

$$1) \Delta v = I_{sp} g_0 \ln\left(\frac{m_0}{m_f}\right)$$

$$\Delta v = 7.6 \text{ km/s} = 7600 \text{ m/s}$$

$$I_{sp} = 400 \text{ s}$$

$$g_0 = 9.8 \text{ m/s}^2$$

$$m_0 = m_{prop} + m_{pay} + m_{roll}$$

$$m_f = m_{pay} + m_{roll}$$

$$\frac{19}{9.8} = \ln\left(\frac{m_0}{m_f}\right)$$

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$$e^{\frac{19}{9.8}} = \frac{m_0}{m_f} = \frac{m_{prop}}{m_f} + 1$$

$$m_{prop} = \left(e^{\frac{19}{9.8}} - 1 \right) m_f$$

$$5.95 = \frac{m_{prop}}{m_f}$$

$$m_0 = m_{prop} + m_f$$

$$m_0 = m_{prop} \left(\frac{6.95}{5.95} \right)$$

$$\frac{m_{prop}}{m_0} = \left(\frac{5.95}{6.95} \right) \approx 0.856$$

$$2) \frac{dm}{dt} = -\dot{m} \quad \frac{dm}{dt} = -\dot{m}$$

$$m = \frac{m(t)}{m_0} = \frac{m_0 - \dot{m}t}{m_0}$$

$$F_{net} = \frac{c\dot{m}}{m} - mg$$

$$m \frac{dv}{dt} = \frac{c\dot{m}}{m} - mg$$

$$m \frac{dv}{dm} \frac{dm}{dt} = \frac{c\dot{m}}{m} - mg$$

$$-m \dot{m} \frac{dv}{dm} = \frac{c\dot{m}}{m} - mg$$

$$-\dot{m} \frac{dv}{dm} = \frac{n(m_0 \dot{m})}{m} - mg$$

$$\frac{m_0 - \dot{m}t}{m_0}$$

(b)

$$\frac{dz}{dt} = -g + \frac{n m_0 g}{\dot{m}} \ln\left(\frac{m}{m_0}\right)$$

$$m = m_0 - \dot{m}t \quad \frac{dv}{dt} = \frac{c\dot{m}}{m} - mg$$

$$\frac{dv}{dt} = \frac{c\dot{m} - (m_0 - \dot{m}t)g}{m - \dot{m}t}$$

$$z = -gt + \frac{n m_0 g}{\dot{m}} \ln\left(\frac{m}{m_0}\right)$$

$$\frac{dv}{dm} = \left[\frac{n(m_0 \dot{m})}{m} - g \right] \frac{1}{\dot{m}}$$

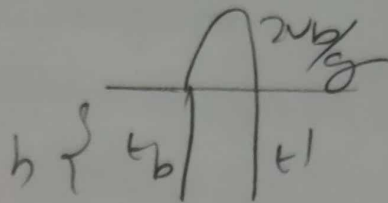
$$-v = \frac{n m_0 g}{\dot{m}} \ln\left(\frac{m}{m_0}\right) - \frac{g}{\dot{m}} (m_0 - \dot{m}t)$$

$$v = -gt - \frac{n m_0 g}{\dot{m}} \ln\left(\frac{m}{m_0}\right)$$

(c) burnout time t_b

$$t_b + \left(\frac{2v_b}{g} \right) + t'$$

free fall



$$h = v_b t' + \frac{1}{2} g (t')^2$$

(d) $\eta = \frac{F_{thrust}}{m_0 g}$ - exhaust speed

3.
8350

$$\Delta v = v_{ex} \ln \left(\frac{m_0}{m_f} \right)$$

$$\frac{16}{8350} = \frac{4000}{9} \ln \left(\frac{m_0}{m_f} \right)$$

$$e^{\frac{16}{9}} = \frac{m_0}{m_f} \quad m_0 = 5.93 m_f$$

$$4.93(m_{prop} + m_r) = m_{prop}$$

$$4.93(m) = m - 10$$

$$m_0 = 5.93 m$$

$$4. \Delta v = I_{sp} g_0 \ln(MR)$$

$$MR = \frac{m_i}{m_f} = \frac{\overset{\text{propellant}}{m_p} + \overset{\text{rocket mass}}{m_s} + \overset{\text{payload}}{m_{pl}}}{m_s + m_{pl}}$$

$$\epsilon = \frac{m_p}{m_i} = \frac{m_i - m_f}{m_i} = 1 - \frac{m_f}{m_i} = 1 - \frac{1}{MR} = \frac{MR-1}{MR}$$

$$\lambda = \frac{m_s}{m_p + m_s} = \frac{m_s}{m_i - m_{pl}} = \frac{\frac{m_s}{m_i}}{1 - \frac{m_{pl}}{m_i}} \Rightarrow \frac{m_s}{m_i} = \left(1 - \frac{m_{pl}}{m_i}\right) \lambda$$

$$1 - \lambda \left(\frac{m_{pl}}{m_i} \right) = \frac{m_s}{m_i}$$

$$\lambda = \frac{1}{m_i} (m_s + \lambda m_{pl})$$

$$1 = \frac{m_{pl}}{m_i} + \frac{m_p}{m_i} + \frac{m_s}{m_i}$$

$$1 = \frac{m_{pl}}{m_i} + \epsilon + \frac{m_s}{m_i}$$

$$\left(1 - \epsilon - \frac{m_{pl}}{m_i}\right) = \frac{m_p}{m_i}$$

$$m_i = \frac{m_{pl}}{\left(1 - \frac{\epsilon}{1-\lambda}\right)}$$

$$m_i = \frac{2000}{\left(1 - \frac{\epsilon}{1-\lambda}\right)}$$

hyperbola

