Fast Control of Multimode Cavities with Conditional Displacements

Eesh Gupta, S. Chakram, …

Motivation

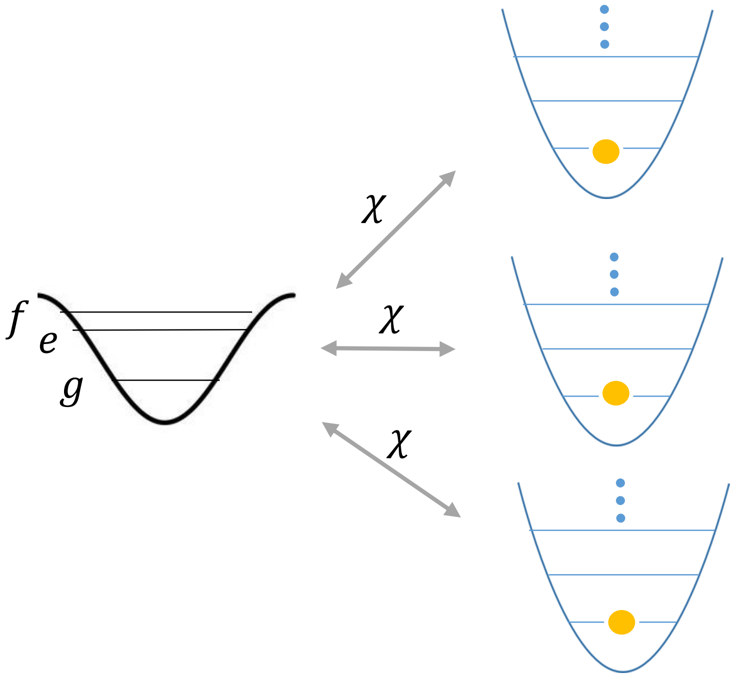
- Goal: Enact gates on cavity modes
- Typical Schemes (SNAP/GRAPE) use $\chi a^\dagger a \sigma_z$

Increase χ for faster gates

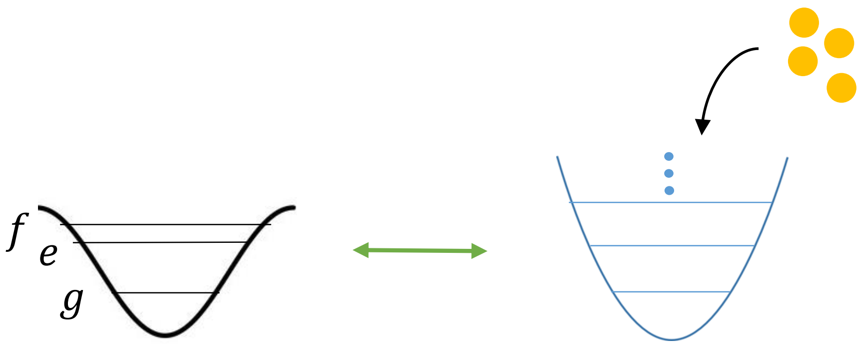
- Coupling to the lossy ancilla reduces mode coherence

$$T_1^{cav} \leq \frac{\Delta^2}{g^2} T_1^q \sim \frac{2\alpha}{\chi} \mathrm{T}_1^{\mathrm{q}}$$

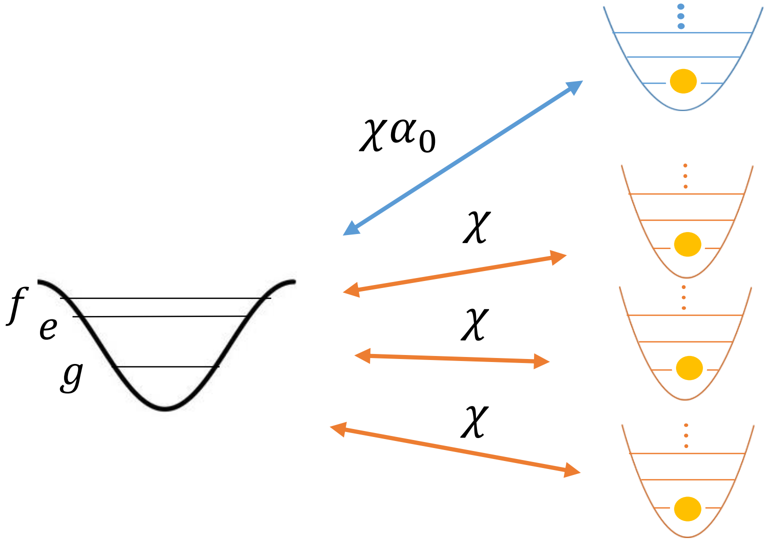
Decrease χ for better mode coherence



Large Displacements



$$\chi a^\dagger a \sigma_z \xrightarrow{D(\alpha_0)} \boxed{\chi\,(\alpha_0 a^\dagger + \alpha_0^\star a)\,\sigma_z}$$



N non-target modes

Advantage in Multimode Context:

Gate Speed $g_{gate} = \chi\alpha_0$

Coherent Errors: $\epsilon_{coh} = \frac{N\chi}{g_{gate}} = \frac{\boldsymbol{N}}{\boldsymbol{\alpha_0}}$

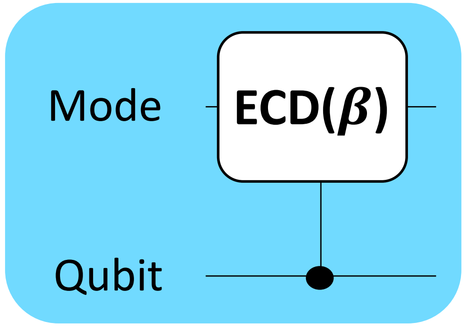
- Hacohen-Gourgy, S., Martin, L., Flurin, E. *et al.* *Nature* **538**, 491–494 (2016).
- Eickbusch, A., Sivak, V., Ding, A.Z. *et al.* *Nat. Phys.* **18**, 1464–1469 (2022).

Echoed Conditional Gates

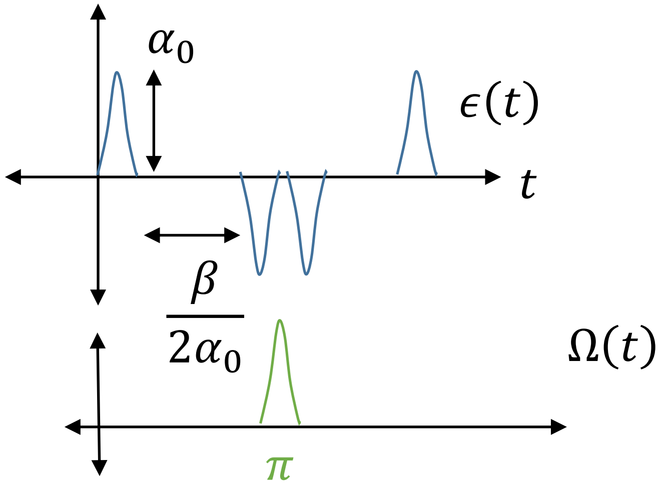
$$\chi(a^\dagger + \alpha^*)(a + \alpha)\sigma_z$$

$$=$$

$$\chi a^\dagger a \sigma_z \quad + \quad \chi\,(\alpha_0 a^\dagger + \alpha_0^* a)\,\sigma_z \quad + \quad \chi|\alpha|^2\sigma_z$$

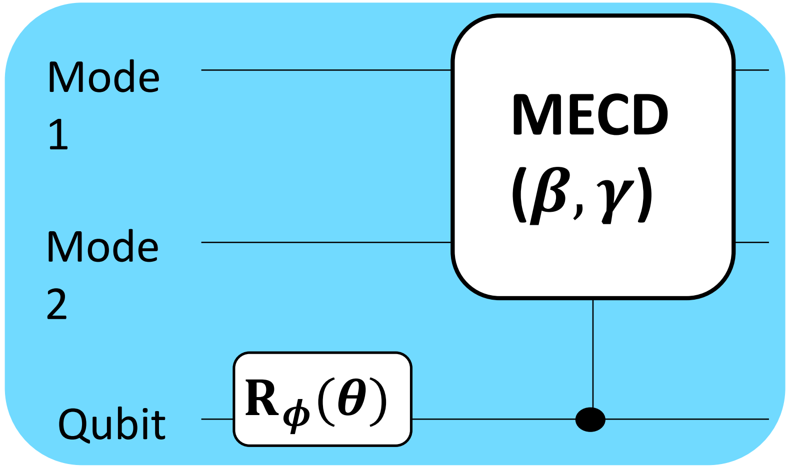


$$= \quad D\left(\frac{\beta}{2}\right)|e\rangle\langle g| + D\left(-\frac{\beta}{2}\right)|g\rangle\langle e| \quad =$$



A. Eickbusch, ..., R. Schoelkopf, M. Devoret. ArXiv preprint arXiv:2111.06414 (2021)

Multimode ECD



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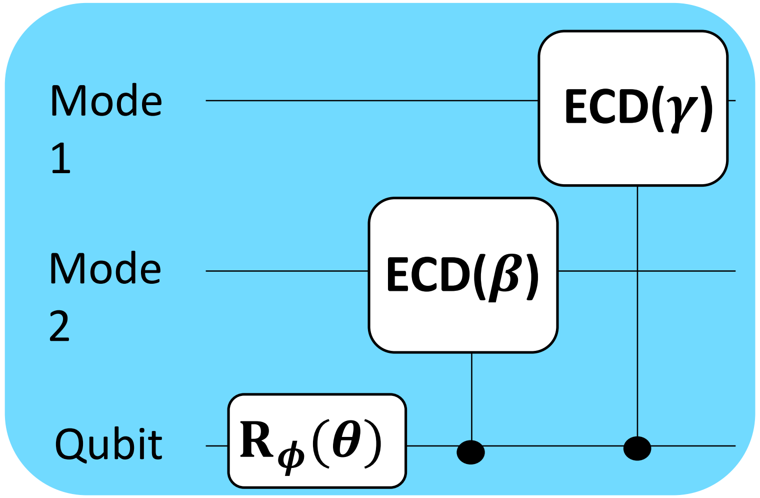
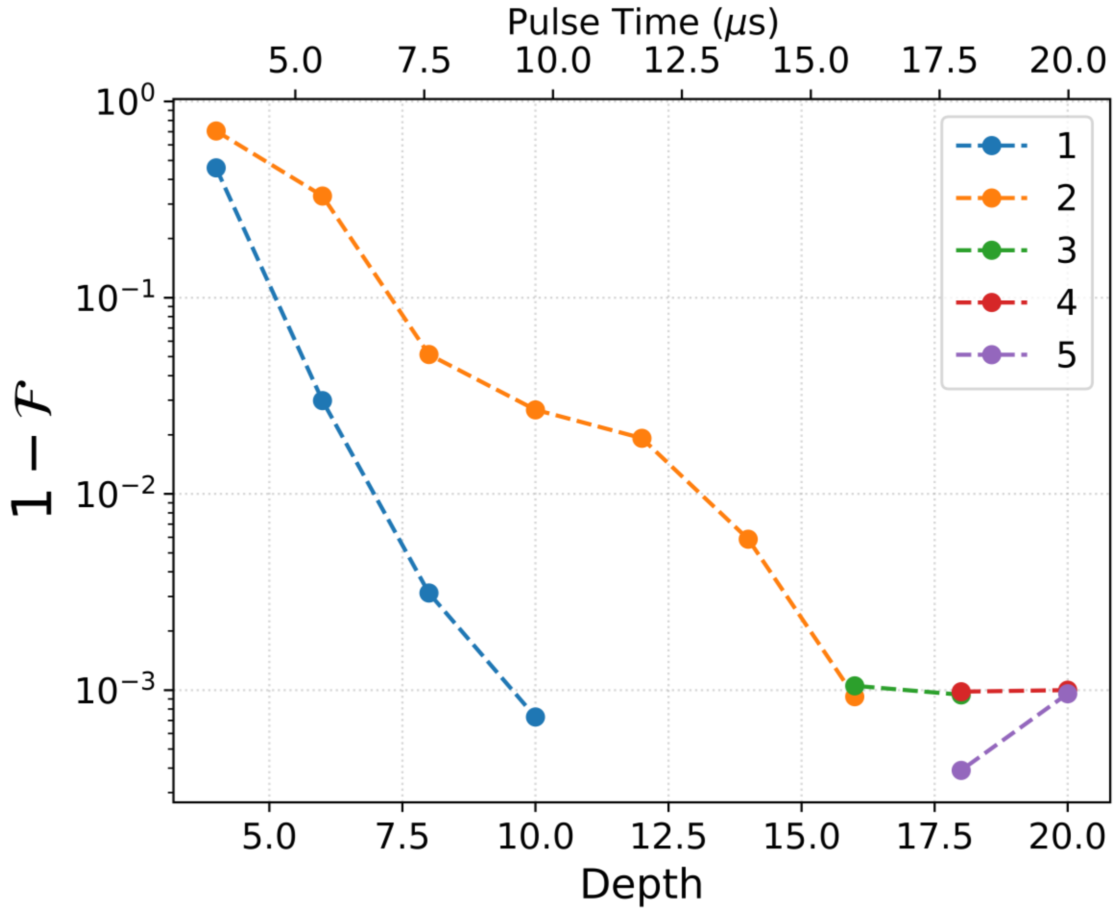


- Universal Control for Two Modes
- Asimultaneous drives to prevent heating of modes [1,2] and amplification of cross kerr terms

[1] Eickbusch, Alec , et al. W34. 00005. APS March Meeting (2022).
[2] Diringer, Asaf A., et al. *arXiv preprint arXiv:2301.09831* (2023).

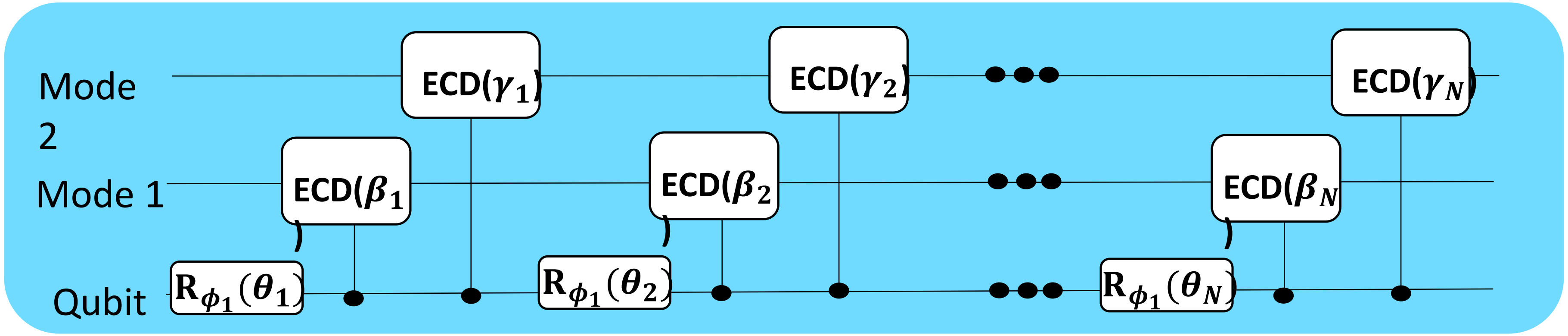
Two Mode ECD: State Transfer



$$\mathrm{g} \otimes |0\mathrm{n}\rangle \rightarrow \mathrm{g} \otimes |n0\rangle$$

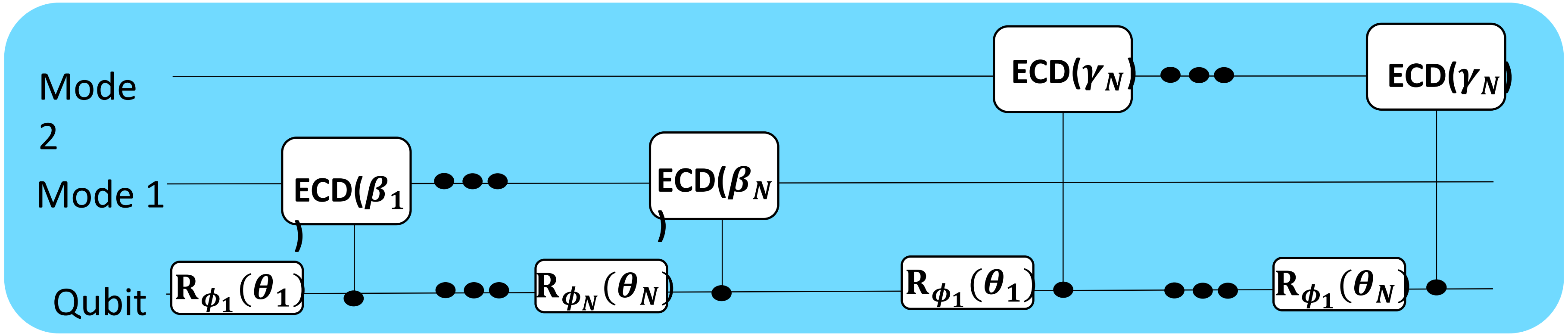
Two Mode ECD: State Transfer

$$g \otimes (|n0\rangle \rightarrow |0n\rangle)$$



$$g \otimes (|n\rangle \rightarrow |0\rangle)$$

$$g \otimes (|0\rangle \rightarrow |n\rangle)$$



Two Mode ECD: State Transfer

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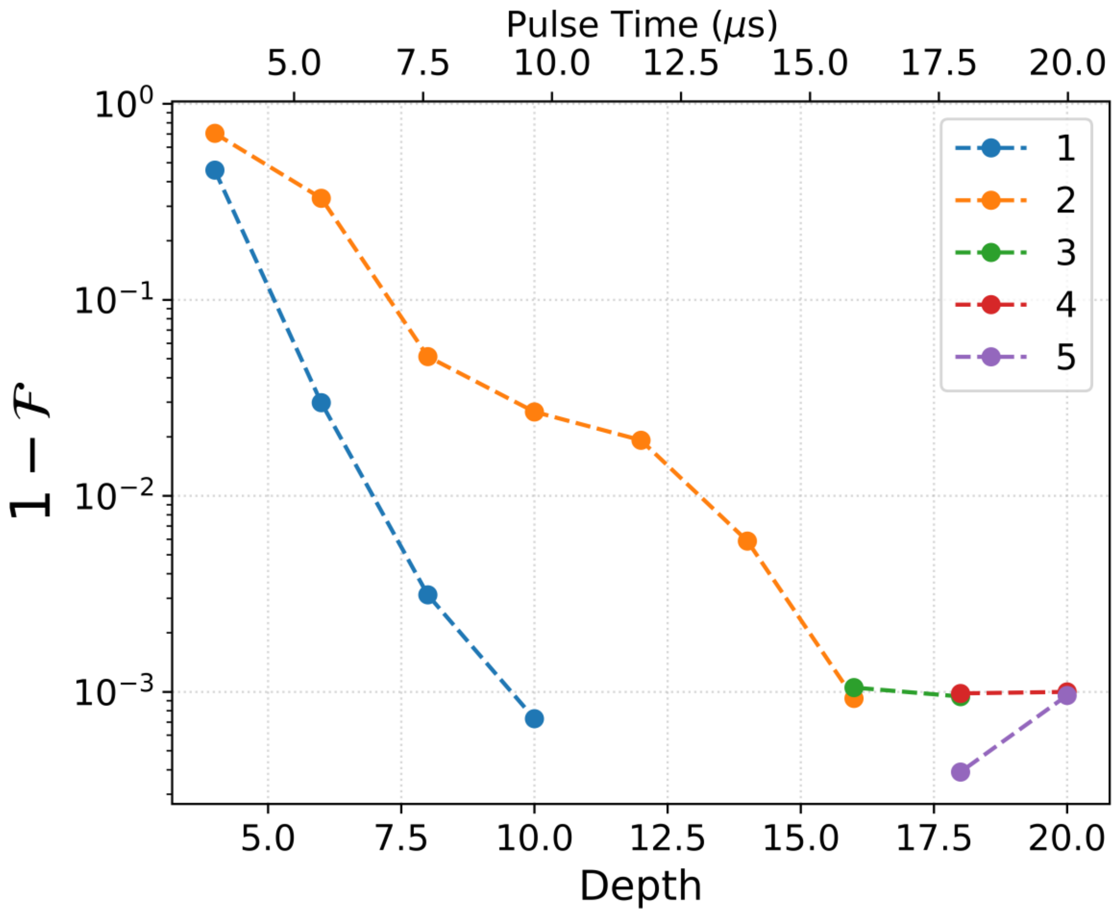
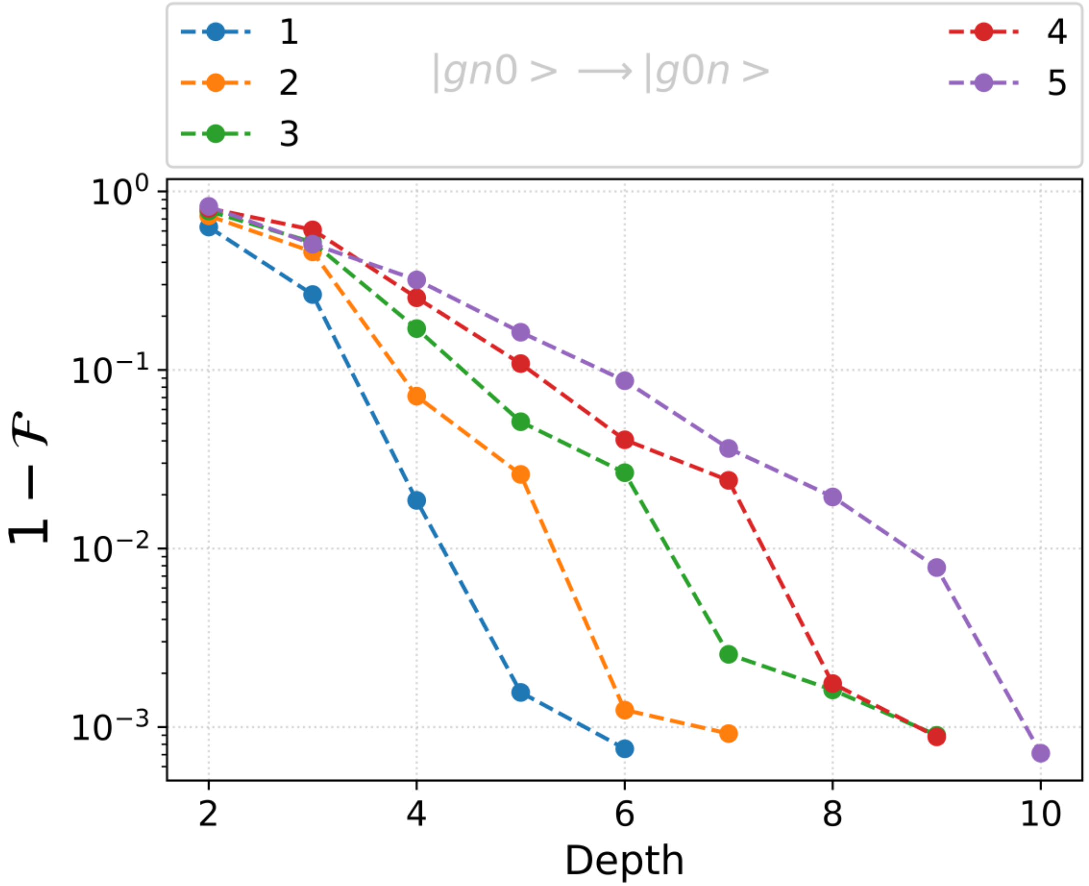
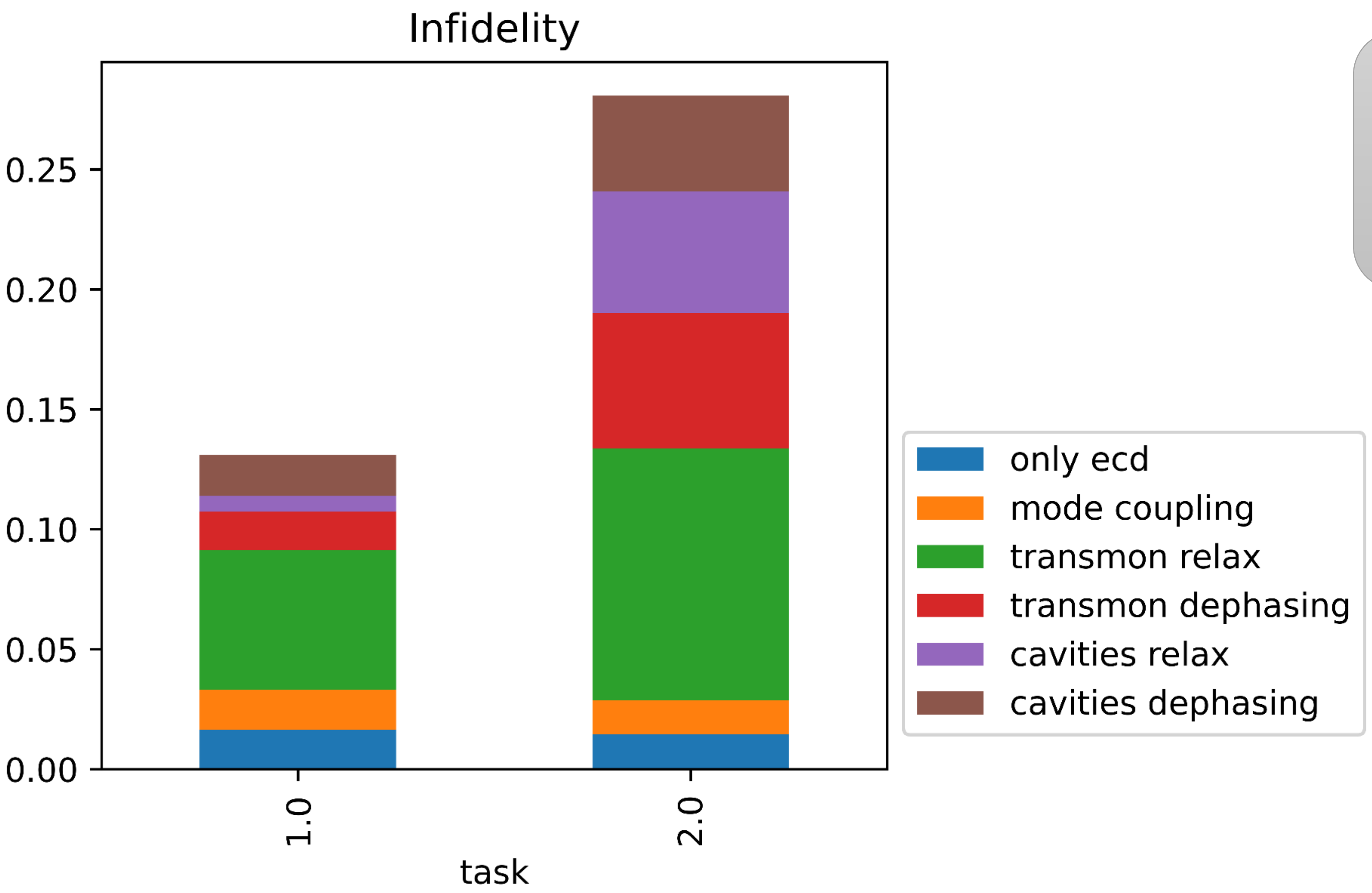


$$g \otimes (|0\rangle \rightarrow |n\rangle)$$

$$g \otimes (|n\rangle \rightarrow |0\rangle)$$



Multimode ECD: Error Budget

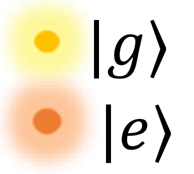


- $T_{1,q} = 85\ \mu s$
- $T_{2,q} = 98\ \mu s$
- $T_{1,c} = 2\ ms$
- $T_{\phi,c} = 150\ ms$ *

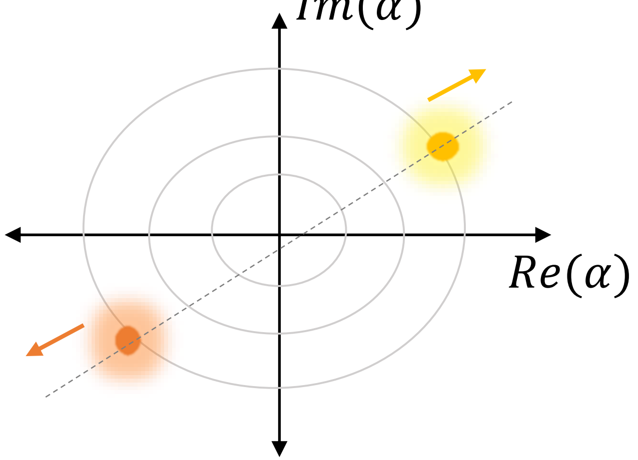
** A. Eickbusch, ..., R. Schoelkopf, M. Devoret. ArXiv preprint arXiv:2111.06414 (2021)*

Circle Grape

- Qubit Drive Optimized
- Cavity mode always driven far from origin in phase space
- Cavity drives detuned

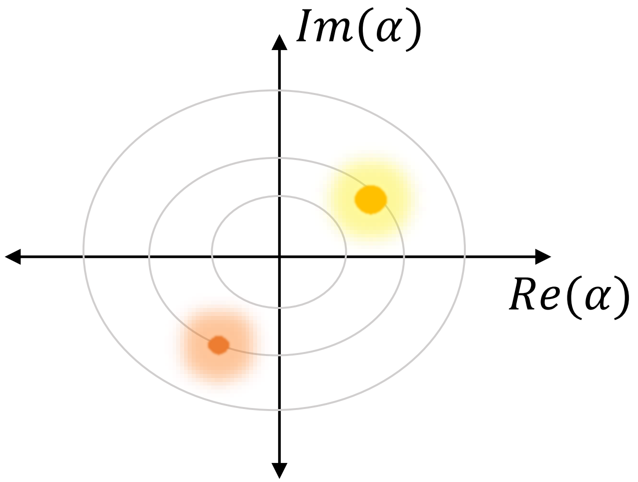


$$\mathrm{H} = \chi(\alpha \mathrm{a}^{\dagger} + \alpha^{*}\mathrm{a})\sigma_z$$



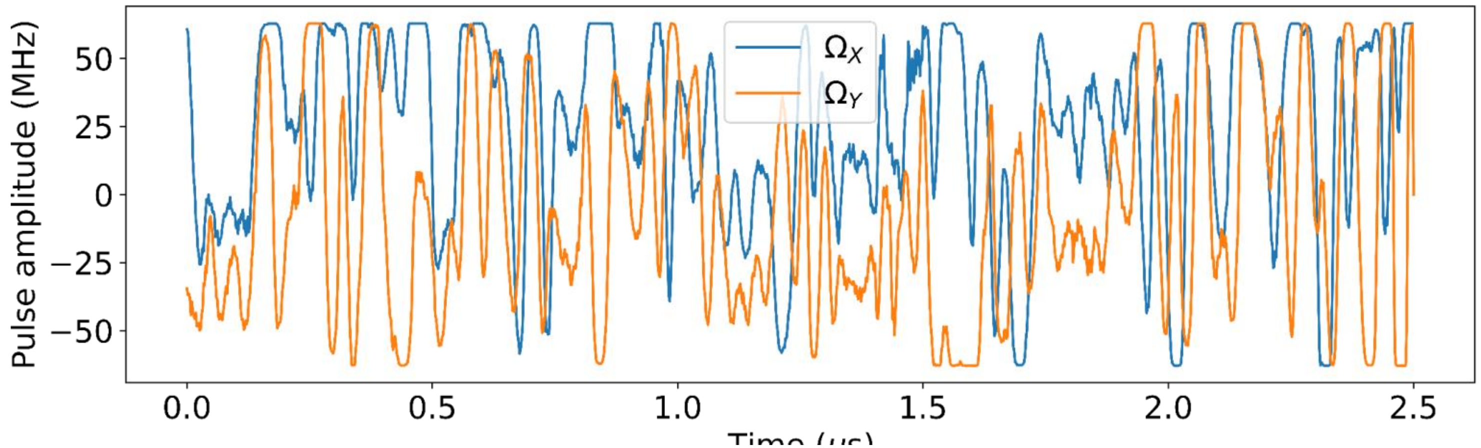
$$\mathrm{H} = \Delta_c \mathrm{a}^{\dagger}\mathrm{a} + \chi(\alpha \mathrm{a}^{\dagger} + \alpha^{*}\mathrm{a})\sigma_z$$

Rotate in circle because of detuning; is this a spiral?

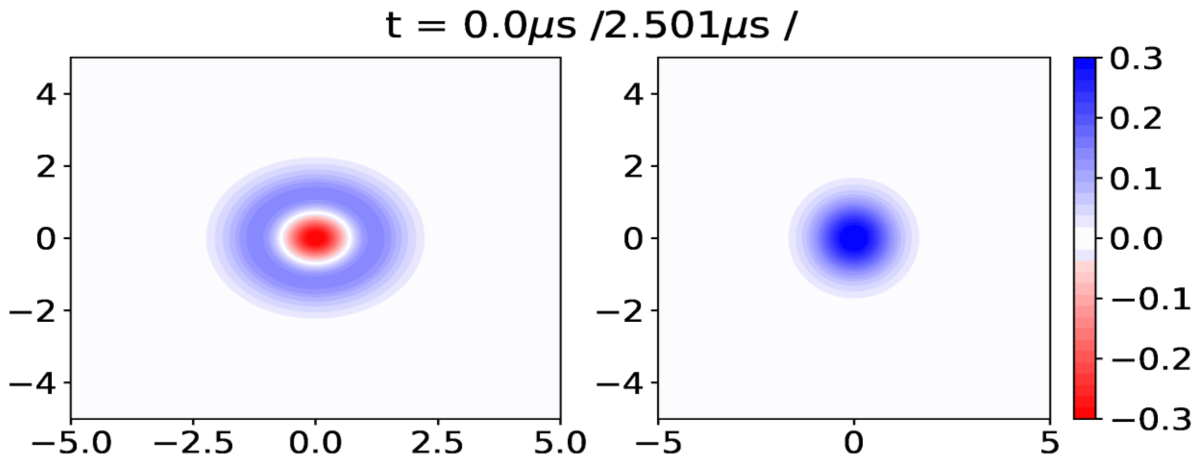


Elder S., et al. Bulletin of the American Physical Society 66 (2021)

Example: $|g10\rangle \to |g01\rangle$



Simulation Parameters
- $\Delta_c = 10$ Mhz
- $|\Omega| = 10$ Mhz
- $\chi_1, \chi_2/2\pi = 33$ kHz
- $\alpha_1, \alpha_2 = 30$



Sideband Drives Method

Since α oscillatory,

$$H = \chi a^{+} a \sigma_z + \chi(\alpha a^{+} + \alpha^{*} a)\sigma_z + \chi|\alpha|^2\sigma_z + \Omega_R \sigma_x$$

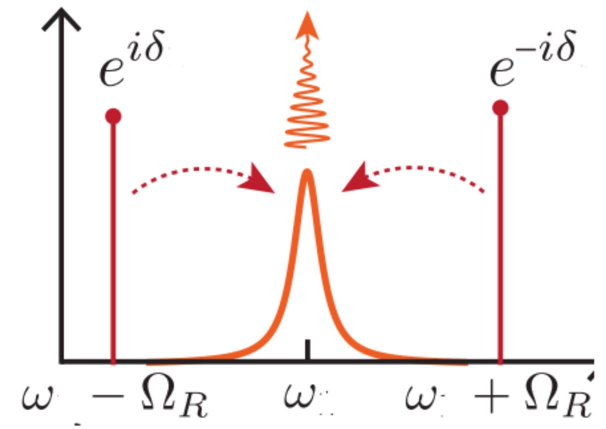
$\omega = 0$ $\quad\quad$ $\omega = \Omega_R$ $\quad\quad$ $\omega = 2\Omega_R$

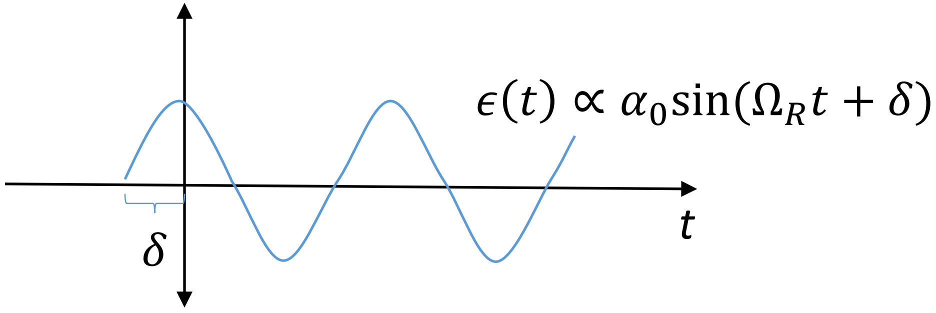
Frame Transformations:

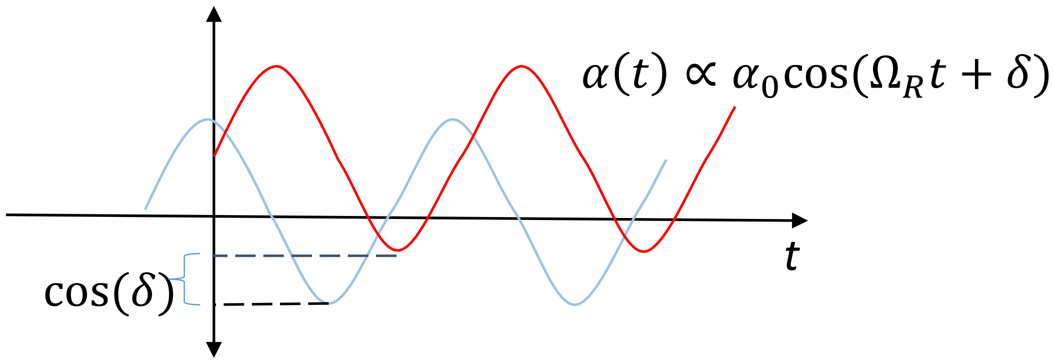
1. $\sigma_x \leftrightarrow \sigma_z$ $\longrightarrow$ $\Omega_R \sigma_z$
2. Rotating Frame of the qubit $\quad$ $\cancel{\Omega_R \sigma_z}$

$$H = \chi\alpha_0(a^{+} + a) \otimes (\sigma_x \cos\delta + \sigma_y \sin\delta) + \ldots$$

$\omega = 0$ $\quad\quad$ $\omega \geq \Omega_R$

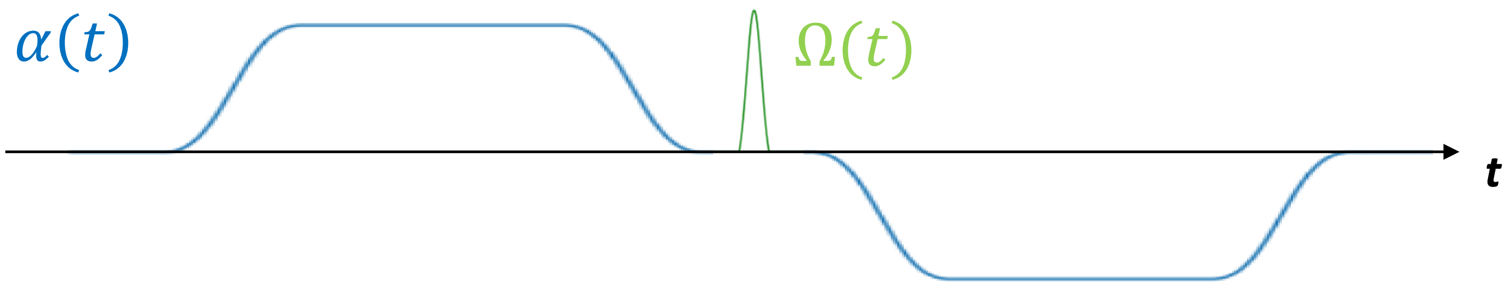






Shay Hacohen-Gourgy, …, Irfan Siddiqi. Nature 538-7626 (2016).

Echoing in ECD



Not completely echoed out !

$$\chi a^{+} a \sigma_z \quad \longrightarrow \quad \chi a^{+} a(-\sigma_z)$$

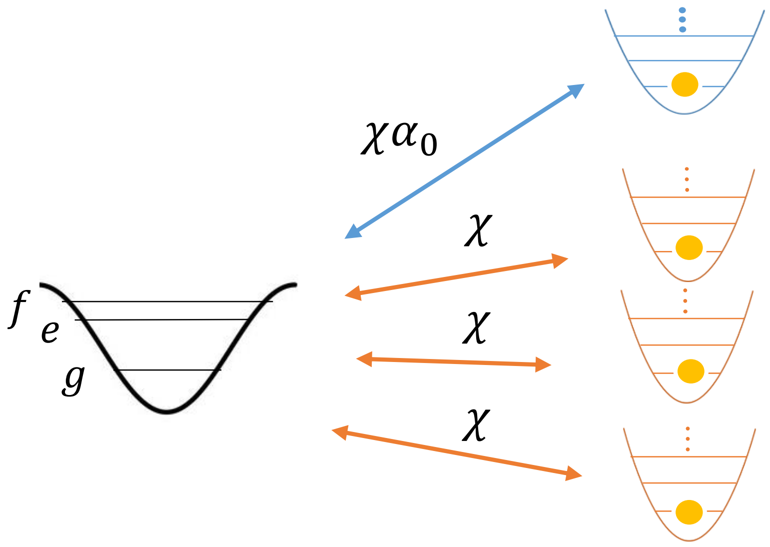
Echo

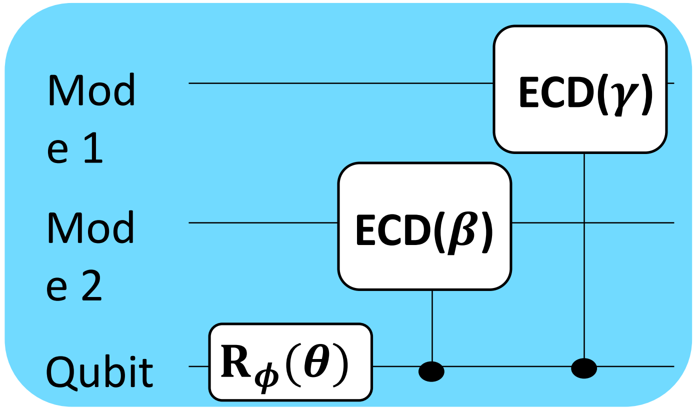
$$\chi(\alpha a^{+} + \alpha^{*} a)\sigma_z \quad \longrightarrow \quad \chi(\alpha a^{+} + \alpha^{*} a)\sigma_z$$

$$\chi|\alpha|^2\sigma_z \quad \longrightarrow \quad \chi|\alpha|^2(-\sigma_z)$$

A. Eickbusch, ..., R. Schoelkopf, M. Devoret. ArXiv preprint arXiv:2111.06414 (2021)

Conclusions and Future Work

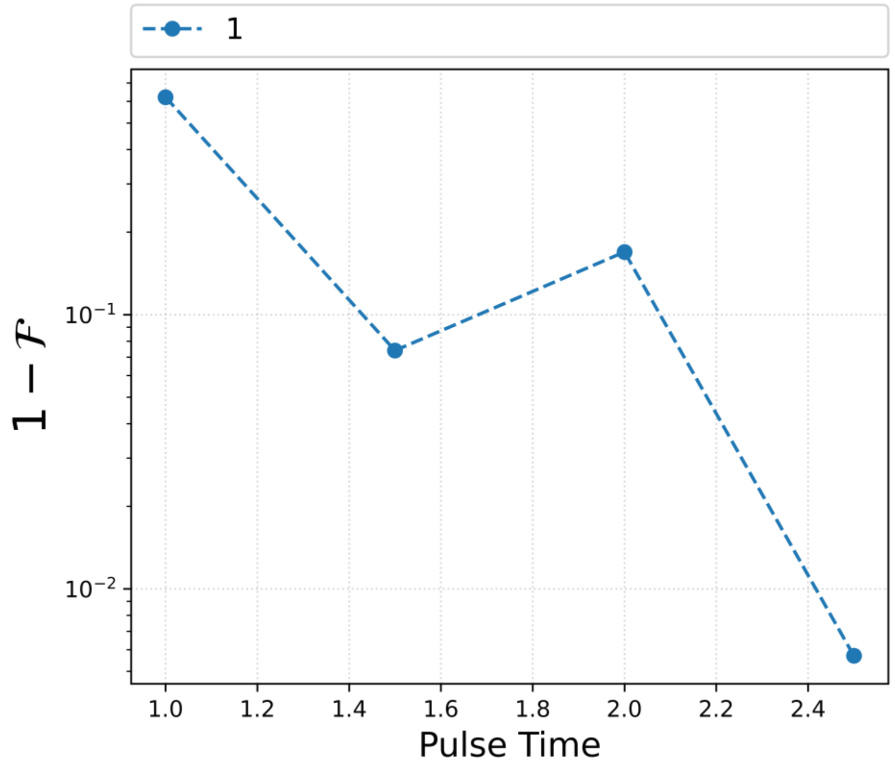




- Suppression of cross-talk errors
- Achieve >0.999 fidelity for fock state transfer using Double ECD
- Future Work:
  - Unite ECD with Sidebands scheme and CNOD

Circle Grape Results

$g \otimes (|n0\rangle \rightarrow |0n\rangle)$



$g \otimes (|0\rangle \rightarrow |n\rangle)$

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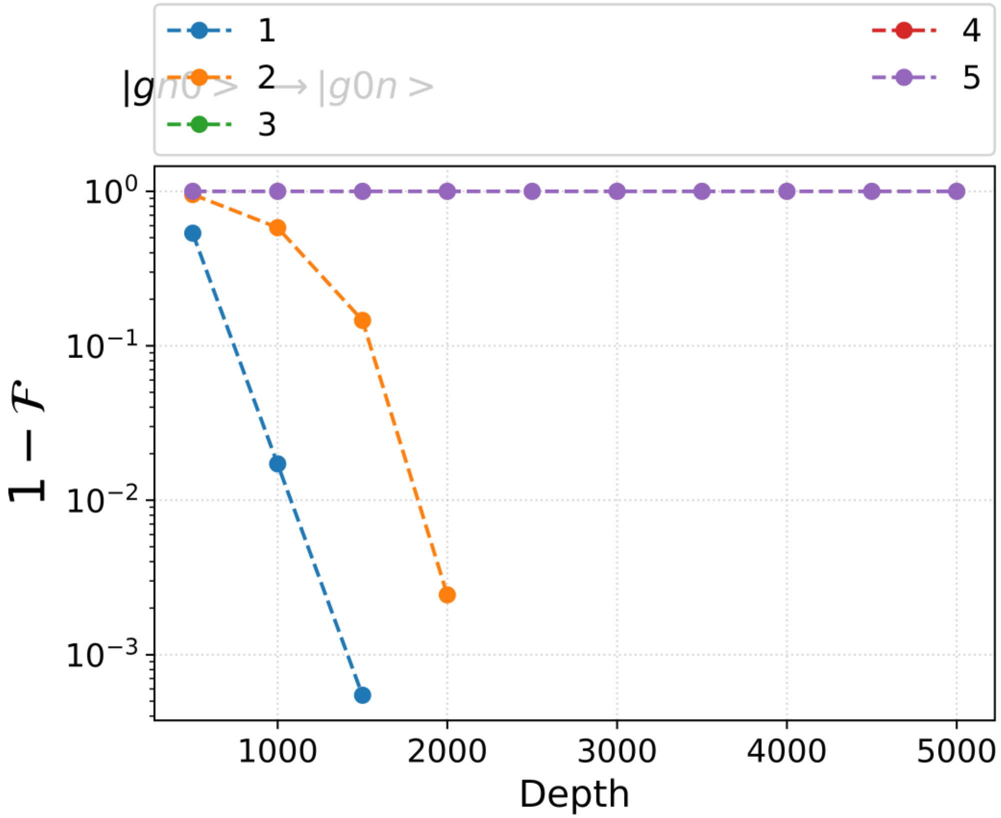


Uniting with other schemes: Dealing with Unwanted Terms

The **displaced frame** transformation, however, divides the **initial ac-Stark shift** term into the following 3 terms

$$\chi(a^\dagger + \alpha^*)(a + \alpha)\sigma_z$$

$$\downarrow$$

$$\chi a^\dagger a \sigma_z \quad + \quad \underbrace{\chi(\alpha a^\dagger + \alpha^* a)\sigma_z}_{\text{desired}} \quad + \quad \chi|\alpha|^2\sigma_z$$

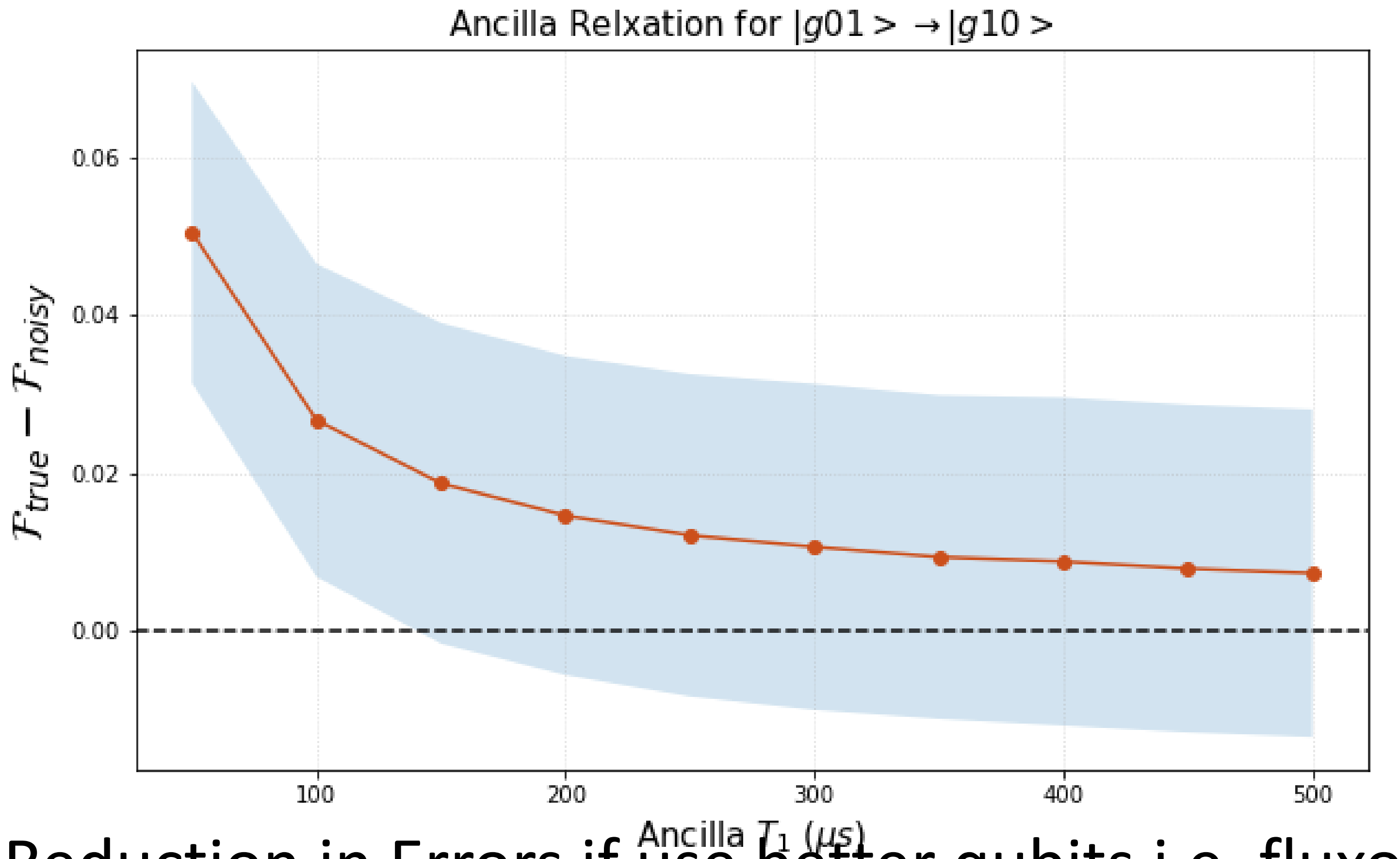
Sideband Drives

- Make terms **oscillate at different** frequencies
- Invoke RWA in a frame where only desired term is stationary

Echoed Cond. Displacements

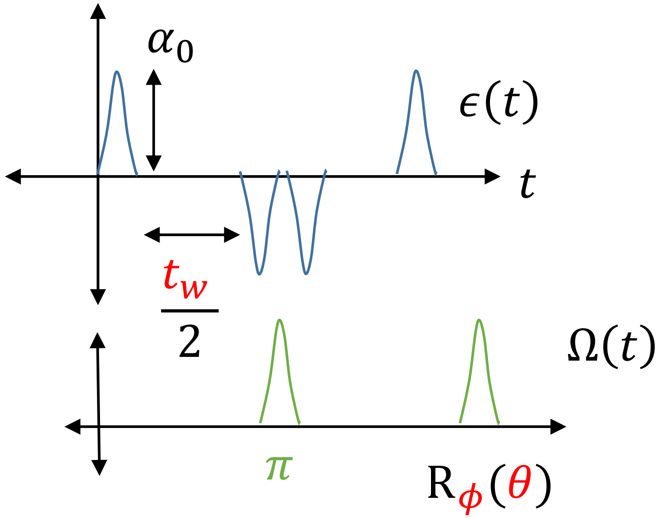
- Terms have different no. of α's but only a single σ_z
- **Clever flipping of α and $\boldsymbol{\sigma_z}$** can echo out unwanted terms

Transmon Relaxation



- Reduction in Errors if use better qubits i.e. fluxonium

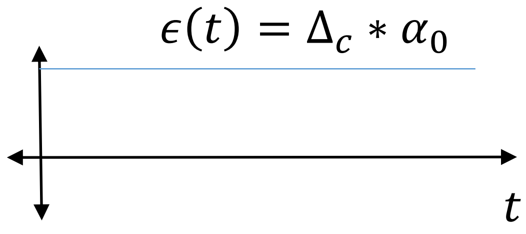
ECD



Optimizer

$\vec{\beta} = \alpha_0 \overrightarrow{t_w} \quad \vec{\phi}, \vec{\theta}$

Circle Grape

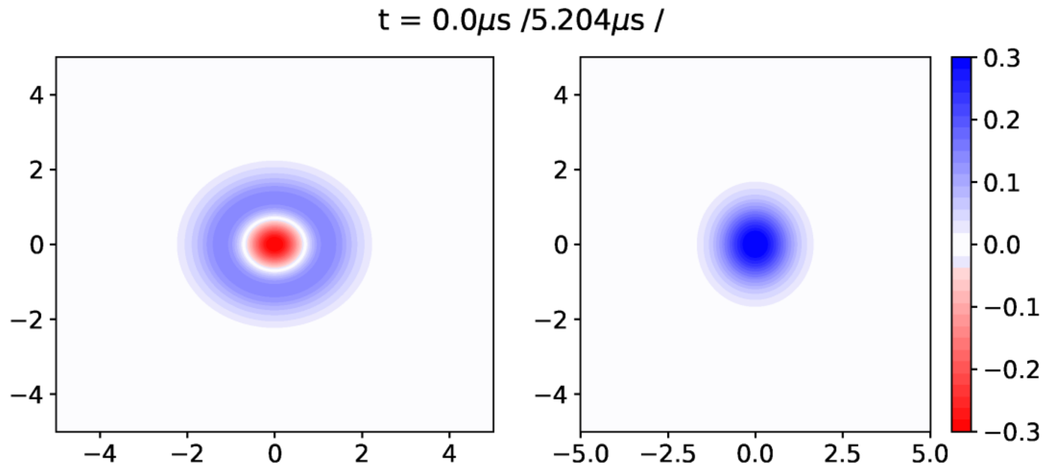


Optimizer

$\Omega_x(t), \Omega_y(t)$

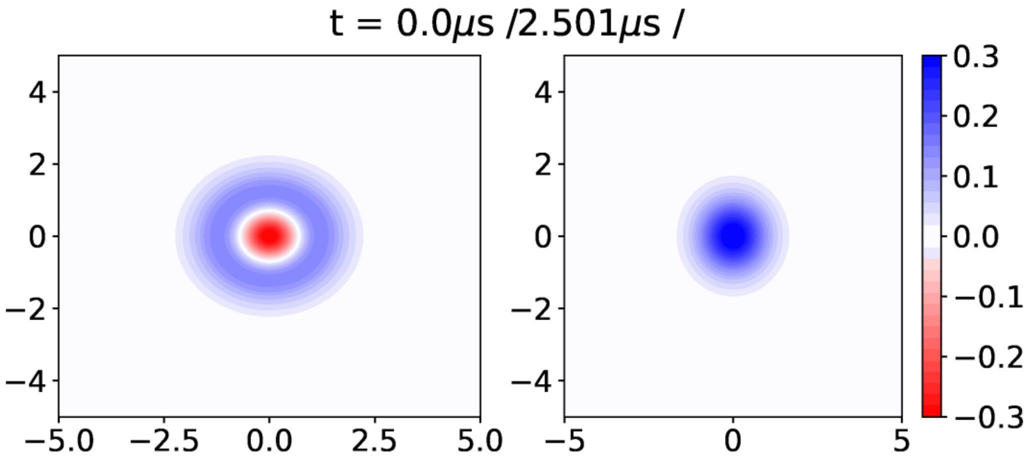
Comparing Grape and MECD

ECD



Type equation here

Circle Grape



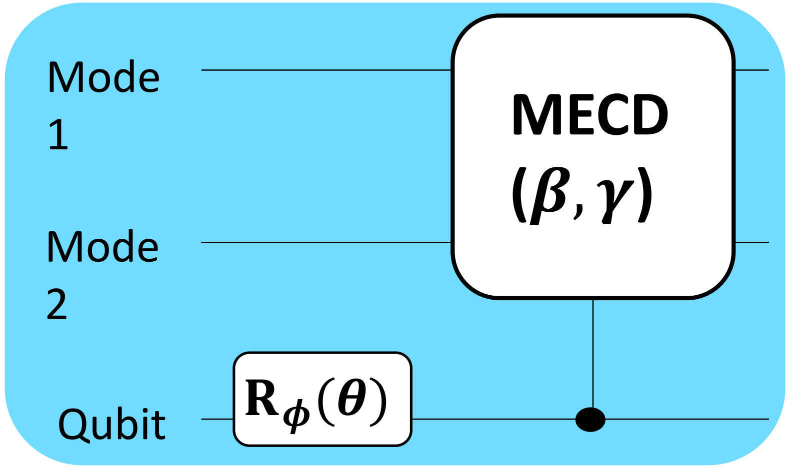
Circle Grape

$$H = \chi a^{+} a \sigma_z + \chi(\alpha_0 a^{+} + \alpha_0^{*} a)\sigma_z + \chi|\alpha_0|^2 \sigma_z + \Omega(t)\sigma_x$$

Sent to Optimizer

- Continuous version
- Currently uses simulatenous drives
- Phase Space Dynamics

Multimode ECD



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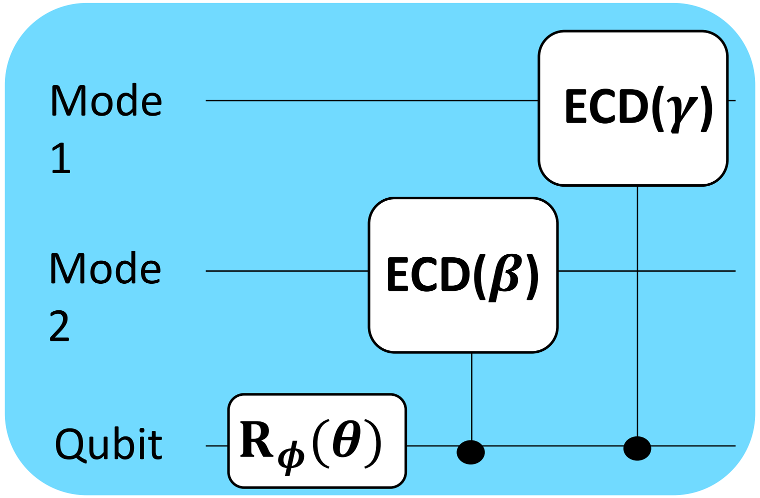
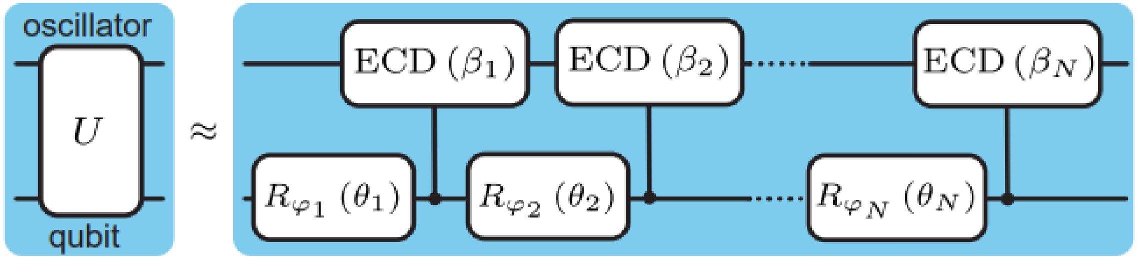


$$MECD(\beta,\gamma) = \begin{pmatrix} D_1\left(-\frac{\beta}{2}\right)D_2\left(\frac{\gamma}{2}\right) & 0 \\ 0 & D_1\left(\frac{\beta}{2}\right)D_2\left(-\frac{\gamma}{2}\right) \end{pmatrix}$$

Prev. Work: **Echoed** Cond. Disp.

Parameter Optimization



$$ECD(\beta) = D\left(\frac{\beta}{2}\right)|e\rangle\langle g| + D\left(-\frac{\beta}{2}\right)|g\rangle\langle e|$$

Pulse Optimization

A. Eickbusch, ..., R. Schoelkopf, M. Devoret. ArXiv preprint arXiv:2111.06414 (2021)

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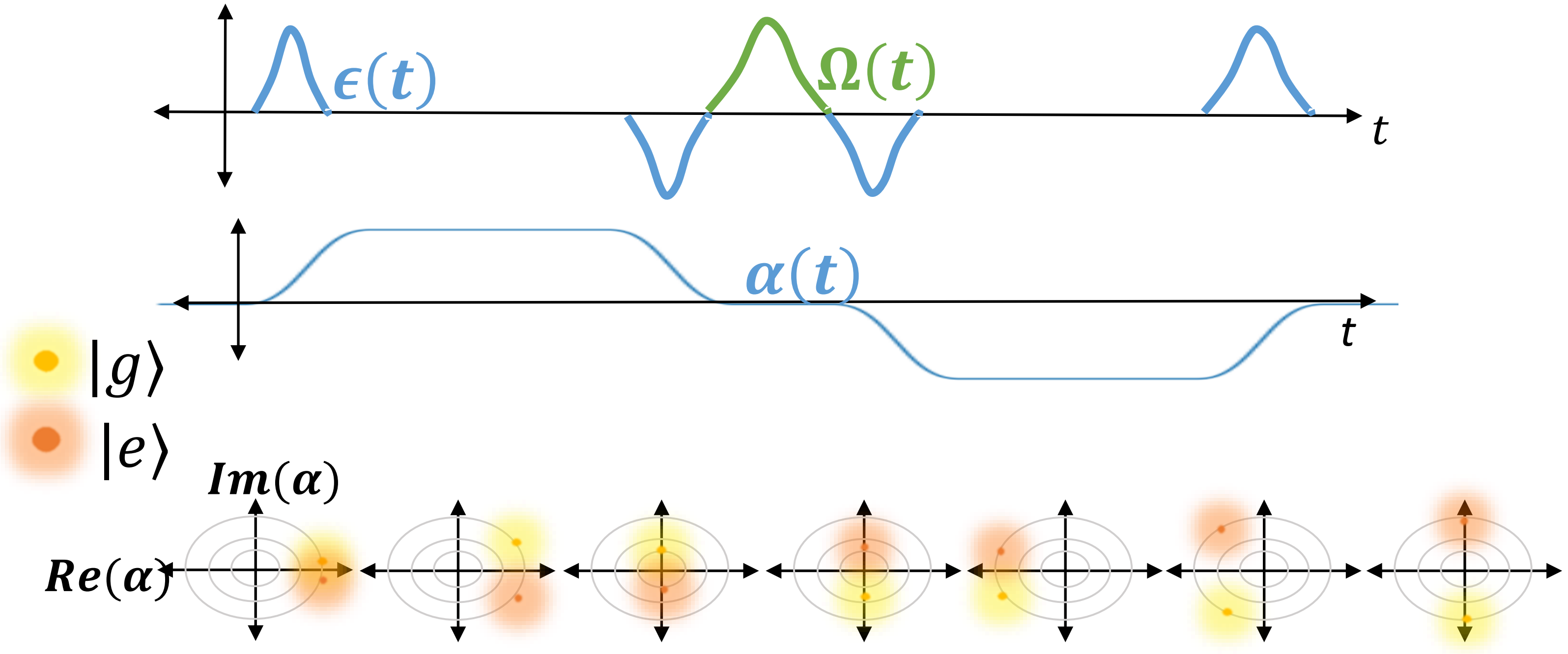

A. Eickbusch, ..., R. Schoelkopf, M. Devoret. *ArXiv preprint arXiv:2111.06414 (2021)*

Two Mode ECD : Unwanted Cross Kerr Terms

$$\chi_{ab} a^{+} a\, b^{+} b \xrightarrow{\text{Displaced Frame Transformation}} \chi_{ab}(a^{+} + \alpha^{*})(a + \alpha)(b^{+} + \beta^{*})(b + \beta)$$

Terms of form :	How to avoid :
$\chi_{ab}\boldsymbol{\alpha\beta}\, a^{+} b^{+}$	α, β should not be simultaneously nonzero
$\chi_{ab}\lvert\boldsymbol{\alpha}\rvert^{2}\boldsymbol{\beta}\, b^{+}$	Echoed out when β flips
$\chi_{ab}\lvert\boldsymbol{\alpha}\rvert^{2} b^{+} b$	Make $\chi_{ab} \ll \chi_a, \chi_b \approx 10$ kHz Note $\chi_{ab} = \sqrt{\kappa_a \kappa_b} = \frac{\chi_a \chi_b}{\alpha'} \approx 0.33$ Hz ... good! ($\alpha' \leq 300$ MHz for transmons)