationale and FAQ

10.1. Is this really necessary? If I'm writing the program with the requisite care and competence, problems noted in the introduction will never arise. Should they arise, they should be fixed "at the source" and not with a "band aid" to cover up bad practice.

This surprised me when it was first raised. But some of the feedback I've received makes me thing that it's a widely held view. The best answer is to consider the examples in the Tutorials and Motivating Examples section of the library documentation. I believe the convincingly demonstrate that any program that doesn't use this library is absent of arithmetic errors.

10.2. Can safe types be used as drop-in replacements for built-in types?

Almost. Replacing all built-in types with their safe counterparts should result in a program that will compile and run as expected. Occasionally compile time errors will occur and adjustments to the source code will be required. Typically these will result in code which is more correct.

10.3. Why are there special types for literal such as safe_signed_literal<42>? Why not just use std::integral_const<int, 42>?

By defining our own "special" type we can simplify the interface. Using std::integral_const requires one to specify both the type *and* the value. Using safe_signed_literal<42> doesn't require a parameter for the type. So the library can select the best type to hold the specified value. It also means that one won't have the opportunity to specify a type-value pair which are inconsistent.

10.4. Why is safe...literal needed at all? What's the matter with const safe<int>(42)?

const safe<int>(42) looks like it might be what we want: An immutable value which invokes the "safe" operators when used in an expression. But there is one problem. The std::numeric_limits<safe<int>> is a range from INTMIN to INTMAX even though the value is fixed to 42 at compile time. It is this range which is used at compile time to calculate the range of the result of the operation.

So when an operation is performed, the range of the result is calculated from [INTMIN, INTMAX] rather than from [42,42].

10.5. Are safe type operations constexpr? That is, can they be invoked at compile time?

Yes. safe type construction and calculations are all constexpr. Note that to get maximum benefit, you'll have to use safe...literal to specify the independent values at compile time.

10.6. Why define safe_literal? Isn't it effectively the same as std::integral_constant?

Almost, but there are still good reasons to create a different type.

- std::integral_constant<int, 42> requires specification of type as well as value so it's less convenient than safe_signed_literal which maps to the smallest type required to hold the value.
- std::numeric_limits<std::integral_constant<int, 42>>::is_integer returns false. This would complicate implementation of the library
- type trait is_safe<std::integral_constant<int, 42>> would have to be defined to return true.
- But globally altering the traits of std::integral_constant might have unintended side-effects related to other code. These might well be surprises which are create errors which are hard to find and hard to work around.
- **10.7.** Why is Boost.Convert not used?

I couldn't figure out how to use it from the documentation.

10.8. Why is the library named "safe ..." rather than something like "checked ..." ?

I used "safe" in large part because this is what has been used by other similar libraries. Maybe a better word might have been "correct" but that would raise similar concerns. I'm not inclined to change this. I've tried to make it clear in the documentation what the problem that the library addressed is.

10.9. Given that the library is called "numerics" why is floating point arithmetic not addressed?

Actually, I believe that this can/should be applied to any type T which satisfies the type requirement Numeric type as defined in the documentation. So there should be specializations safe<float> and related types as well as new types like

safe<fixed_decimal> etc. But the current version of the library only addresses integer types. Hopefully the library will evolve to match the promise implied by its name.

10.10. Isn't putting a defensive check just before any potential undefined behavior often considered a bad practice?

By whom? Is leaving code which can produce incorrect results better? Note that the documentation contains references to various sources which recommend exactly this approach to mitigate the problems created by this C/C++ behavior. See [Seacord]

10.11. It looks like the implementation presumes two's complement arithmetic at the hardware level. So this library is not portable - correct? What about other hardware architectures?

As far as is known as of this writing, the library does not presume that the underlying hardware is two's complement. However, this has yet to be verified in any rigorous way.

10.12. Why is it necessary to specialize numeric_limits for "safe" types?

safe<T> behaves like a "number" just as int does. It has max, min, etc Any code which uses numeric limits to test a type T should work with safe<T>. safe<T> is a drop-in replacement for T so it has to implement all the operations.

10.13. According to C/C++ standards, unsigned integers cannot overflow - they are modular integers which "wrap around". Yet the safe numerics library detects and traps this behavior as errors. Why is that?

The guiding purpose of the library is to trap incorrect arithmetic behavior - not just undefined behavior. Although a savvy user may understand and keep present in his mind that an unsigned integer is really a modular type, the plain reading of an arithmetic expression conveys the idea that all operands are integers. Also in many cases, unsigned integers are used in cases where modular arithmetic is not intended, such as array indices. Finally, the modulus for such an integer would vary depending upon the machine architecture. For these reasons, in the context of this library, an unsigned integer is considered to be a representation of a subset of integers. Note that this decision is consistent with [INT30-C], "Ensure that unsigned integer operations do not wrap" in the CERT C Secure Coding Standard [Seacord].

10.14. Why does the library require C++14?

The original version of the library used C++11. Feedback from CPPCon, Boost Library Incubator and Boost developer's mailing list convinced me that I had to address the issue of run-time penalty much more seriously. I resolved to eliminate or minimize it. This led to more elaborate meta-programming. But this wasn't enough. It became apparent that the only way to really minimize run-time penalty was to implement compile-time integer range arithmetic - a pretty elaborate sub library. By doing range arithmetic at compile-time, I could skip runtime checking on many/most integer operations. While C++11 constexpr wasn't quite powerful enough to do the job, C++14 constexpr is. The library currently relies very heavily on C++14 constexpr. I think that those who delve into the library will be very surprised at the extent that minor changes in user code can produce guaranteed correct integer code with zero run-time penalty.

10.15. This is a C++ library - yet you refer to C/C++. Which is it?

C++ has evolved way beyond the original C language. But C++ is still (mostly) compatible with C. So most C programs can be compiled with a C++ compiler. The problems of incorrect arithmetic afflict both C and C++. Suppose we have a legacy C program designed for some embedded system.

- Replace all int declarations with int16_t and all long declarations with int32_t.
- · Create a file containing something like the following and include it at the beginning of every source file.

```
#ifdef TEST
// using C++ on test platform
#include <cstdint>
#include <boost/numeric/safe_numerics/safe_integer.hpp>
```

```
#include <cpp.hpp>
using pic16_promotion = boost::numeric::cpp<
    8, // char
    8, // short
    8, // int
    16, // long
    32 // long long
// define safe types used in the desktop version of the program.
template <typename T> // T is char, int, etc data type
using safe_t = boost::numeric::safe<
    Τ,
    pic16_promotion,
    boost::numeric::default_exception_policy // use for compiling and running tests
typedef safe_t<std::int_least16_t> int16_t;
typedef safe_t<std::int_least32_t> int32_t;
#else
/* using C on embedded platform */
typedef int int_least16_t;
typedef long int_least16_t;
#endif
```

- Compile tests on the desktop with a C++14 compiler and with the macro TEST defined.
- Run the tests and change the code to address any thrown exceptions.
- Compile for the target C platform with the macro TEST undefined.

This example illustrates how this library, implemented with C++14 can be useful in the development of correct code for programs written in C.

11. Pending Issues

The library is under development. There are a number of issues still pending.

- The library is currently limited to integers.
- Conversions to safe integer types from floating point types is not explicitly addressed.
- Note that standard library stream conversion functions such as strtoi etc. DO check for valid input and throw the exception std::out_of_range if the string cannot be converted to the specified integer type. In other words, strtoi already contains some of the functionality that safe<int> provides.
- Although care has been taken to make the library portable, it's likely that at least some parts of the implementation particularly checked arithmetic depend upon two's complement representation of integers. Hence the library is probably not currently portable to all other possible C++ architectures.
- Currently the library permits a safe<int> value to be uninitialized. This supports the goal of "drop-in" replacement of C++/C built-in types with safe counter parts. On the other hand, this breaks the "always valid" guarantee.

12. Acknowledgements

This library would never have been created without inspiration, collaboration and constructive criticism from multiple sources.

David LeBlanc

This library is inspired by David LeBlanc's SafeInt Library . I found this library very well done in every way and useful in my embedded systems work. This motivated me to take it to the "next level".

Andrzej Krzemienski

Andrzej Commented and reviewed the library as it was originally posted on the Boost Library Incubator. The consequent back and forth motivated me to invest more effort in developing documentation and examples to justify the utility, indeed the necessity, for this library. He also noted many errors in code, documentation, and tests. Without his interest and effort, I do not believe the library would have progressed beyond its initial stages.

Boost

As always, the Boost Developer's mailing list has been the source of many useful observations from potential users and constructive criticism from very knowledgeable developers. During the Boost formal review, reviews and comments were posted by the following persons:

- Paul A. Bristow
- · Steven Watanabe
- · John Maddock
- · Antony Polukhin
- · Barrett Adair
- · Vicente J. Botet Escriba
- · John McFarlane
- Peter Dimov

13. Change Log

This is the third version.

14. Bibliography

Bibliography

[coker] Zack Coker. Samir Hasan. Jeffrey Overbey. Munawar Hafiz. Christian Kästner. *Integers In C: An Open Invitation To Security Attacks?* . JTC1/SC22/WG21 - The C++ Standards Committee - ISOCPP . January 15, 2012. Coker

[crowl1] Lawrence Crowl. *C++ Binary Fixed-Point Arithmetic* . JTC1/SC22/WG21 - The C++ Standards Committee - ISOCPP . January 15, 2012. Crowl

[crowl2] Lawrence Crowl. Thorsten Ottosen. *Proposal to add Contract Programming to C++* . WG21/N1962 and J16/06-0032 - The C++ Standards Committee - ISOCPP . February 25, 2006. Crowl & Ottosen

[dietz] Will Dietz. Peng Li. John Regehr. Vikram Adve. *Understanding Integer Overflow in C/C++* . Proceedings of the 34th International Conference on Software Engineering (ICSE), Zurich, Switzerland . June 2012. Dietz

[garcia] J. Daniel Garcia. *C++ language support for contract programming*. WG21/N4293 - The C++ Standards Committee - ISOCPP . December 23, 2014. Garcia

- [katz] Omer Katz. SafeInt code proposal. Boost Developer's List. Katz
- [keaton] David Keaton, Thomas Plum, Robert C. Seacord, David Svoboda, Alex Volkovitsky, and Timothy Wilson. *As-if Infinitely Ranged Integer Model*. Software Engineering Institute. CMU/SEI-2009-TN-023.
- [leblanc1] David LeBlanc. *Integer Handling with the C++ SafeInt Class*. Microsoft Developer Network . January 7, 2004. LeBlanc
- [leblanc2] David LeBlanc. SafeInt. CodePlex. Dec 3, 2014. LeBlanc
- [lions] Jacques-Louis Lions. Ariane 501 Inquiry Board report. Wikisource. July 19, 1996. Lions
- [matthews] Hubert Matthews. *CheckedInt: A Policy-Based Range-Checked Integer*. Overload Journal #58. December 2003. Matthews
- [mouawad] Jad Mouawad. F.A.A Orders Fix for Possible Power Loss in Boeing 787. New York Times. April 30, 2015.
- [plakosh] Daniel Plakosh. Safe Integer Operations. U.S. Department of Homeland Security . May 10, 2013. Plakosh
- [seacord1] Robert C. Seacord. *Secure Coding in C and C++* . 2nd Edition. Addison-Wesley Professional. April 12, 2013. 978-0321822130. Seacord
- [seacord2] Robert C. Seacord. *INT30-C. Ensure that operations on unsigned integers do not wrap* . Software Engineering Institute, Carnegie Mellon University . August 17, 2014. INT30-C
- [seacord3] Robert C. Seacord. *INT32-C. Ensure that operations on signed integers do not result in overflow* . Software Engineering Institute, Carnegie Mellon University . August 17, 2014. INT32-C
- [stone] David Stone. C++ Bounded Integer Library. Stone
- [stroustrup] Bjarn Stroustrup. *The C++ Programming Language Fourth Edition*. Addison-Wesley . Copyright © 2014 by Pearson Education, Inc.. January 15, 2012. Stroustrup
- [forum] Forum Posts. C++ Binary Fixed-Point Arithmetic . ISO C++ Standard Future Proposals . Forum