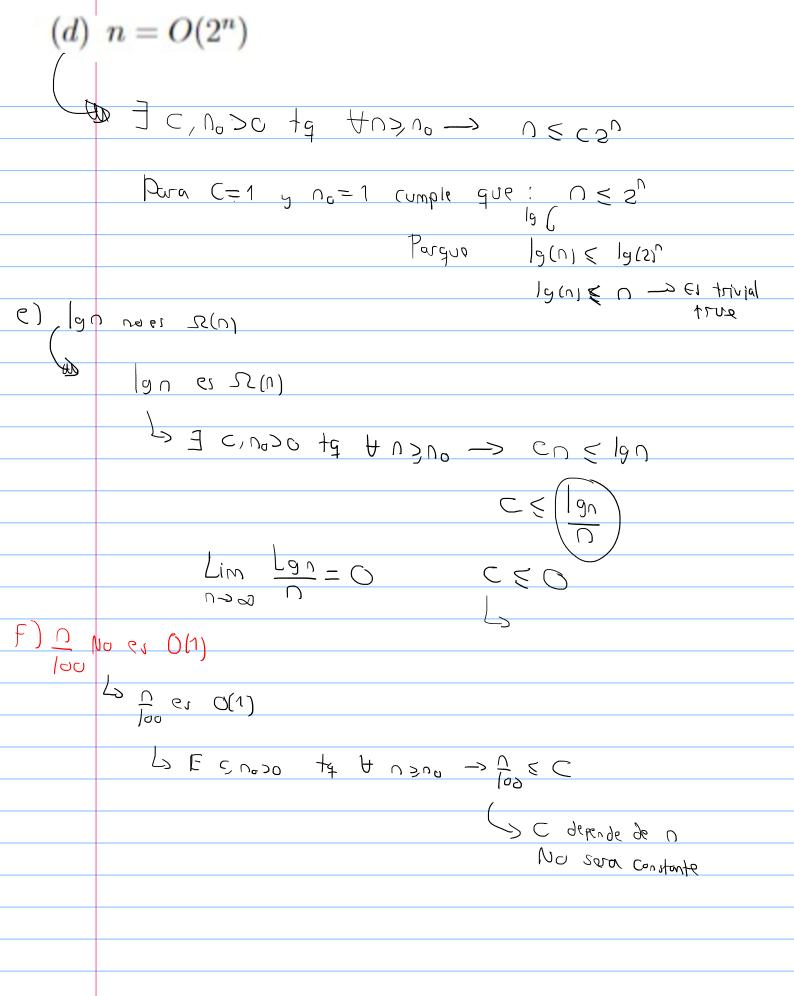
$$\begin{cases} a_{1} \leq a_{1} \leq a_{2} \\ b_{1} \leq b_{2} \end{cases} & b_{1} \leq b_{2} \\ b_{2} \leq b_{2} \leq b_{3} \leq b_{4} \\ b_{3} \leq b_{4} \leq b_{3} \leq b_{4} \\ b_{4} \leq b_{4} \leq b_{4} \leq b_{4} \\ b_{5} \leq b_{5} \leq b_{5} \leq b_{5} \\ b_{5} \leq$$



(h)
$$\frac{1}{3}(n+1)(n-2) - 5 = \Theta(n^2)$$
.

$$\frac{1}{3}(n^2 - n^{-2}) - 5 = \Theta(n^3)$$

$$\frac{1}{3}n^2 - \frac{1}{3}n - \frac{2}{3} - 5 = \Theta(n^3)$$

$$\frac{1}{3}n^2 - \frac{1}{4}n - \frac{13}{3} = \Theta(n^2)$$

$$\frac{1}{3}n^2 - \frac{1}{3}n - \frac{13}{3} = \frac{1}{3}n^2 - \frac{1}{3}n - \frac{1}n - \frac{1$$

(i)
$$n \lg n - \lceil 2n/3 \rceil - \lg n + 4 \operatorname{es} \Omega(2n \lg n)$$

$$C \geq n \lg n \leq n \lg n + 4 \operatorname{es} \Omega(2n \lg n) \qquad + 4 \operatorname{es} \Omega(2n \lg n$$

(j)
$$\lg n! \operatorname{es} \Omega(n \lg n)$$

$$|g \cap | =$$
 $|g \cap + |g(n-1) + |g(n-2) + ... |g(1)$

$$\sum_{\lambda=1}^{n} |g(\lambda)| = \sum_{\lambda=1}^{n} n |g(\lambda)|$$

$$= \int_{\mathcal{I}} \frac{1}{\zeta_{n}} \int_{0}^{\infty} \frac{1}{\zeta_{n$$

$$\frac{1}{2} \sum_{j=1}^{n} \frac{1}{|g(i)|} \leq \sum_{j=1}^{n$$

$$\frac{1}{\sum_{\lambda=\frac{1}{2}+1}^{N}} |g(\lambda)| \leq \frac{1}{\sum_{\lambda=\frac{1}{2}+1}^{N}} |g(\lambda)| \leq \frac{1}{\sum_{\lambda=\frac{1}$$

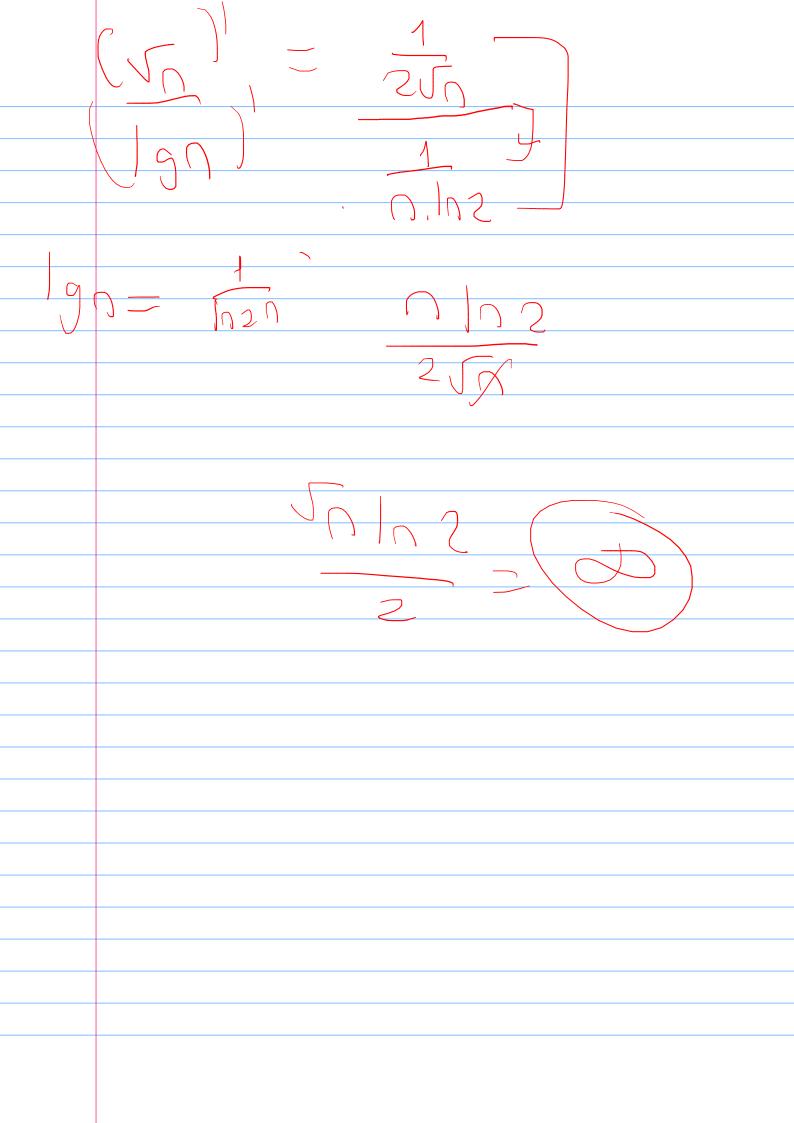
$$\frac{-\frac{1}{2}+1+1}{\frac{1}{2}} \frac{1}{9} \frac{1$$

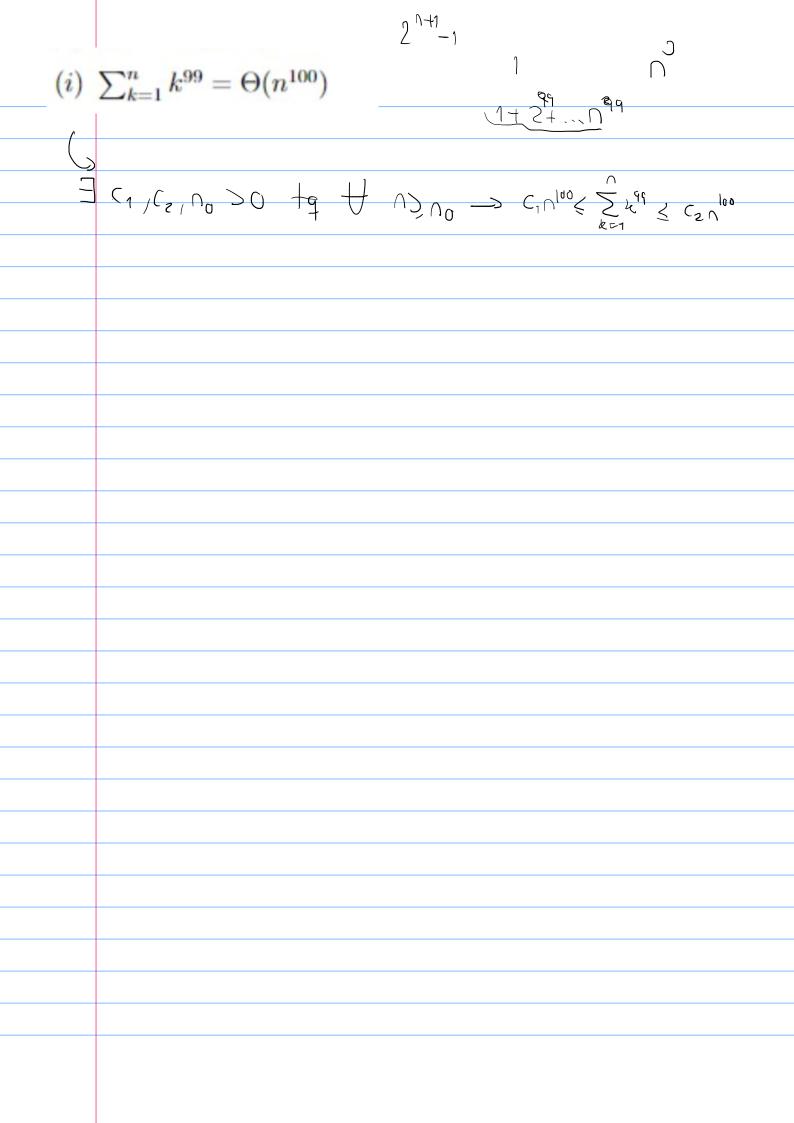
$$\frac{1}{2} |g(n)| + \frac{1}{2} |g(n)| \leq \frac{1}$$

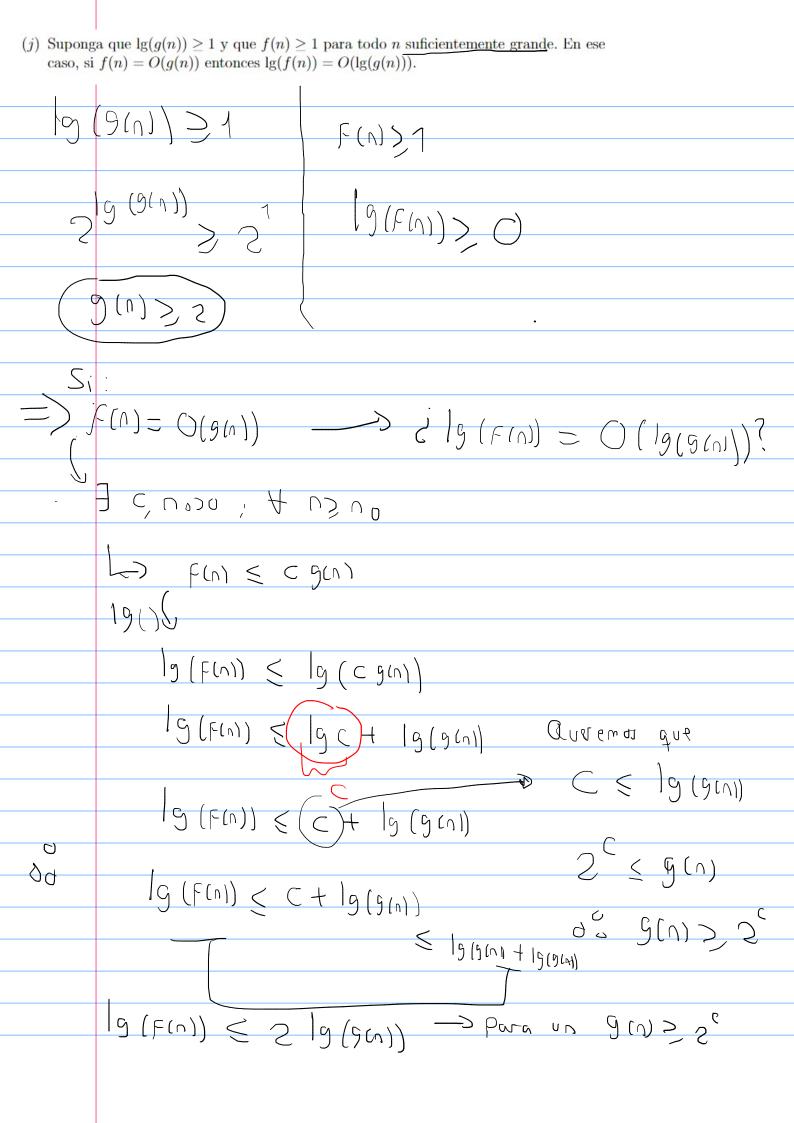
```
(a) \lg \sqrt{n} = O(\lg n)
             D∃ < , n, >0 , +q + n>, 0 -> (g, 5) ≤ < lg ∩
                                                            1/90 € C 190
                Es ustad para C=1 y no=1
                  ya que tendre mar: 1/9n = 19n -> Esta es vertad
ya que la cur
                                                                  ya que la Función
                                                                  logaritmica es
                                                                   C26016046
   (b) Si f(n) = O(g(n)) y g(n) = O(h(n)) entonces f(n) = O(h(n))
     F(n) = O(g(n))
       F(n) < C_19^{(n)}
    Q(u) \neq Q(p(u))
            C19(n) < (1x (2 h(n)
              f(n) \leq C_1 f(n) \leq C_h(n)
              f(n) \in Ch(n) \Longrightarrow f(n) = O(h(n))
(c) Si f(n) = O(g(n))y g(n) = \Theta(h(n))entonces f(n) = \Theta(h(n))
   5; F(n) = O(g(h))
                         \wedge \qquad g(n) = \Theta(h(n))
          L> F(n) ≤ C<sub>1</sub> G(n) (2 h(n) ≤ G h(n) = ) { F(n) = 0 (h(n))?
                                                                V ≤ V ∈ V3
           \bigcup_{S} - \Im \cup \leqslant \bigcup_{S}
                                         \frac{1}{2}\binom{8}{7}+2 \leq \binom{7}{2} \leq \binom{7}{7}+2
                                                       V<sub>5</sub>+5 € V<sub>5</sub>-20
```

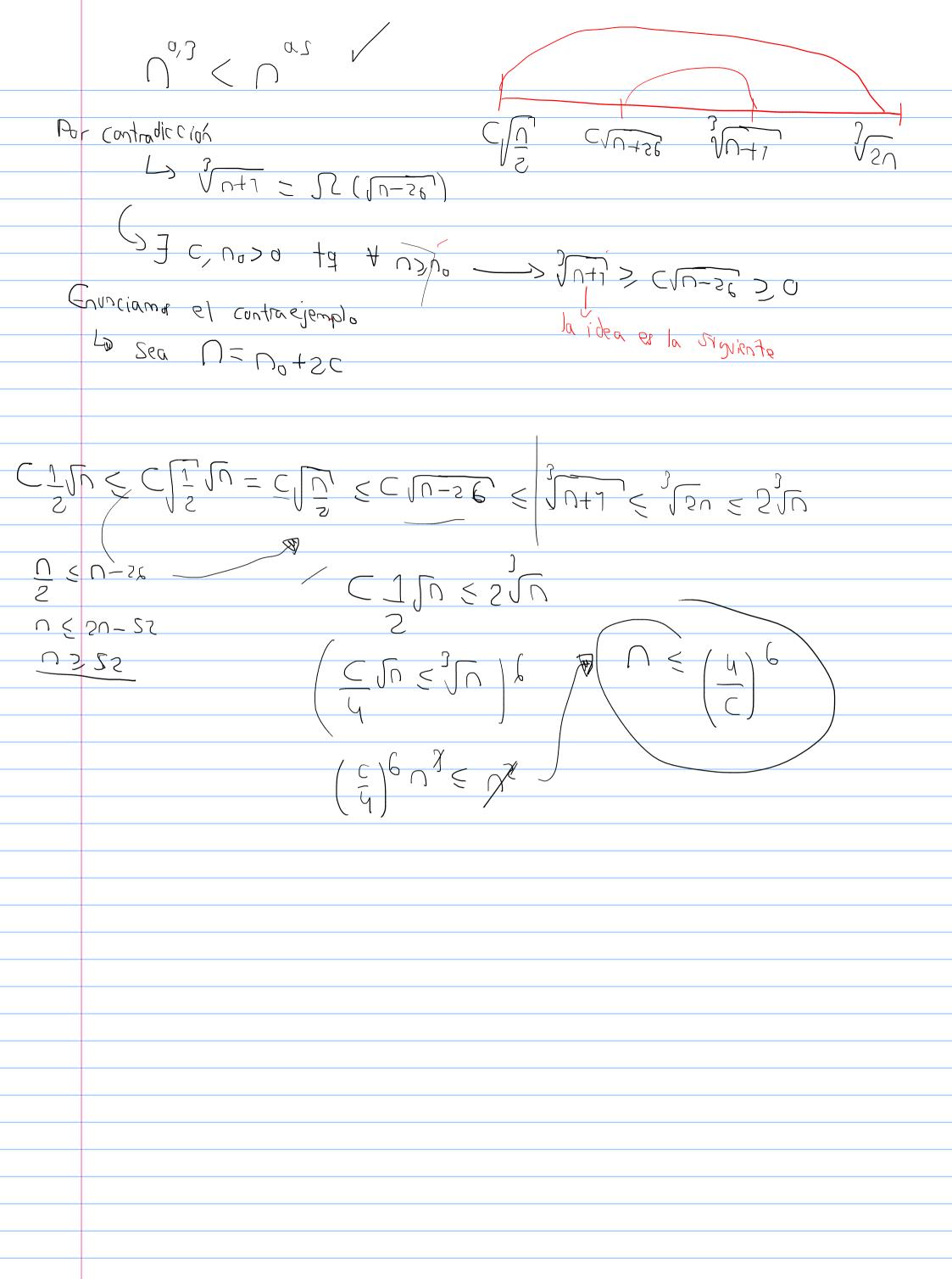
$$(g) (n + a)^{b} = \Theta(n^{b}), \text{ donde } a, b \in \mathbb{R} \text{ y } b > 0.$$

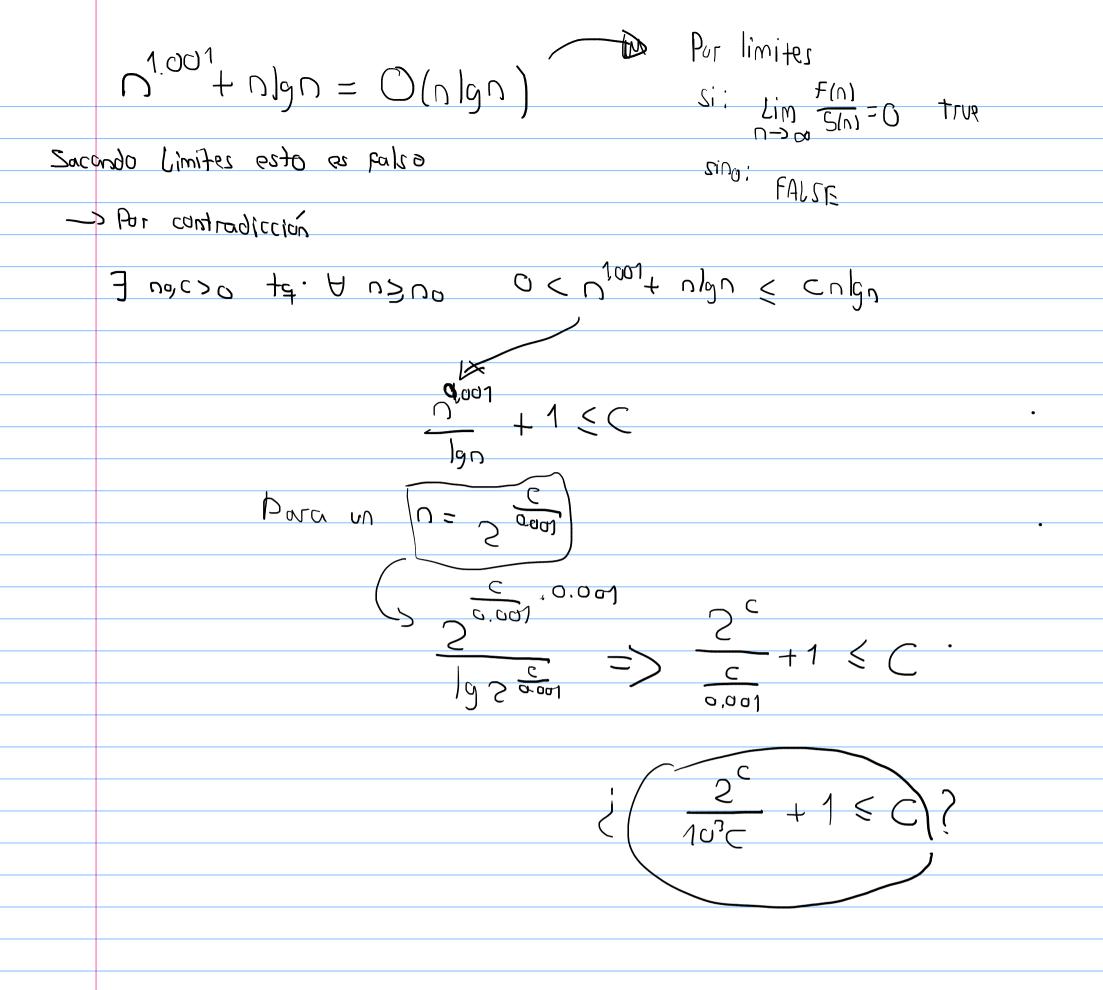
$$(c_{1} \land b \leq \land b + \ldots + \land b \leq \land b$$

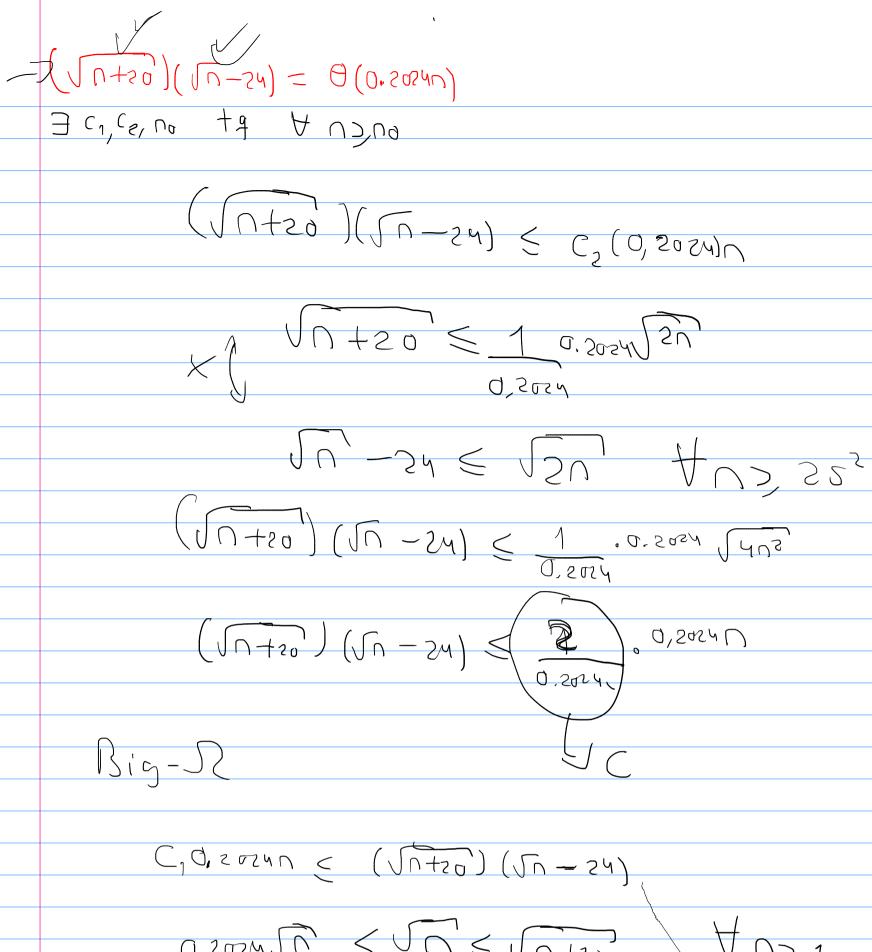












$$0.50501U \leq (20.501) \leq (20.501)$$

$$0.50540 \in (10+50)(10-54) + 051$$
 $0.50540 \in (10+50)(10-54) + 051$

$$207 - 202302 - 20230 | 90 + 10|0 | 920 + 1 = 0 (\frac{1}{2} n^3)$$

$$50-5053\frac{1}{3}-5053\frac{1}{3}$$
 $-10\frac{10}{10}$ $+1$ $=50$ $+1$ $=10$

$$\frac{5}{2003}$$

$$= 2 \cdot 2 \cdot \left(\frac{1}{4}\right)^{3}$$

$$\frac{1}{503} - \frac{1}{3053} \frac{1}{0} - \frac{1}{3053} \frac{1}{0} \frac{1}{0}$$

(a)
$$n = \lfloor \frac{n}{3} \rfloor + \lfloor \frac{n+1}{3} \rfloor + \lfloor \frac{n+2}{3} \rfloor$$
 for all $n \in \mathbb{Z}$

$$\left[\frac{3}{3}k + \frac{1}{3}\right] + \left[\frac{3}{3}k + \frac{3}{3}\right] + \left[\frac{3}{3}k + \frac{3}{3}\right]$$

$$3$$
 $n=3u+2$

$$\left[\frac{3}{3} + \frac{3}{3}\right] + \left[\frac{3}{3} + \frac{3}{3}\right] + \left[\frac{3}{3} + \frac{3}{3}\right]$$

$$\frac{3}{2} = \frac{3}{2} + \frac{3}{2} + \frac{3}{2} = \frac{3}{2}$$

