4.

Table 2.10 Regression Output When Y is Regressed on X for Labor Force Participation Rate of Women

Variable	Coefficient	s.e.	t-Test	p-value
Constant	0.203311	0.0976	2.08	0.0526
X	0.656040	0.1961	3.35	< 0.0038
$n = 19$	$R^2 = 0.397$	$R_a^2 = 0.362$	$\hat{\sigma} = 0.0566$	df = 17

Let Y and X denote the labor force participation rate of women in 1972 and 1968, respectively, in each of 19 cities in the United States. The regression output for this data set is shown in Table 2.10. It was also found that SSR = 0.0358 and SSE = 0.0544. Suppose that the model $Y = \beta_0 + \beta_1 X + \varepsilon$ satisfies the usual regression assumptions.

(a) Compute $\text{Var}(Y)$ and $\text{Cor}(Y, X)$.

(b) Suppose that the participation rate of women in 1968 in a given city is 45%. What is the estimated participation rate of women in 1972 for the same city?

(c) Suppose further that the mean and variance of the participation rate of women in 1968 are 0.5 and 0.005, respectively. Construct the 95% confidence interval for the estimate in (b).

(d) Construct the 95% confidence interval for the slope of the true regression line, β_1.

(e) Test the hypothesis: $\text{H}_0 : \beta_1 = 1$ versus $\text{H}_1 : \beta_1 > 1$ at the 5% significance level.

(f) If Y and X were reversed in the above regression, what would you expect R^2 to be?