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Test Case :- A = [1, 3, 5]

Experiment - 4

Q) We define $f(x, y)$ as no. of different corresponding bits in binary representation of $x \Delta y$. For ex $\Rightarrow f(2) = f(2, 7) = 2 \Rightarrow$ First & third bit differ.

You are given an array of N positive integers. Find sum of $f(A_i, A_j)$ for all pairs such that $1 \leq i, j \leq N$.

S) Brute Force Approach :-
Check every pair & count no. of different bits b/w them.

Two numbers differ at a bit position if their XOR has 1.

Steps -> i) Loop through all pairs (i, j)
ii) Compute :-

$$XOR = A[i] \Delta A[j]$$

iii) Count no. of set bit

iv) Add it to total answer

Code \Rightarrow public class Main {

```
public static void main(String[] args) {
    // Ex- int[] arr = new int[]{1, 3, 5};
    int n = arr.length;
    int totalCount = 0;
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            if (i != j) {
                int xor = arr[i] ^ arr[j];
                int count = 0;
                for (int k = 0; k < 32; k++) {
                    if ((xor >> k) & 1 == 1) count++;
                }
                totalCount += count;
            }
        }
    }
}
```

totCount += count;

}

}

return totCount;

Return totCount;

$$T.C = O(N^2)$$

→ Optimal Approach -

For every bit position from 0 to 32 & Count no. of zeroes & ones.

Then add $\text{count}_0 * \text{count}_1$ to total answer.

Code -

```
long answer = 0;  
for (int bit = 0; bit < 32; bit++) {  
    long countOne = 0;  
    for (int i = 0; i < N; i++) {  
        if (A[i] & (1 << bit)) {  
            countOne++;  
        }  
    }  
    long countZeroes = N - countOne;  
    answer = (answer + (countOne * countZeroes));  
}
```

answer = (answer + (countOne * countZeroes));
 $10^9 + 7$ %

return answer;

$$O(N^2)$$

$$O(1)$$