

# Scheduling in a Real-time Network-on-Chip

Period minimization using metaheuristics

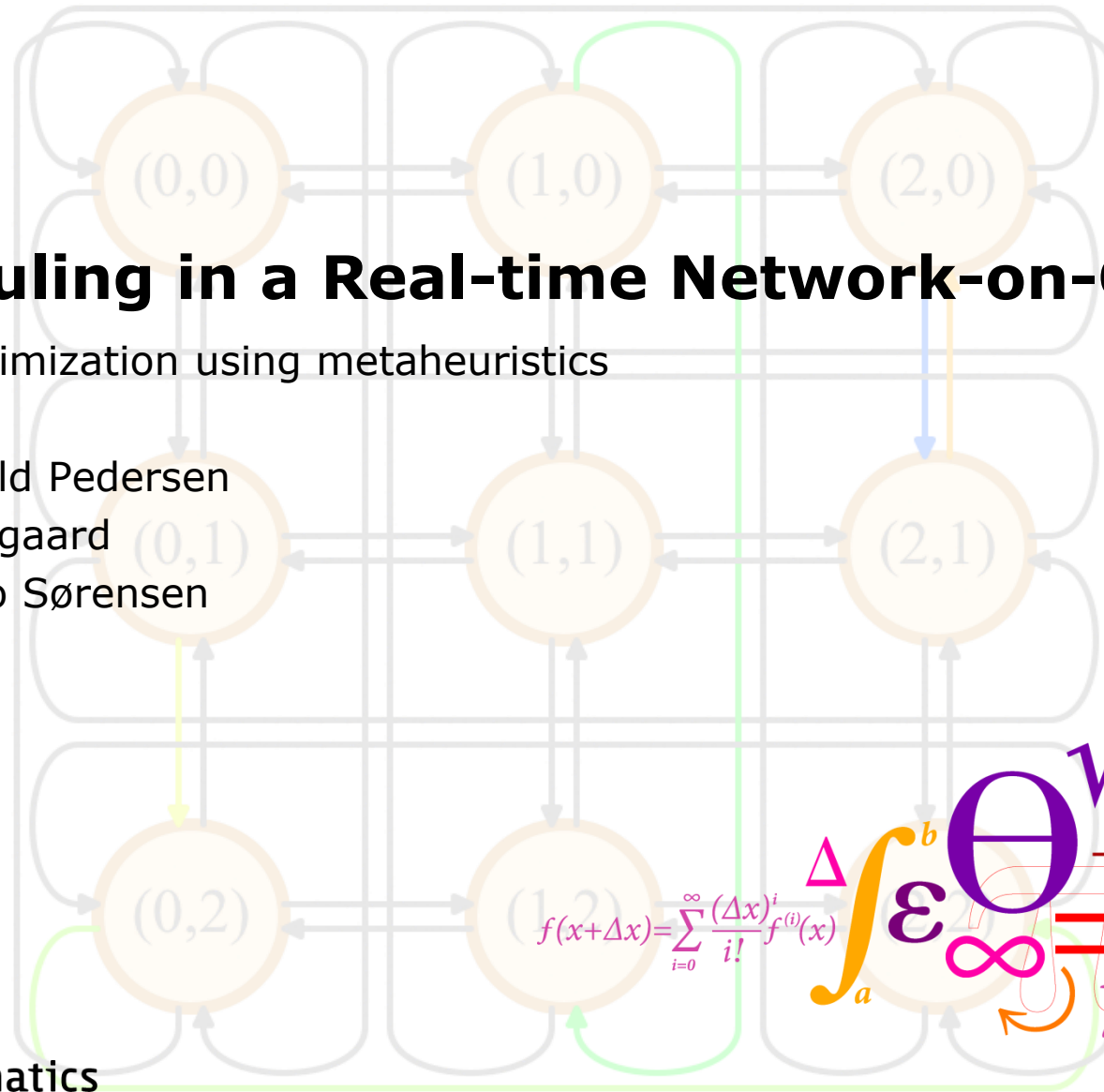
Mark Ruvald Pedersen

Jaspar Højgaard

Rasmus Bo Sørensen

DTU Informatics

Department of Informatics and Mathematical Modeling



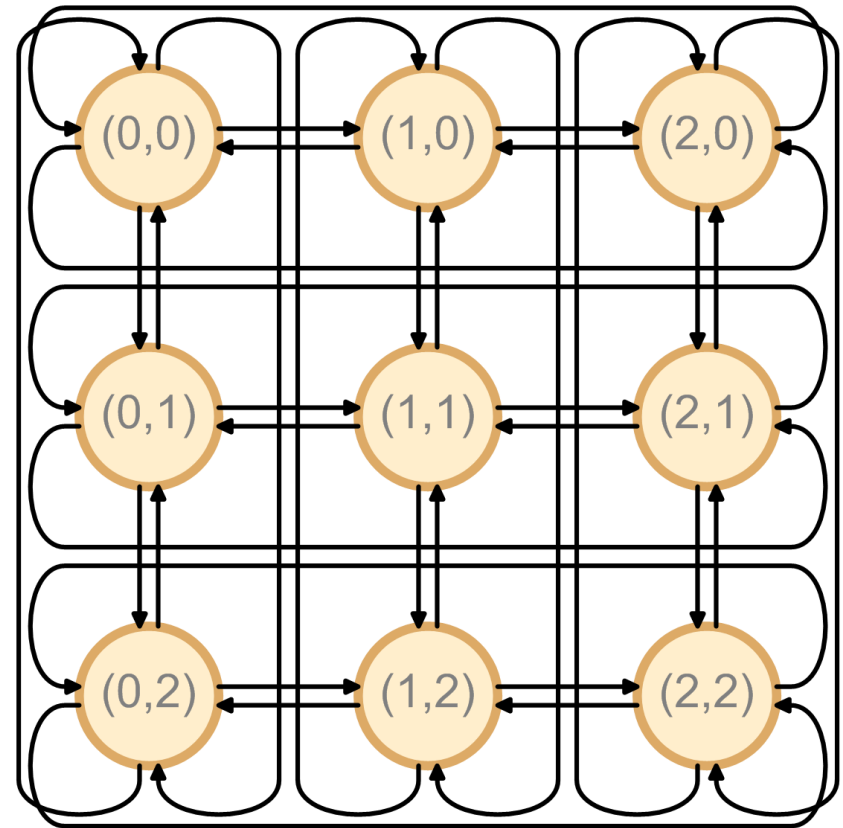
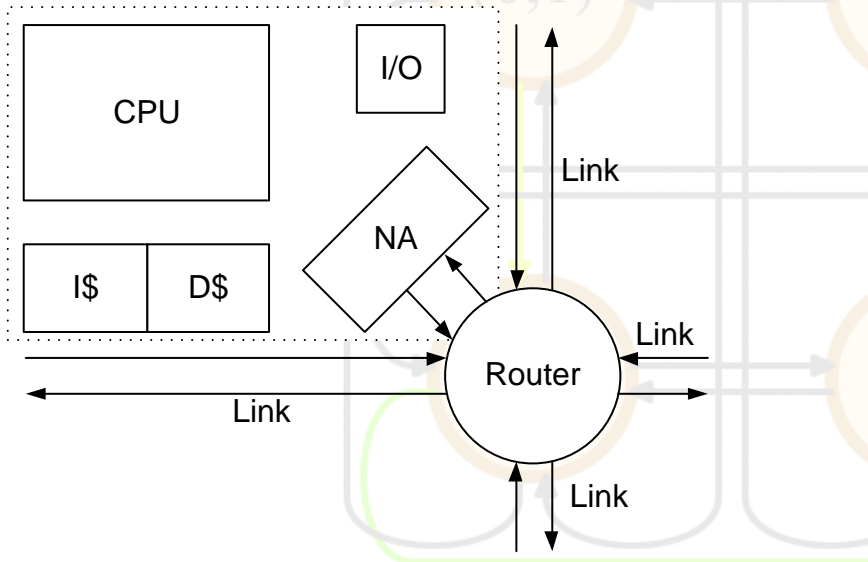
$$f(x+\Delta x) = \sum_{i=0}^{\infty} \frac{(\Delta x)^i}{i!} f^{(i)}(x)$$

$$\Delta \int_a^b \epsilon \Theta^{\sqrt{17}} + \Omega \int \delta e^{i\pi} = \{2.7182818284\}$$

$$\infty = \chi^2 \sum \rangle \text{!}$$

# Problem domain

- NP-complete: Integer multi-commodity flow problem
- No buffering
- Real-time system
- Network-on-Chip
- Inter-processor communication
- Scheduling communication





# Operators

Destroy and rebuild paths.

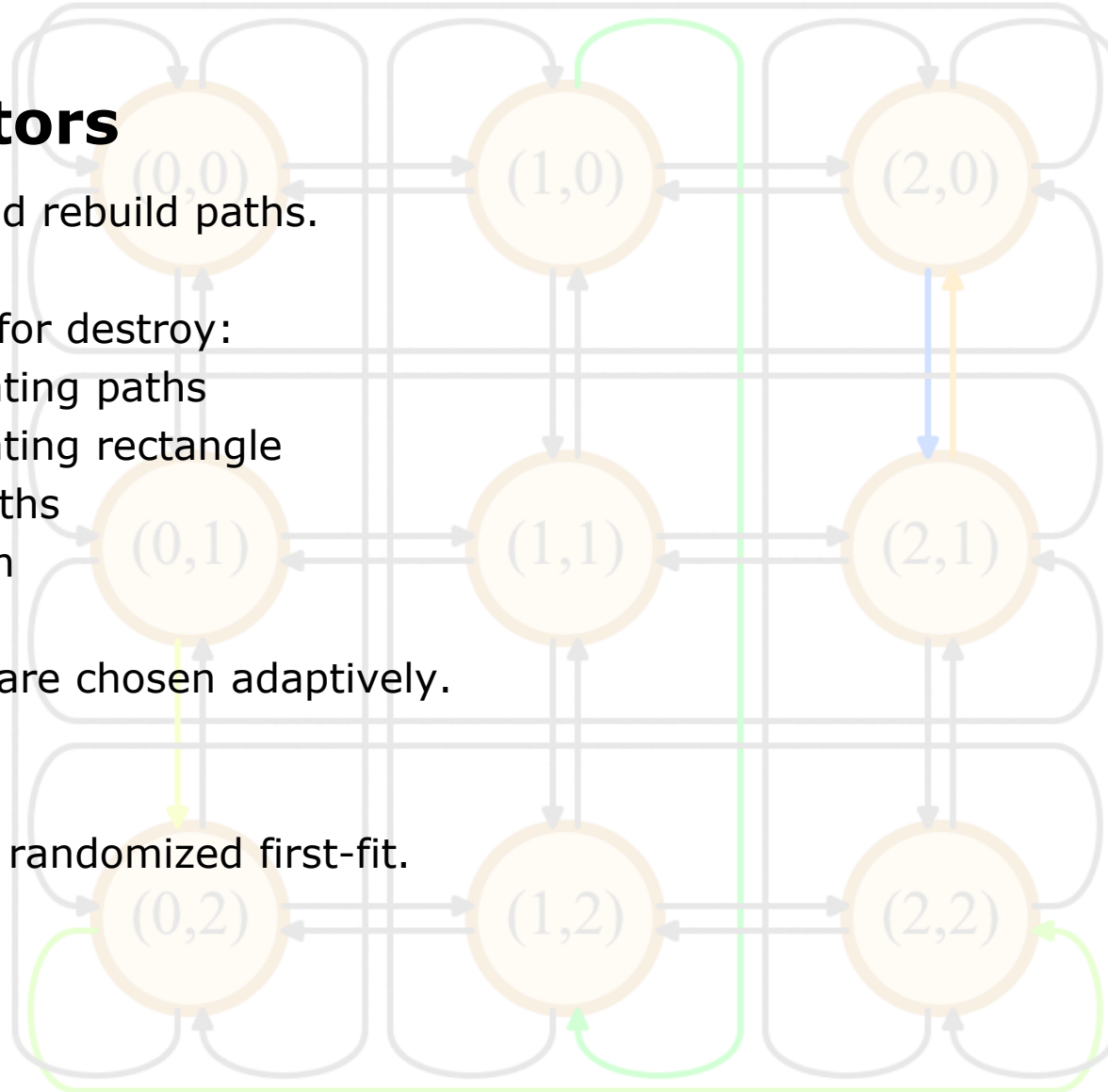
Operators for destroy:

- Dominating paths
- Dominating rectangle
- Late paths
- Random

Operators are chosen adaptively.

Rebuild:

- Greedy randomized first-fit.



# Metaheuristics

## Greedy randomized search procedure (GRASP)

```
procedure our_grasp( $\beta$ )
  best = infinite
  while (time left)
    current = initial_solution( $\beta$ )
    if (current shorter than best) then best = current
    {
      operator = choose_operator()
      chosen = operator()
      destroy(chosen)
      repair(chosen)
    }
    if (current shorter than best) then best = current
    punish_reward(operator)
  return best
```

- Local search of GRASP is choose\_operator, destroy and repair.
- Random-operator not used.
- Problems with no clear local neighborhood.
- Very large solution spaces.

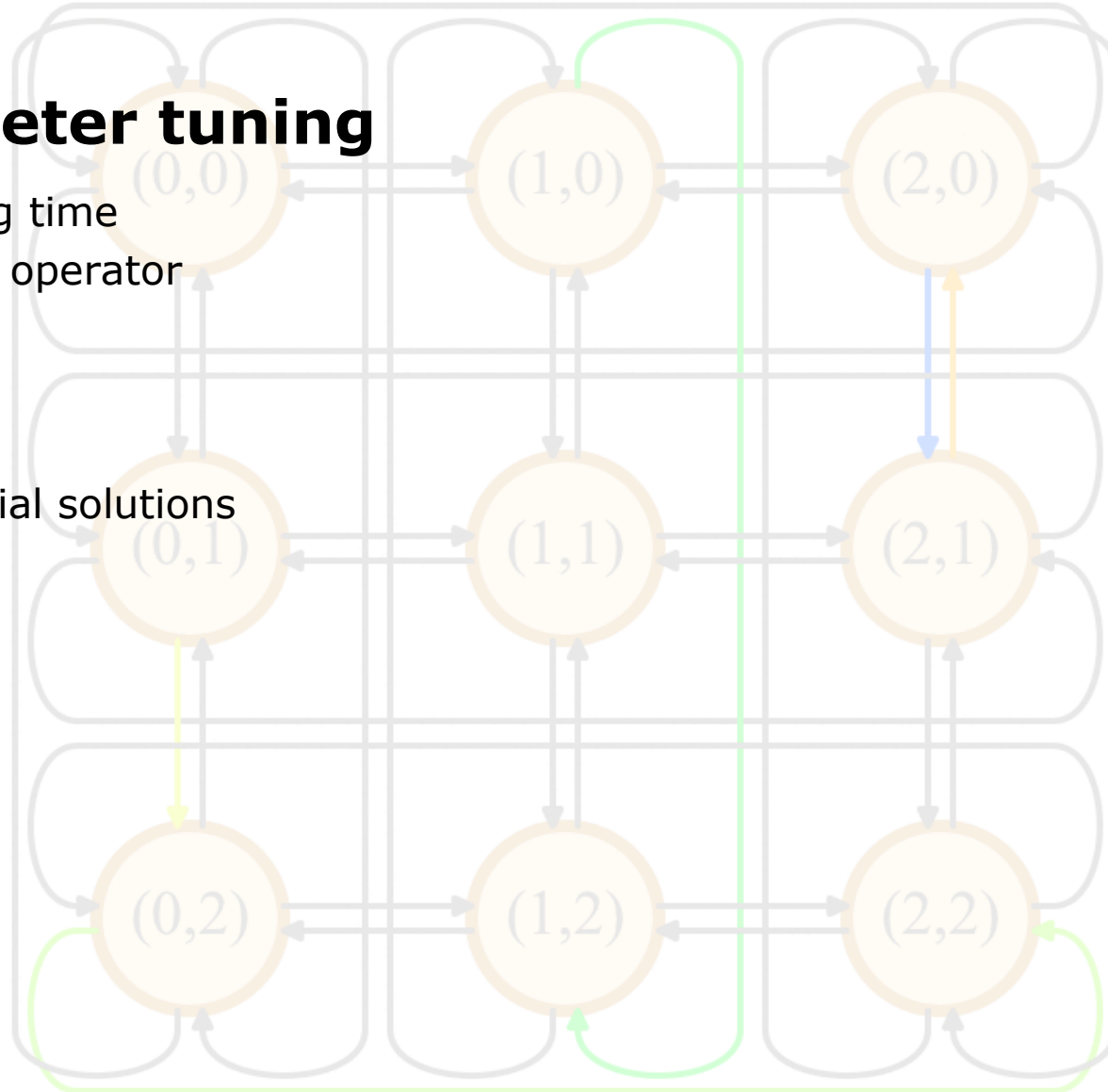
# Metaheuristics

## Adaptive Large Neighborhood Search (ALNS)

```
procedure our_alns()  
    best = current = initial_solution()  
    while (time left)  
        operator = choose_operator()  
        chosen = operator()  
        destroy(chosen)  
        repair(chosen)  
        if (current shorter than best) then best = current  
        punish_reward(operator)  
  
    return best
```

- Finds feasible solution easily.
- Destroy and repair gives very large neighborhood.
- Iteratively tries shortening the schedule.
- Escaping faster from local minima: All new solutions are accepted.

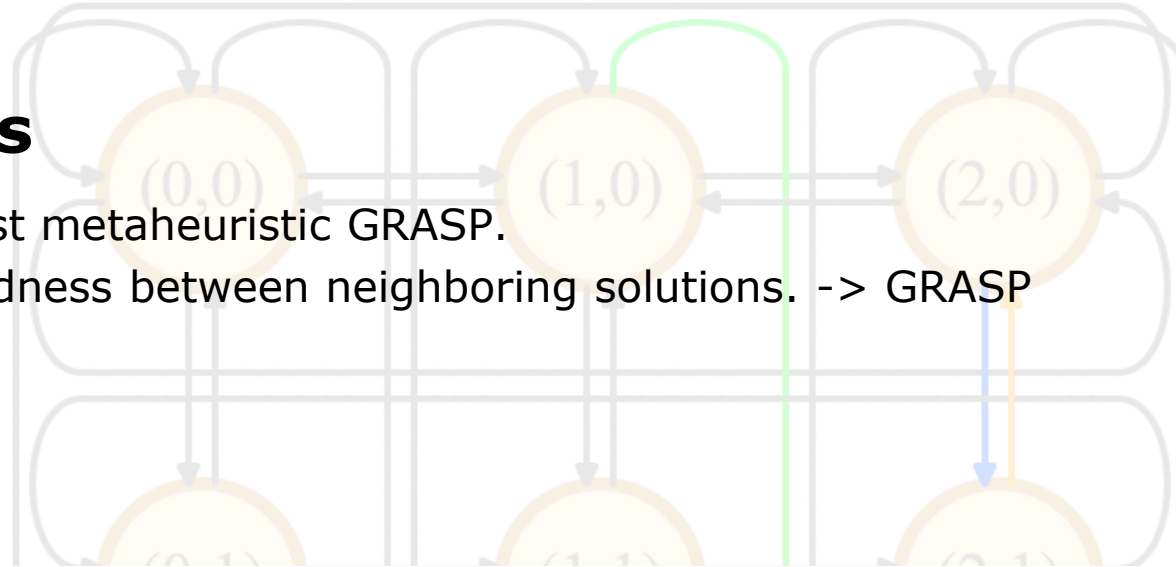
- Running time
- Choose operator
- GRASP
  - $\beta$
- ALNS
  - Initial solutions



## Results

Overall best metaheuristic GRASP.

Low relatedness between neighboring solutions. -> GRASP



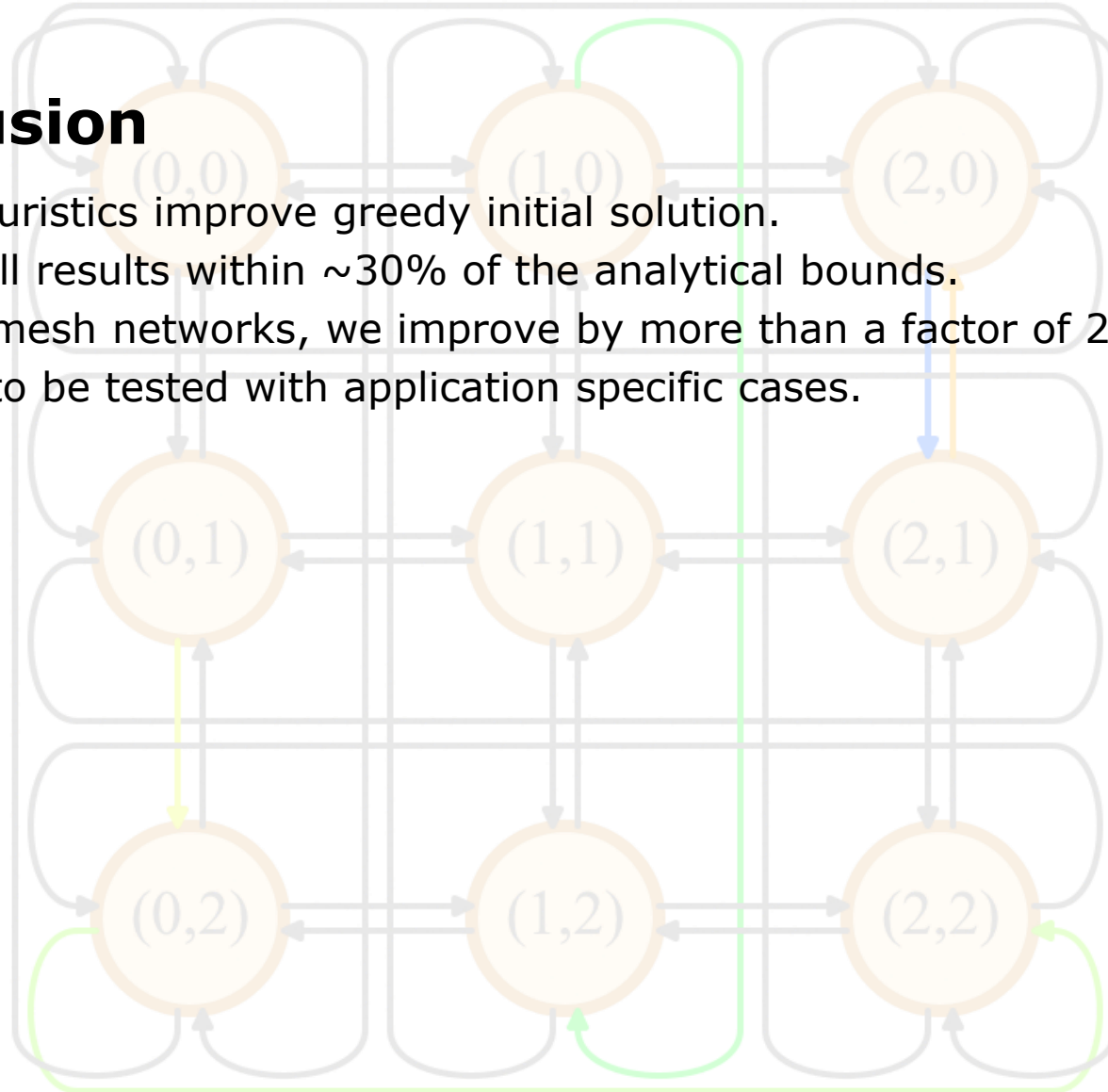
Size	Mesh					Bi-torus				
	Bounds[1]	[2]	GREEDY	ALNS	GRASP	Bounds[1]	[2]	GREEDY	ALNS	GRASP
$3 \times 3$	8 (10)	28	13	<b>11</b>	<b>11</b>	8 (10)	11	12	<b>10</b>	<b>10</b>
$4 \times 4$	16 (18)	59	24	<b>21</b>	<b>21</b>	15 (18)	20	21	<b>19</b>	<b>19</b>
$5 \times 5$	25 (34)	112	41	39	<b>37</b>	24 (28)	<b>28</b>	32	30	30
$6 \times 6$	54	–	66	65	<b>61</b>	35	–	45	45	<b>43</b>
$7 \times 7$	66	–	98	97	<b>94</b>	48	–	64	63	<b>61</b>
$8 \times 8$	128	481	144	144	<b>138</b>	64	88	87	86	<b>85</b>
$9 \times 9$	135	–	201	201	<b>195</b>	90	–	<b>113</b>	<b>113</b>	<b>113</b>
$10 \times 10$	250	974	271	271	<b>267</b>	125	158	154	153	<b>151</b>
$15 \times 15$	600	3467	<b>886</b>	<b>886</b>	899	420	481	<b>471</b>	<b>471</b>	474

Table 4: Results compared to the heuristic results of [2]. Numbers in parenthesis are optimal schedule periods



## Conclusion

- Metaheuristics improve greedy initial solution.
- All-to-all results within  $\sim 30\%$  of the analytical bounds.
- For all mesh networks, we improve by more than a factor of 2,0.
- Needs to be tested with application specific cases.



# Scheduler output

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