# Community Detection through Representation learning in Evolving Heterogenous Networks

A Master's Thesis proposal

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Recent developments in big data and graph representation learning have allowed researchers to make breakthroughs in social network analysis and the identification of communities. While opening a lot of research opportunities, such approaches are highly limited to snapshots of rapidly evolving social networks. This, in fact, is a great simplification of the real-world situation which is always evolving and expanding by the user and/or machine interactions.

Relying on novel research of dynamic graph representation learning, the goal of my thesis project is to build a framework for community detection and representation in evolving heterogeneous networks. To verify the merit of the proposed framework, it will be evaluated against baselines on static heterogeneous graphs, and analyzed against gathered twitter dataset on covid measures.

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# 1 INTRODUCTION AND BACKGROUND

Social Network Analysis (SNA) is a huge part of the Network Science field and is concerned with the process of investigating social structures that occur in the real-world using Network and Graph Theory. These social structures usually include social media networks, economic transaction networks, knowledge networks, and disease transmission networks.

One main issue to address while studying this type of real-world events lies in the identification of meaningful substructures hidden within the overall complex system. The SNA is therefore applied to extract patterns from the data usually in form of information flow, identification of high throughput nodes and paths, and discovery of communities and clusters. In this thesis, we are going to focus on the problem of community discovery.

This thesis proposal is structured as follows: in this section, we are going to introduce basic concepts and challenges of Dynamic Community Detection. In section 2 a brief literature survey is conducted on identifying the current state of the art and approaches to Dynamic Community Detection. In section 3 we will describe the problem we are trying to solve as well as formulate the research questions. In section 4 we will elaborate on our proposed methodology for solving the posed problem and answering the research questions. Finally, in **??** the concrete planning for the research project is laid out.

## 1.1 Community Detection

The problem of partitioning a complex network into *communities* which represent groups of individuals with high interaction density, while individuals from different communities have comparatively low interaction density is known as Community Discovery (CD). CD is a task of fundamental importance within SNA as it discloses deeper properties of networks. It provides insight into networks' internal structure and its organizational principles.

Many useful applications of CD have been studied by researchers including identification of criminal groups [44], social bot detection [22], targeted marketing [32], and public health/disease control [43].

With the explosion of human- and machine-generated data, often collected by social platforms, more datasets are emerging having rich temporal information that can be studied. CD operates only on static networks. Meaning that their temporal dimension is often omitted, which often does not yield a good representation of the real world, where networks constantly evolve. Such networks are often referred to as dynamic networks as their components such as nodes and edges may appear and fade from existence. Accordingly community detection on such dynamic networks is called Dynamic Community Detection (DCD).

DCD algorithms incorporate additional temporal data are often able to both outperform their counterpart CD algorithms [10, 13, 29, 39], as well as provide additional information about communities for analysis [35]. This additional information comes in form of community events such as (birth, growth, split, merging, and death) or in form of the ability to track the membership of certain individuals over time.

## 1.2 Challenges in Community Detection

DCD is seen as the hardest problem within Social Network Analysis. The reason for this is mainly because DCD, unlike CD, also involves tracking the found communities over time. This tracking relies on the consistency of the detected communities, as usually slight changes to the network may

cause a different community membership assignment. Not properly accounting for this uncertainty may cause community and result drift [7].

Additionally, the increasing richness of the data is not only limited to temporal data. The real-world data often connects entities of different modalities. This multi-modality occurs through the fact that the entities and relations themselves may be of different types (meta topology-based features). For example users, topics, and documents in a social network (or vehicles and landmarks in a traffic network). More complex networks may include asymmetric relationships, and temporal networks may include appearing, disappearing, or streaming edges/nodes.

Another example of multi-modality in networks comes in form of node and relation features (content-based features). These features may come in form of structured (numerical, categorical, or vector data) or unstructured data such as images and text. It is of high importance to explore this multi-modal data as it may not always be possible to explain the formation of communities using network structural information alone.

Finally, a more systematic issue is that there is no common definition for a community structure. Within networks, it is usually described in terms of membership assignment, while in more content-based settings communities are described in terms of modeled topics (that usually represent interest areas) or distributions over latent similarity space. Both definitions have their shortcomings as they often fail to account for more complex community structures (such as overlapping and hierarchical communities) and non-linearity of structures often found in the real world.

Task of community detection is often compared to clustering and graph clustering, which not always may be a fair comparison as a main focus point in many CD algorithms is the fact that the amount of communities is unknown a priori. Communities are not are never planted in the real world and the algorithms should detect them in an unsupervised manner.

## 2 LITERATURE REVIEW

The problem of dynamic community detection was noticed quite early on within the SNA community and a considerable amount of research has been made in order to provide a comprehensive analysis of the network. While the said research was mostly focused on the discovery of communities using topologically-based features and node connectivity, the covered methods did research the limitations and challenges posed by a temporal context.

In recent years, significant developments have been made in the space of deep learning. Mainly in the development of new deep learning methods capable of learning graph-structured data [4, 18, 24] which is fundamental for SNA. Because of this, various problems within the field have been revisited, including community detection problems. The approaches have been expanded by incorporation of more complex features, solving the problems concerning multi-modality, and the introduction of unsupervised learning.

Despite this resurgence, the DCD problem has received little attention. Though a few efforts have been made to incorporate the deep learning methods by introducing content-based similarity dynamic, the definition of unified constraints for end-to-end learning, and usage of graph representation-based CD algorithms within a temporal context, the current state of the art leaves a lot to be desired.

We structure the literature as follows: first, we describe the various interpretations of the Community Structure in section 2.1. Next, we explore various approaches and techniques related to Graph Representation Learning in section 2.2. Then, we provide an overview of the current state-of-the-art

approaches for Community Detection and Dynamic Community Detection tasks in section 2.3 and section 2.4. Finally, we discuss the ways to evaluate the said algorithms in section 2.5 and the datasets available in section 2.6.

## 2.1 Community Structures

The goal of this section is to introduce fundamental structures for the Dynamic Community Detection task. We do this by combining various definitions used in the relevant literature as well as establishing the purpose for these structures, before proceeding into approaches for detecting communities in the following sections.

### 2.1.1 Communities

Communities in real-world networks can be of different kinds: disjoint (students belonging to different educational institutions), overlapping (person having membership in different social groups) and hierarchical (components of a car). One of the main reasons behind the complexity of CD is that there is not one unique definition what a community actually is.

The *link-based* (also referred to as classic) community detection methods intuitively describe communities as groups of nodes within a graph, such that the intra-group connections are denser than the inter-group ones. This definition is primarily based on the *homophily* principle, which refers to the assumption that similar individuals are those that are densely connected together. Therefore, these kind of methods look for sub-graph structures such as cliques and components that identify connectedness within the graph structure to represent the communities.

Unfortunately, in most cases link-based methods fall short to identify communities of similar individuals. This is mainly due to two facts: (i) many similar individuals in a social network are not explicitly connected together, (ii) an explicit connection does not necessarily indicate similarity, but may explained by sociological processes such as conformity, friendship or kinship [8, 10].

A more general definition is introduced in [6] to create an underlying concept generalizing all variants found in the literature (+? ]). In link-based methods, a direct connection is considered as a particular and very important kind of action, while newer methods also consider content or interest overlap.

> **Community** A community in a complex network is a set of entities that share some closely correlated sets of actions with the other entities of the community.

### 2.1.2 Dynamic Communities

Similar to how communities can be found in static networks, dynamic communities extend this definition by utilizing the temporal dimension to define their life cycle/evolution over a dynamic network. A dynamic community is characterized by a collection of communities and a set of transformations on these communities over time.

This persistence of communities across time subjected to progressive changes is an important problem to tackle. Though, as noted by [40] the problem can be compared to the famous "the ship of Theseus" paradox. Because (verbatim), *deciding if an element composed of several entities at a given instant is the same or not as another one composed of some—or even none—of such entities at a later point in time is necessarily arbitrary and cannot be answered unambiguously.*

Most of the works agree on two atomic transformations on the communities, including node/edge appearance and vanishing. While some such as [1, 35, Cazabet et al. [5]] define a more extensive

set of transformations (also referred to as events) which may be more interesting for analytical purposes:

- Birth, when a new community emerges at a given time.
- Death, when a community disappears. All nodes belonging to this community lose their membership.
- Growth, when a community acquires some new members (nodes).
- Contraction, when a community loses some of its members.
- Merging, when several communities merge to form a new community.
- Splitting, when a community is divided into several new ones.
- Resurgence, when a community disappears for a period and reappears.

These events/transformations are often not explicitly used during the definition and/or representation of dynamic communities. Nevertheless, most of the methods covered in the following sections do define a way in their algorithm to extract such events from the resulting data.

Finally, it is important to note that dynamic networks can differ in representation. They can be represented as either a time series of static networks (also referred to as snapshots) or as a real-time stream of edges (referred to as temporal networks). Within the global context of dynamic community detection, they can be seen as equivalent as the conversion between the two representations can be done in a lossless way. The latter, temporal networks are often used to handle incremental changes to the graph and are most commonly applied within real-time community detection settings.

## 2.2 Graph Representation Learning

The representation-based approaches stem from the field of computational linguistics which relies heavily on the notion of *distributional semantics* stating that words occurring in similar contexts are semantically similar. Therefore the word representations are learned as dense low-dimensional representation vectors (embeddings) of a word in a latent similarity space by predicting words based on their context or vice versa [31, 37]. Using the learned representations similarity, clustering and other analytical metrics can be computed.

The success of these representation learning approaches has spread much farther than just linguistics as similar ideas are also applied to other fields including graph representation learning. Methods such as deepwalk [38], LINE [45], and node2vec [15] use random walks to sample the neighborhood/context in a graph (analogous to sentences in linguistic methods) and output vector representations (embeddings) that maximize the likelihood of preserving the topological structure of the nodes within the graph.

Whereas previously the structural information features of graph entities had to be hand-engineered, these new approaches are data-driven, save a lot of time labeling the data, and yield superior feature/representation vectors. The methods can be trained to optimize for *homophily* on label prediction or in an unsupervised manner on link prediction tasks.

Newer approaches introduce the possibility for the fusion of different data types. GraphSAGE [17] and Author2Vec [48] introduce a methodology to use node and edge features during the representation learning process. Other approaches explore ways to leverage heterogeneous information present within the network by using *metapath* based random walks (path defined by a series of node/link types) [9] or by representing and learning relations as translations within the embedding space [3]. In Nguyen et al. [34] the authors introduce a way to encode temporal information by adding chronological order constraints to various random walk algorithms. Other

relevant advancements within the field include Graph Convolutional Networks (GCN) [25] and (Variational) Graph Auto-Encoders (GAE) [23] which present more effective ways to summarize and represent larger topological neighborhoods or whole networks.

## 2.3 Link-based Approaches

Link-based approaches to (Dynamic) Community Detection rely on connection strength to find communities within the network. The main criteria for communities are the assumed property that intra-group connections are denser than inter-group ones. The networks are partitioned in such a way, that optimizes for a defined measure characterizing this property.

We start this section by covering the fundamentals of link-based community detection by introducing commonly used community quality measures and algorithms for optimizing them. Next, we introduce the link-based DCD problem and the unique challenges that arise as opposed to CD. Then we proceed to cover the current state of the art by describing the related works, their solutions to the said challenges, and possible extensions to the problem.

### 2.3.1 Community Detection

Different metrics exist quantifying the characteristic of *homophily* over edge strength. The most common metric is Modularity which measures the strength of the division of a network into modules (communities). Its popularity stems from the fact that it is bounded and cheap to compute, though it has other problems such as resolution limit (making detecting smaller communities difficult). Other metrics that can be found in the literature include but are not limited to:

- Conductance: the percentage of edges that cross the cluster border
- Expansion: the number of edges that cross the community border
- Internal Density: the ratio of edges within the cluster with respect to all possible edges
- Cut Ratio and Normalized Cut: the fraction of all possible edges leaving the cluster
- Maximum/Average ODF: the maximum/average fraction of nodes' edges crossing the cluster border

*Modularity.* Modularity directly measures the density of links inside a graph and is therefore computed on communities (sets of nodes) individually by weighing edges based on community similarity (or exact matching). Calculation of modularity is done by aggregating for each pair of nodes the difference between the expected connectivity (amount of edges between the nodes) and the actual connectivity (existence of an edge) given their degrees (eq. 1). The final result represents the delta difference by how much the given graph exceeds a random graph as expected connectivity is determined by a random rewiring graph. Because intra-community pairs are weighted lower than inter-community pairs the score can vary.

$$Q = \frac{1}{2m} \sum_{vw} \sum_{r} \left[ \overbrace{A_{vw}}^{\text{Connectivity}} - \underbrace{\frac{k_v k_w}{2m}}_{\text{Expected Connectivity}} \right] \overbrace{S_{vr} S_{wr}}^{\text{Community Similarity}} \tag{1}$$

*Louvain Method.* Finding an optimal partition of a graph into communities is an NP-hard problem. This is because, while calculating the modularity score can be done in a timely manner, still all possible node to community assignments have to be considered. Therefore heuristic-based methods such as the Louvain method are usually used.

Louvain method [2] is a heuristic-based hierarchical clustering algorithm. It starts by assigning each node in the graph to its own community. Then it merges these communities by checking for each node the change in modularity score produced by assigning it to a neighbor community (based on the existence of a connection). Once the optimal merges are performed, the resulting communities are grouped into single nodes and the process is repeated.

Since modularity changes can be computed incrementally, the complexity of this method is $O(n \log n)$. Additionally, due to the flexibility of the modularity measure, it allows detecting communities in graphs with weighted edges.

*Label Propagation algorithm.* Another way to sidestep the complexity issue is using the Label Propagation algorithm as it uses the network structure directly to define partitions and doesn't require any priors (quality metrics). The intuition for the Label Propagation algorithm is as follows: When propagating a label through connections in the network, a single label quickly becomes dominant within a group of densely connected nodes, but these labels usually have trouble crossing sparsely connected regions.

The algorithm starts by assigning each node their own label. After that, for each iteration, each node updates its label to the majority label among its neighbors where ties are broken deterministically. The algorithm stops after a fixed amount of iterations or once it has converged. An important feature of this algorithm is that a preliminary solution can be assigned before each run, therefore only updating existing membership assignments.

### 2.3.2 Dynamic Community Detection

Dynamic Community Detection can be seen as an extension to community detection by the addition of the Community Tracking task. Tracking relies on the coherency and stability of found communities to define their evolution through time. The said properties are not be taken for granted and introduce new challenges when designing DCD methods. The main issue is in fact that they are competitive with each other causing a trade-off between community coherency/quality and community temporal stability.

Various strategies dealing with this trade-off are categorized by Rossetti and Cazabet [40] and Dakiche et al. [7] where authors reach a consensus over three main groups. In the following sections, we briefly introduce these strategies and describe the current state of the art in similar order.

*Independent Community Detection and Matching.* Also referred to as the two-stage approach. Works by splitting the DCD task into two stages. The first stage applies CD directly to every snapshot of the network. Followed by the second stage matching the detected communities between the subsequent snapshots.

The advantages of this approach include the fact that it allows for use of mostly unmodified CD algorithms for the first step and that it is highly parallelizable as both detection and matching steps can be applied to each snapshot independently. The main disadvantage is the instability of underlying CD algorithms which may disrupt the community matching process. Many CD methods may give drastically different results in response to slight changes in the network. During the matching, it becomes difficult to distinguish between this algorithm instability and the evolution of the network.

In Wang et al. [46] the authors circumvent this instability issue by looking at the most stable part of the communities, namely core/leader nodes. In their research, they observe that in various datasets most of the nodes change dramatically while only a small portion of the network persists stably.

To exploit this feature, the algorithm CommTracker is introduced which first detects the said core nodes, and then defines rules to both extract communities as well as their evolutional events. The community members are assigned based on their connectivity relative to core nodes.

Rossetti [39] proposes a way to detect overlapping communities in dynamic networks. A more robust two-phase community detection method (ANGEL) is proposed to ensure the stability of the found communities. The first phase extracts and aggregates local communities for each node by applying Label Propagation on their Ego-Graph (graph with the said node removed). Because the found communities are biased due to a partial view of the network, they are merged in the second step based on their overlap yielding more stable communities with the possibility of overlap. During the matching for each snapshot, a step forward and backward in time is considered where community splits and merges are detected by reusing the matching criteria of the second phase of the CD step.

*Dependent Community Detection.* Dependent Community Detection strategy works detecting communities in each snapshot based on the communities found in the previous snapshots. This approach introduces temporal smoothness because the previous solution is reused making the matching process obsolete. Though as part of the described trade-off it can impact the long-term coherence of the dynamic communities. Mainly, because each step introduces a certain amount of error into the results (community drift) which may get amplified within further iterations (error accumulation). Another disadvantage is the fact that the strategy has limited possibilities of parallelization due to its dependent nature.

To lessen the complexity of continuous re-detection of the communities some algorithms process the changes incrementally by limiting the change to a local neighborhood. While this approach has many benefits, it is important to note that these algorithms face a problem where only applying local changes can cause communities to drift toward invalid ones in a global context.

He and Chen [19] introduces an efficient algorithm by modifying the Louvain method algorithm. Based on the observation that between consecutive timesteps only a fraction of connections changes and do not affect communities dramatically, they argue that if all community nodes remain unchanged, the community also remains unchanged. With this in mind, they make a distinction between two types of nodes, ones that change the connection in a snapshot transition and ones that do not. The former have to be recomputed, while the latter maintain their community label. The nodes that maintain their community are merged into community nodes with edges to other community nodes and changed nodes weighted proportionally to their real connectivity (amount of edges when ungrouped). This simplified graph is passed to the Louvain method algorithm for community detection. By reusing the community assignments temporal smoothness is maintained and due to the incremental nature of this algorithm, the overall complexity remains low.

Guo et al. [16] envision the target network as an adaptive dynamical system, where each node interacts with its neighbors. The interaction will change the distances among nodes, while the distances will affect the interactions. The intuition is that nodes sharing the same community move together, and the nodes in different communities keep far away from each other. This is modeled by defining the so-called Attractor algorithm, which consists of three interaction patterns that describe how node connection strength is influenced by neighboring nodes. The edge weights are initialized using Jaccard distance and the propagation is run until convergence. The communities can be extracted by thresholding on edge weight/distance. Thereafter, all changes are treated as network disturbances. The disturbance can be limited to a certain area using a disturbance factor which defines a bound on the possible propagation.

More recently the Yin et al. [51] has proposed an evolutionary algorithm by looking at the DCD from an Evolutionary Clustering Perspective. They detect community structure at the current time under the guidance of one obtained immediately in the past by simultaneously optimizing for community quality score (modularity) and community similarity between subsequent time steps (NMI). In the methodology, a way is proposed to encode a graph efficiently into a genetic sequence. Additionally, new mutation and crossover operators are proposed which maximize either of the two objectives. By using a local search algorithm, building a diverse initial population, and selecting for dominant candidates the communities maximizing both objectives are obtained.

*Simultaneous community detection.* The final strategy we consider sidesteps the matching issue by considering all snapshots of the dynamic network at once. This is done by flattening the network in the temporal dimension and coupling edges between the same nodes at different timesteps. These approaches usually don't suffer from instability or community drift. The disadvantages include that the standard principle of a unique partition for each time step can not be applied, limiting the number of possible algorithms. Handling real-time changes to the graph are also usually not considered.

Mucha et al. [33] adopt a simple yet powerful solution to this problem by connecting identical nodes between different time steps within the unified network. On this network, they apply a modified Louvain method algorithm to extract the communities whose members can be split over different timesteps.

Ghasemian et al. [12] apply stochastic block model-based approach. They make a distinction between two edge types: (i) spatial edges (edges between neighbors) and (ii) temporal edges (edges connection nodes in different timesteps). Using this distinction, they define a Belief Propagation equations to learn marginal probabilities of node labels ($\mu_s^i(t)$) over time. Additionally in their research, they introduce a way to derive a limit to the detectability of communities. This is, because some communities may not be detectable as their probability nears that of chance.

## 2.4 Representation-based Approaches

The main difference between Representation-based approaches and link-based approaches is the fact that they usually don't directly model the network based on connections. Instead they learn an intermediate representation of the graph or its components to which CD detection can be applied to. While also relying on the idea of *homophily*, most of methods define additional objectives to improve community quality.

The main reasoning for this is the fact that real-world networks are non-linear, meaning that there may be no connections when then make sense and vice versa [47]. By using deep neural networks to learn these embeddings one can address such non-linearity as they are in general very robust against noise. Other notable benefits to using representation-based approaches include the fact that they compress the data efficiently as real-world networks are very sparse. They can also represent multi-modal features, network (meta) structure and temporal dimension by defining them all in a compatible similarity space or learning mappings to this space. Finally, representations are naturally easy to compute similarity on.

In this section we describe representation based approaches by covering both CD and DCD approaches. To provide a more cohesive overview of the methods, we group them by their innovations instead.

*Affiliation Graph Models.* While arguably not being representational by itself, Affiliation Graph Network (AGM) model introduced in Yang and Leskovec [50] is very influential within deep learning / representation learning CD field.

The AGM models a network as a bipartite graph with communities as first class citizens and is represented by the following equation $B(V, C, M, \{p_c\})$, where $V$ represents nodes, $C$ set of communities, $M$ node-community memberships and $\{p_c\}$ model parameters (a single probability $p_c$ per community). It can model non-overlapping, overlapping and hierarchical communities by defining rules on membership sets in $M$. AGM can used in both generative and discriminative settings.

The generative scenario goes as follows: Given an AGM $F$ generate links between each pair of nodes exceeding a baseline probability $p$. The can be done by considering that according to AGM, each pair of nodes in community $A$ is connected with a probability $p_A$. Therefore, the probability of two nodes having a connection is proportional to the amount of communities they share (which is defined in the model).

The discriminative scenario is defined as: Given a graph $G$ and , find a model $F$ that may have generated it. By assuming that the graph was generated using an AGM, the parameters $M$, number of communities $|C|$ and $\{p_c\}$ have to be found. Process for finding such a model to the graph usually max likelihood fitting. AGM is relaxed to have membership strengths $F_{uC}$, which helps to define probability of nodes $u$ and $v$ connecting through community $C$ ($P_C(u, v)$), and in terms of that by themselves $P(u, v)$. Using this a probability $P(G|F)$ can be constructed quantifying how well the model fits the data. Finally, gradient ascent can be applied optimizing the model parameters.

### 2.4.1 Graph Reinforcement

The first class of methods we consider are Graph Reinforcement methods. These methods use representation based learning techniques to to enhance the graph by adding valuable edges or reduce the noise by removing noisy connections. This is usually by training a model on a link-prediction task. A notable benefit of this approach is that other well known CD methods can be used on the enhanced graph afterwards.

Kang et al. [21] present a CD algorithm agnostic pre-processing method for strengthening community structure of a graph by adding non-existing predicted intra-community edges and deleting existing predicted inter-community edges. Their strategy is to learn topological embedding using a graph representation learning algorithm (node2vec) based on existing link prediction task. The similarity is computed between different node pairs and put into buckets. Then with assumption of *homophily* the buckets with higher value can be considered holding intra-community while buckets with lower inter-community connections. Right buckets are picked from both extremes to create or delete edges. Preemptive CD is done to greedily guide pair-wise similarity computation and avoid a high complexity.

Jia et al. [20] solves issue of detecting overlapping communities by proposing CommunityGAN algorithm which jointly optimizes for node and community representations. First they define a method for efficient motif (in their case clique) sampling from the graph (true/clique, and false/vertex subset). Then, they define a GAN based structure for learning representational vectors where the generator $G$ tries to learn $p_{true}(m|\mathbf{v}_c)$ as preference distribution of motifs to generate most likely vertex subsets most likely to be real motifs. Discriminator $D$ tries to learn probability of a vertex subset being a real motif, therefore creating a minimax game of progressively optimizing embeddings to be able to encode rich information about network topology.

Both components ($G$ and $D$) are implemented as a modified the relaxed AGM model with a to a more general definition be able to handle the motif generation (rather than edge generation). The probability of a set of vertices being a motif is defined in terms of their probability being a motif through a community, therefore making them community-aware as they now represent the affiliation weight between a vertex and a community. Number of communities are chosen by training and testing part of data on link prediction task.

### 2.4.2 Multi-objective optimization

Another subject where representation based approaches excel is multi-objective optimization. Usually a combined objective is defined in terms of a community quality, temporal consistency or homophily measure. These measures in turn use the proximity between the representation to be able to back-propagate the combined error and optimize the representation(function) directly.

In Rozemberczki et al. [42] authors propose a method which learns cluster centers along with node embeddings. They define objective function as a combination of three terms: normalization term (ensures embeddings are centered at the origin), proximity term (forces nodes with similar neighborhoods to be embedded close), cluster quality term (forces nodes to be close to their nearest cluster). Additionally, a "social network cost" or *homophily* term is added as a regularizer to optimize for proximity between nodes within the same cluster. During training the clustering coefficient is annealed to ensure convergence and negative sampling is employed to avoid large softmax cost.

Yang et al. [49] propose a similar idea of combining embedding and clustering tasks and solving them in an end-to-end manner. In their work they employ an Deep Denoise Autoencoder (DAE) to learn topological information of the network by optimizing for reconstruction loss. To learn cluster/community centers they define their own GRACE cluster module which first computes soft cluster assignment matrix $Q$ by utilizing the embeddings and cluster centers which contains probabilities $q_{ik}$ of node $i$ belonging to cluster $k$. The clustering loss is defined as KL-divergence between the soft clustering $Q$ and auxiliary target distribution $P$ which is defined by squaring and normalizing the soft-assignments to reinforce more confident clustering results while preventing formation of too large clusters. Both embeddings and clustering are optimized alternatively until convergence.

Ma et al. [30] proposed a novel approach to constructing community-aware dynamic network embeddings by leveraging multi-objective optimization and extending it into a temporal dimension. They a adopt a Graph Autoencoder structure which works by encoding the full graph into a lower-dimensional structure and decoding it again into a graph. Assuming a well tuned network, this allows authors to encode the network (and its nodes) into more efficient representation vectors which characterize the network well

The objective function they use is defined by three terms: the reconstruction error term minimizing the distance between the ground-truth and the autoencoder output, local structure/homophily preservation term minimizing first- and second-order proximity between connected nodes, and the community evolution preservation term maximizing temporal smoothness of communities at different granularity levels given their representation as aggregation of their members.

The inital community assignment is generated using Louvain method for high level communities and using k-means for fine grained communities given a max community size parameter $w$. After that, embeddings at each snapshot are optimized by employing dependent community detection like strategy.

Wang et al. [47] employ a similar to DCD detection by utilizing the Graph Autoencoder architecture. As an addition authors add an additional community score term to the objective function also minimizing the distance between nodes in the same community. At last K-means is run on the representational vectors to detect communities at different timesteps while reusing the outputs from the previous step.

### 2.4.3   Multi-modal community detection

In Fani et al. [10] the authors describe their method to identifying user communities through multi-modal feature learning. First user embeddings are learned based on their temporal content similarity by looking topics of interest. Per user a heat map is constructed measuring user's interest over time and topic axes. By considering users like-minded if their heat maps overlap enough they train low-dimensional content embeddings spanning this user similarity space. Next, they use random walk based GNN methods to learn topological similarity embeddings for network nodes. Finally, they modify the graph by setting edge weights proportionally to node proximity in this combined embeddings space. After that, Louvain method is applied to extract these time and content aware communities.

## 2.5   Evaluation

As described in the previous sections, the definition for both community and dynamic community may be quite ambiguous. In this section we will cover how detection and tracking results can be evaluated in a lesser ambiguous setting to compare various approaches. To disambiguate the process a little, during evaluation, the resemblance/detection and matching/tracking tasks are evaluated separately.

### 2.5.1   Annotated

Evaluation of detected (dynamic) communities becomes much easier when the *ground truth communities* are provided. The evaluation is then done by comparing the difference between the produced communities and the effective ones. To perform this comparison, information theory based metric Normalized Mutual Information (NMI) is used which converts community sets to bit-strings and quantifies the "amount of information" can be obtained about one community by observing the other [28].

A possible drawback of this measure is that its complexity is quadratic in terms of identified communities. In [41] alternative measure (NF1) with linear complexity is introduced which similarly to F1 score uses the trade-off between precision and recall (of the average of harmonic means) of the matched communities. In the follow-up work [39] the authors describe a way to apply this measure within the context of DCD by calculating this score for all the snapshots and aggregating the results into one single measure.

In real-world there are usually no ground truth communities. Therefore this approach is usually applied on synthetic datasets where the communities and their dynamicity is sampled from a distribution. Alternative approach some papers take is by defining ground truth communities using the metadata and node attributes present within the datasets. Some datasets may include annotated communities, but this is not common within DCD datasets.

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A possible drawback of this measure is that its complexity is quadratic in terms of identified communities. In [41] alternative measure (NF1) with linear complexity is introduced which similarly to F1 score uses the trade-off between precision and recall (of the average of harmonic means) of the matched communities. In the follow-up work [39] the authors describe a way to apply this measure within the context of DCD by calculating this score for all the snapshots and aggregating the results into one single measure.

In real-world there are usually no ground truth communities. Therefore this approach is usually applied on synthetic datasets where the communities and their dynamicity is sampled from a distribution. Alternative approach some papers take is by defining ground truth communities using the metadata and node attributes present within the datasets. Some datasets may include annotated communities, but this is not common within DCD datasets.

### 2.5.3 Task specific

In [36] the authors criticize these evaluation approaches by proving that they introduce severe theoretical and practical problems. For one, they prove the no free lunch theorem for CD, ie. they prove that algorithmic biases that improve performance on one class of networks must reduce performance on others. Therefore, there can be no algorithm that is optimal for all possible community detection tasks, as quality of communities may differ by the optimized metrics. Additionally, they demonstrate that when a CD algorithm fails, the poor performance is indistinguishable from any of the three alternative possibilities: (i) the metadata is irrelevant to the network structure, (ii) the metadata and communities capture different aspects of network structure, (iii) the network itself lacks structure. Therefore, which community is optimal should depend on it's subsequent use cases and not a single measure.

## 2.6 Datasets

### 2.6.1 Synthetic Datasets

| Paper | Description |
| --- | --- |
| Lancichinetti et al. [27] | Static networks (widely used) |
| Greene et al. [14] | Generate Graphs based on Modularity measure |
| Granell et al. [13] | |
| Hamilton et al. [18] | Generate Time dependent Heterogeneous graphs using modularity optimization and multi-dependency sampling |
| SYN - Ghalebi et al. [11] | |
| SBM - Lancichinetti and Fortunato [26] | extracted from the dynamic Stochastic Block Model |

### 2.6.2 Real World Datasets

| Dataset | Description |
| --- | --- |
| Enron | Includes: Persons, Email Categories, Sentiment, Email Content |
| KIT (dead) | |

| Dataset | Description |
| --- | --- |
| Weibo | Includes: Persons, Tweets, Followers; **Excludes: Tweet Content** |
| Digg | Includes: Persons, Stores, Followers, Votes; **Excludes: Content** |
| Slashdot | Includes: Persons, Votes; **Excludes: Content** |
| IMDB | Actor movie network; Content is implicitly defined |
| WIKI-RFA | Wikipedia Adminitrator Election; Network of Voters and Votees. Links are votes and vote comments |
| FB-wosn | User friendship links and User posts on users walls; **Excludes: Content** |
| TweetUM (dead) | Twitter Tweets, User Profiles and Followers; Includes: Content |
| Reddit Pushift | User Submissions and Posts on Subreddits; With timestamps |
| Bitcoin Trust Network | Network Nodes and peer Ratings; With timestamps |
| LastFM1k | User - Song Listen histories; With timestamps |
| MovieLens25M | Users and Movie Ratings; With timestamps |
| Memetracker | |
| Rumor Detection | Rumor Detection over Varying Time Windows; Twitter data; With timestamps |

## 3   RESEARCH QUESTIONS

## 4   APPROACH

## PLANNING

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