Clumppling Manual V.0.1.0 (Beta Version)

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1 Introduction

Clumppling is a new method proposed for aligning multiple clustering replicates of population structure analysis. Comparing to exiting methods like Clumpp [3], Clumpak [4] and Pont [1], it provides a better tradeoff between alignment quality and computational efficiency, as well as new functionalities that are not available in those methods.

2 Quick Start

If you are familiar with Python and command line tools, then simply follow the steps given in this section to get a quick start on using *Clumppling*. If you are not familiar with these, do not worry. Detailed instructions are provided in the following sections.

- 1. Have Python 3 installed on your system (if not yet). Make sure it is callable via python from the command-line shell. You may check this by python --version to see if the expected Python 3 version is being used.
- 2. (Otional, but highly recommended) Install conda and create a virtual environment

```
conda create -n clumppling-env python conda activate clumppling-env
```

- 3. Install the package in one of the two following ways:
 - (a) Download the package files from https://github.com/PopGenClustering/Clumppling, then navigate to its home directory "Clumppling", and run the command

```
pip install -e .
```

(b) Directly install the package by

```
pip install git+https://github.com/PopGenClustering/Clumppling
```

then download the example files and scripts from https://github.com/PopGenClustering/Clumppling/tree/master/input and https://github.com/PopGenClustering/Clumppling/tree/master/scripts.

You should see all the dependencies of the program being installed.

4. Run the program with default parameters via the command

```
python -m clumppling -i INPUT_PATH -o OUTPUT_PATH -f INPUT_FORMAT
```

where INPUT_PATH is the directory of all input files (clustering results), <code>OUTPUT_PATH</code> is a directory that does not exist and will be created to save the output files, and <code>INPUT_FORMAT</code> is the format of input, chosen from <code>structure</code>, <code>admixture</code>, <code>fastStructure</code> and <code>generalQ</code>.

The output of the program will be saved in the specified directory.

5. To see the usage of the program with a list of all required and optional parameters, run

```
python -m clumppling -h
```

3 Download and Installation

3.1 Install Python 3

Clumppling is based on Python 3, so you first need to have Python 3 installed on your system.

Python 3 Version Python version of at least 3.8 is recommended. The original package is written under Python 3.8, and has been tested under Python 3.9, Python 3.10, and Python 3.11.

Linux Linux users can install Python 3 from the command window using the package manager. Make sure you have the root user access for the installation.

For RHEL (Red Hat Enterprise Linux) and CentOS users, you can install via

```
sudo yum install -y python3
```

For Ubuntu and Debian users, use

```
sudo apt-get install python3
```

MacOS and Windows MacOS and Windows users can download Python 3 from https://www.python.org/downloads/. Follow the links and get the corresponding installer for your system, then double-click on the installer file and follow the instructions to install Python 3.

3.2 Check Python Command

If you already have Python installed on your machine, you may run the following command in the command-line shell to check the current Python installations.

```
which python # or: which python3
```

On some systems with both Python 2 and Python 3 installed, command python starts the interactive Python 2 interpreter and python3 starts the interactive Python 3. However, for convenience, we will only be using python prompt for the rest of the manual.

If your system uses Python 3, you can either switch all python commands in this manual to python3 and switch all pip commands to pip3, or set the alias by running

```
alias python=python3
```

You can check the version of your Python via the command

```
python --version
```

Now you should be able to open a Python interpreter by typing

```
python -i
```

You will see information about the current Python version and some prompts, and your cursor should appear after >>>. To exit the interpreter, type the exit() after >>>.

*Note that there may be issues when using certain shells on Windows, like GitBash. The solution is to run winpty python -i instead, or to set the alias by python=winpty.

3.3 [Highly Recommended] Install Conda and Create Virtual Environment

We recommend creating a virtual environment using **Conda**, which will help manage separate package installations for different projects.

3.3.1 Install conda

You can download the installer for Anaconda at https://www.anaconda.com/download then follow the instruction to install it.

Alternatively, you may use Miniconda (https://docs.conda.io/en/latest/miniconda).

3.3.2 Create a virtual environment

Here we show how to use conda to manage the virtual environment.

Before getting started, make sure you have the Anaconda Python distribution installed and accessible. You may check this by

```
conda -V
```

To see a list of all of your environments, run

```
conda info --envs
```

Next, conda create -n yourenvname python=x.x anaconda

You may refer to the official document (https://conda.io/projects/conda/en/latest/user-guide/tasks/manage-environments.html) for more information on the environment management with conda. In brief, you can create a virtual environment named clumppling-env with Python by

```
conda create -n clumppling-env python
```

Press y to proceed when prompted. You may use your preferred name instead of clumppling-env for the virtual environment. You may also specify a Python version by the python=3.8.

To activate the environment, run

```
conda activate clumppling-env # for conda 4.6 and later versions
source activate clumppling-env # for conda versions prior to 4.6
```

If you are prompted to run conda init, follow the instructions.

All the installation and program running should happen in this virtual environment. Once you are done using the program, deactivate the environment.

To deactivate the environment, run

```
conda deactivate
```

To remove the environment permanently, run

```
conda remove -n clumppling-env --all
```

3.4 Install Clumppling

There are two ways to install the package.

The first is to install the package from the GitHub repository directly, then download the example files and scripts if you want to try the demo in Section 7.

The second is to download all package files to the local from GitHub, then install the package locally.

3.4.1 Install directly

Install To install *Clumppling* directly, run:

```
pip install git+https://github.com/PopGenClustering/Clumppling
```

Download Because direct installation would not automatically download the example files and scripts, you will need to get them separately from the folder "input" and "scripts" under https://github.com/PopGenClustering/Clumppling.

3.4.2 Install after downloading

You can also install the package after downloading the files to local.

Download Download the entire directory by clicking the link https://github.com/PopGenClustering/Clumppling/archive/refs/heads/master.zip. Unzipping the zipped file on your local machine, you should see a folder named "Clumppling-master", which contains the "README.md" file. Rename this directory "Clumppling". Note that this renaming step is recommended for the sake of notation consistency across this manual.

Alternatively, you may clone the package files from GitHub using Git. To install Git, download the installer and follow the instructions from https://git-scm.com/downloads. Next, navigate to the local directory you would like to put the files. You can then clone the repository by

```
git clone https://github.com/PopGenClustering/Clumppling.git
```

Under your current directory, a folder named "Clumppling" will show up, which contains all the files of the package.

Install Next, navigate to the directory named "Clumppling" where you see the files including "README.md" and "pyproject.toml". The package can be installed by

```
pip install -e .
```

After the pip install command, on your console, you will see the text ending with "successfully installed" followed by a list of packages that are newly installed, including clumppling-0.1.0, indicating that your installation has succeeded. If are any compatibility issues, please resolve them first and then retry the installation.

3.5 Check usage

You should have installed the package now. If you're not sure where the package is installed, you can run

```
pip show clumppling
```

This will show you the installation location as well as basic information about the package.

To check the success of the installation, you may run the following command to see the help message for the main module clumppling:

```
python -m clumppling -h
```

If the package has been installed successfully, you will see the following output in your command window

```
usage: __main__.py [-h] -i INPUT_PATH -o OUTPUT_PATH -f INPUT_FORMAT [-v VIS
   [--cd_param CD_PARAM]
                   [--use_rep USE_REP] [--merge_cls MERGE_CLS] [--cd_default
                       CD_DEFAULT] [--plot_modes PLOT_MODES]
                   [--plot_modes_withinK PLOT_MODES_WITHINK] [--
                      plot_major_modes PLOT_MAJOR_MODES]
                   [--plot_all_modes PLOT_ALL_MODES] [--custom_cmap
                      CUSTOM_CMAP]
required arguments:
 -i INPUT_PATH, --input_path INPUT_PATH
                        path to load input files
  -o OUTPUT_PATH, --output_path OUTPUT_PATH
                        path to save output files
 -f INPUT_FORMAT, --input_format INPUT_FORMAT
                        input data format
optional arguments:
 -v VIS, --vis VIS
                       whether to generate visualization: 0 for no, 1 for
     yes (default)
```

```
--cd_param CD_PARAM the parameter for community detection method (
   default 1.0)
--use_rep USE_REP
                   whether to use representative replicate as mode
   consensus: 0 for no (default), 1 for yes
--merge_cls MERGE_CLS
                      whether to merge all pairs of clusters to align K+1
                         and K: O for no (default), 1 for yes
--cd_default CD_DEFAULT
                      whether to use default community detection method (
                         Louvain): 0 for no, 1 for yes (default)
--plot_modes PLOT_MODES
                      whether to display aligned modes in structure plots
                         over a multipartite graph: 0 for no, 1 for
                      yes (default)
--plot_modes_withinK PLOT_MODES_WITHINK
                      whether to display modes for each K in structure
                         plots: 0 for no (default), 1 for yes
--plot_major_modes PLOT_MAJOR_MODES
                      whether to display all major modes in a series of
                         structure plots: 0 for no (default), 1 for
                      ves
--plot_all_modes PLOT_ALL_MODES
                      whether to display all aligned modes in a series of
                         structure plots: 0 for no (default), 1 for
--custom_cmap CUSTOM_CMAP
                      customized colormap as a comma-separated string of
                         hex codes for colors: if empty (default),
                      using the default colormap, otherwise use the user-
                         specified colormap
```

4 Running Clumppling

The main module of the package runs the alignment algorithm on clustering outputs of the same model on the same set of individuals, namely, it runs the alignment on different membership matrices $Q: N \times K$ with the same number of rows N, but not necessarily the same number of columns K. This function takes in three required arguments and several optional ones:

- input_path (-i, required): path to the folder that contains the input files, i.e. the clustering results
- output_path (-o, required): path to a folder that the user wants to save the alignment results to, where the folder must not exist yet
- input_format (-f, required): the input data format, chosen from structure, fastStructure, admixture, and generalQ.
- vis (-v, optional): whether to generate visualization: 0 for no, 1 for yes (default)
- cd_param (optional): a numerical value of the resolution parameter for the community detection Louvain algorithm (default 1.0)
- use_rep (optional): whether to use representative replicate as mode consensus: 0 for no (default), 1 for yes
- merge_cls (optional): whether to merge all pairs of clusters to align K+1 and K: 0 for no (default), 1 for yes
- cd_default (optional): whether to use the default Louvain algorithm for community detection: 0 for no, 1 for yes (default). If no, then extra steps need to be taken to add a custom community detection function in the source code (see Section 9).

- plot_modes, plot_modes_withinK, plot_major_modes, and plot_all_modes (optional): whether to generate corresponding visualizations of the results: 0 for no, 1 for yes. If yes, the corresponding figure(s) will be generated.
 - plot_modes (default 1): all aligned modes in structure plots over a multipartite graph, where better alignment between the modes is indicated by the darker color of the edges connecting their structure plots, and the cost of optimal alignment is labeled on each edge.
 - plot_modes_withink (default 0): A set of figures, one for each number of clusters, with all modes with the same number of clusters in structure plots in one figure.
 - plot_major_modes (default 0): the major modes of each K aligned in a series of structure plots.
 - plot_all_modes (default 0) all aligned modes in a series of structure plots.
- custom_cmap (optional): a string that is either empty (default "") or contains a list of colors to be used for a customized colormap. If the string is empty then the default colormap will be used. The customized colormap, if provided, should be a list of colors in hex code in a comma-delimited string. An example colormap with five colors looks like "#FF0000, #FFFF00, #00EAFF #AA00FF, #FF7F00". If the provided colormap does not have enough colors for all clusters, colors will be cycled.

The default function can be called by python -m clumppling followed by the arguments. You can provide arguments in either of the following ways:

```
python -m clumppling -i INPUT_PATH -o OUTPUT_PATH -f INPUT_FORMAT

or
```

```
python -m clumppling --input_path INPUT_PATH --output_path OUTPUT_PATH --
input_format INPUT_FORMAT
```

or

```
python -m clumppling --input_path="INPUT_PATH" --output_path="OUTPUT_PATH"
    --input_format="INPUT_FORMAT"
```

where the INPUT_PATH, OUTPUT_PATH, and INPUT_FORMAT denote the user-specific arguments. You may also use a backslash at the end of a line for a line break:

```
python -m clumppling \
-i INPUT_PATH \
-o OUTPUT_PATH \
-f INPUT_FORMAT
```

Details about different input data formats supported by Clumppling are described in Section 5.

5 Input Data Format

The alignment function clumppling supports various input formats. It can be used with the alignment of the outputs of widely-used popular population structure inference methods, *Structure*, *fastStructure*, and *Admixture*, as well as the general output of any mixed-membership clustering method stored as membership matrices.

5.1 Clustering From Structure

To specify the input format as Structure results files, you need to use the following argument for the function clumppling

```
--input_format structure # or -i structure
```

The input_path should point to the "Results" folder that stores the output files of *Structure*. This folder should be automatically generated when you run a *Structure* job. For instance, when you run *Structure* on a project with parameter set named xxx for 100 runs, this folder will contain files with names xxx_run_1_f to xxx_run_100_f. This input format is also the one we use for the demonstration in this manual.

5.2 Clustering From Admixture

To specify the input format as *Admixture* results files, you need to use the following argument for the function clumppling

```
--input_format admixture
```

The input_path should point to the a folder that stores the output files of Admixture, namely, those ending with "K.Q", where K is the number of clusters, or those ending with ".indivq" (where additional individual information is available). These files store the ancestry fractions, as in membership matrices. It is fine to leave other files, if any, in the same folder. The program will ignore all files not with the corresponding extension. I.e., if there are 50 ".Q" files, then Clumpplinq will attempt to align these 50 runs of the clustering.

5.3 Clustering From fastStructure

To specify the input format as fastStructure results files, you need to use the following argument for the function clumppling

```
--input_format fastStructure
```

The input_path should point to the folder that stores the output files of fastStructure. Specifically, this folder needs to contain the output ".K.meanQ" files, where K is the number of clusters for the run. The ".meanQ" contain the posterior mean of admixture proportions. If the folder contains other files, like ".meanP", ".varP", and ".varQ", the program will simply ignore them, so there is no need to filter those files out after running fastStructure. You simply need to use the output directory of fastStructure as the input_path for Clumppling.

5.4 General Membership Matrices From Any Clustering

Clumppling also accepts input as general membership matrices, regardless of the clustering methods used for generating them. To specify such input format, which we term "general Q matrices", you need to use the following argument for the function clumppling

```
--input_format generalQ
```

The file format in the folder that $input_path$ is pointing to should be the same as that for the input data coming from Admixture output, the Q files. The files should end with ".Q". There is no need to include K in the file name, as the program will automatically detect the number of clusters when loading the clustering results. Each ".Q" file should contain the space-delimited membership matrix of a run. For instance, if there are 100 individuals clustered into 4 ancestries, then each row should contain 4 values, separated by space and summing up to 1, which correspond to the membership coefficients of an individual, and there should be 100 rows in the file.

6 Output Files

The main function clumppling generates outputs in a folder specified by output_path and zips them into a zip file "OUTPUT_PATH.zip". The folder shall include six subfolders and an output file "output.log". An "output.log" file contains all the output to the console when running *Clumppling*, which also documents the run time. The contents of the six subfolders are described in detail in the following subsections.

Alignment pattern. In the output files, the optimal alignment between a pair of replicates (or modes) is recorded as a space-separated group of numbers. For instance, if Replicate 1 and Replicate 2, each with five clusters, have the alignment pattern 4 2 1 5 3, the five clusters in Replicate 2 should be matched to clusters 4, 2, 1, 5, and 3 in Replicate 1, respectively. The number of clusters in Replicate 2 will always be no less than that in Replicate 1. Because multiple clusters in Replicate 2 may be matched to the same cluster in Replicate 1,

6.1 The "input" folder

The "input" folder contains the following files:

- ".Q" files of membership matrices which are the input clustering results loaded and processed by *Clumppling*. The naming of the ".Q" files, which are the labels of the replicates used by *Clumppling*, follows the pattern of "1_K5R2.Q", where 1 is the index of the clustering results used in by *Clumppling*, 5 is the number of clusters, and 2 is the index of this replicate in all replicates with this number of cluster.
- A comma-delimited "input_files.txt" file with two fields. The first field is the name of processed ".Q" files and the second field is the corresponding name of the original input file.
- A "ind_info.txt" file if the input data format provides population labeling of the individuals. It contains auxiliary information on the individuals like identification label and population, where the order of the individuals is the same as that in the membership matrices.

6.2 The "alignment_withinK" folder

The "alignment_withinK" folder stores the results of all pairwise alignment of replicates with the same number of clusters. It contains one comma-delimited text file for each K value in the input. Each file contains three fields: three fields: Replicate1-Replicate2, Cost, and Alignment. Replicate1-Replicate2 records the labels of the two replicates. Cost records the cost of optimal alignment between the two replicates. Alignment records the optimal alignment pattern between the two replicates in a space-separated group of numbers. Each line in the file, except for the header, corresponds to the alignment results of a pair of replicates with the specified number of clusters.

For example, the following line

```
151_K5R1-152_K5R2,0.01769820597265037,4 2 1 5 3
```

records the alignment results between replicate 151_K5R1 and replicate 152_K5R2. The optimal alignment pattern between them is 4 2 1 5 3, and under this optimal alignment, the cost between the aligned replicates is 0.01769820597265037.

6.3 The "modes" folder

The "modes" folder contains the following files:

- ".Q" files of the consensus membership matrices of all modes detected. The naming of the ".Q" files, which are the labels of the modes used by *Clumppling*, follows the pattern of "K5M1_avg.Q", where 5 is the number of clusters, 1 is the index of this mode in all modes with this number of cluster, and mean stands for using the mean memberships as the consensus of mode. An alternative is rep, which tells the program to use the representative replicate as the consensus of mode.
- A comma-delimited "mode_alignments.txt" file with four fields: Mode, Representative, Replicate, and Alignment. A line in the file looks like this:

```
K5M1,152_K5R2,151_K5R1,3 2 5 1 4
```

Mode records the label of the mode, e.g., K5M1. Representative records the label of the representative replicate of the mode, e.g., 152_K5R2. Replicate records the label of the focal replicate, e.g., 152_K5R1. Alignment records the space-separated alignment pattern between the representative and the focal replicates.

- A comma-delimited "mode_stats.txt" file with five fields: Mode, Representative, Size, Cost, and Performance. Mode and Representative are the same as in "mode_alignments.txt". Size, Cost, and Performance record the size (number of clusters) of the mode, the averaged cost of the alignment between all pairs of clusters in the mode, and the averaged performance measure, calculated as the H' similarity, of all the pairwise alignments in the mode. A lower cost and a higher performance value indicate a better alignment quality for the mode detected.
- A comma-delimited "mode_average_stats.txt" file with five fields: K, Size, NS-Size, Cost, and Performance. K is the number of clusters. Size is the total number of replicates. NS-Size is the number of replicates not belonging to singleton modes (i.e., modes with only one replicate). Cost is the weighted average of the cost of all modes not including the singletons, weighted by the mode size. Performance is the weighted average of the performance measure (H' similarity) of all modes not including the singletons, weighted by the mode size.

6.4 The "alignment_across_K" folder

The "alignment_across_K" folder contains two files for each type of consensus membership of the mode, specified by the suffixes "_avg" and "_rep".

- A comma-delimited "alignment_acrossK.txt" file with three fields: Mode1-Mode2, Cost, and Alignment. Each line in the file, except for the header, corresponds to the alignment results of a pair of modes. Mode1-Mode2 records the labels of the two modes, where the second mode has a number of clusters no less than the first mode. Cost records the cost of optimal alignment between the two modes. Alignment records the optimal alignment pattern between the two modes in a space-separated group of numbers.
- A comma-delimited "best_pairs_acrossK.txt" file with five fields: Best Pair, Cost, Alignment, Separate-Cluster Cost, and Separate-Cluster Alignment. Best Pair is the best pair of modes between adjacent K in terms of the alignment performance, e.g., K4M1-K5M1. Cost and Performance record the cost and performance measure of optimal alignment between this pair of modes by merging the clusters in Mode 2 that get matched to the same cluster in Mode 1 and comparing two membership matrices of the same size after the merging. Separate-Cluster Cost and Separate-Cluster Performance record the cost and performance measurement that are calculated by comparing each pair of clusters that are matched and summing over the value for all clusters. For two or more clusters from Mode 2 that are matched to the same cluster in Mode 1, the average cost and performance of them are considered.

6.5 The "modes_aligned" folder

The "modes_aligned" folder contains the following files:

- ".Q" files of the consensus membership matrices of all modes that are aligned across different numbers of clusters. The best pair of modes for each pair of adjacent K values are used as anchors. The rest of the modes with the same K are aligned to the anchor according to results in "mode_alignments.txt" (in the "modes" folder), then the anchors are aligned according to results in the "alignment_across_K" folder. The naming of the ".Q" files follows the pattern of "K5M1_aligned_avg.Q", where the suffix "_avg" denotes the type of consensus membership used.
- A comma-delimited "all_modes_alignment.txt" file for each type of consensus membership of the mode specified by the suffixes "_avg" and "_rep". A line in the file looks like this

```
K5M1:4 3 2 1 5
```

where before the colon is the mode, and after the colon is the permutation pattern that is used to generate the aligned mode in "modes_aligned" from the unaligned ones in the "modes" folder.

6.6 The "visualization" folder

The "visualization" folder contains all the output figures if the corresponding parameters are set to T.

- "colorbar.png" is the colorbar showing the colormap used in visualization, where each color represents a distinct cluster, indexed from 1 to K. The colormap may be specified by the user by setting the custom_cmap parameters.
- "modes_aligned_multipartite_avg.png" and "modes_aligned_multipartite_rep.png" plot the aligned modes over a multi-partite graph picturing the alignment relationships across different K. The modes are plotted in stacked bar plots. Better alignment between the modes is indicated by the darker color of the edges connecting their bar plots, and the cost of optimal alignment is labeled on each edge. These figures will only be generated if the parameter plot_modes is 1.
- "major_modes_aligned_avg.png" and "major_modes_aligned_rep.png" plot the memberships in a series of stacked bar plots for the major modes for all K, ordering from the smallest K to the largest. These figures will only be generated if the parameter plot_major_modes is 1.
- One figure for each K for each type of consensus membership, with the name following "K5_modes_avg.png". The figure plots the memberships in a series of stacked bar plots for all aligned modes of the specific K. These figures will only be generated if the parameter plot_modes_withinK is 1.

• "modes_aligned_avg.png" and "modes_aligned_rep.png" plot the memberships in a series of stacked bar plots for all aligned modes for all K, ordering from the smallest K to the largest and mode indexes from small to large. These figures will only be generated if the parameter plot_modes is 1.

In all the figures, each color represents a cluster, where the colors are specified by the customized colormap if custom_cmap is provided.

7 Examples

To run the demonstrations, make sure that your current directory is the "Clumppling" directory and that the folder with input files is put under "Clumppling/input". If you previously downloaded the data files as a zip file, unzip them to a folder with the same name. You may check your current working directory by running the command pwd.

The commands provided in this section can be used to run the examples. Alternatively, they can be run through the bash scripts which contain all the commands. To run the bash scripts, you need to install Bash on the system if it is not already there. The example bash scripts to run the demonstrations, as well as the default parameter files, are under the directory "Clumppling/scripts".

7.1 Datasets

To demonstrate the usage of this package, we use several published genetic datasets, and run clustering algorithms on those datasets to get the input to our alignment framework.

7.1.1 Human genotype data

The human genotype data contains genotype information of 44 individuals in the admixed population of Cape Verde and selected West African and Western European populations from the HGDP dataset [9]. Admixture was run 50 times independently for each K value from 2 to 5, resulting in a total of 200 clustering replicates. This dataset is used to demonstrate the alignment of Admixture output files.

7.1.2 Chicken microsatellite data

The chicken microsatellite data comprises of 27 microsatellite loci genotyped in 600 individuals from 20 chicken populations [7]. We run Structure [5] on the full set of loci for 20 runs for each K from 17 to 21, then align all the 100 replicates using Clumppling. This dataset is used to demonstrate the alignment of Structure output files.

7.2 Running clumppling on Admixture output files

To run align the clustering outputs on our example dataset from different runs of the program Admixture using the default community detection and visualization settings, you can run the following command

```
python -m clumppling \
--input_path input/capeverde \
--output_path output/capeverde_default \
--input_format admixture
```

Alternatively, you may write the command in a bash script and run the bash script. For example, when you are in the "Clumppling" directory, you can run the same example using the bash script in "run_ex1_default' as follows

```
bash scripts/run_ex1_default.sh
```

This example will generate the following outputs in the console

```
Using default community detection method: True
Community detection parameter: 1.0
Using a representative replicate as the mode consensus: False
Merging all possible pairs of clusters when aligning two replicates with K
  differing by one: False
----- [Plotting] -----
Providing customized colormap: False
Plotting aligned modes on top of a multipartitie graph: True
Plotting modes of the same K: False
Plotting major modes: False
Plotting all modes: False
_____
====== Running Clumppling ======
>>> Processing input data files and checking arguments
Time: 3.247s
>>> Aligning replicates within K and detecting modes
Time: 17.273s
>>> Aligning modes across K
Time: 0.152s
>>> Plotting alignment results
Time: 11.139s
>>> Zipping files
====== Total Time: 32.443s =======
```

The results, including figures and text files, will be saved in the output folder. For instance, the file "modes_stats.txt" under the "modes" folder look like

```
Mode, Representative, Size, Cost, Performance
K2M1, 3_K2R3, 50, 8.043782926676283e-14, 0.9999997631447923
K3M1, 59_K3R9, 50, 3.0678737343358222e-09, 0.9999591847910263
K4M1, 145_K4R45, 39, 0.0007341008438339235, 0.9788891519804838
K4M2, 112_K4R12, 11, 0.04944348952966262, 0.7918294897008602
K5M1, 179_K5R29, 18, 0.03704964921858028, 0.8188413674149748
K5M2, 165_K5R15, 18, 0.050741851309627946, 0.7939365967826061
K5M3, 189_K5R39, 14, 0.02550705761774155, 0.847881111372104
```

7.3 Running clumppling on Structure output files

To run align the clustering outputs on our example dataset from different runs of the program *Structure* using the default community detection and visualization settings, you can run the following command

```
python -m clumppling \
--input_path input/chicken \
--output_path output/chicken_default \
--input_format structure --cd_param=1.05
```

Alternatively, you may write the command in a bash script and run the bash script. For example, when you are in the "Clumppling" directory, you can run the same example using the bash script in "run_ex2_default.sh" as follows

```
bash scripts/run_ex2_default.sh
```

This example will generate the following outputs in the console:

```
Input data format: structure
Output path: output/chicken_default
----- [Methods] -----
Using default community detection method: True
Community detection parameter: 1.05
Using a representative replicate as the mode consensus: False
Merging all possible pairs of clusters when aligning two replicates with K
  differing by one: False
----- [Plotting] -----
Providing customized colormap: False
Plotting aligned modes on top of a multipartitie graph: True
Plotting modes of the same K: False
Plotting major modes: False
Plotting all modes: False
_____
_____
====== Running Clumppling ======
>>> Processing input data files and checking arguments
Time: 3.386s
>>> Aligning replicates within K and detecting modes
Time: 6.609s
>>> Aligning modes across K
Time: 1.055s
>>> Plotting alignment results
Time: 182.411s
>>> Zipping files
====== Total Time: 194.730s ======
```

The results, including figures and text files, will be saved in the output folder. For instance, the first five lines of the file "modes_stats.txt" under the "modes" folder look like

```
Mode, Representative, Size, Cost, Performance
K17M1,1_K17R1,6,0.048931782944444425,0.7918254748602578
K17M2,14_K17R14,5,0.06331773349999999,0.7626459575134236
K17M3,9_K17R9,5,0.12416171116666663,0.6498140751787831
K17M4,2_K17R2,4,0.09807973263888886,0.6932660053254581
```

7.4 Running clumppling on outputs with a non-consecutive number of clusters

To demonstrate Clumppling's ability to align replicates when the number of clusters are not consecutive, we provide an additional example with a subset of runs from Example 2, with K = 17, 19, and 21. The command stays the same, except for the input path, and the corresponding bash script is

```
bash scripts/ex3.sh
```

and the commands in the script are

8 Additional Functionalities

Besides aligning different replicates generated by a clustering model and detecting modes, *Clumppling* provide two extensions to compare memberships of the same individuals generated using different models, and to align memberships of different sets of individuals when they have population labels.

8.1 clumppling.diffModel: aligning memberships of the same individuals from different models

When the memberships are generated using different models, and within each model, there are several replicates with different numbers of clusters K, we may not want to align all replicates and aggregate all into consensus memberships for each K. Instead, we want to obtain the consensus for results generated using each model, then directly compare all the models. Clumppling adds this functionality by first detecting modes for each model, then aligning modes with the same K from different models to the first mode from the first model, where the order of the models can be manipulated by users. In this case, Clumppling provides the function clumppling.diffModel to first perform within-model alignment of the clustering results, then perform across-model alignment, and output intuitive visualizations for a direct comparison of clustering results generated based on different models.

8.1.1 How to run clumppling.diffModel

clumppling.diffModel can be used to call the program to align memberships of the same individuals from different
models. By running the command

```
python -m clumppling.diffModel -h
```

you will get

```
usage: diffModel.py [-h] -i INPUT_PATH -o OUTPUT_PATH [--consensus CONSENSUS
                    [--custom_cmap CUSTOM_CMAP]
required arguments:
 -i INPUT_PATH, --input_path INPUT_PATH
                       path to the input files
  -o OUTPUT_PATH, --output_path OUTPUT_PATH
                        path to the output files
optional arguments:
  --consensus CONSENSUS
                        what to use as mode consensus, either avg (default,
                        for average memeberships) or rep (for representative
                        replicate)
  --custom_cmap CUSTOM_CMAP
                        customized colormap as a comma-separated string of
                        codes for colors: if empty (default), using the
                        default colormap, otherwise use the user-specified
                        colorm
```

This function takes in two required arguments and two optional arguments:

- input_path (-i, required): path to the parent folder that contains the alignment results of each model
- output_path (-o, required): path to the folder that the user wants to save the results of alignment
- consensus (optional, default: "avg"): Either "avg" or "rep", indicating which consensus membership of the modes is to be used for the alignment. "avg": average memberships of replicates in the mode. "rep": a representative replicate from the mode.

• custom_cmap (optional, default: the empty string""): The customized colormap, which should be a list of colors in hex code in a comma-delimited string. If the string is empty then the default colormap will be used. An example colormap with five colors looks like "#FF0000 #FFFF00 #00EAFF #AA00FF #FF7F00". If the provided colormap does not have enough colors for all clusters, colors will be cycled.

The default function can be called by

```
python -m clumppling.diffInd \
--input_path PARENT_DIRECTORY_OF_ALIGNMENT_RESULTS \
--output_path OUTPUT_PATH
```

8.1.2 Outputs

The function clumppling.diffModel generates outputs in a folder specified by output_path containing three files and zips them into a zip file "OUTPUT_PATH.zip". Besides the inputs to clumppling.diffModel that come from the results of clumppling, the folder contains four files:

- 1. An "output.log" file with all the output to the command window when running clumppling.diffModel. It documents the run time.
- 2. A comma-delimited "multiple_inputs.txt" file with two fields. The first field is the index and the second field is the corresponding name of the input (model), where the inputs are the alignment results from clumppling. The name of the input needs to be the same as the name for the output directory of clumppling.
- 3. A comma-delimited "multiple_alignment.txt" file with five fields: K, input1_index, input2_index, optimal_obj, and alignment. K is the number of clusters. input1_index and input2_index are the indices of two inputs (models). optimal_obj and alignment are the objective of the ILP and the pattern of the optimal alignment that is identified via ILP between the first modes ("M1") of the specified K for the two inputs. For instance, a line

```
5,1,2,0.44606332580777075,4 3 1 5 2
```

means that K5M1 of the first input and K5M1 of the second input are optimally aligned by the pattern 4 3 1 5 2 with an objective of 0.44606332580777075.

4. A figure "aligned_all.png" plotting the modes of different models side by side. The models are aligned by the first mode of each model, and ordered from left to right in the same way that their results are in the parent directory specified by input_path. The modes are ordered from smallest K to largest K from top to bottom.

8.1.3 Example

Dataset An HGDP (human genome diversity cell line panel) human microsatellite dataset is used to demonstrate the alignment of replicates obtained from different clustering models

This first HGDP dataset, analyzed in [2], contains a sample of 978 individuals each genotyped at 791 microsatellite (STR) loci, including 13 CODIS loci. This is used to demonstrate the use of the diffModel method.

Recall that by "different models", we follow the definition in [4] to denote the scenarios where clustering results are obtained from different programs, different model choices, or different subsets of genetic markers across the same data set. We run Structure on the first HGDP dataset using two different models: one based on all 791 loci, and one based on 13 CODIS loci. We run Structure 10 times for each K from 2 to 6 using each model, using a burn-in period of 10,000 steps followed by 10,000 iterations.

Commands The following example aligns memberships of the same individuals from running *Structure* on the full set of 791 loci and a selected set of 13 CODIS loci in the first HGDP dataset.

```
python -m clumppling \
-i input/diffModel/791loci \
-o output/diffModel/791loci \
-f structure --cd_default 0
python -m clumppling \
```

```
-i input/diffModel/13loci \
-o output/diffModel/13loci \
-f structure --cd_default 0
python -m clumppling.diffModel \
-i output/diffmodel \
-o output/diffmodel
```

Note that the output paths for the two calls of the main function, need to be subfolders of the same directory "output/diffModel", which is the input path for clumppling.diffModel. This example considers the clustering results using only two different models, but *Clumppling* can support the alignment for more than two models, as long as their within-model alignment results are put under the same directory for the input_path of diffModel. Alternatively, you can run the example by

```
bash scripts/ex4.sh
```

Results The alignment results are shown in Figure 1, which is saved in a figure titled "aligned all.png" in the output directory. *Clumppling* first aligns the replicates and detects the modes for each model, then aligns modes between models and shows them side by side.

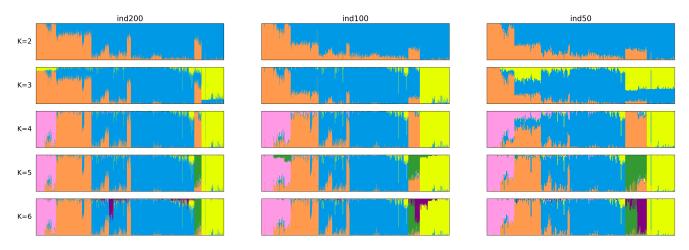


Figure 1: Aligned modes for population structure inferred from models using different loci in HGDP data: (left) the full set of 791 loci and (right) the 13 CODIS loci.

8.2 clumppling.diffInd: aligning memberships of different individuals from (possibly different) models

When the memberships of populations are generated using different set of individuals, for example, subsets of different sample sizes from the same populations, the membership matrices Q will no longer be of the same size. In this case, Clumppling provides the function clumppling.diffInd to perform the alignment based on their population-wise average memberships and compare the alignment results side by side for each set of individuals. Note that the alignment of clustering results from a different set of individuals is only appropriate when the population label, or some other types of labels that encode some grouping information so that individuals with the same label show relative consistency in their membership coefficients inferred, can be assigned to each individual. This is because the alignment across different individual sets relies on calculating population-wise membership coefficients from individual membership coefficients and then aligning the replicates based on the population-wise memberships.

Taking the same notations from the manuscript, we denote the number of modes detected for each K as m_K , and denote the modes as M_K^1 through $M_K^{m_K}$, with $M_K^i \cap M_K^j = \emptyset$ for all $i, j \in [m_k]$. The corresponding consensus memberships are \bar{Q}_K^1 through $\bar{Q}_K^{m_K}$ with size $N \times K$. Suppose a first set of outputs A have modes $\left\{(^AM_K^\ell, ^A\bar{Q}_K^\ell) : \ell \in [m_K]\right\}_{K \in \mathcal{K}}$ where N_A individuals are from populations [PA], and a second set of outputs B have modes $\left\{(^BM_K^\ell, ^B\bar{Q}_K^\ell) : \ell \in [m_K]\right\}_{K \in \mathcal{K}}$ where N_B individuals are from populations [PB]. Then for each K

where these outputs overlap, we select the concensus memberships ${}^A\bar{Q}_K^1$ and ${}^B\bar{Q}_K^1$, and compute the populationwise average memberships as

$${}^{A}\mathcal{Q}_{jk} = \sum_{i \in [j]} {}^{A}\bar{Q}_{ik}^{1} \tag{1}$$

and ${}^B\mathcal{Q}_{jk}$, similarly, for each population $j \in [PA] \cup [PB]$ and each $k \in [K]$. Both population-wise membership matrices ${}^A\mathcal{Q}$ and ${}^B\mathcal{Q}$ have size $|[PA] \cup [PB]| \times K$.

Pairwise alignment between ${}^A\bar{Q}_K^1$ and ${}^B\bar{Q}_K^1$ is then done by ILP using their population-wise average memberships ${}^A\mathcal{Q}$ and ${}^B\mathcal{Q}$ and a modified between-cluster distance weighted by population sizes. That is, the dissimilarity between two clusters is modified to be

$$C'(q_i, p_j) = \sum_{\ell=1}^{|[PA] \bigcup [PB]|} \frac{N_{A,\ell} + N_{B,\ell}}{N_A' + N_B'} |Q_{\ell i} - P_{\ell j}|, \tag{2}$$

where N_A' and N_B' correspond to the total number of individuals in the overlapped populations between A and B, and $N_{A,\ell}$ and $N_{B,\ell}$ correspond to the number of individuals in population ℓ . The rest of the alignment follow the same procedure as in the individual membership alignment. The modes $\{{}^A\bar{Q}_K^\ell\}_{\ell\in[m_K]}$ and $\{{}^B\bar{Q}_K^\ell\}_{\ell\in[m_K]}$ for each K are then aligned based on the optimal alignment between ${}^A\bar{Q}_K^1$ and ${}^B\bar{Q}_K^1$. Clumppling presents the aligned modes based on each set of outputs side by side, with modes of the same K starting at the same row.

8.2.1 How to run clumppling.diffInd

clumppling.diffInd can be used to call the program to align memberships of different individuals. By running the command

```
python -m clumppling.diffInd -h
```

you will get

```
usage: diffInd.py [-h] -i INPUT_PATH -o OUTPUT_PATH [--consensus CONSENSUS]
                  [--custom_cmap CUSTOM_CMAP]
required arguments:
 -i INPUT_PATH, --input_path INPUT_PATH
                       path to the input files
  -o OUTPUT_PATH, --output_path OUTPUT_PATH
                        path to the output files
optional arguments:
  --consensus CONSENSUS
                        what to use as mode consensus, either avg (default,
                        for average memeberships) or rep (for representative
                        replicate)
  --custom_cmap CUSTOM_CMAP
                        customized colormap as a comma-separated string of
                        codes for colors: if empty (default), using the
                        default colormap, otherwise use the user-specified
                        colormap
```

This function takes in two required arguments and two optional arguments:

- input_path (-i, required): path to the parent folder that contains the alignment results of each set of input
- output_path (-o, required): path to the folder that the user wants to save the results of alignment
- consensus (optional, default: "avg"): Either "avg" or "rep", indicating which consensus membership of the modes is to be used for the alignment. "avg": average memberships of replicates in the mode. "rep": a representative replicate from the mode.

• custom_cmap (optional, default: the empty string""): The customized colormap, which should be a list of colors in hex code in a comma-delimited string. If the string is empty then the default colormap will be used. An example colormap with five colors looks like "#FF0000 #FFFF00 #00EAFF #AA00FF #FF7F00". If the provided colormap does not have enough colors for all clusters, colors will be cycled.

The default function can be called by

```
python -m clumppling.diffModel \
--input_path PARENT_DIRECTORY_OF_ALIGNMENT_RESULTS \
--output_path OUTPUT_PATH
```

Note that running clumppling.diffInd requires some labeling information of the individuals, for instance, their populations. If the population label is provided as input to *Structure*, the labeling can be automatically extracted when running clumppling with input_type="structure. If the population label is provided in the ".indivq" files as the outputs of *Admixture*, then it will also be extracted automatically. However, currently *Clumppling* does not support automatic extraction of individual information with other input data format, so a comma-delimited file named "ind_info.txt" needs to be manually added to the "data" directory in the outputs of clumppling with a field "Pop" storing the population label information (more in Section 6). This space-delimited file should have the column names of the individual information data on the first line. There must be a column named "Pop" which contains the population label of the individuals. The individuals must be of the same order as they appear in the clustering membership matrices.

8.2.2 Outputs

The function clumppling.diffInd generates outputs in a folder specified by output_path containing three files and zips them into a zip file "OUTPUT_PATH.zip". Besides the inputs to clumppling.diffInd that come from the results of clumppling, the folder contains four files:

- 1. An "output.log" file with all the output to the command window when running clumppling.diffInd. It documents the run time.
- 2. A comma-delimited "popwise_inputs.txt" file with two fields. The first field is the index and the second field is the corresponding name of the input (set of individuals), where the inputs are the alignment results from clumppling. The name of the input needs to be the same as the name for the output directory of clumppling.
- 3. A comma-delimited "popwise_alignment.txt" file with five fields: K, input1_index, input2_index, optimal_obj, and alignment. K is the number of clusters. input1_index and input2_index are the indices of two inputs (sets of individuals). optimal_obj and alignment are the objective of the ILP and the pattern of the optimal alignment that is identified via ILP between the first modes ("M1") of the specified K for the two inputs. For instance, a line

```
5,2,3,0.013166727300769145,2 1 5 3 4
```

means that K5M1 of the second input and K5M1 of the third input are optimally aligned by the pattern 2 1 5 3 4 with an objective of 0.013166727300769145.

4. A figure "aligned_all.png" plotting the modes of clustering results using different sets of individuals side by side. The different sets are aligned by the first mode of each, and ordered from left to right in the same way that their results are in the parent directory specified by input_path. The modes are ordered from smallest K to largest K from top to bottom.

8.2.3 Example

Dataset A second HGDP dataset is used to demonstrate the alignment of replicates generated on different sets of labeled individuals. The second HGDP dataset, analyzed in [8], contains 377 autosomal microsatellites in 1,056 individuals from 52 populations. This is used to demonstrate the use of the diffInd method.

Using the second HGDP dataset, we follow [6] and subset 50, 100, and 200 individuals from each of the seven regions, resulting in 339, 639 and 1,005 individuals in total, respectively. We then run Structure 5 times for each K from 2 to 6 on each of the three sets of individuals. Again, we use a burn-in period of 10,000 steps and 10,000 iterations.

Commands The following example aligns memberships output by *Structure* on the second HGDP dataset, where a subset of 50, 100, or 200 individuals for each population is sampled to be input into *Structure*.

```
python -m clumppling \
-i input/diffInd/ind200 \
-o output/diffInd/ind200 \
-f structure --cd_default 0
python -m clumppling \
-i input/diffInd/ind100 \
-o output/diffInd/ind100 \
-f structure --cd_default 0
python -m clumppling \
-i input/diffInd/ind50 \
-o output/diffInd/ind50 \
-o output/diffInd/ind50 \
-f structure --cd_default 0
python -m clumppling.diffInd \
-i output/diffInd \
-i output/diffInd
```

Similar to clumppling.diffModel the output paths for the three calls of the main function, all need to be subfolders of the directory "output/diffModel", which is the input path for clumppling.diffInd. This example considers the clustering results using three sets of different individuals, but *Clumppling* can support the alignment for more, as long as their own alignment results are put under the same directory for the input_path of diffInd.

Alternatively, you can run the example by

```
bash scripts/ex5.sh
```

Results The alignment results are shown in Figure 2, which is saved in a figure titled "aligned_all.png" in the output directory. Based on the population-wise memberships, the population structure generated using different sample sizes of data can be aligned and compared intuitively.

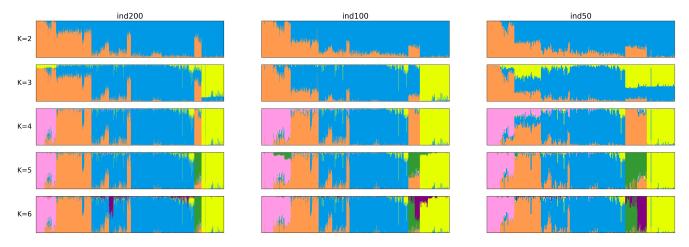


Figure 2: Aligned modes for population structure inferred from subsets of different sample sizes in HGDP data: (left) 200 individuals from each region; (middle) 100 individuals from each region; (right) individuals from each region.

9 Customizable Algorithms

It is not hard to modify *Clumppling* to implement customized algorithms, although this will require the modification of provided Python code files.

If you install the package via downloading the package files, you can find the code files under the "Clumppling' clumppling" folder. If you install the package directly using git, you may locate your package files by

```
pip show clumppling
```

and then navigate to the location shown.

9.1 Custom community detection method

To use a custom community detection method, you need to modify the code file "custom_funcs.py" to implement the customized community detection function cd_custom and change the corresponding parameter in the parameter file. Once you locate the file, make changes to the following function

```
def cd_custom(G):
   """Customized community detection method (need to be modified)
   Parameters
    _____
   G : networkx.Graph
       the similarity network of replicates, with edges weighted by
           similarity after optimal alignment
   Returns
    _____
   partition_map
       a dictionary where keys are the indices of replicates and values are
            the indices of the communities they belong to
   # Please comment out the following line and customize your community
       detection method here.
   partition_map = {i:0 for i in range(G.number_of_nodes())}
   return partition_map
```

The cd_custom function takes in a NetworkX graph object, where nodes are replicates we want to align, and edges between each pair of replicates are negatively weighted by the optimal alignment cost between them. In general, nodes that are more densely connected (having edges with higher weights among them) should belong to the same community, while nodes that are connected by weaker edges (those with lower weights) should belong to different communities. The function should output a Python dictionary object containing the information of partitioning the nodes into communities.

The current function provided contains a dummy line of assigning all nodes (replicates, indexed starting from 0) into one community (mode, labeled 0). You should comment out this dummy line and implement your own community detection method that gives a valid partition map. You may refer to our default Louvain method implemented in the cd_default function in the file "funcs.pv" as an example.

Next, reinstall the program by calling pip install -e . again, then you can run *Clumppling* with your customized community detection method for mode detection by setting the parameter "cd_default" to 0 in input arguments.

9.2 Alternative p-value for testing the existence of community structure

The default p-value threshold used for testing the existence of community structure is p = 0.01. If you want to use a different p-value, you may change one line in the file "funcs.py":

Locate the following line, which is in the function detect_modes() in the function file,

```
has_comm_struc = test_comm_struc(adj_mat, alpha = 0.01)
```

and change the value 0.01 to the specific p-value you want to use.

Next, reinstall the program by calling pip install -e ., then you can run *Clumppling* with your customized community structure test.

If you do not want to download the package and run it locally, we also offer the option to use it online directly via a Google Colaboratory notebook at https://colab.research.google.com/drive/1PiM5pUKm9cx-dCzOYLWwaJcNcTQHyUm8#offline=true&sandboxMode=true.

In order to execute the code, you need to sign in to a Google account. Once you open the notebook, it will automatically create a copy and all the modifications and executions you make will be on this copy. You can also explicitly make a copy of the notebook in Drive.

To run the alignment, you need to prepare a zip file containing all the input files, i.e., the clustering results. Once you have the file ready, simply follow the instructions on the notebook to use *Clumppling*. Click the little round button with an arrowhead on it on the left side of each block to run the block. After clicking through the blocks for installing the package and setting up, upload the input per instruction. Then choose your input data format, set any optional parameters if you want to, and run the program. Once the program finishes running, you can download the output files that are zipped together in one file. You may also choose to view the output figures directly in the notebook by following the instruction.

References

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