Multivariate Forecasting with Deep Learning Model

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1. Problem Statement

The goal of this homework is to forecast stock return using firm's financial and operating data. Given the quarter data of Fortune 500 companies, we tested our deep learning models and made predictions among 25 of them.

2. Methodology

The raw data consists of 14 variables: i) Company Name, ii) Ticker Symbol, iii) Asset Total, iv) Cash, iv) Cost of Goods Sold, v) Long-Term Debt-Total, vi) Income Before Extraordinary Items, vii) Inventories – Total, viii) Sales/Turnover (Net), x) Selling, General and Administrative Expenses, xi) Research and Development Expense, xii) quarterly closed price, xiii) data date, xiv) quarterly close date.

2.1 Data Preprocessing

In the data, we initially chose a random subset of 25 companies by gathering the unique values of Ticker Symbol and/or Company Name. Doing this method there was a substantial number of missing values. We then opted to choose the look for companies with no missing values in the column of Quarterly Closed Price and chose a random subset of 25 companies from that list. Doing this, even with the minute amount of data, we at least have more observations than the previous method.

After we get the 25 companies, we checked the data quality of the 12 variables. It turns out that only the variables *iii*) Assets – Total, vi) Income Before Extraordinary Items and xii) quarterly closed price have a smaller number of missing values, so we dropped other variables in the dataset to a void the bia sedness. To replace the missing values, we used a backfill method for each company. In addition, we derived a variable 'quarter' from the date and a response variable 'stock_returns' using the quarterly closed price.

Overall, we have quarterly data for 25 companies, mainly from 1962Q1 to 2019Q4.

Once we have the features we wanted to use to approach this problem, we split the data into sequences to create input and output data of a sliding window approach for forecasting. The time step we used is 8, which represents 8 quarters.

2.2 Modeling

We developed three deep learning models to predict the stock returns: Feedforward Neural Network, LSMT, and CNN. These three models are all doing the multi-step time series forecasting with multivariate input data.

2.2.1 Feedforward Neural Network:

Feedforward Neural Networks are simple neural networks. They have a similar type of framework as compared to linear regression, however, it has the exception of being able to capture the nonlinear relationships. Feedforward neural networks are generally used for classification of data like images, and not generally used for historical data. However, with manipulation of our time series data we can use Feedforward networks. This works because we are not providing the general input and output values. We are still providing input and output values, except in this case, our input values are a certain amount of timesteps of observations previous to the output data.

For our Feedforward Neural Network, we created a simple dense model as we did not want to create too many dense layers as that would cause overfitting to our data. Having too many dense layers, too many hidden layers, then the data will be overfitting on the training data and when it comes to the validation data, it would not bode too well. We

initially started with three dense layers and slowly reduced it to two and one dense layer. After the deciding which number of dense layers used, we added one final dense layer of one since we only have one output.

2.2.2 LSTM:

Long Short-term memory models are made for using with feedback and time data, so it was the easiest model to work with. LSTM networks are well suited to making predictions about time series data as they can leverage past information using memory cells.

To improve our model, we tried changing the window size and the layer size as well as adding more LSTM or other layers onto the sequential model. For the PRCCQ prediction we found a timestep of 8 and a simple LSTM of 100 to be effective. For the Stock Return prediction, we used timestep of 12 and an LSTM of 120. For both predictions, we tried adding more layers of LSTM and using the return sequence function, however that seemed to cause overfitting reducing our test accuracy a lot.

2.2.3 CNN:

For the CNN method, we took a dvantage of 1D function in Keras to do the convolution computation. We used only one convolutional data with 16 filter and a kernel size of 3. The input sequence of 8 quarters is performed 16 times and it is read in three time-steps at a time. After this, we used a max pooling layer with pool size of 2 to reduce the features and a flatten layer. Two dense layers were applied, one with 50 neurons and a RELU activation function while anther was with 1 neuron as the output layer. We used ADAM for the optimizer and applied MeanAbsolutePercentageError() as the metrics to calculate the errors.

3. Result (First 5 of the 25)

The results from the three model would display in this part. We calculated the mean, std, min, 25%, 50%, 75% and max of the MAPE for each picked company. We have run our models for both the forecasting the Stock Return and the Quarterly Closing Price.

3.1.1 FFNN (PRCCQ):

| | BA MAPE | BA VAL_MAPE | CMA MAPE | CMA VAL_MAPE | COP MAPE | COP VAL_MAPE | DIS MAPE | DIS VAL_MAPE | DTE MAPE | DTE VAL_MAPE |
|-------|------------|----------------|-------------|-----------------|------------|-----------------|------------|-----------------|------------|-----------------|
| count | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 |
| mean | 16.794519 | 13.219679 | 11.985000 | 12.598897 | 14.999965 | 12.795096 | 20.919505 | 12.451544 | 9.168668 | 8.210564 |
| std | 1.258623 | 2.055917 | 2.384283 | 1.794376 | 5.323958 | 4.511331 | 2.541970 | 1.743589 | 5.635603 | 2.145414 |
| min | 15.111590 | 10.457763 | 10.744922 | 11.437852 | 12.313501 | 10.143296 | 18.362406 | 10.254009 | 7.234123 | 5.261128 |
| 25% | 16.047159 | 11.530826 | 11.098270 | 11.680328 | 13.071098 | 10.513899 | 19.733342 | 11.347426 | 7.716364 | 6.568378 |
| 50% | 16.409464 | 12.547908 | 11.396808 | 11.875088 | 13.678389 | 11.385415 | 20.239102 | 12.229956 | 8.012227 | 7.781499 |
| 75% | 17.261793 | 14.614475 | 11.876237 | 12.703210 | 14.566181 | 13.330541 | 21.338455 | 12.922542 | 9.037271 | 9.709260 |
| max | 24.304295 | 20.039152 | 31.952250 | 21.853954 | 56.576427 | 48.282658 | 40.554947 | 19.606682 | 61.259579 | 16.679686 |

3.1.2 FFNN (Stock Return):

| | BA MAPE | BA VAL_MAPE | CMA MAPE | CMA VAL_MAPE | COP MAPE | COP VAL_MAPE | DIS MAPE | DIS VAL_MAPE | DTE MAPE | DTE VAL_MAPE |
|-------|-------------|----------------|--------------|-----------------|--------------|-----------------|-------------|-----------------|--------------|-----------------|
| count | 100.000000 | 1.000000e+02 | 1.000000e+02 | 100.000000 | 1.000000e+02 | 100.000000 | 100.000000 | 100.000000 | 1.000000e+02 | 100.000000 |
| mean | 388.464875 | 9.018057e+05 | 1.138139e+06 | 301.774114 | 8.500353e+05 | 354.934725 | 271.306945 | 121.493014 | 7.102145e+05 | 277.087429 |
| std | 223.792643 | 8.720103e+05 | 9.434827e+05 | 148.207028 | 6.414978e+05 | 120.419198 | 135.811005 | 32.265772 | 1.021241e+06 | 196.709402 |
| min | 189.743240 | 3.083742e+03 | 2.579486e+05 | 155.573593 | 1.648052e+05 | 149.896240 | 186.222244 | 94.959694 | 1.001141e+05 | 167.695297 |
| 25% | 290.452675 | 2.913139e+05 | 7.960705e+05 | 233.501755 | 5.468213e+05 | 257.645210 | 218.313492 | 107.940239 | 4.539958e+05 | 214.581165 |
| 50% | 357.791641 | 8.282214e+05 | 1.017229e+06 | 287.812424 | 7.431948e+05 | 350.545746 | 251.138016 | 116.436035 | 5.362332e+05 | 236.939018 |
| 75% | 425.826187 | 1.320441e+06 | 1.252590e+06 | 332.800552 | 9.951869e+05 | 448.334656 | 286.995316 | 126.156298 | 7.056370e+05 | 283.824936 |
| max | 2016.093872 | 6.651042e+06 | 9.831613e+06 | 1561.678955 | 6.050369e+06 | 747.781616 | 1502.840576 | 405.213776 | 9.047052e+06 | 2057.612305 |

3.2.2 LSTM (PRCCQ):

| | BA MAPE | BA VAL_MAPE | CMA MAPE | CMA VAL_MAPE | COP MAPE | COP VAL_MAPE | DIS MAPE | DIS VAL_MAPE | DTE MAPE | DTE VAL_MAPE |
|-------|------------|----------------|------------|-----------------|------------|-----------------|------------|-----------------|------------|-----------------|
| count | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 |
| mean | 17.364760 | 16.958536 | 11.666067 | 12.506177 | 12.397726 | 11.622496 | 20.435187 | 11.753319 | 7.683112 | 7.587975 |
| std | 3.059537 | 3.708585 | 3.530077 | 1.754058 | 2.238805 | 0.906815 | 2.665617 | 2.314482 | 4.676444 | 1.528814 |
| min | 14.973848 | 11.809104 | 9.918372 | 10.641964 | 11.160673 | 9.456348 | 17.621639 | 8.842291 | 6.280543 | 4.990706 |
| 25% | 16.253733 | 14.583540 | 10.788033 | 11.832841 | 11.698596 | 11.005472 | 18.785334 | 10.579566 | 6.733569 | 6.275139 |
| 50% | 16.930554 | 16.216039 | 11.272742 | 12.216736 | 12.078443 | 11.572633 | 19.932789 | 11.144541 | 7.050038 | 7.605839 |
| 75% | 17.719303 | 18.269999 | 11.641784 | 12.705415 | 12.432101 | 12.010159 | 21.163120 | 12.020841 | 7.398752 | 8.680420 |
| max | 45.303516 | 33.212734 | 45.601109 | 27.668116 | 33.420918 | 14.860488 | 36.841282 | 24.647840 | 53.043324 | 12.431164 |

3.2.2 LSTM (StockReturn):

| | BA MAPE | BA VAL_MAPE | CMA MAPE | CMA VAL_MAPE | COP MAPE | COP VAL_MAPE | DIS MAPE | DIS VAL_MAPE | DTE MAPE | DTE VAL_MAPE |
|-------|------------|----------------|--------------|-----------------|--------------|-----------------|------------|-----------------|--------------|-----------------|
| count | 100.000000 | 1.000000e+02 | 1.000000e+02 | 100.000000 | 1.000000e+02 | 100.000000 | 100.000000 | 100.000000 | 1.000000e+02 | 100.000000 |
| mean | 278.373789 | 1.409600e+06 | 6.377270e+05 | 177.954557 | 5.871399e+05 | 294.310900 | 236.759369 | 123.769346 | 4.081491e+05 | 167.173303 |
| std | 86.805132 | 1.050003e+06 | 4.327452e+05 | 39.604703 | 3.105978e+05 | 108.878607 | 48.604346 | 15.654529 | 1.960131e+05 | 43.269477 |
| min | 115.133301 | 3.695406e+04 | 9.487715e+04 | 111.107918 | 1.095283e+05 | 100.543091 | 166.787582 | 103.548088 | 9.924547e+04 | 98.009628 |
| 25% | 216.226929 | 3.822532e+05 | 3.248100e+05 | 142.531742 | 3.520035e+05 | 208.291851 | 194.006092 | 111.661860 | 2.709799e+05 | 129.908787 |
| 50% | 281.763412 | 1.186781e+06 | 5.239678e+05 | 180.338982 | 5.110648e+05 | 290.387436 | 221.217255 | 116.857098 | 3.901655e+05 | 163.735603 |
| 75% | 332.919846 | 2.316080e+06 | 7.927743e+05 | 202.925808 | 7.537193e+05 | 379.395226 | 277.771431 | 135.576706 | 5.048496e+05 | 197.601513 |
| max | 587.562744 | 3.845696e+06 | 2.182441e+06 | 293.583130 | 1.666492e+06 | 534.873169 | 340.835022 | 165.984543 | 1.092755e+06 | 270.837158 |

3.3.1 CNN (PRCCQ)

| | BA MAPE | BA VAL_MAPE | CMA MAPE | CMA VAL_MAPE | COP MAPE | COP VAL_MAPE | DIS MAPE | DIS VAL_MAPE | DTE MAPE | DTE VAL_MAPE |
|-------|------------|----------------|-------------|-----------------|-------------|-----------------|------------|-----------------|------------|-----------------|
| count | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 |
| mean | 15.307662 | 17.105733 | 15.721104 | 17.944395 | 15.348411 | 17.048730 | 15.588536 | 17.354278 | 15.506343 | 17.403360 |
| std | 1.034856 | 2.046208 | 1.818769 | 3.599642 | 1.171432 | 1.477935 | 0.972329 | 1.553538 | 1.162364 | 2.883858 |
| min | 13.972986 | 14.769111 | 14.134356 | 15.033408 | 14.213552 | 14.939934 | 14.367871 | 15.392678 | 14.116027 | 14.853895 |
| 25% | 14.680523 | 15.787355 | 14.685185 | 16.100735 | 14.649650 | 16.011806 | 14.852395 | 16.280994 | 14.705063 | 15.867422 |
| 50% | 15.081217 | 16.679216 | 15.102663 | 16.726450 | 15.066828 | 16.749570 | 15.370565 | 16.981009 | 15.290743 | 16.717206 |
| 75% | 15.781825 | 17.577335 | 15.882224 | 18.180110 | 15.800555 | 17.589958 | 16.080242 | 18.070036 | 16.108461 | 17.922693 |
| max | 21.887304 | 28.703806 | 26.794104 | 40.265896 | 23.878508 | 22.217237 | 21.473331 | 23.803232 | 22.767342 | 33.236523 |

3.3.2 CNN (Stock Return)

| | BA MAPE | BA VAL_MAPE | СМА МАРЕ | CMA VAL_MAPE | COP MAPE | COP VAL_MAPE | DIS MAPE | DIS VAL_MAPE |
|-------|---------------|---------------|---------------|-----------------|---------------|-----------------|---------------|-----------------|
| count | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 | 100.000000 |
| mean | 328799.340313 | 141693.725430 | 314128.131563 | 83864.566543 | 341503.224062 | 100127.176270 | 339891.152813 | 103953.665654 |
| std | 72311.974673 | 63453.875082 | 55155.096143 | 36758.287244 | 63958.720796 | 43696.697097 | 66455.051202 | 38619.227498 |
| min | 206308.109375 | 34394.277344 | 187675.718750 | 12569.835938 | 210736.812500 | 31584.970703 | 190306.328125 | 11295.159180 |
| 25% | 269318.625000 | 91989.982422 | 268554.351562 | 58942.333984 | 292441.726562 | 71791.816406 | 295824.421875 | 76937.570312 |
| 50% | 318345.234375 | 133902.093750 | 313989.203125 | 79659.335938 | 345836.437500 | 86838.417969 | 345851.171875 | 96906.367188 |
| 75% | 376639.671875 | 189478.187500 | 348488.882812 | 102952.765625 | 387647.546875 | 125079.419922 | 385584.375000 | 132730.468750 |
| max | 589517.250000 | 297015.250000 | 493461.000000 | 285400.312500 | 505664.656250 | 261915.031250 | 597406.062500 | 211197.515625 |

4. Conclusion

To recap, Feed Forward Neural Networks (FFNN) are not originally intended to handle time series forecasting. For us to use this model, we had to engineer the data to an acceptable input and output. FFNN are simple models and is the least complex of the ones we have tried. Saying this, our FFNN model performed very poorly. CNN model results in the worse MAPE while compare to other two approaches. This might be caused by the overfitting in our model. In conclusion, LSTM seems to be performing the best out of the different model types. This is to be expected since LSTM is designed to work with time sensitive data and our dataset contained date trends. However, even with LSTM our results weren't good since the original dataset had many null values and we didn't know how to best fill them since we were missing industry knowledge.