

## HW of Regression Diagnostics

1. Consider the computer repair problem discussed in Section 2.3. In a second sampling period, 10 more observations on the variable Minutes and Units were obtained. Since all observations were collected by the same method from a fixed environment, all 24 observations were pooled to form one data set. The data appear in Table 4.6.

**Table 4.6** Expanded Computer Repair Times Data: Length of Service Calls (Minutes) and Number of Units Repaired (Units)

| Row | Units | Minutes | Row | Units | Minutes |
|-----|-------|---------|-----|-------|---------|
| 1   | 1     | 23      | 13  | 10    | 154     |
| 2   | 2     | 29      | 14  | 10    | 166     |
| 3   | 3     | 49      | 15  | 11    | 162     |
| 4   | 4     | 64      | 16  | 11    | 174     |
| 5   | 4     | 74      | 17  | 12    | 180     |
| 6   | 5     | 87      | 18  | 12    | 176     |
| 7   | 6     | 96      | 19  | 14    | 179     |
| 8   | 6     | 97      | 20  | 16    | 193     |
| 9   | 7     | 109     | 21  | 17    | 193     |
| 10  | 8     | 119     | 22  | 18    | 195     |
| 11  | 9     | 149     | 23  | 18    | 198     |
| 12  | 9     | 145     | 24  | 20    | 205     |

- (a) Fit a linear regression model relating Minutes to Units.  
(2) Check each of the standard regression assumptions and indicate which assumption(s) seems to be violated.

2. Consider the data in Table 4.8, which consist of a response variable  $Y$  and six predictor variables. Consider fitting a linear model relating  $Y$  to all six  $X$ -variables.

- (a) What least squares assumptions (if any) seem to be violated?  
(b) Compute  $r_i$ ,  $C_i$ ,  $DFITS_i$ .  
(c) Construct the index plots of  $r_i$ ,  $C_i$ ,  $DFITS_i$ .  
(d) Identify all unusual observations in the data and classify each according to type (i.e., outliers, leverage points, etc.)

Suppose that we fit a linear model relating  $Y$  to the first three  $X$ -variables. Justify your answer to each of the following questions with the appropriate added-variable plot:

- (e) Should we add  $X_4$  to the above model? If yes, keep  $X_4$  in the model.  
(f) Should we add  $X_5$  to the above model? If yes, keep  $X_5$  in the model.

(g) Should we add  $X_6$  to the above model?

(h) Which model(s) would you recommend as the best possible description of  $Y$ ? Use the above results and/or perform additional analysis if needed.

**Table 4.8** Data for Exercises 4.12–4.14

| Row | $Y$ | $X_1$ | $X_2$ | $X_3$ | $X_4$ | $X_5$ | $X_6$ |
|-----|-----|-------|-------|-------|-------|-------|-------|
| 1   | 443 | 49    | 79    | 76    | 8     | 15    | 205   |
| 2   | 290 | 27    | 70    | 31    | 6     | 6     | 129   |
| 3   | 676 | 115   | 92    | 130   | 0     | 9     | 339   |
| 4   | 536 | 92    | 62    | 92    | 5     | 8     | 247   |
| 5   | 481 | 67    | 42    | 94    | 16    | 3     | 202   |
| 6   | 296 | 31    | 54    | 34    | 14    | 11    | 119   |
| 7   | 453 | 105   | 60    | 47    | 5     | 10    | 212   |
| 8   | 617 | 114   | 85    | 84    | 17    | 20    | 285   |
| 9   | 514 | 98    | 72    | 71    | 12    | -1    | 242   |
| 10  | 400 | 15    | 59    | 99    | 15    | 11    | 174   |
| 11  | 473 | 62    | 62    | 81    | 9     | 1     | 207   |
| 12  | 157 | 25    | 11    | 7     | 9     | 9     | 45    |
| 13  | 440 | 45    | 65    | 84    | 19    | 13    | 195   |
| 14  | 480 | 92    | 75    | 63    | 9     | 20    | 232   |
| 15  | 316 | 27    | 26    | 82    | 4     | 17    | 134   |
| 16  | 530 | 111   | 52    | 93    | 11    | 13    | 256   |
| 17  | 610 | 78    | 102   | 84    | 5     | 7     | 266   |
| 18  | 617 | 106   | 87    | 82    | 18    | 7     | 276   |
| 19  | 600 | 97    | 98    | 71    | 12    | 8     | 266   |
| 20  | 480 | 67    | 65    | 62    | 13    | 12    | 196   |
| 21  | 279 | 38    | 26    | 44    | 10    | 8     | 110   |
| 22  | 446 | 56    | 32    | 99    | 16    | 8     | 188   |
| 23  | 450 | 54    | 100   | 50    | 11    | 15    | 205   |
| 24  | 335 | 53    | 55    | 60    | 8     | 0     | 170   |
| 25  | 459 | 61    | 53    | 79    | 6     | 5     | 193   |
| 26  | 630 | 60    | 108   | 104   | 17    | 8     | 273   |
| 27  | 483 | 83    | 78    | 71    | 11    | 8     | 233   |
| 28  | 617 | 74    | 125   | 66    | 16    | 4     | 265   |
| 29  | 605 | 89    | 121   | 71    | 8     | 8     | 283   |
| 30  | 388 | 64    | 30    | 81    | 10    | 10    | 176   |
| 31  | 351 | 34    | 44    | 65    | 7     | 9     | 143   |
| 32  | 366 | 71    | 34    | 56    | 8     | 9     | 162   |
| 33  | 493 | 88    | 30    | 87    | 13    | 0     | 207   |
| 34  | 648 | 112   | 105   | 123   | 5     | 12    | 340   |
| 35  | 449 | 57    | 69    | 72    | 5     | 4     | 200   |
| 36  | 340 | 61    | 35    | 55    | 13    | 0     | 152   |
| 37  | 292 | 29    | 45    | 47    | 13    | 13    | 123   |
| 38  | 688 | 82    | 105   | 81    | 20    | 9     | 268   |
| 39  | 408 | 80    | 55    | 61    | 11    | 1     | 197   |
| 40  | 461 | 82    | 88    | 54    | 14    | 7     | 225   |

Source: Chatterjee and Hadi (1988)