# **SEM2DPACK**

A Spectral Element Method tool for 2D wave propagation and earthquake source dynamics

User's Guide

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## Chapter 1

## Introduction

#### 1.1 Overview

The SEM2DPACK package is a set of software tools for the simulation and analysis of the seismic response of sedimentary basins and dynamic earthquake ruptures. Its core is SEM2D, an explicit Spectral Element solver for the 2D elastic wave equation. The general flow of a simulation project is:

- 1. Mesh generation: a domain decomposition made of quadrilateral elements, linearly (Q4) or quadratically (Q9) deformed.
- 2. Mesh quality verification, return to previous step if needed.
- 3. Numerical simulation.
- 4. Post-processing, analysis and visualization of the output.

SEM2DPACK provides tools for each step. However, no general mesh generation code is included. Instead SEM2D can import unstructured quadrilateral meshes generated externally. As an example we provide an interface to EMC2, one of the few public domain 2D mesh generators including quadrilateral elements and a Graphical User Interface <sup>1</sup>.

This User's Guide explains the usage of the SEM2D solver. For more details, additional results, and for the 3D extension of the algorithm, please refer to Komatitsch (1997), Komatitsch and Vilotte (1998), Komatitsch et al. (1999) and also Vai et al. (1998).

An introduction to mesh generation with EMC2 is also provided. For more details you must refer to the EMC2 documentation.

This is a research code, constantly under development and provided "as is", and therefore it should not be considered by the user as a 100 % bug-free software package. We welcome comments, suggestions, feature requests, module contributions and bug reports.

<sup>&</sup>lt;sup>1</sup>EMC2 can be downloaded from http://www-rocq.inria.fr/gamma/cdrom/www/emc2/eng.htm

#### 1.2 History and credits

The main part of the elastic-isotropic solver was written in the mid 90's by Dimitri Komatitsch while he was preparing his Ph.D. at the *Institut de Physique du Globe de Paris*, under the advise of Prof. Jean-Pierre Vilotte. The elastic-anisotropic solver and several significant improvements to the isotropic code were added by D. Komatitsch later as part of a research contract with DIA Consultants. Further functionalities were added by myself, Jean-Paul Ampuero, while preparing my Ph.D. at IPGP, also under the advise of Prof. Jean-Pierre Vilotte. Most of these additional features were motivated by an ECOS-NORD/FONACYT research project for the study of the seismic response of the valley of Caracas, Venezuela. That became the version 1.0 of the SEM2DPACK, released in April 2002.

For the current version, 2.x, the code was almost completely rewritten in a more objectoriented style in preparation to the implementation of higher level functionalities, such as multigrid, subcycling, adaptivity and multiscale coupling. While the extensive use of objectoriented features of FORTRAN 90 can degrade performance this is not critical in 2D simulation, the emphasis has been rather in facilitating code reuse and expansion.

A simultaneous development for the simulation of earthquake dynamics was undertaken and is the main new feature of the current version. Spontaneous rupture along multiple non-planar faults can be currently modelled. Although there is no intrinsic limitation on applying different friction laws, as of Version 2.2 only linear slip weakening friction is implemented. Dynamic source simulations using methods that discretize the bulk, such as finite difference, finite element and spectral element methods, are more prone to high frequency numerical noise than boundary element methods (e.g. when the size of the process zone is not well resolved). Methods to control this problem were presented in the author's Ph.D. dissertation (Ampuero, 2002)<sup>2</sup> and in Gaetano Festa's Ph.D. dissertation<sup>3</sup>, and will be implemented in a forthcoming version of SEM2DPACK.

SEM2DPACK has been used in the following work:

- Madariaga et al. (2006): dynamic rupture and seismic wave radiation on faults with geometrical complexities (kinks)
- Haney et al. (2007): fault reflections from fluid-infiltrated faults
- De la Puente et al. (2007): as benchmark method for anisotropic wave propagation
- Kaneko et al. (2008): dynamic earthquake rupture with rate-and-state friction

#### 1.3 Installation

- Uncompress and expand the SEM2DPACK package: tar xvfz sem2dpack.tgz
- Go to the source directory: cd SEM2DPACK/SRC

<sup>&</sup>lt;sup>2</sup>Available in French at http://www.sg.geophys.ethz.ch/geodynamics/ampuero/phd.html

http://people.na.infn.it/~festa/

- Edit the Makefile according to your FORTRAN 95 compiler, following the instructions therein.
- Modify the optimization parameters declared and described in SRC/constant.f90.
- Compile: make
- Move to the SEM2DPACK/POST directory, edit the Makefile and compile.

On normal termination you should end up with a set of executable files, among which sem2dsolve, in /home/yourhome/bin/. I have been developping the code with the Lahey/Fujitsu 1f95 compiler and, more recently, with the Intel compiler for Linux <sup>4</sup>. Other compilers are not being tested on a regular basis, so please report any related problems.

#### 1.4 Help requests, feature requests and bug reports

Since November 2006 (version 2.2.5) current and old versions of SEM2DPACK are hosted by SourceForge at http://sourceforge.net/projects/sem2d/. To take advantage of the convenient features offered by this host you must create a SourceForge.net account at http://sourceforge.net/account/newuser\_emailverify.php.

The code repository is at http://sourceforge.net/project/showfiles.php?group\_id=182742. To receive notification emails about new releases of SEM2DPACK sign up for the "Package Monitor" at http://sourceforge.net/project/filemodule\_monitor.php?filemodule\_id=212397.

A "tracking system" is available at http://sourceforge.net/tracker/?group\_id=182742, with three separate lists. Requests for implementation of new features must be submitted to the "Feature Requests" tracker. Questions related to the usage of SEM2DPACK must be submitted to the "Support Requests" tracker. Bug reports must be submitted to the "Bugs" tracker. The three tracker lists are browsable and searchable. To browse the complete list of a tracker set "Status" to "Any". Before submitting an issue make sure you are running the most recent version of SEM2DPACK, that you understand the changes listed in SEM2DPACK's ChangeLog file and that your problem has not been treated in previous submissions. When relevant, a new submission must include the input files needed to reproduce your problem (Par.inp, \*.ftq, etc). You will receive email notifications of any update of your submitted item, until it is closed. If the item is declared "Pending" you are expected to reply to the last message of the developer within two weeks, otherwise the item will be closed. For more instructions see http://sourceforge.net/support/getsupport.php?group\_id=182742.

Contributions to SEM2DPACK by experienced programmers are always welcome and encouraged. A "Developers Forum" is available at http://sourceforge.net/forum/forum.php? forum\_id=635737, where the implementation of new features can be discussed. Although the code is stable for my research purposes, there is still a number of missing features. Their

 $<sup>^4</sup>$ This code works properly with the Intel compiler starting with version 8.0.046-pe047.1, so make sure you have a recent version of ifort!

1.5 License 7

implementation could make SEM2DPACK interesting for a broader audience in mechanical engineering, geotechnical engineering, applied geophysics and beyond. The ToDo file included with SEM2DPACK contains a list of missing features that range from basic functionalities to complex code re-engineering. Chapter 4 gives some guidelines for programmers.

#### 1.5 License

This software is freely available for academic research purposes. If you use this software in writing scientific papers include proper attributions to its author, Jean-Paul Ampuero.

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## Chapter 2

## The solver SEM2D

#### 2.1 About the method

Based on a mesh of quadrangular spectral elements and a set of material properties, sources and receivers SEM2D solves the elastic wave equation applying a Spectral Element Method (SEM) in space and a second-order explicit Newmark scheme in time. The SEM, introduced by Patera (1984) in Computational Fluid Dynamics, can be seen as a domain decomposition version of Pseudospectral Methods or as a high order version of the Finite Element Method. It inherits from its parent methods the accuracy (spectral convergence) and the geometrical flexibility and natural implementation of mixed boundary conditions, respectively.

Introductory texts to the SEM can be found at www.math.lsa.umich.edu/~karni/m501/boyd.pdf (chapter draft, by J.P. Boyd), at www.mate.tue.nl/people/vosse/docs/vosse96b.pdf (a tutorial exposition of the SEM and its connection to other methods, by F.N. van de Vosse and P.D. Minev) and at www.siam.org/siamnews/01-04/spectral.pdf (a perspective paper). Details about the elastodynamic algorithm and study of some of its properties are presented by Komatitsch (1997), Komatitsch and Vilotte (1998), Komatitsch et al. (1999), Komatitsch and Tromp (1999) and Vai et al. (1998).

The implementation of fault dynamics is similar to that in FEM, or the "traction at split nodes" method explained by Andrews (1999). More details can be found in the author's Ph.D. dissertation (Ampuero, 2002)<sup>1</sup> and in Gaetano Festa's Ph.D. dissertation<sup>2</sup>.

More accesible tutorial code, written in Matlab, can be downloaded from the author's website, at www.sg.geophys.ethz.ch/geodynamics/ampuero/SEM\_matlab.tar.gz.

<sup>1</sup>www.sg.geophys.ethz.ch/geodynamics/ampuero/phd.html

<sup>&</sup>lt;sup>2</sup>people.na.infn.it/~festa/

#### 2.2 What SEM2D is and what it is not

SEM2D is an explicit spectral element solver for the 2D elastic wave equation. It is written in FORTRAN 90, with some (useful but not essential) FORTRAN 95 features.

There is no built-in general mesh generator for unstructured grids, only some basic mesh functionalities. If your geological model is complicated you need to generate a mesh with some external tool. An example using EMC2 is described in a later chapter.

There is currently a limited number of post-processing and graphic tools included. Most output is in the form of raw binary or ASCII data files and sample scripts are provided for Seismic Unix, Gnuplot and Matlab.

#### 2.3 Format of the input file

The input file must be called Par.inp. Most of the file is made of FORTRAN 90's NAMELIST input blocks. The general syntax of a NAMELIST can be found in any FORTRAN 90 textbook and will not be repeated here. The typical structure of Par.inp is illustrated by two examples in Figure 2.1 and Figure 2.2. The full documentation of the input blocks is presented after these examples. You should get acquainted with the syntax of the input blocks you are most likely to use. The mandatory or more important input blocks are:

- ECHO
- GENERAL
- MESH\_DEF, followed by a MESH\_Method block
- MATERIAL, followed by a MAT\_Material block
- BC\_DEF (one for each boundary condition), followed by a BC\_Kind block
- TIME
- SRC\_DEF, followed by STF\_SourceTimeFunction and SRC\_Mechanism blocks
- REC\_LINE

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```
Par.inp
 Jan 14, 08 19:57
                                                                        Page 1/1
# Parameter file for SEM2DPACK 2.0
#---- Some general parameters -----
&ECHO title = 'Test SH', verbose='1111'
      ItInfo = 1000, ItSnapshots = 100000 /
&GENERAL iexec=1, ngll= 6, fmax=1.25d0 , ndof=1 /
#---- Build the mesh -----
&MESH_DEF method = 'CARTESIAN' /
&MESH_CART xlim=0.d0,30.d0 ,zlim=0.d0,30.d0 , nelem=60,60/
#---- Elastic material parameters ------
&MATERIAL tag=1, isElastic=T /
&MAT_ELASTIC rho=1.d0, cp=1.7321d0, cs=1.d0 /
#---- Boundary conditions -----
&BC_DEF tag = 2 , kind = 'ABSORB' / &BC_ABSORB side = 'R' , stacey=F/
&BC_DEF tag = 3 , kind = 'ABSORB' / &BC_ABSORB side = 'U' , stacey=F/
#---- Time scheme settings ------
&TIME TotalTime=35.d0, courant = 0.3d0 /
#---- Sources ------
&SRC_DEF stf= 'RICKER' ,coord= 0.d0,0.d0 , mechanism= 'FORCE' / &STF_RICKER f0= 0.5d0, onset = 3.d0, ampli = 0.25d0 /
&SRC_FORCE angle = 0d0/
#---- Receivers ------
&REC_LINE number = 7 , field='D', first = 0.d0,0.d0, last = 30d0,0.d0, isamp=1 /
#----- Plots settings -----
&PLOTS postscript=F , bin=F /
Monday January 14, 2008
```

Figure 2.1: Input file Par.inp for an elementary example in EXAMPLES/TestSH/: a boxed region with a structured mesh.

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```
Par.inp
 Jan 14, 08 21:17
                                                                        Page 1/1
#---- Some general parameters -----
&ECHO Title = 'Palos Grandes NS meshed with EMC2'
      Verbose='1111', ItInfo = 1000, ItSnapshots = 1000/ !3500 /
&GENERAL lexec =1 , Ngll = 5 , fmax = 1.5 , ndof=1/
#---- Build the mesh ----
&MESH_DEF Method = 'EMC2' /
&MESH_EMC2 File= 'NS03qb.ftq'
#---- Elastic material parameters ------
&MATERIAL tag=1, isElastic=T /
&MAT_ELASTIC rho=1800.d0, cp=850.d0, cs=450.d0/
&MATERIAL tag=2, isElastic=T /
&MAT_ELASTIC rho=2100.d0, cp=1800.d0, cs=650.d0/
&MATERIAL tag=3, isElastic=T /
&MAT_ELASTIC rho=2400.d0, cp=2300.d0, cs=850.d0/
&MATERIAL tag=4, isElastic=T /
&MAT_ELASTIC rho=2600.d0, cp=3800.d0, cs=2200.d0/
#&MAT_ELASTIC rho=2500.d0, cp=5000.d0, cs=2900.d0/
#---- Boundary conditions -----
&BC_DEF Tag = 2, Kind = 'ABSORB' /
&BC_ABSORB Side='D',Stacey=F /
&BC_DEF Tag = 3, Kind = 'ABSORB' /
&BC_ABSORB Side='L', Stacey=F, let_wave=T /
&BC_DEF Tag = 4, Kind = 'ABSORB' /
&BC_ABSORB Side='R', Stacey=F /
#---- Time scheme settings -----
&TIME TotalTime=25.d0, Courant = 0.55d0 /
&TIME_NEWMARK alpha=1.d0, beta=0.d0, gamma=0.5d0 /
#--- Sources -----
&SRC_DEF stf='RICKER', Mechanism='WAVE' Coord= -1160000.d0,-2000.d0 /
&STF_RICKER f0 = 1.d0 , Onset = 1.5d0 , Ampli = 1.d0 / &SRC_FORCE Angle = 90. /
&SRC_WAVE Angle = 30. , phase='S' /
#---- Receivers ------
# receivers located at the surface by giving a very large vertical position
# locating them at the nearest computational node (AtNode=.true. is the default)
&REC_LINE Number = 31 , First = -1\overline{1}63068.0d0,1.d3, Last = -1159697.36d0,1.d3,
         Isamp=10 /
#----- Plots settings -----
&PLOTS fields='V', components='x' /
&PLOTS_POSTSCRIPT Mesh=T,Vectors=F,Color=T, Interpol = T, DisplayPts=9,
                   ScaleField=0.2d0 /
Monday January 14, 2008
```

Figure 2.2: Input file Par.inp for a more realistic example: a sedimentary basin with an unstructured mesh generated by EMC2. Available in EXAMPLES/UsingEMC2/.

= Self-documentation for the INPUT BLOCKS of the SEM2D code = \_\_\_\_\_ NAME : BC\_ABSORB GROUP : BOUNDARY\_CONDITION PURPOSE: Absorbing boundary SYNTAX : &BC\_ABSORB side, stacey / [char] [none] Which side of the model corresponds to this side υ, boundary: Up, top 'D' Down, bottom L' Left 'R.' Right [log] [F] Apply Stacey absorbing conditions for P-SV. stacey Higher order than Clayton-Engquist (the default). let\_wave [log] [T] Allow incident waves across this boundary NOTE : Only implemented for vertical and horizontal boundaries. NAME: BC\_DIRNEU GROUP : BOUNDARY\_CONDITION PURPOSE: Dirichlet (null displacement) and/or Neumann (null or time-dependent traction) boundary conditions on vertical or horizontal boundaries SYNTAX : &BC\_DIRNEU h, v, hsrc, vsrc / possibly followed by one or two STF\_XXXX blocks [char]['N'] Boundary condition on the horizontal component h [char]['N'] Boundary condition on the vertical component : 'N' : Neumann 'D' : Dirichlet [name]['null'] Name of the source time function for a hsrc time-dependent horizontal traction: 'RICKER', 'TAB', 'USER', etc (see STF\_XXXX input blocks) [name]['null'] Same for the vertical component vsrc NAME : BC\_DEF PURPOSE: Define a boundary condition

\_\_\_\_\_

SYNTAX : &BC\_DEF tag, tags, kind /

followed eventually by &BC\_XXXX blocks

tag [int] [none] A number assigned to the boundary. If you are using SEM2D built-in structured mesher the conventions are:

1 bottom

2 right

3 up

4 left

If you are importing a mesh, you must use the tags assigned to the boundaries during the mesh construction.

tags [int(2)] [none] Two tags are needed for interfaces (split-node) and for periodic boundaries.

kind [char\*6] [none] Type of boundary condition. The following are implemented:

'DIRNEU', 'ABSORB', 'PERIOD', 'LISFLT', 'SWFFLT'

NOTE : you must DEFINE FIRST ALL PERIODIC BOUNDARIES

NOTE : Some of the boundary conditions need additional data. See their

respective input blocks if any.

\_\_\_\_\_

NAME : BC\_LSF

GROUP : BOUNDARY\_CONDITION

PURPOSE: Linear slip fault, a displacement discontinuity interface

where stress and disp.discont. are linearly related

SYNTAX : &BC\_LSF Ktang, Knorm /

Ktang [dble] [Inf] Tangential stiffness
Ctang [dble] [0d0] Tangential compliance
Knorm [dble] [Inf] Normal stiffness
Cnorm [dble] [0d0] Normal compliance

NOTE: for each component you can set K \_or\_ C, but \_not\_both\_

NOTE: if one of the C=OdO or K=Inf (the default) then no displacement discontinuity is allowed for that component (transparent),

if K=0d0 the fault is a free stress boundary for that component In summary the fault can behave as:

- -1 transparent T&N (Tangent and Normal)
- 0 stress free T&N
- linear-slip/free T, transparent N
- transparent T, linear-slip/free N
- 3 linear-slip/free T&N

NAME : BC\_SWFFLT GROUP : BOUNDARY\_CONDITION PURPOSE: Slip weakening friction fault SYNTAX : &BC\_SWFFLT Dc | DcHet, MuS | MuSHet , MuD | MuDHet, Tn | TnHet, Tt | TtHet, Sxx | SxxHet, Sxy | SxyHet, Sxz | SxzHet, Syz | SyzHet, Szz | SzzHet FirstOutput, DtOutput, IxOut / possibly followed by &DIST\_XXX blocks for Dc,MuS,MuD,Tn and/or Tt (the order is important) NOTE: for better results, use dynamic faults with the leapfrog time scheme and with a layer of damping material (Kelvin-Voigt) near the fault. Friction law: Dc [dble] [0.5d0] Critical slip MuS [dble] [0.6d0] Static friction coefficient MuD [dble] [0.5d0] Dynamic friction coefficient Initial stress, can be a superposition of tractions and background stress: Tn [dble] [0d0] Normal traction (positive = tensile) Tt [dble] [0d0] Tangential traction (positive antiplane: y>0) Sxx [dble] [0d0] sigma\_xx Sxy [dble] [0d0] sigma\_xy Sxz [dble] [0d0] sigma\_xz [dble] [0d0] sigma\_yz Syz Szz [dble] [0d0] sigma\_zz NOTE: arguments with the suffix "Het" are used to give non uniform values to friction and initial stress parameters. For instance, DcHet='GAUSSIAN' followed by a DIST\_GAUSSIAN block sets a gaussian distribution of Dc. Several heterogeneous distributions are available, See DIST\_XXX for their syntax. For outputs in FltXX\_sem2d.dat: DtOutput [dble] [0.d0] Time lag between outputs (in seconds) Default resets DtOutput = global timestep FirstOutput [dble] [0.d0] Start output at this time

[int(3)] [(1,huge,1)] First node, last node and stride Default resets Ixout(2) = last point

NOTE: DtOutput is internally adjusted to the nearest multiple of the global timestep

-----

NAME : DIST\_GAUSSIAN
GROUP : DISTRIBUTIONS\_2D

PURPOSE: Bell shaped (Gaussian) 2D distribution

SYNTAX: &DIST\_GAUSSIAN centered\_at, length, offset, ampli /

centered\_at [dble(2)] [none] Coordinates of the center point.
length [dble(2)] [none] Characteristic lengths on each axis.

offset [dble] [none] Background level.

ampli [dble] [none] Amplitude from background.

-----

NAME : DIST\_GRADIENT
GROUP : DISTRIBUTIONS\_2D

PURPOSE: Constant gradient 2D distribution.

SYNTAX: &DIST\_GRADIENT file,valref ,grad,angle/

file [name] [none] Name of the file containing the coordinates

of the points defining the reference line. It is an ASCII file with 2 columns per line:

(1) X position (in m) and (2) Z position (in m)  $\,$ 

valref [dble] [none] Value along the reference line

grad [dble >0] [none] Positive gradient (valref\_units/meter)
angle [dble] [none] Angle (degrees) between the vertical down
and the grad+ direction. Anticlockwise convention (grad+
points down if 0, right if 90)

NOTE: Be sure that your angle and ref-line are compatible. The code will abort if the ref-line is too short: some points of the domain cannot be projected to ref-line in the angle direction.

NAME : DIST\_HETE1

GROUP : DISTRIBUTIONS\_2D

PURPOSE: Linear interpolation of values from a regular 2D grid.

SYNTAX : &DIST\_HETE1 file, col /

file [name] [none] Name of the file containing the definition

of the regular grid and values at grid points.

The format of this ASCII file is:

Line 1: ncol nx nz x0 z0 dx dz

ncol = [int] number of data columns

nx,nz = [2\*int] number of nodes along x and z

```
x0,z0 = [2*dble] bottom-left corner
                           dx,dz = [2*dble] spacing along x and z
                         Line 2 to nx*nz+1 : [ncol*dble] values at grid points
                           listed from left to right (x0 to x0+nx*dx),
                           then from bottom to top (z0 to z0+nz*dx)
 col
                  [int] [1] Column of the file to be read
NOTE
       : The same file can contain values for (ncol) different properties,
         (e.g. rho, vp, vs) but each DIST_HETE1 block will read only one.
NOTE
       : Even if the original model domain has an irregular shape,
         the regular grid where input values are defined must be rectangular
         and large enough to contain the whole model domain.
         The regular grid possibly contains buffer areas with dummy values.
         These dummy values should be assigned carefully (not random nor zero)
         because SEM2D might use them during nearest-neighbor interpolation.
NAME
       : DIST_LINEAR
GROUP : DISTRIBUTIONS_1D
PURPOSE: Piecewise linear 1D distribution along X.
SYNTAX : &DIST_LINEAR file, length /
 file
          [name] [none] Name of the ASCII file containing
              the data to be interpolated, two columns per line:
              (1) X position, sorted in increasing order, and
              (2) data value at X
 length
          [dble] [0]
                        Smoothing length for sliding average window
                            No smoothing if length=0
       : DIST_ORDERO
NAME
GROUP : DISTRIBUTIONS_2D
PURPOSE: Blockwise constant 2D distribution.
SYNTAX : &DIST_ORDERO xn, zn /
         x(1) ... x(xn-1)
         z(1) \ldots z(zn-1)
         v(1,1) \dots v(xn,1)
           v(1,zn) \dots v(xn,zn)
          [int] [none] Number of zones along X
 zn
          [int] [none] Number of zones along Z
          [dble(xn-1)] [none] Boundaries of X-zones: first zone X < x(1),
 X
               second zone x(1) < X < x(2), \ldots, last zone x(xn-1) < X
```

```
[dble(zn-1)] [none] Boundaries of Z-zones
 z
          [dble(xn,zn)] [none] Values inside each zone
NAME
       : DIST_PWCONR
GROUP : DISTRIBUTIONS_2D
PURPOSE: Piecewise constant radial (2D) distribution.
SYNTAX : &DIST_PWCONR num, ref /
            r(1) ... r(num-1)
         v(1) \ v(2) \dots v(num-1) \ v(num)
 num
          [int] [none] Number of radial zones (including outermost)
          [dble(2)] [(0d0,0d0)] Reference point: center of radial zones
 ref
          [dble(num-1)] [none] External radius of zones:
 r
               first zone R < r(1), second r(1) = < R < r(2), ...
               last r(num-1) = < R
          [dble(num)] [none] Values inside each zone
NAME
       : DIST_SPLINE
GROUP : DISTRIBUTIONS_1D
PURPOSE: Spline interpolated 1D distribution along X.
SYNTAX : &DIST_SPLINE file /
 file
          [name] [none] Name of the ASCII file containing
              the data to be interpolated, two columns per line:
              (1) X position, sorted in increasing order, and
              (2) data value at X
       : ECHO
NAME
PURPOSE: Parameters controlling runtime output
SYNTAX : &ECHO Verbose, ItInfo, ItSnapshots, ItSnapshot1 /
 Title
                  [word] [none] Title of the simulation
                  [char(4)] ['1101'] Verbose flags for input, initialization,
 Verbose
                       check and solver phases. Example: '0001' is verbose only
                       during solver.
 ItInfo
                  [int] [100] Frequency (in number of timesteps) at which
                       solver echoes some basic information.
                  [int] [100] Frequency (in number of timesteps) at which
 ItSnapshots
                       snapshots are dumped (usually PostScript)
                              Time step at which first snapshot is dumped
 ItSnaphot1
                  [int] [0]
```

\_\_\_\_\_\_

NAME : GENERAL

PURPOSE: General parameters

SYNTAX : &GENERAL iexec,ngll,fmax /

iexec [int] [0] Run level:

0 = just check

1 = solve

ngll [int] [9] Number of GLL nodes per edge on each spectral element

(polynomial order +1). Usually 5 to 9.

fmax [dble] [0.d0] Maximum frequency to be well resolved. Mandatory.

This is a target frequency, the code will check if it is compatible with the mesh and eventually issue a warning. To improve the resolution for a given fmax you must increase ngll (but you will have to use shorter timesteps) or refine/redesign the mesh.

ndof [int] [2] Number of degrees of freedom per node

1 = SH waves, anti-plane
2 = P-SV waves, in-plane

\_\_\_\_\_\_

NAME : MAT\_DAMAGE GROUP : MATERIALS

PURPOSE: Set material properties for the damage rheology of

Lyakhovsky, Ben-Zion and Agnon (J. Geophys. Res. 1997)

and Hamiel et al (Geophys. J. Int. 2004)

SYNTAX : &MAT\_DAMAGE cp,cs,rho,phi,alpha,Cd,beta,R,e0,ep /

cp [dble][0d0] P wave velocity cs [dble][0d0] S wave velocity

rho [dble][0d0] density

phi [dble][0d0] internal friction angle

alpha [dble][0d0] initial value of damage variable Cd [dble][0d0] damage evolution coefficient beta [dble][0d0] damage evolution exponent

R [dble][0d0] damage-related plasticity coefficient

e0 [dble(4)][0d0] initial total strain (11, 22, 33 and 12) ep [dble(4)][0d0] initial plastic strain (11, 22, 33 and 12)

\_\_\_\_\_

NAME : MAT\_ELASTIC GROUP : MATERIALS

PURPOSE: Set material properties for a linear elastic medium SYNTAX: &MAT\_ELASTIC rho|rhoH, cp|cpH, cs|csH / if isotropic

```
possibly followed by DIST_XXXX blocks, in the order: rho,cp,cs
         or &MAT_ELASTIC rho, c11,c13,c33,c44 / if anisotropic
          [dble] [0d0] P wave velocity
 ср
          [dble] [0d0] S wave velocity
 cs
 rho
          [dble][0d0] density
                  [name][''] name of non uniform distribution in the
 cpH,csH,rhoH
                       DISTRIBUTIONS_2D group, to set non uniform values
 c11,c13,c33,c44 [dble][0d0] anisotropic elastic moduli
NAME
       : MATERIAL
PURPOSE: Define the material type of a tagged domain
SYNTAX : &MATERIAL tag, isElastic, isKelvinVoigt, isDamage /
         Followed by MAT_XXXX input locks
          [int] [none] Number identifying a mesh domain
 tag
 isElastic
                  [log] [F] Elastic material (see MAT_ELAST)
                  [log] [F] Kelvin-Voigt material (see MAT_KV)
 isKelvinVoigt
 isDamage [log] [F] Damage material (see MAT_DMG)
NOTE
       : Multiple material type can be assigned to a domain.
         The MAT_XXXX blocks must then be given in a specific order.
         The following multiple combinations are allowed:
          . elastic then Kelvin-Voigt
NAME
       : MAT_KV
GROUP : MATERIALS
PURPOSE: Set material properties for Kelvin-Voigt viscosity
         Adds a damping term C*v = K*eta*v
         where eta is a viscous time
SYNTAX : &MAT_KV eta|etaH, ETAxDT /
  possibly followed by a DIST_XXX input block.
 eta [dble][0d0] Viscosity coefficient
 etaH [char*][] If eta is distributed non uniformly
 give here the name of the distribution (see DIST_XXX)
 ETAxDT [log][T] If eta is given in units of dt (timestep)
NOTE: useful as artificial damping layer in fault zones to control
      high frequency noise. Set eta=0.1*dt and a thickness of 4-5 GLL nodes.
```

NAME : MESH\_CART GROUP : MESH\_DEF

PURPOSE: Rectangular box with structured mesh.

SYNTAX : &MESH\_CART xlim,zlim,nelem /

xlim [dble(2)] [none] X limits of the box (min and max)
zlim [dble(2)] [none] Z limits of the box (min and max)

nelem [int(2)] [none] Number of elements along each direction FaultX [log] [F] Cut the box in the middle by a horizontal fault If enabled, nelem(2) must be even

NOTE: the following tags are automatically assigned to the boundaries:

- 1 Bottom
- 2 Right
- 3 Top
- 4 Left
- Fault, bottom sideFault, top side

NAME : MESH\_CART\_DOMAIN

PURPOSE: Define a subdomain within a structured meshed box.

SYNTAX : &MESH\_CART\_DOMAIN tag,ex,ez /

tag [int] [none] Tag number assigned to this domain.

ex [int(2)] [none] First and last element along the X direction. ez [int(2)] [none] First and last element along the Z direction.

NOTE : If you ignore this input block a single domain (tag=1) will span

the whole box

\_\_\_\_\_\_

NAME : MESH\_EMC2 GROUP : MESH\_DEF

PURPOSE: Imports a mesh from INRIA's EMC2 mesh generator in FTQ format

SYNTAX : &MESH\_EMC2 file /

file [name] [none] Name of the FTQ file, including suffix

\_\_\_\_\_\_

NAME : MESH\_DEF

PURPOSE: Selects a method to import/generate a mesh.

SYNTAX : &MESH\_DEF method /

method [name] [none] 'CARTESIAN', 'LAYERED' or 'EMC2'

The &MESH\_DEF input block must be followed by a 
&MESH\_method input block

NAME : MESH\_LAYERED [mesh]

PURPOSE: Structured mesh for layered medium

with surface and interface topography.

SYNTAX : &MESH\_LAYERED xlim,zmin,nx,file,nlayer /

xlim [dble(2)] [none] X limits of the box (min and max)

zmin [dble] [none] bottom Z limit of the box

nx [int] [none] Number of elements along X direction

file [string] [''] Only for flat layers,

name of ASCII file containing layer parameters, one line per layer, listed from top to bottom,

- 3 columns per line:
- (1) vertical position of top boundary,
- (2) number of elements along Z direction
- (3) material tag

nlayer [int] [none] Number of layers

If a file name is not given the layer parameters must be given immediately after the &MESH\_LAYERED block by nlayer &MESH\_LAYER input blocks, one for each layer, listed from top to bottom.

NOTE: the following tags are automatically assigned to the boundaries:

- 1 Bottom
- 2 Right
- 3 Top
- 4 Left
- 5 Fault, bottom side
- 6 Fault, top side

\_\_\_\_\_

NAME : MESH\_LAYER GROUP : MESH\_DEF

PURPOSE: Define mesh parameters for one layer SYNTAX : &MESH\_LAYER nz, ztop, ztopH, tag /

nz [int] [none] Number of elements in layer along Z direction

ztop [dble] [none] Only for layers with flat top surface:

vertical position of top boundary

ztopH [string] ['none'] Only for layers with irregular top boundary:

name of distribution, 'LINEAR', 'SPLINE' or any other

```
1D distribution available through a DIST_XXXX block.
               If ztopH is set, the MESH_LAYER block must be
               followed by the appropriate DIST_XXXX block.
 tag
          [int] [none] Material tag
                If not given, a tag is automatically assigned to the layer,
                sequentially numbered from top to bottom (top layer tag =1)
NAME
       : PLOTS
PURPOSE: Selects a format to export snapshots
SYNTAX: &PLOTS fields, components, bin, visual3, avs, postscript, gmt /
 fields
          [char*] ['V'] fields to export in snapshots
                (begining of output file names given in parenthesis)
                'D'
                        displacements (dx,dy,dz,da)
                , γ,
                        velocity (vx,vy,vz,va)
                ,Α,
                        acceleration (ax,ay,az,aa)
                'E'
                        strain (e11,e22,e12,e23,e13)
                s,
                        stress (s11,s22,s12,s33,e13,e23)
 components [char*] ['ya'] components for PostScript outputs
                      'x','y','z' and/or 'a' (amplitude)
                      (in SH only 'y' is considered)
 postscript [log] [T] PostScript
          [log] [F] output triangulation file grid_sem2d.gmt
 gmt
                to be used in "pscontour -T" of the General Mapping Tool (GMT)
 avs
          [log] [F] AVS
          [log] [F] Visual3
 visual3
 bin
          [log] [T] binary
NOTE
       : If you choose PostScript you may need also a $POSTSCRIPT input block.
         Other formats apply only to 'DVA' fields, 'ES' are exported as binary.
NAME
       : PLOTS_POSTCRIPT
GROUP : PLOTS
PURPOSE: Preferences for PostScript snapshots
SYNTAX: &PLOTS_POSTSCRIPT vectors, mesh, background, color,
              isubsamp, boundaries, symbols, numbers, legend,
              ScaleField, Interpol, DisplayPts /
 vectors
                  [log] [F] Plots a vectorial field with arrows
 mesh
                  [log] [F] Plots the mesh on background
 background
                  [char] [''] Filled background, only for vector plots:
                                       none
                                  'P' P-velocity model
```

'S' S-velocity model γТγ domains [int] [3] Subsampling of the GLL nodes for the isubsamp output of velocity model. The default samples every 3 GLL points. boundaries [log] [T] Colors every tagged boundary symbols [log] [T] Plots symbols for sources and receivers numbers [log] [F] Plots the element numbers [log] [T] Writes legends legend color [log] [T] Color output ScaleField [dble] [0d0] Fixed amplitude scale (saturation), convenient for comparing snapshots and making movies. The default scales each snapshot by its maximum amplitude Interpol [log] [T] Interpolate field on a regular subgrid inside each element DisplayPts [log] [3] Size of interpolation subgrid inside each element is DisplayPts\*DisplayPts. The default plots at vertices, mid-edges and element center. NAME : REC\_LINE PURPOSE: Defines a line of receivers SYNTAX : &REC\_LINE number, isamp, field, first, last, file, AtNode, irepr / number [int] [0] Number of stations in the line isamp [int] [1] Sampling stride (in number of timesteps). Note that for stability reasons the timestep can be very small. field [char] ['V'] The field in the seismogram: 'D' displacement , V , velocity , Δ, acceleration first [dble(2)] Receivers can be located along a line, this is the position (x,z) of the first receiver [dble(2)] Position (x,z) of the last receiver, last other receivers will be located with regular spacing between First and Last. file [name] ['none'] Station positions can instead be read from an ASCII file, with 2 columns per line: (1) X position (in m) and (2) Z position (in m) AtNode [log] [T] Relocate the stations at the nearest GLL node irepr [char] ['D'] Abscissa for the seismic multitrace plot:

'X' Horizontal position

'D' Distance to the first station

'Z' Depth

NOTE : to locate receivers at the free surface set their vertical position

above the free surface and AtNode=T

-----

NAME : SRC\_FORCE

GROUP : SOURCE MECHANISM
PURPOSE: Point force source
SYNTAX : &SRC\_FORCE angle /

angle [dble] [0d0] For P-SV, the angle of the applied force,

in degrees, counterclockwise from Z-UP, e.g.:

(90 points left, 180 points down)

For SH, angle is ignored.

\_\_\_\_\_

NAME : SRC\_DEF

PURPOSE: Define the sources.

SYNTAX : &SRC\_DEF stf, mechanism, coord, file /

followed by one SOURCE MECHANISM block (SRC\_XXXX) and one SOURCE TIME FUNCTION block (STF\_XXXX)

stf [name] [none] Name of the source time function:

'RICKER', 'TAB', 'HARMONIC' or 'USER'

mechanism [name] [none] Name of the source mechanism:

'FORCE', 'EXPLOSION', 'DOUBLE\_COUPLE', 'MOMENT' or 'WAVE'

coord [dble] [huge] Location of the source (m).

file [string] ['none'] Station coordinates and delay times can

be read from an ASCII file, with 3 columns per line:

- (1) X position (in m),
- (2) Z position (in m) and
- (3) time delay (in seconds)

-----

NAME : SRC\_DOUBLE\_COUPLE GROUP : SOURCE MECHANISM

PURPOSE: Define a double-couple source
SYNTAX : &SRC\_DOUBLE\_COUPLE dip /

dip [dble] [90] Dip angle, in degrees, clockwise

from the positive X direction

NOTE : Sign convention: if the source amplitude is positive the right block

moves up (positive Z direction) in PSV and forward (positive Y

direction) in SH.

\_\_\_\_\_\_

NAME : SRC\_MOMENT GROUP : SOURCE

PURPOSE: Define a moment tensor source

SYNTAX : &SRC\_MOMENT Mxx, Mxz, Mzx, Mzz, Myx, Myz /

Mxx,Mxz,Mzx,Mzz [dble] [0] Tensor components for PSV Myx,Myz [dble] [0] Tensor components for SH

-----

NAME : SRC\_WAVE

GROUP : SOURCE MECHANISM

PURPOSE: Incident plane wave through the absorbing boundaries

SYNTAX : &SRC\_WAVE angle, phase /

angle [dble] [0d0] Incidence angle in degrees within [-180,180] counterclockwise from the positive Z (up) direction

to the wave vector direction:

Exs: incidence from below if angle in ]-90,90[ normal incidence from below if angle=0

from bottom right if angle=+45
from bottom left if angle=-45

phase [char] ['S'] 'S' or 'P' (only needed in PSV, ignored in SH)

NOTE : Incident waves enter through the absorbing boundaries.

An incident wave is applied on every absorbing boundary unless "let\_wave = F" in the respective BC\_ABSO block.

Incident waves are not implemented for "Stacey" absorbing boundaries.

\_\_\_\_\_\_

NAME : STF\_HARMONIC

GROUP : SOURCE TIME FUNCTIONS

PURPOSE: Harmonic source time function f(t) = ampli\*sin(2\*pi\*t\*f0)

SYNTAX : &STF\_HARMONIC ampli, f0 /

ampli [dble] [0d0] Amplitude f0 [dble] [0d0] Frequency

-----

NAME : STF\_RICKER

GROUP : SOURCE TIME FUNCTIONS

PURPOSE: The Ricker wavelet is the second derivative of a gaussian.

SYNTAX : &STF\_RICKER ampli, f0, onset / [real] [1.] Signed amplitude of the central peak ampli f0 [real >0] [0] Fundamental frequency (Hz). distribution: it has a peak at f0 and an exponential decay at high frequency. The cut-off high frequency is usually taken as  $fmax = 2.5 \times f0$ . [real >1/f0] [0] Delay time (secs) with respect to the peak value. onset NOTE : The spectrum has a peak at f0 and decays exponentially at high frequencies. Beyond 2.5\*f0 there is little energy, this is a recommended value for fmax. NOTE : onset>1/f0 is needed to avoid a strong jump at t=0, which can cause numerical oscillations. Ignore if using incident waves. : STF\_TAB NAMEGROUP : SOURCE TIME FUNCTIONS PURPOSE: Source time function spline-interpolated from values in a file SYNTAX : &STF\_TAB file / [string] ['stf.tab'] ASCII file containing the source time function, file two columns per line: (1) time (2) value NOTE : time can be irregularly sampled NOTE : assumes value=0 before min(time) and after max(time) NAME : STF\_USER GROUP : SOURCE TIME FUNCTIONS PURPOSE: A template for user-supplied source time function. File stf\_user.f90 must be modified by the user to fit special needs. SYNTAX: &STF\_USER ampli, onset, par1, par2, ipar1, ipar2 / ampli [dble] [1.] Amplitude onset [dble] [0] Delay time (secs) [dble] [0] Example parameter par1 [dble] [0] Example parameter par1 par1 [int] [0] Example parameter par1 [int] [0] Example parameter

-----

NAME : TIME

PURPOSE: Defines time integration scheme

SYNTAX: &TIME kind, NbSteps, Dt, Courant, TotalTime /

kind [char\*10] ['leapfrog'] Type of scheme:

'newmark' Newmark-alpha
'leapfrog' Central difference
'symp\_PV' Position Verlet

'symp\_PFR' Position Forest-Ruth (4th order)

'symp\_PEFRL' Extended PFR (4th order)

NbSteps [int] [none] Number of timesteps to be performed

Dt [dble] [none] Amplitude of the timestep

Courant [dble] [0.5d0] Courant stability number: the maximum ratio

Dt\*wave\_velocity/dx where dx is the inter-GLL node distance
Tipically <= 0.5

TotalTime[int] [none] Total duration (in seconds) of simulation

NOTE : Not all combinations of parameters need to be set at once.

You can set the total duration (secs) or the number of steps.

You can set the timestep or the Courant number (or use default).

NOTE : The leap-frog scheme is equivalent to the Newmark scheme with alpha=1, beta=0, gamma=1/2. However it is faster and requires less memory. Dynamic faults require this scheme.

NAME : TIME\_NEWMARK

PURPOSE: Parameters of the explicit Newmark or HHT-alpha time scheme

SYNTAX : &TIME\_NEWMARK alpha|gamma, beta|rho /

beta [dble] [0.5d0] The algorithm is fully explicit if beta=0 otherwise it is a single-predictor-corrector scheme

gamma [dble] [1.d0]

alpha [dble] [0.5d0] parameter in the Hilber-Hughes-Taylor method

Actually, here alpha = 1 + their original definition of alpha

rho [dble] [1.d0] high frequencies are damped by a factor>=rho.

The default is non-dissipative. Dissipation is limited however to rho>=0.5. For max dissipation you should work close to the stability limit (Courant around 0.56 for rho=0.5).

NOTE: For second order schemes only two parameters need to be set: (alpha OR gamma) AND (beta OR rho)

NOTE: Dissipative schemes (0.5<=rho<1) are slightly more unstable,

i.e. they require slightly smaller Courant number (0.56 for rho=0.5, compared to 0.6 for rho=1)

#### 2.4 Verifying the settings and running a simulation

Once the code has been successfully compiled, the simulation can be started by typing sem2dsolve from your working directory, which contains the file Par.inp. The computations can be run in background and the screen output saved in a file (e.g. info) by typing sem2dpack > info &.

A typical screen output of SEM2D, corresponding to the first example, is shown on the following pages. The parameters of the simulation and some verification information are reported there in a self-explanatory form. You are advised to do a first run with <code>iexec=0</code> in the <code>GENERAL</code> input block and check all these informations prior to the real simulation. You should always verify the following:

• Stability: the CFL stability number should be smaller than  $0.55 \sim 0.60$  for second order time schemes. This number is defined at each computational node as

$$CFL = c_P \Delta t / \Delta x$$

where  $\Delta t$  is the timestep,  $c_P$  the P-wave velocity and  $\Delta x$  the local grid spacing. Note that  $\Delta x$  is usually much smaller than the element size h ( $\approx \text{Ngll}^2$  times smaller) because SEM internally subdivides each element onto a non-regular grid of Ngll×Ngll nodes clustered near the element edges (Gauss-Lobatto-Legendre nodes). If the computation is unstable, the maximum displacement, printed every ItInfo time steps, increases exponentially with time. Stability can be controlled by decreasing Dt or Courant in Par.inp.

• Resolution: the number of nodes per shortest wavelength  $\lambda_{min}$  should be larger than  $4.5 \sim 5$ . The minimum wavelength is defined as

$$\lambda_{min} = \min(c_S)/f_{max}$$

where  $c_S$  is the S-wave velocity and  $f_{max}$  the highest frequency you would like to resolve, e.g. the maximum frequency at which the source spectrum has significant power (for a Ricker wavelet  $f_{max} = 2.5 \times f_0$ ). For an element of size h and polynomial order p = Ngll - 1, the number of nodes per wavelength G is

$$G = \frac{p \lambda_{min}}{h}$$
.

Typical symptoms of poor resolution are ringing and dispersion of the higher frequencies. However, in heterogeneous media these spurious effects might be hard to distinguish from a physically complex wavefield, so mesh resolution must be checked beforehand. If resolution is too low the mesh might be refined by increasing Ngll in Par.inp (p-refinement) or by generating a denser mesh (h-refinement). If you were using EMC2 as a mesh generator, the script PRE/href.csh can be useful for h-refinement.

• Cost: the total CPU time an memory required for the simulation are as much as you can afford. Estimates of total CPU time are printed at the end of check mode. Details about memory usage can be found in MemoryInfo\_sem2d.txt.

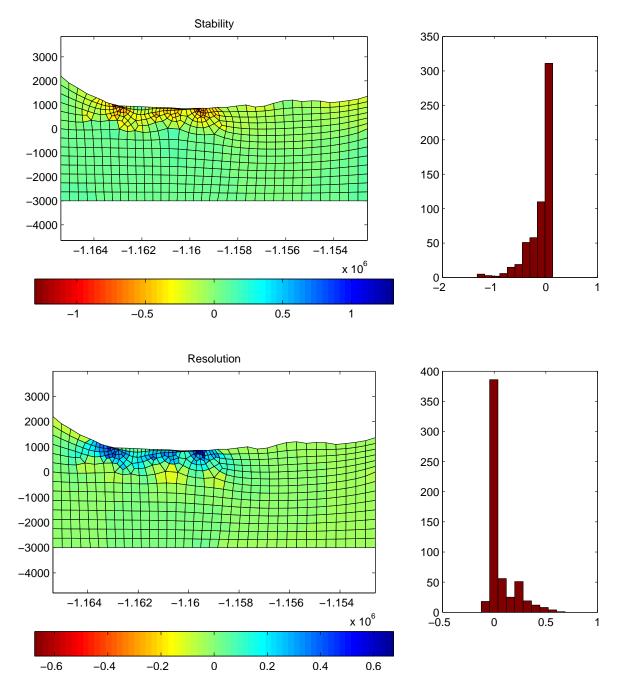


Figure 2.3: Checking the quality of a mesh with PRE/ViewMeshQuality.m for the example in EXAMPLES/UsingEMC2/. The balance of the stability and resolution properties of the mesh can be analyzed: logarithmic stability index (top) and logarithmic resolution index (bottom). Histograms of these indices (in number of elements) are shown on the right.

The quality of the mesh can be inspected with the Matlab script PRE/ViewMeshQuality.m which produces plots like in Figure 2.3. The proper balance of the mesh with respect to the following two criteria can be analyzed:

- Stability criterion, related to the largest stable timestep. On each element we define a stability index as the logarithm of  $\min(\Delta x/c_P)$  normalized by its median value over the whole mesh. Red elements (small stability index) are relatively unstable and require small timesteps  $\Delta t$ . Because  $\Delta t$  is constant over the whole mesh and the computational cost is inversely proportional to  $\Delta t$  these red elements penalize the computational efficiency. The mesh should be redesigned to increase their size, as much as possible, while keeping them small enough to resolve the shortest wavelength (see next).
- Resolution criterion, related to the number of nodes per shortest wavelength. On each element we define a resolution index as the logarithm of  $\min(c_S/h)$  normalized by its median value over the whole mesh. Red elements (small resolution index) have relatively poor resolution, in their vicinity the maximum frequency resolvable by the mesh is limited. The mesh should be redesigned to decrease their size, as much as possible. Conversely, elements with very high resolution index (blue) are smaller than required and might increase the computational cost.

To minimize the CPU and memory cost of a simulation an ideal mesh design should minimize the spread of the two indices above, by aiming at a ratio of element size to wave velocity, h/c, as uniform as possible across the whole mesh. However, in some cases a poorly balanced mesh is inevitable: in the example of Figure 2.3 the worst elements are near the edges of the sedimentary basin, at a sharp velocity contrast. Small element sizes on the rock side are inherited from the sediment mesh.<sup>3</sup>

Similar information is plotted by gv Stability\_sem2d.ps and gv Resolution\_sem2d.ps. The indices in these files are however not logarithmic and are not normalized by the median.

<sup>&</sup>lt;sup>3</sup>In future releases of SEM2DPACK this penalty on computational efficiency will be reduced by non-conformal meshing with mortar elements, by timestep subcycling or by implicit/explicit timestep partitioning.

Printed by Jean Paul Ampuero

Number of material sets . . . . . . . . = 1

	Printed by C	Jean Paul Ampuerd
Jun 01, 07 1:06	info	Page 2/4
Material number Type P-wave velocity S-wave velocity Mass density Poisson's ratio First Lame parameter Lambda Second Lame parameter Mu Bulk modulus K. Young's modulus E.	(mode) = ISOTR (cp) = 1.732E+00 (cs) = 1.000E+00 .(denst) = 1.000E+00 .(poiss) = 250.02IE-03 .(alam) = 1.000E+00	
Boundary Condition	s ==	
Boundary tag Boundary condition Type of absorbing boundary Periodicity	(tag) = 2 (kind) = ABSORB .(stacey) = Clayton-Engquis (periodic) = F	t
Boundary tag	(tag) = 3 (kind) = ABSORB .(stacey) = Clayton-Engquis (periodic) = F	t
Source Functions		
X-position (meters)	= Ricker = 500.000E-03 = 3.000E+00 = 250.000E-03 = Collocated Force	
Receivers		
Number of receivers	ording (isamp) = 1 (field) = D	
Snapshot Outputs		
Save results in PS file or not Save results in AVS file or not Save results in Visual3 file or Save results in binary file or Selected fields: Displacement Velocity		
Selected components for PostScr: X	F	

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Jun 01, 07 1:06		info		Page 3/4	
	**************************************	******** nase *			
	********	*****			
Saving node	FEM mesh [OF coordinates in file nt connectivity in f	MeshNodesCoor			
Spectral	elements	grid ======			
	L points [OK of GLL points		01		
	nt/node table in bir es coordinates		ol_sem2d.dat .	[OK]	
	rid coordinates (coordinates (c				
Material	propertie	S ==			
Defining ela	input velocity mode sticity work arrays del [OK]				
Mesh pro	perties ======				
Max mesh size Min mesh size	Checking mesh [OK] Max mesh size = 142.616E-03 Min mesh size = 58.736E-03 Ratio max/min = 2.428E+00				
RESOLUTION: n	RESOLUTION: nodes per min wavelength = 8.000E+00				
	ipt Resolution_sem2d ipt Stability_sem2d				
Time sol					
Time step (secs) = 17.621E-03 Number of time steps = 1987 Total duration (secs) = 35.013E+00 Courant number = 300.000E-03					
STABILITY: CFL number = 300.000E-03 Initializing kinematic fields [OK] Max displ = 0.000E+00 Max veloc = 0.000E+00 Building the mass matrix [OK] Defining boundary conditions [OK] Initializing receivers					
Receiver					
Receivers have been relocated to the nearest GLL node					
Receiver x-requ	ested z-requested	x-obtained	z-obtained	distance	
	0E+00 0.000E+00		0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00	

6 25.0002+00 0.000E+00 25.000E+00 0.000E+00 0.000E+00 0.000E+00 7 30.000E+00 0.000E+00 30.000E+00 0.000E+00 0.000E+0	Jun 01, 07 1:06		info		Page 4/4
Sampling rate (Hz) = 56.751E+00 Sampling timestep (secs) = 17.621E-03 Total number of samples = 1988 Number of receivers = 7  [GK] Initializing sources  Source ces =================================					
Number of receivers = 7  [OK]	Maximum distance bet	ween asked and	l real = 0.0	00E+00	
Initializing sources  Source 8 ====================================	TOTAL HUMBEL OF SAM	)TES - 1300	751E+00 521E-03		
Sources have been relocated to the nearest GLL node  Source x-requested z-requested x-obtained z-obtained distance  1 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00  Maximum distance between requested and real = 0.000E+00  [OK] Timestep # 0 t = 0.0E+00 vmax = 0.000E+00 dmax = 0.000E+00  Snapshot at timestep = 0  **********************************		cces			
Source x-requested z-requested x-obtained z-obtained distance  1 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00  Maximum distance between requested and real = 0.000E+00 [OK] Timestep # 0 t = 0.0E+00 vmax = 0.000E+00 dmax = 0.000E+00  Snapshot at timestep = 0  **********************************					
1 0.000E+00 0.000E+00 0.000E+00 0.000E+00 0.000E+00  Maximum distance between requested and real = 0.000E+00 [OK] Timestep # 0 t = 0.0E+00 vmax = 0.000E+00 dmax = 0.000E+00  Snapshot at timestep = 0  **********************************	Sources have been re	located to the	nearest GLL n	ode	
Maximum distance between requested and real = 0.000E+00 [OK] Timestep # 0 t = 0.0E+00 vmax = 0.000E+00 dmax = 0.000E+00 Snapshot at timestep = 0  **********************************	Source x-requested	d z-requested	x-obtained	z-obtained	distance
[OK] Timestep # 0 t = 0.0E+00 vmax = 0.000E+00 dmax = 0.000E+00  Snapshot at timestep = 0  **********************************	1 0.000E+0	0.000E+00	0.000E+00	0.000E+00	0.000E+00
Timestep # 0 t = 0.0E+00 vmax = 0.000E+00 dmax = 0.000E+00  Snapshot at timestep = 0  **********************************		ween requested	l and real =	0.000E+00	
**************************************		= 0.0E+00	vmax = 0.0	00E+00 dmax =	0.000E+00
* Solver phase * ***********************************	Snapshot at timestep	= 0			
CPU TIME INFORMATION (in seconds):     CPU time for initialization . 863.869E-03     CPU time per timestep 15.302E-03     Total solver CPU time 30.404E+00	CPU time for initial CPU time per timeste Total solver CPU time (m:	lization 86  p 1  ne 2  ins) 49	33.869E-03 4.997E-03 29.799E+00 96.651E-03		
CPU time for initialization . 863.869E-03 CPU time per timestep 15.302E-03 Total solver CPU time 30.404E+00	Timestep # 1000 t	= 17.6E+00	vmax = 91.6	61E-03 dmax =	28.653E-03
Program S P E C F E M : end  Test SH  Date: 01 - 06 - 2007 Time: 01:06:31	CPU time for initial CPU time per timeste Total solver CPU time (m:	lization 86 pp 1 ne 3 ins) 50	53.869E-03 .5.302E-03 80.404E+00 06.740E-03		
Program S P E C F E M : end  Test SH  Date: 01 - 06 - 2007	Storing sismos data	(SEP format)			
Program S P E C F E M : end					
Test SH  Date: 01 - 06 - 2007	Program SPECFE	M : end			
Date: 01 - 06 - 2007 Time: 01:06:31	Test SH				

#### 2.5 Outputs and their visualization

In addition to the screen output described above, sem2dsolve generates different files and scripts that allow the user to control the parameters of the simulation and to display the results. All the outputs files follow the naming convention SomeName\_sem2d.xxx, where xxx is one of the following extensions: tab for ASCII data files, txt for other text files, dat for binary data files, etc. This makes it easy to clean a working directory with a single command like rm -f \*\_sem2d\*.

#### 2.5.1 Spectral element grid

As explained in the previous section, sem2dsolve generates two PostScript files for mesh quality checking purposes: Stability\_sem2d.ps and Resolution\_sem2d.ps. The relevant information is contained in the files Stability\_sem2d.tab and Resolution\_sem2d.tab and can also be inspected with the Matlab script PRE/ViewMeshQuality.m.

#### 2.5.2 Source time function

sem2dsolve generates a file called SourcesTime\_sem2d.tab containing the source time function sampled at the same rate as the receivers. It is important to verify that the spectrum of the source has little power at those high frequencies that are not well resolved by the mesh (those that correspond to less than 5 nodes per wavelength). If this is not the case you must be very cautious in the interpretation of the seismograms in the high frequency range, or low-pass filter the results.

#### 2.5.3 Snapshots

sem2dsolve generates snapshots at a constant interval defined by the input parameter ItSnapshots. An example is shown in Figure 2.4. Requested fields are exported in binary data files called xx\_XXX\_sem2d.dat, where xx is the field code defined in the documentation of the PLOTS input block and XXX is the 3-digit snapshot number. The user is encouraged to inspect the Matlab script POST/sample\_snapshots.m to find more about the data formats and their manipulation.

If requested PostScript files xx\_XXX\_sem2d.ps are also dumped. A movie file movie.gif can be generated by the script POST/movie.csh and displayed by xanim movie.gif.

#### 2.5.4 Seismograms

The seismograms are stored using the SEP format, a simple binary block of single precision floats. The components of the vector field (velocity by default) are stored in separate files U\*\_sem2d.dat, where \* is x or z in P-SV and y in SH. The seismograms header is in the file

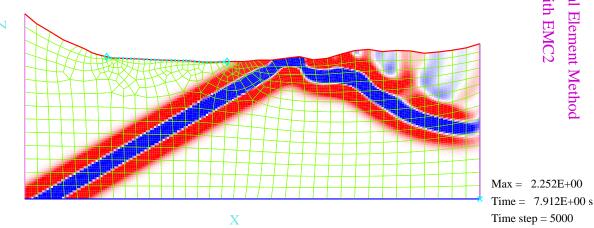


Figure 2.4: Sample snapshot from EXAMPLES/UsingEMC2/: an obliquely incident SH plane wave impinging on a sedimentary basin. The unstructured mesh of spectral elements is plotted on background.

SeisHeader\_sem2d.hdr. Its second line contains the sampling timestep DT, the number of samples NSAMP and the number of stations NSTA. The stations coordinates, XSTA and ZSTA, are listed from the third line to the end of file. With this notations, U\*\_sem2d.dat contains a NSAMP×NSTA single precision matrix.

You can view the seismograms using any tool that is able to read the SEP format, which is the case of almost all the softwares able to deal with seismic data. sem2dsolve generates scripts for the XSU-Seismic Unix visualization tool<sup>4</sup>:

- Xline\_sem2d.csh displays all seismograms together on screen
- PSline\_sem2d.csh plots all seismograms on PostScript files U\*Poly\_sem2d.ps
- Xtrace\_sem2d.csh prompts the user for a trace number (between 1 and NSTA) and then displays this particular trace on screen
- PStrace\_sem2d.csh does the same as Xtrace, but exports the traces as PostScript files U\*TraceXXX\_sem2d.ps where XXX is the number of that particular trace

The program post\_seis.exe performs similar basic manipulation and plotting (through gnuplot) of the seismograms. Its interactive menu is self-explanatory. It is usually called inside a script, as in POST/seis\_b2a.csh (converts all seismograms to ASCII) or POST/seis\_plot.csh (plots all seismograms together, an example is shown in Figure 2.5).

The script POST/sample\_seis.m shows how to manipulate and plot seismogram data in Matlab. It uses the functions POST/read\_seis.m and POST/plot\_seis.m.

#### 2.5.5 Fault outputs

Fault data from dynamic rupture simulations is stored in FltXX\_sem2d.dat, where XX is the boundary tag of the first side of the fault, tags(1) of the BC\_SWFFLT input block. Every DELT seconds (NSAMP total output times) NDAT lines with NPTS columns, one per fault node, are written <sup>5</sup>. Stress fields are relative to their initial values, which are contained in the first NDAT lines. The header file FltXX\_sem2d.hdr contains the information needed to read the data file. Its format, line by line, is:

- 1. NPTS NDAT NSAMP DELT (name of parameters)
- 2. Value of parameters above
- 3. Name of data fields, separated by ":"
- 4. XPTS ZPTS (name of coordinate axis)

<sup>&</sup>lt;sup>4</sup>Seismic Unix is freely available from the Colorado School of Mines at http://timna.mines.edu/cwpcodes

<sup>5</sup>The actual number of columns is NPTS +2: Fortran adds a one-word tag at the front and end of each record.

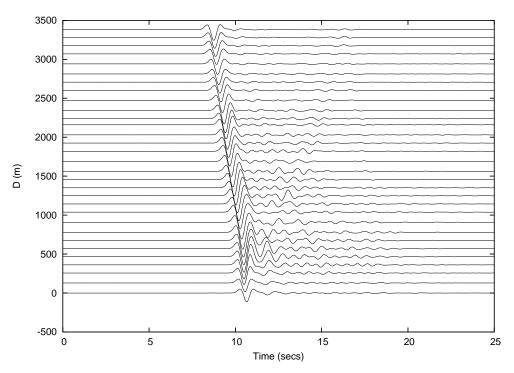


Figure 2.5: Sample seismograms from EXAMPLES/UsingEMC2/ generated with POST/seis\_plot.csh.

5. from here to the end of file, a two-column table of coordinates of the output fault nodes

The script FltXX\_sem2d.csh shows how to extract ASCII time series of different fields at given locations on the fault, using Seismic Unix tools.

The program post\_fault.exe performs basic manipulations of the fault data, including conversion to an ASCII file readable by gnuplot. Its interactive menu is self-explanatory.

The script POST/sample\_fault.m shows how to manipulate and plot fault data in Matlab.

## Chapter 3

# Generating a mesh with EMC2

#### 3.1 The mesh generator EMC2

EMC2 is one of the few public domain 2D mesh generators including quadrilateral elements and a Graphical User Interface. It is a C code which sources and executables can be freely downloaded from http://www-rocq.inria.fr/gamma/cdrom/www/emc2/eng.htm . Although a complete documentation can be found in that package, we show here an example featuring the most useful functionalities.

Before starting you must provide files containing 2-column data (X,Z), without headers, of all the points needed to define the geometry of the model (topography, sediment bottom).

Once installed, you can run EMC2 by typing emc2.

#### 3.2 Notations

The following notations are assumed in this chapter:

- (XXX) = click XXX on top menu bar
- (xxx) = click xxx on bottom menu bar
- $\bullet$  <XXX< = click XXX on left menu bar
- $\bullet$  >XXX> = click XXX on right menu bar
- \$xxx\$ = enter xxx from keyboard or from the calculator in the right panel
- "xxx" = type xxx in bottom prompt
- $\{xxx\}$  = perform action xxx
- \*xxx = do xxx as many times as needed

• n\*xxx = do xxx n times

#### 3.3 Basic step-by-step

A typical EMC2 session has three steps:

STEP I: CONSTRUCT, defines the geometry of the model

1. Switch to the construction tool:

<CONSTRUCTION<

2. Load the points:

(POINT) (xy file) "palosgrandes.dat"

You must give the full path to your points-file, the root directory being the one where you launched emc2.

3. Reset the figure window to fit all points:

>SHOW ALL>

The original data has some geometrical features that are too complex to be meshed by quadrilaterals, for instance the corners at the N and S ends of the basin, you may want to smooth out these features. You also need to define the extreme boundaries of the region to be modelled (N,S and bottom absorbing boundaries) and some additional points on the free surface outside the basin. You must modify the data set (add and delete points):

- 4. Add new points:
  - a. with the mouse:

```
(POINT) (mouse) *{click in figure window}
```

b. by coordinates:

This is the safest way to get really vertical and horizontal boundaries needed for the absorbing conditions in SPECFEM90. You probably need to get the coordinates of an existent reference point:

```
(POINT) < QUERY < (point) *{click on point}
```

- c. you can also reload another point-file (I2)
- 5. Delete points,

```
(POINT) < DESTRUCT < (point) *{click on point}
```

Now you must define the geometry of the domains. These macro-blocks are intended to be internally meshed by deformed quadrilaterals. Their geometry follows the geometry of the geological model (one domain per material). Each domain must be bounded by segments or splines:

6. Segments:

```
(SEGMENT) (point) 2*{click extreme point}
```

7. Splines:

(SPLINE) (point) \*{click point}

You will see the spline evolve as you click points.

STEP II: PREPARE, defines the properties of the discrete spectral element mesh

1. Switch to the preparing mesh tool:

<PREP MESH<

2. Define domains with rock n:

(DOMAIN REF) \$n=\$ (any) \*{click inside domain}

You will see the domains edges get colored and the domains get numbered with n.

3. At any moment you can decide to show or not the domain decomposition:

To hide the domain decomposition:

>REFRESH>

Show the domain decomposition:

(SHOW) (ALL)

4. Remove a domain definition:

(REMOVE) (DOMAINE) (any) {click inside domain}

WARNING: corrections to the domain decomposition are sometimes displayed only after refreshing the figure window.

5. Now you must define the subdivision of each domain in quadrilateral finite elements. Define the number n of elements on each edge:

(NB INTERVAL) \$n=\$ (any) {click edge}

You will see the intermediate points appear. The number of intervals n is mainly dictated by the resolution criterion: elements should be smaller than the smallest wavelength you want to propagate. Moreover, a domain can be quadrangulated only if the total number of intervals along its perimeter is even (the sum of all n along its boundaries). However, a quality mesh is not always guaranteed and you need to proceed by trial and error (emc2 allows you to jump back and forth between the different steps of the meshing procedure).

6. Finally you must define the external boundaries of the modelled region which will have a special treatment. You must associate a tag (a number) to each absorbing boundary. No convention is assumed but you should remember those tags later when setting the boundary conditions in SEM2D. It is also useful to assign a tag to the free surface boundary, that will be eventually used by SEM2D to locate the receivers or sources.

Define a boundary with index n:

(LINE REF) \$n=\$ (any) \*{click edge}

Of course each boundary can be composed of many domain edges. Refresh the display to better see the boundaries. The same procedure applies to define split-node interfaces such as faults and cracks: you must assign a different tag to each side of the fault.

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7. Save your work in EMC2 format:

<SAVE< "name"

The resulting file is name.emc2\_bd

STEP III: EDIT, generates the mesh

1. Switch to the edit mesh tool:

<EDIT\_MESH<

Press ENTER 4 times.

A triangles mesh appears. You must convert it to a quad mesh:

2. Convert the triangle mesh to a quad mesh:

<QUADRANGULATE> <ALL>

You can smooth the mesh with: <REGULARIZE> \*<ALL>

The final mesh is displayed. If there remain some triangles come back to the previous step and figure out how to modify the points per edge to help the mesher. Some experience is needed here.

3. Renumber the mesh, in order to optimize computations:

\*<RENUMBER>

4. Define the boundary condition for the 4 corner nodes of the model: (these nodes belong to 2 external boundaries so they were given a reference number =0)

(MODIF\_REF) \$n=\$ (corner) {click close to corner, inside element}

Where n is the reference number of one of the 2 boundaries containing the corner node. Zooming can be useful. The same operation must be performed for the corner nodes of the subdomains belonging to an external boundary, and for the the crack tip nodes. However, as a special case, crack tip nodes must be assigned the -1 tag.

5. Export the mesh:

<SAVE<

Two questions are asked in the bottom prompt:

- Format of the file, you must select:
  - "ftq"
- Prefix name for the file
  - "name"

The resulting file name will be name.ftq

#### 3.4 Further tips

- Whenever possible it is better to mesh a domain with a *structured* mesh (a deformed cartesian grid). This can be done with (QUADRANGULATE), during the PREPARE step. See our FAQ for further details.
- To load an existent project, in the construction tool or in the preparation mesh tool: <RESTORE<"name"

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EMC2 will look for the file name.emc2\_bd. Beware: the project loaded will replace the actual project if any, there is no superposition.

- BUG WARNING (13/07/01): the Sun release of EMC2 has a bug with the reference indices in the ftq format This bug is fixed in the 2.12c version. If you work on a Sun station, download the most recent version of the sources, rather than the executable, and compile it yourself.
- To densify (h-refinement) an existent mesh use the script SEM2DPACK/POST/href.csh. It edits the \*.emc2\_bd file, then you can restore it in EMC2 and save it in \*.ftq format.
- To create a fault, in EDIT\_MESH mode:
  - a. Crack an existent edge: (CRACK) (segment)
  - b. Give a reference number to each side of the fault :  $(MODIF\_REF) n=$ (segment)$
  - c. Give the tag "-1" to crack tip nodes:
     (MODIF\_REF) \$-1=\$ (corner) \*{click close to crack tip node, inside element}
- Note that only Q4 elements (4 control nodes) are supported. For a smoother description of boundaries Q9 would be desirable.

## Chapter 4

# Adding features to SEM2D (notes for advanced users)

Sometimes you will need to add new capabilities to the SEM2DPACK solver, by modifying the program. The following notes are intended to guide you through this process. We will not give here a comprehensive description of the code architecture, only enough details to get you started in performing safely the most usual and evident modifications.

#### 4.1 Overview of the code architecture

```
[ ... in progresss ...]
```

#### 4.2 Accessible areas of the code

Some areas of the code have been written in such a way that a moderately experienced Fortran 95 programmer, with a limited understanding of the code architecture, can introduce new features without breaking the whole system. This is achieved through modularity, encapsulation and templates. The modifications that are currently accessible are:

- boundary conditions, see bc\_gen.f90
- material rheology, see mat\_gen.f90
- source time functions, see stf\_gen.f90
- spatial distributions, see distribution\_general.f90

The source files listed above contain step-by-step instructions, just follow the comments starting by !!.

## Chapter 5

# Frequently Asked Questions

#### $5.1 \quad SEM2D$

#### Segmentation fault

This problem is often related to a small stack size in your computer settings. In your Linux shell do: ulimit -s unlimited. Place this command in your .bashrc.

#### 5.2 EMC2

#### I can't get rid of a few triangles

Obtaining a quality quad mesh is not always a trivial task. Trial and error and experience is needed. This can be by far the most time consuming stage of modeling.

First make sure that the total number of element edges along the perimeter of each mesh domain is even. This is a necessary topological condition to generate a quad-only mesh.

When the geometry seems too complicated for quad meshing you should consider simplifying the geometry, especially those details that are much smaller than the dominant wavelength.

If the above fails or does not apply, you have to help the mesher. The recommended procedure in EMC2 is:

- 1. Divide your original mesh into simple domains, in such a way that *most* domains have exactly four sides (possibly curved) and the remaining non-four-sided domains are as small as possible.
- 2. Generate a structured quad-mesh (a regular grid) inside each four-sided domain with the (QUADRANGULATE) tool of the PREP\_MESH mode, as described in section 5.2.13

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- of EMC2's manual (note that this is not the same as the <QUADRANGULATE> button in the EDIT\_MESH mode).
- 3. Proceed as usual (triangulation followed by quadrangulation) inside the remaining non-four-sided domains. If these are small enough EMC2 should not have problems doing a correct tri-to-quad meshing.

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