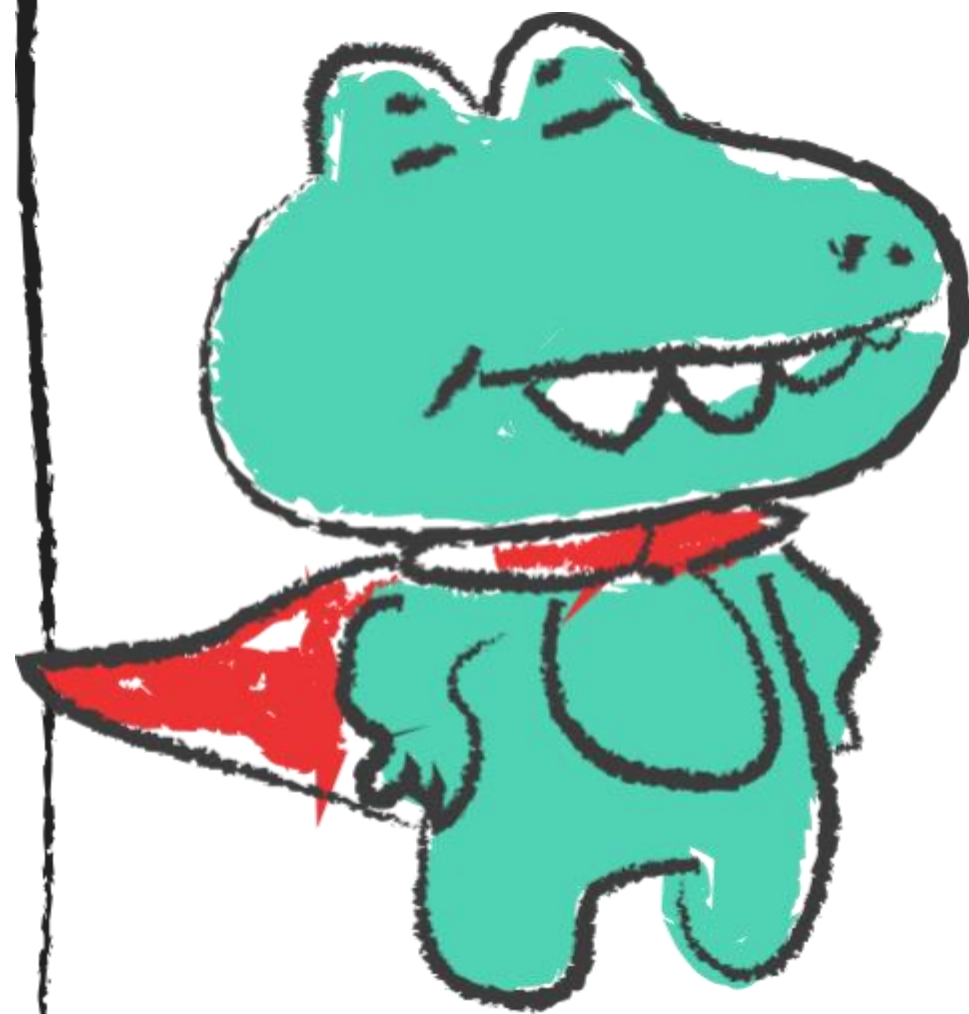


# Quick Sort



Smart Device engineering  
19011773 MOON\_EeSun



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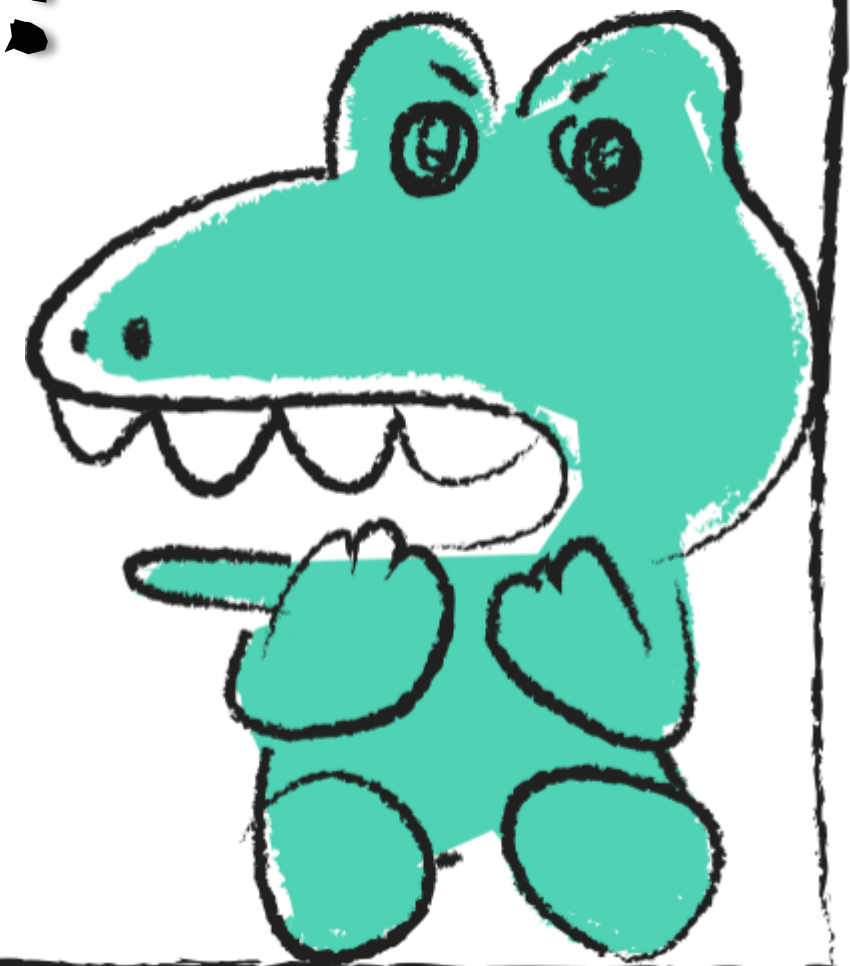
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What is  
✦ Quick Sort? ✦ ✦







# First. Description & Techniques<sup>✦</sup>

**Quick sort** : To divide one list into two unequal sizes based on pivots, arrange the segmented list, and then combine the two sorted partial lists to make the whole list sorted.

## Divide and Conquer method

- **Divide** : Divide the array into two subarrays, based on the pivot  
left - elements smaller than pivot / right - elements larger than pivot
- **Conquer** : Arranges the sub-arrangement.
- **Combine** : Merge aligned partial arrays into one array.

Time Complexity : best case -  $O(n \log n)$  / worst case -  $O(n^2)$



# First. Description & Techniques ✨

Init status

6	4	9	5	10	2	7	15
---	---	---	---	----	---	---	----

6	4	9	5	10	2	7	15
---	---	---	---	----	---	---	----



5	4	2	6	10	9	7	15
---	---	---	---	----	---	---	----

smaller

pivot

bigger



2	4	5	6	7	9	10	15
---	---	---	---	---	---	----	----

smaller pivot

smaller pivot bigger



# First. Description & Techniques ✨

Init status

6	4	9	5	10	2	7	15
---	---	---	---	----	---	---	----

2	4	5	6	7	9	10	15
---	---	---	---	---	---	----	----

smaller pivot

smaller pivot bigger

2	4	5	6	7	9	10	15
---	---	---	---	---	---	----	----

pivot

pivot

Repeat until array size is 1

Sorted status

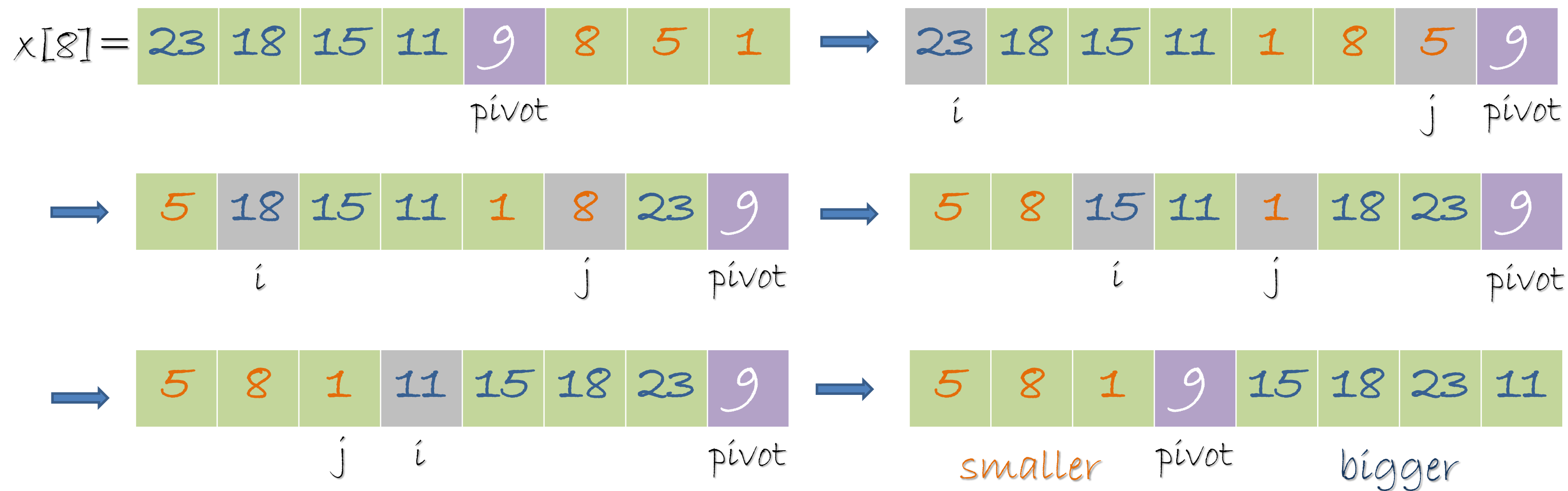
2	4	5	6	7	9	10	15
---	---	---	---	---	---	----	----



# Second. Example

Example 1. the worst case - Reverse

$x[8] = \{23, 18, 15, 11, 9, 8, 5, 1\}$



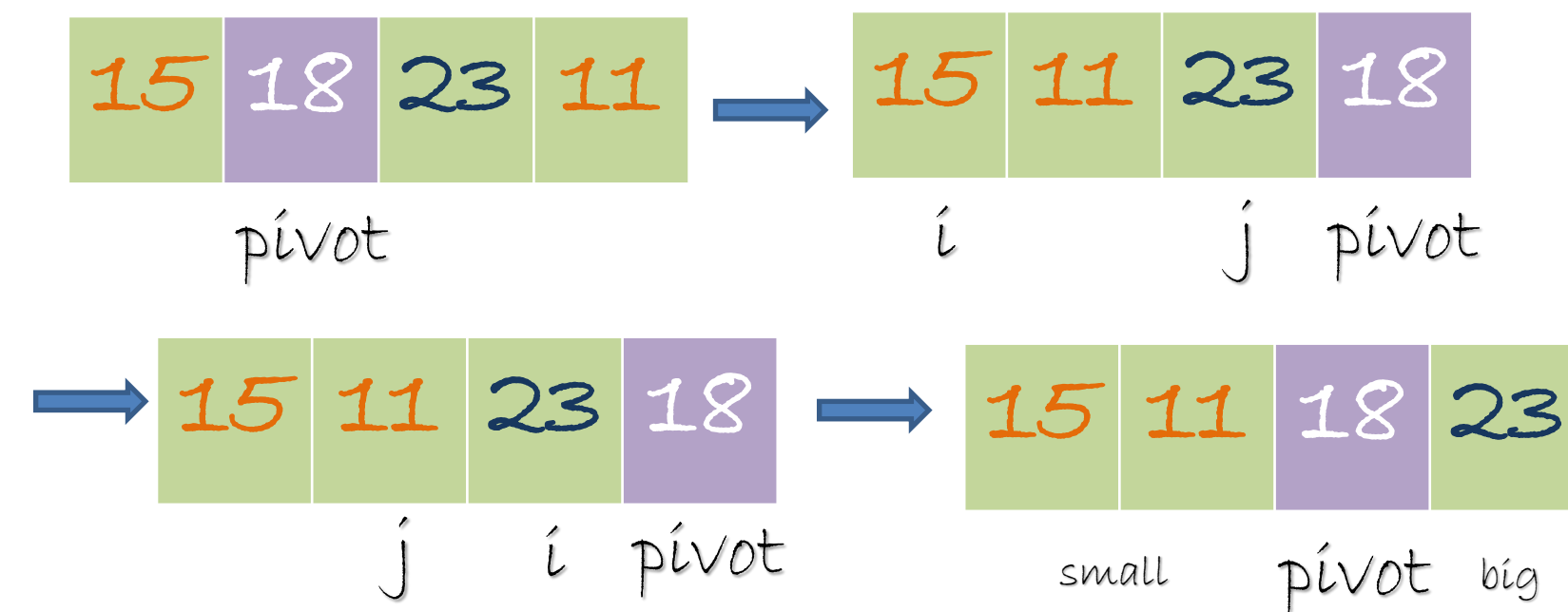
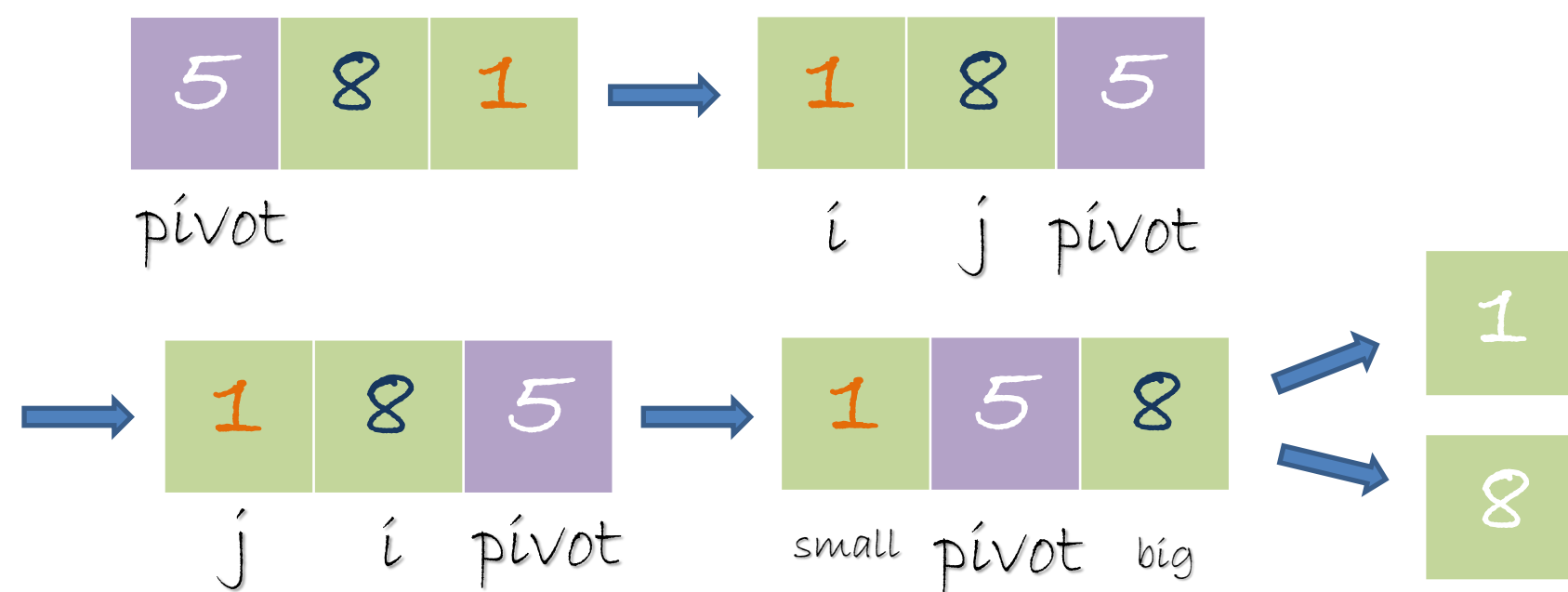
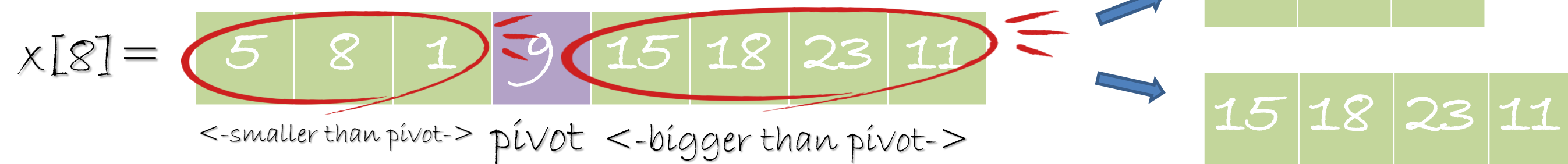




# Second. Example

Example 1. the worst case - Reverse

$x[8] = \{23, 18, 15, 11, 9, 8, 5, 1\}$



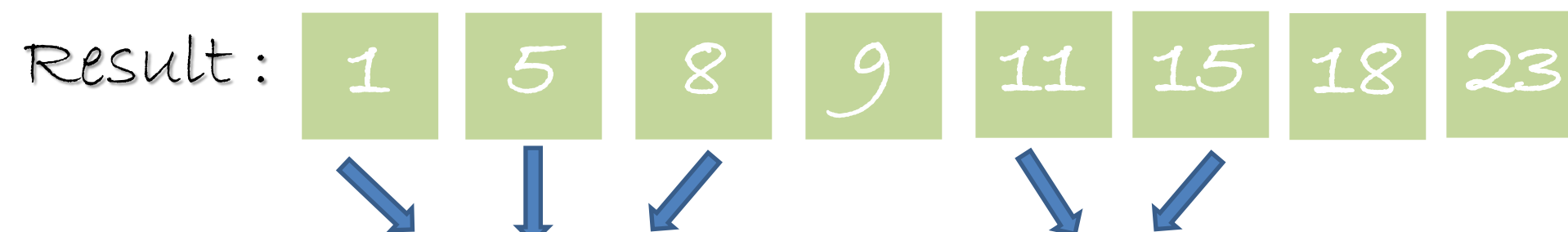
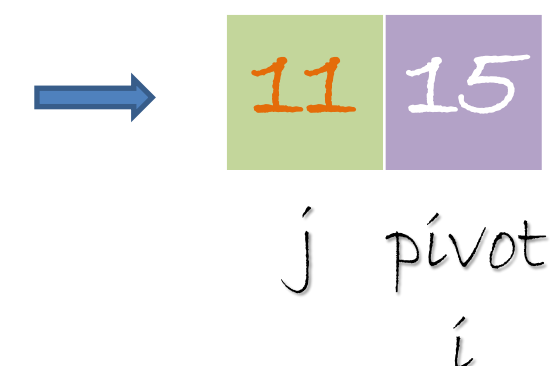
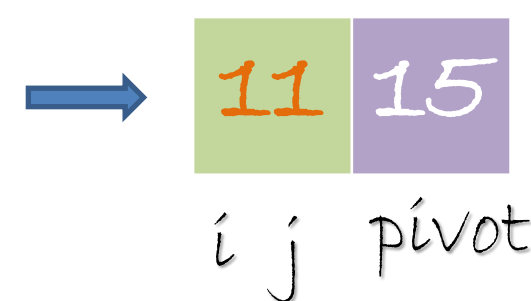
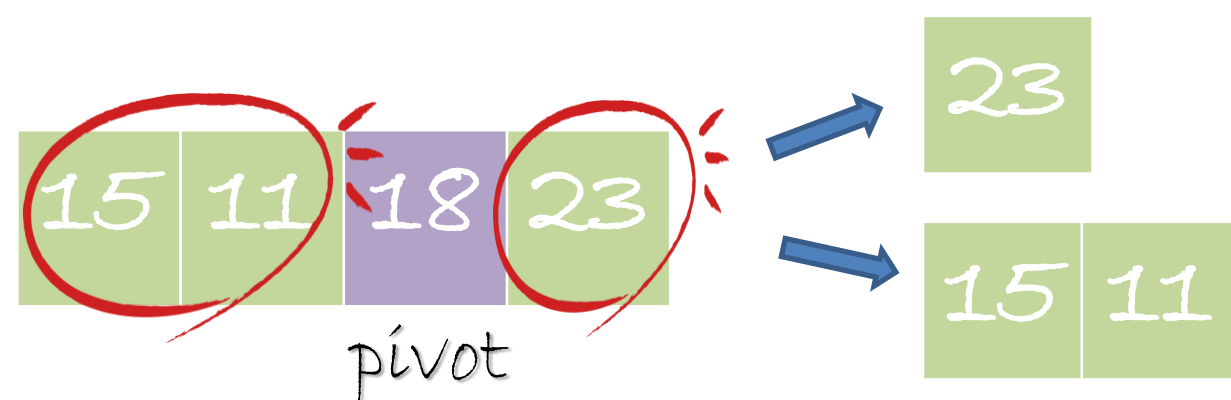




# Second. Example

Example 1. the worst case - **Reverse**

$x[8] = \{23, 18, 15, 11, 9, 8, 5, 1\}$



Combine  
: recursive

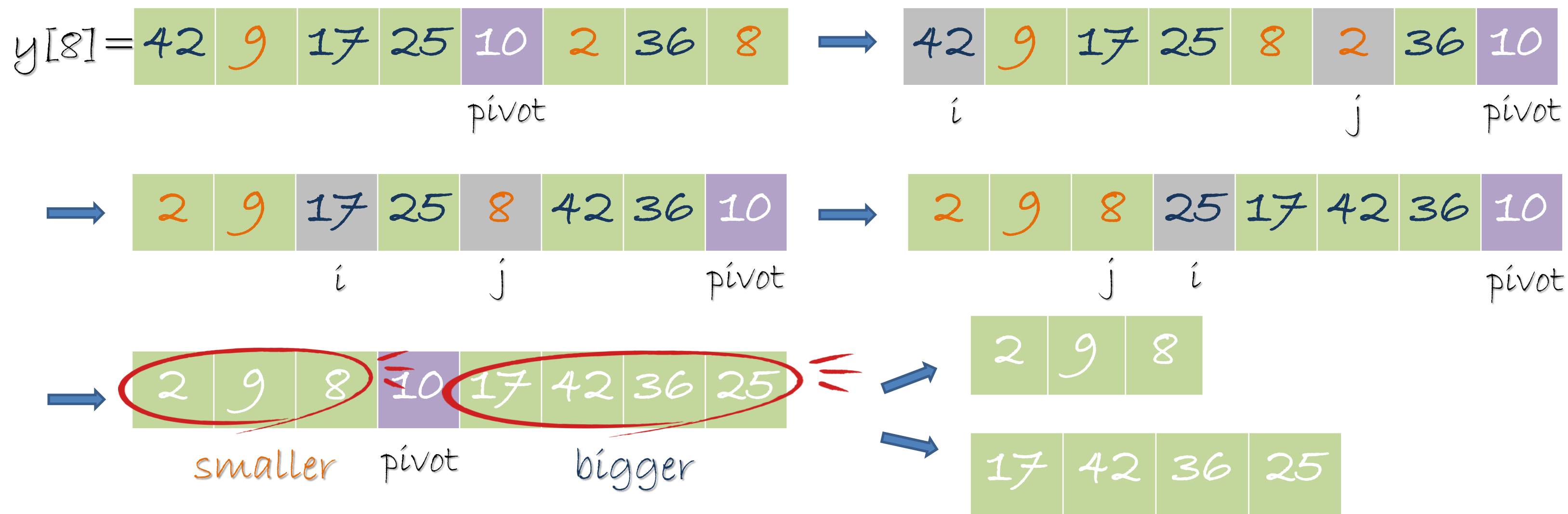




# Second. Example

Example 2.

$y[8] = \{42, 9, 17, 25, 10, 2, 36, 8\}$

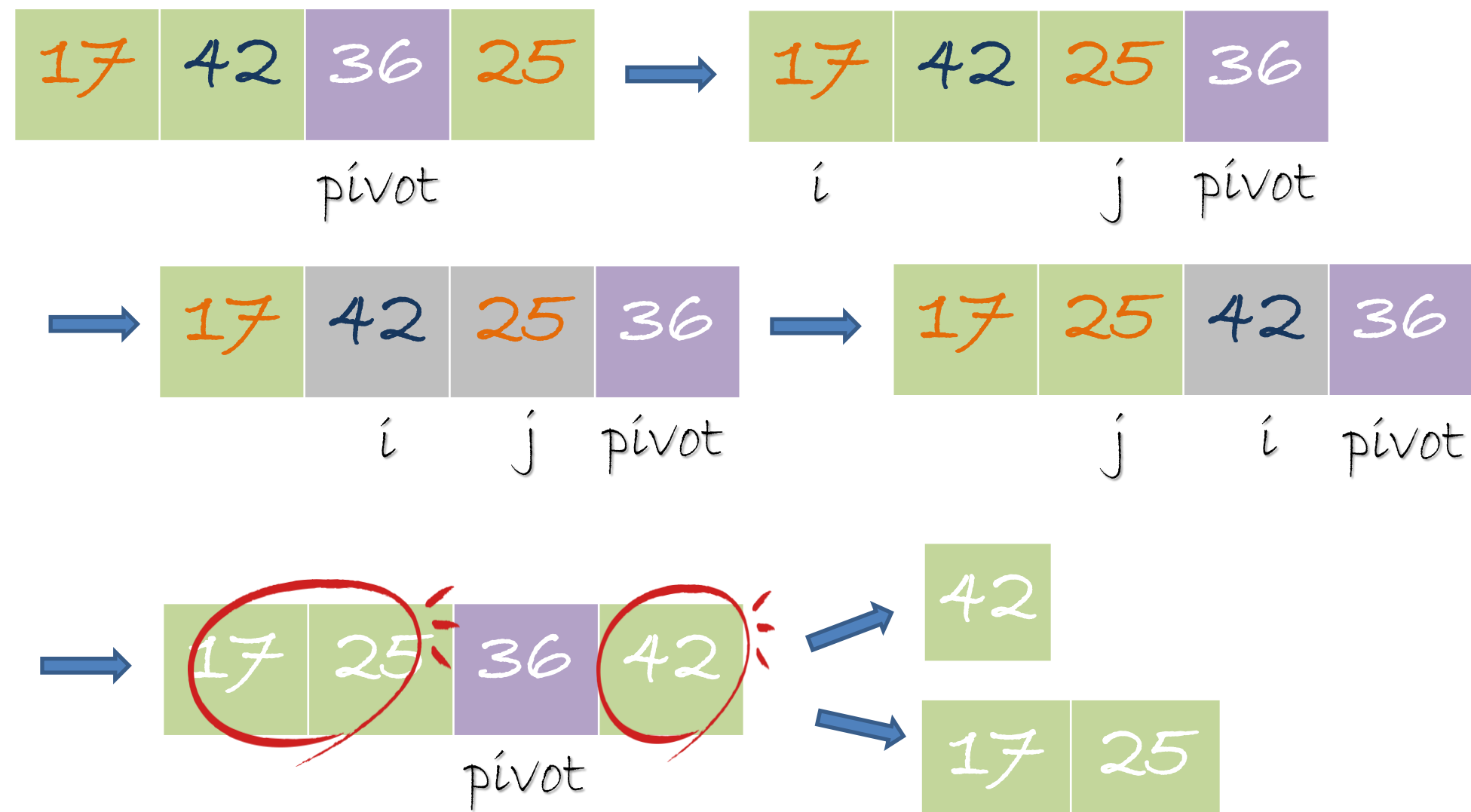
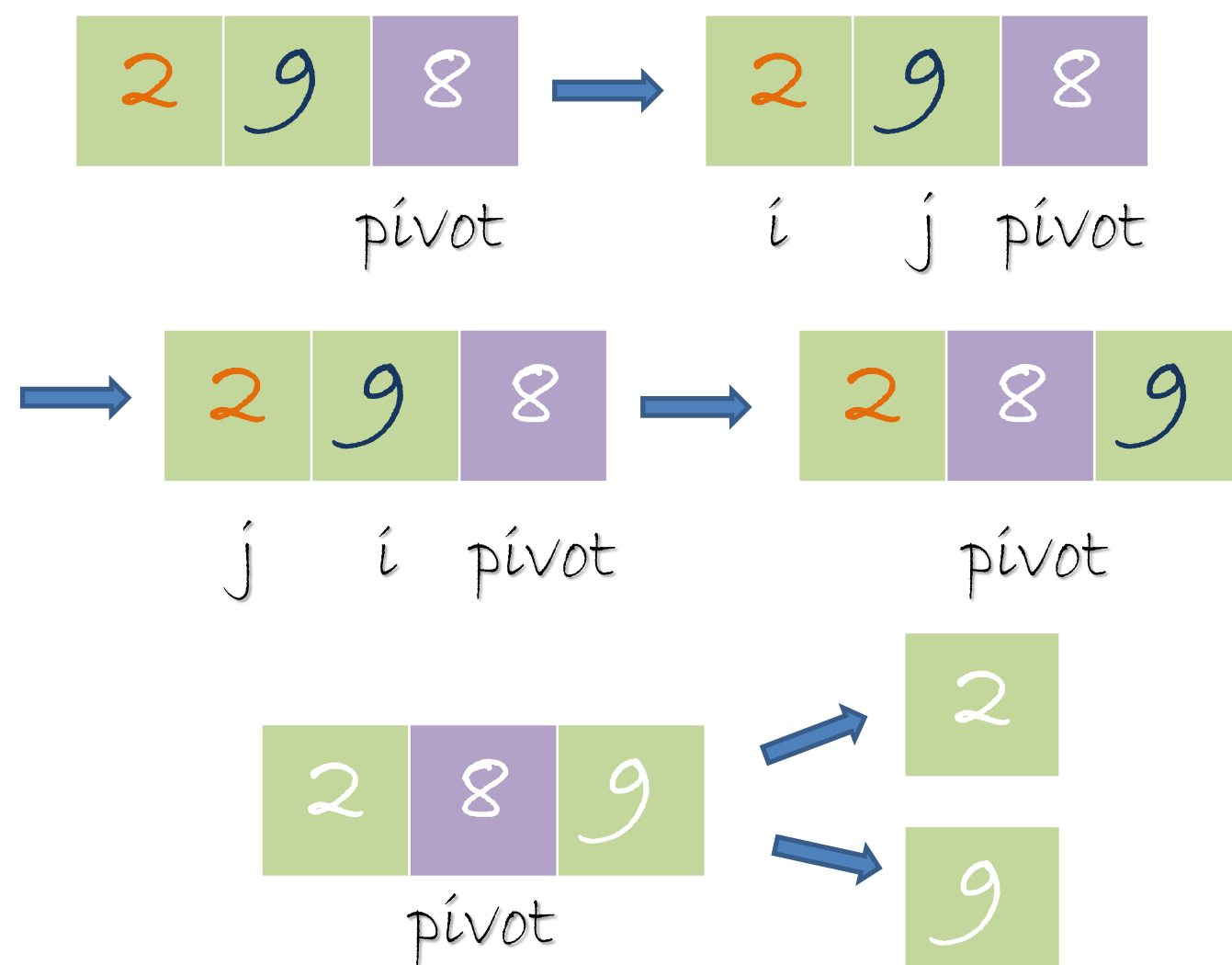




# Second. Example

Example 2.

$y[8] = \{42, 9, 17, 25, 10, 2, 36, 8\}$

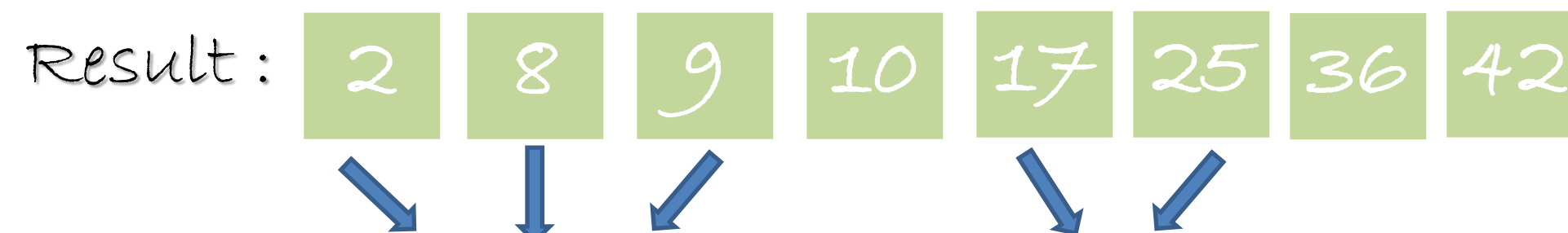




# Second. Example

Example 2.

$y[8] = \{42, 9, 17, 25, 10, 2, 36, 8\}$



Combine  
: recursive





# Third. Pseudocode

## Fuction

- Swap(int Q[], int a, int b)  
: Change ath index element and bth index element
- Median(int Q[], int a, int b, int c)  
: To select a pivot, choose the middle value of the three numbers
- Find\_pivot\_index(int Q[], int l, int r)  
: choose three random numbers, and choose the middle of the three random numbers
- inPlacePartition(Q, l, r, k)  
: Function to sort by pivot
- inPlaceQuickSort(Q, l, r)  
: Quick sort algorithm
- Main(void)  
: Enters an array of size N and executes a quick sort



# Third. Pseudocode

- Swap(int Q[], int a, int b)

input array Q, index a, b

output array Q changed ath index element and bth index element

```
tmp <- Q[a]
```

```
Q[a] <- Q[b]
```

```
Q[b] <- tmp
```

- Median(int Q[], int a, int b, int c)

input array Q, index a, b, c

output index of the middle values of Q[a], Q[b], Q[c]



# Third. Pseudocode

- Find\_pivot\_index(Q, l, r)

input array of Q, index l, r

output index of the middle values of p1, p2, p3

p1 <- random number from l to r

p2 <- random number from l to r

p3 <- random number from l to r

pivot\_index <- median(Q, p1, p2, p3)

return pivot\_index



# Third. Pseudocode

- `inPlacePartition(Q, l, r, k)`

input array  $Q[l...r]$  of distinct elements, index  $l, r, k$

output final index of the pivot resulting from partitioning  $Q[l...r]$  into

`p ← Q[k]`

`swap(Q, k, r)`

`i ← l`

`j ← r-1`

`while (i ≤ j)`

`while (i ≤ j ∧ Q[i] ≤ p) i++`

`while (j ≥ i ∧ Q[j] ≥ p) j--`

`swap(Q, i, r)`

`return i`





# Third. Pseudocode

- `inPlaceQuickSort(Q, l, r)`

input array `Q`, position `l`, `r`

output array `Q` with elements of position from `l` to `r` rearranged in increasing order

if  $(l \geq r)$  return

`pivot`  $\leftarrow$  `find_pivot_index(Q, l, r)`

`a`, `b`  $\leftarrow$  `inPlacePartition(Q, l, r, pivot)`

`inPlaceQuickSort(Q, l, a-1)`

`inPlaceQuickSort(Q, b+1, r)`

- `Main(void)`

`N`  $\leftarrow$  input

`Q`  $\leftarrow$  malloc

for  $i=0$  to `N`

`Q[i]`  $\leftarrow$  input

`inPlaceQuickSort(Q, 0, N-1)`

print(`Q`, 0, `N-1`)



# Fourth. C-code ✨

```
1  #pragma warning(disable:4996)
2  #include <stdio.h>
3  #include <stdlib.h>
4  #include <time.h>
5
6  void swap(int Q[], int a, int b)
7  {
8      int tmp;
9      tmp = Q[a];
10     Q[a] = Q[b];
11     Q[b] = tmp;
12 }
13
```

Declare  
Header File

function swapping with ath  
element and bth element

```
14 int median(int Q[], int a, int b, int c)
15 {
16     int max = Q[a], min = Q[a];
17     if (max < Q[b]) max = Q[b];
18     if (max < Q[c]) max = Q[c];
19     if (min > Q[b]) min = Q[b];
20     if (min > Q[c]) min = Q[c];
21     if (max == Q[a]) {
22         if (min == Q[b]) return c;
23         else return b;
24     }
25     else if (max == Q[b]) {
26         if (min == Q[a]) return c;
27         else return c;
28     }
29     else {
30         if (min == Q[a]) return b;
31         else return a;
32     }
33 }
34
```

a function that indexes the intermediate  
elements between the ath element and  
the bth element and the cth element



## Fourth. C-code ✨

a function that randomly selects three pivot indexes and sets the middle value of them as pivot.

```
35 int find_pivot_index(int Q[], int l, int r)
36 {
37     int pivot_index, p1, p2, p3;
38     srand(time(NULL)); //initialize base point with current time
39
40     //random index designation between lth index to rth index
41     p1 = rand() % (r - l) + l;
42     p2 = rand() % (r - l) + l;
43     p3 = rand() % (r - l) + l;
44
45     pivot_index = median(Q, p1, p2, p3); //the middle value of p1, p2, p3
46     return pivot_index;
47 }
48
```



# Fourth. C-code ✨

a function that randomly selects three pivot indexes and sets the middle value of them as pivot.

```
49 int inplacePartition(int Q[], int l, int r, int k)
50 {
51     int i, j, p;
52     p = Q[k];
53     swap(Q, k, r); //Swap pivot(p) to the last element
54     i = l; j = r - 1;
55
56     //Align to the right of the pivot if greater than or equal to the pivot,
57     //or to the left of the pivot if smaller or equal to the pivot.
58     while (i <= j)
59     {
60         while (i <= j && Q[i] <= p) i++;
61         while (j >= i && Q[j] >= p) j--;
62         if (i < j) swap(Q, i, j);
63     }
64     swap(Q, i, r); //If i and j reverse, change the pivot and ith number
65
66     return i;
67 }
68
```





# Fourth. C-code ✨

```
69 void inPlaceQuickSort(int Q[], int l, int r)
70 {
71     int pivot, a, b, tmp;
72
73     if (l >= r) return; //return if l reverse r
74
75     pivot = find_pivot_index(Q, l, r); //find the pivot index
76
77     //sorting by pivot
78     //b is the last index of the same element as pivot
79     b = inPlacePartition(Q, l, r, pivot);
80
81     tmp = b;
82     while (1)
83     {
84         if (Q[tmp] != Q[b]) {
85             a = tmp + 1;
86             break;
87         }
88         tmp--;
89     }
90
91     inPlaceQuickSort(Q, l, a - 1);
92     inPlaceQuickSort(Q, b + 1, r);
93 }
94
```

The same number of index ranges as pivots are a, b, the process of obtaining a through b.

Quick Sort algorithms

```
94
95 void main()
96 {
97     int N, *Q, x, i, a, b;
98     scanf("%d", &N); //enter the array size
99     //Dynamic assignment of arrays of size N
100     Q = (int*)malloc(sizeof(int)*N);
101     for (i = 0; i < N; i++)
102     {
103         scanf("%d", &x);
104         Q[i] = x;
105     } //save input elements in array
106
107     inPlaceQuickSort(Q, 0, N - 1);
108
109     for (i = 0; i < N; i++)
110         printf(" %d", Q[i]); //print a sorted array
111 }
```

Main function : Enter array size N, and store the entered integer by dynamically assigning an array of size N. Declares a quick-sort algorithm and print an ordered array.



Thank you

