# Heterogeneous Network Representation Learning: A Unified Framework with Survey and Benchmark

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## 1 GOALS

- we aim to provide a unified framework to **deeply summarize and evaluate existing research** on heterogeneous network embedding (HNE)
  - we first formulate a unified yet flexible mathematical paradigm of HNE algorithms
  - we propose a generic objective function of *network smoothness*, and reformulate all
    existing models into this uniform paradigm while highlighting their individual novel
    contributions
- we provide a generic paradigm for the **systematic categorization and analysis over the merits** of various existing HNE algorithms
- we create four benchmark datasets with various properties regarding scale, structure, attribute/label availability, and etc. from different sources, towards handy and fair evaluations of HNE algorithms
- we carefully refactor and amend the implementations and create friendly interfaces for 13 popular HNE algorithms

#### 2 PRELIMINARIES

- HNE: Heterogenous network embedding
- Hadamard product: element-wise product

#### 3 CHALLENGES

real-world objects and interactions are often multi-modal and multi-typed

# 4 PREVIOUS WORK / CITATIONS

- •
- This Work: ...

# 5 DEFINITIONS

- Heterogeneous network:  $H = \{V, E, X, R, \phi, \psi\}$ 
  - $-v_i$  ∈ V: vertices,  $e_{ij}$  ∈ E: edges
  - $-\phi(v_i)$ : Node type,  $\psi(e_{ij})$ : Link type
  - $X_i^o$ : Node attribute,  $U_{ij}^o$ : Link attribute
- Meta-Path: Path  $o_1 \rightarrow l_1 \ o_2 \rightarrow l_2 \ ... o_m \rightarrow l_{m+1} \ o_{m+1}$ 
  - Where *o* and *l* are node/link types
  - Carries semantics (composed relation)
  - Allows computing multi-modal proximity
- Network embedding:  $\Phi: V \to \mathbb{R}^{|V| \times \overline{d}}$
- Heterogenous network embedding:  $\{\Phi_k: V \to \mathbb{R}^{|V_k| \times d}\}_{k=1}^K$ 
  - where *K* is number of node types
- Smoothness Objective:  $\mathcal{J} = \sum_{u,v \in V} w_{uv} d(e_u, e_v) + \mathcal{J}_R$ 
  - Where  $e_u, e_v$  are node embeddings

- $w_{vw}$ : proximity weight
- $d(\cdot, \cdot)$ : distance function

#### 6 OUTLINE / STRUCTURE

# 6.1 Taxonomy

- 6.1.1 Proximity-Preserving Methods.
  - Goal of network embedding is to capture network topological information
  - Preserving different types of proximity among nodes
  - Approaches:
    - Random Walk Approaches (DeepWalk [29])
      - \* metapath2vec: randomwalk -> skipgram (context based) (negative sampling)
      - \* hin2vec: max likelihood based on path count/probability approximation (but employs a negative sampling like approach)
    - First/Second-order Proximity (LINE [30])
      - \* PTE: Split into multiple bipartite networks. Per network maximize the co-occurrence objective (skipgram)
        - · Instead of co-occurrence counts, edge weight is used (based on different type edge counts)
      - \* HEER:
        - · each edge type has embedding  $\mu_l$
        - · each edge has embedding  $g_{uw}$
        - · assume:

$$\boldsymbol{\mu}_l^T \boldsymbol{g}_{uv} = \boldsymbol{e}_u^T \boldsymbol{A}_l \boldsymbol{e}_v$$

- · Again max likelihood across bi networks
- considered as shallow network embedding, due to their essential single-layer decomposition
- 6.1.2 Message Passing Methods.
  - aim to learn node embeddings  $e_u$  based on  $x_u$  by aggregating the information from u's neighbors.
  - Considered as deep network embedding due to multiple layers of learnable projection functions
  - In unsupervised setting: objective is link prediction
  - Meta path based neighborhood:  $\mathcal{N}_{\mathcal{M}}(u) = \{v | v \text{ connexts with } u \text{ via meta-path } \mathcal{M}\}$
  - $a_{uv}^{\mathcal{M}}$ : Learned weight of of neighbors
  - β<sub>M</sub>: Meta path weight
- 6.1.3 Relation-Learning Methods.
  - Knowledge Graphs are a special case of heterogeneous networks
  - Explicitly model the relation types of edges via parametric algebraic operators
  - Focus on the designs of triplet based scoring functions
    - learn a scoring function  $s_l(u, v)$  which evaluates an arbitrary triplet (where l is relation type)
  - Usually margin based ranking loss is used + regularizer
    - Which has very similar form to negative sampling loss (!)
  - Works:
    - **TransE**: assume  $e_u$  +  $e_l$  ≈  $e_v$  when relation l holds (translation of embedding)
      - \* Optimizes by maximizing margin between related and unrelated pairs

- Distmult: exploits similarity based scoring (usually  $e_u^T A_l e_v$ ) (aka the alignment score with some diagonal matrix inbetween)
- ComplEx: utilizes complex valued representations which allows capturing asymmetric relations

# 7 EVALUATIONS

- Tested: Classification and Link prediction
- Proximity-preserving algorithms: **often perform well** on both tasks under the unsupervised unattributed HNE setting
- Message-passing methods: perform poorly except for HGT, especially on node classification. But are known to excel due to their integration of node attributes, link structures, and training labels (which are not available).
- Relation learning methods: perform well on link predictions (when there are a lot of link types)

## 8 CODE

• https://github.com/yangji9181/HNE)

## 9 RESOURCES

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# 10 NOTE (TO SELF)

• Read more about transformers and check out [85]